



# Defect Evolution in Structural Materials from SEAKMC Simulations: Opportunities and Challenges

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# Why do we study defect evolution?

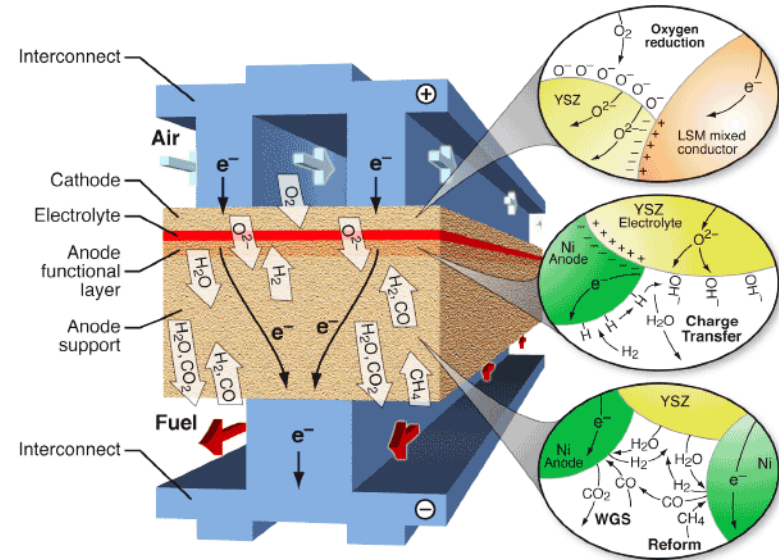
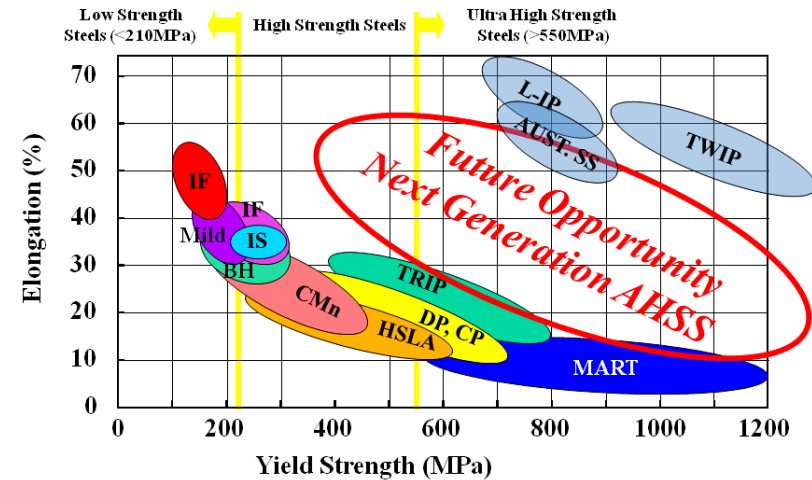
- Collective effects of defects determine real materials properties

- Strength, toughness, conductivity, etc.
- Underpinnings of our energy technologies

- Performance limits are rarely the result of insurmountable physical principles

Structural alloys exhibit strengths that are typically only 5-10% of theoretical limits

- Increased understanding of defects will result in new materials with substantially improved properties



<http://www.coloradofuelcellcenter.org/pages/projects/fundamental.html>

# Evolution of Cascade Defects

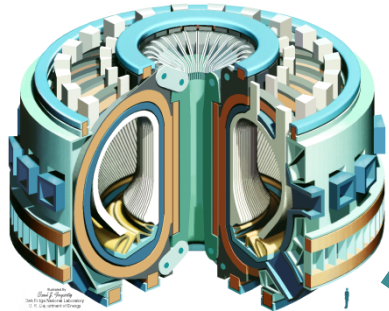
**Defect Production in Cascade**  
 $10^{-13} - 10^{-11}$

**Defect Diffusion and Interaction**  
 $10^{-9} - 10^{-6}$

**Radiation Damage**  
 $10^7$

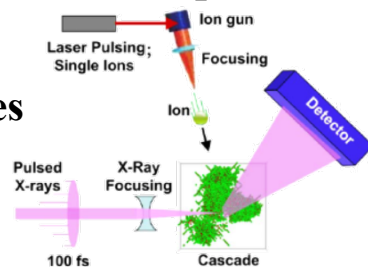


**International Thermonuclear Experimental Reactor(ITER)**



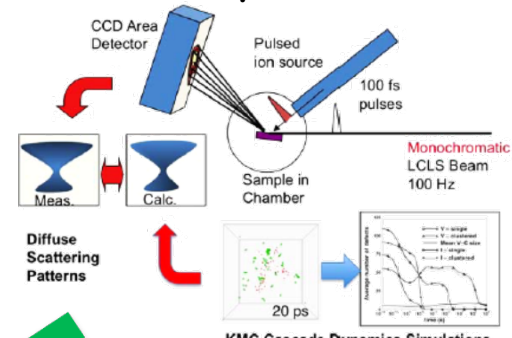
## Experimental Techniques

**LCLS: ps-ns**



Sub-picosecond to nanosecond resolution by ion time of arrival signal

**APS:  $\mu$ s-ms**

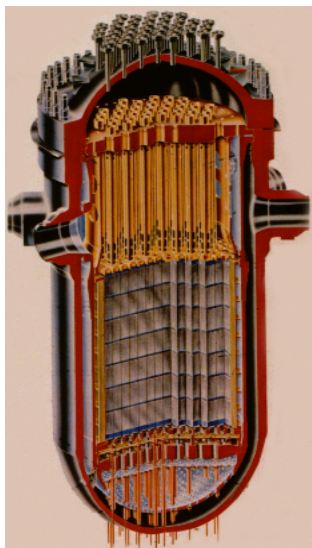
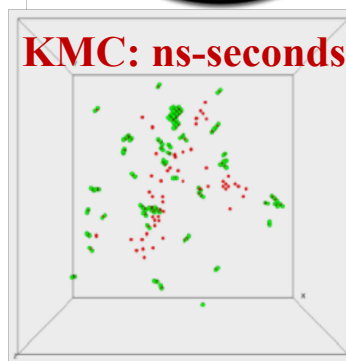
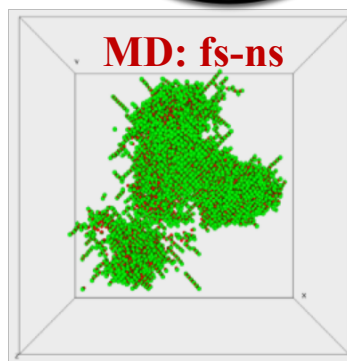
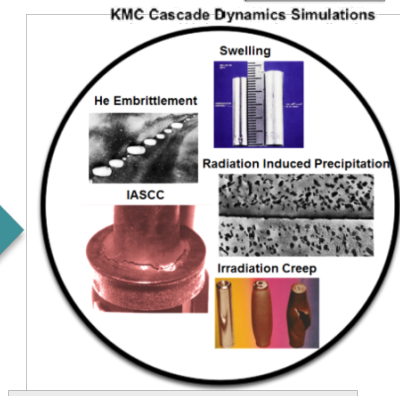
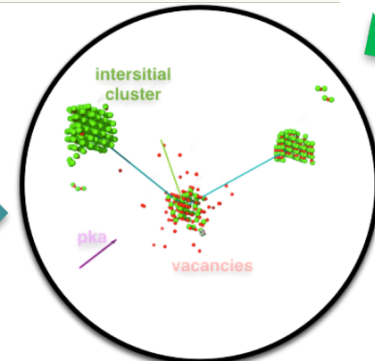
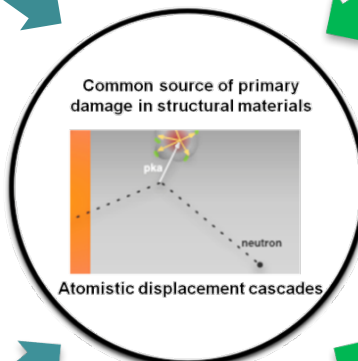


KMC Cascade Dynamics Simulations

**Fusion**

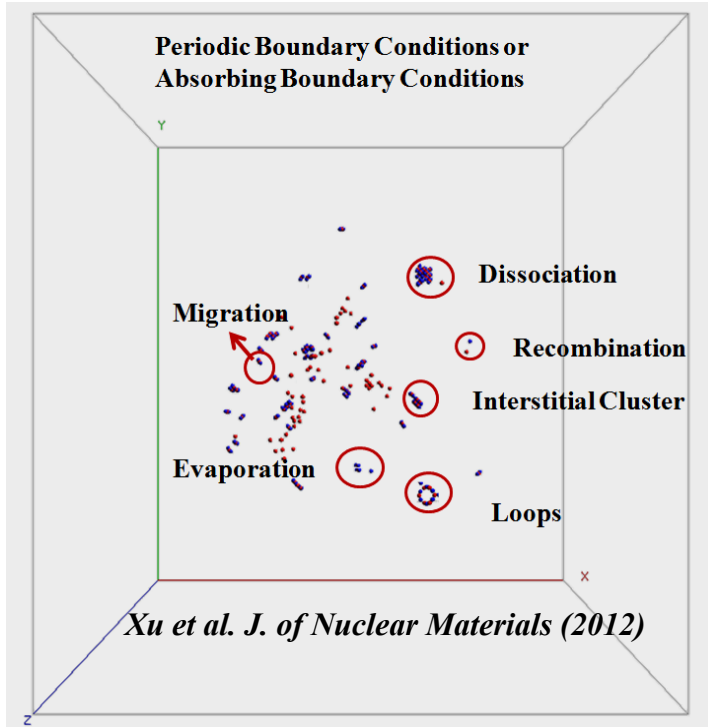
**Fission**

**Simulation Techniques**



**Light Water Reactor(LWR)**

# Conventional Object KMC for Long-Term Defect Evolution



## Processes Related

- Diffusion mechanism
  - 3D, 1D, or 1D+Rotation
- Migration energy and prefactors
  - *ab initio* or empirical potential
- Dissociation of clusters
- Reaction distance

## Deficiencies

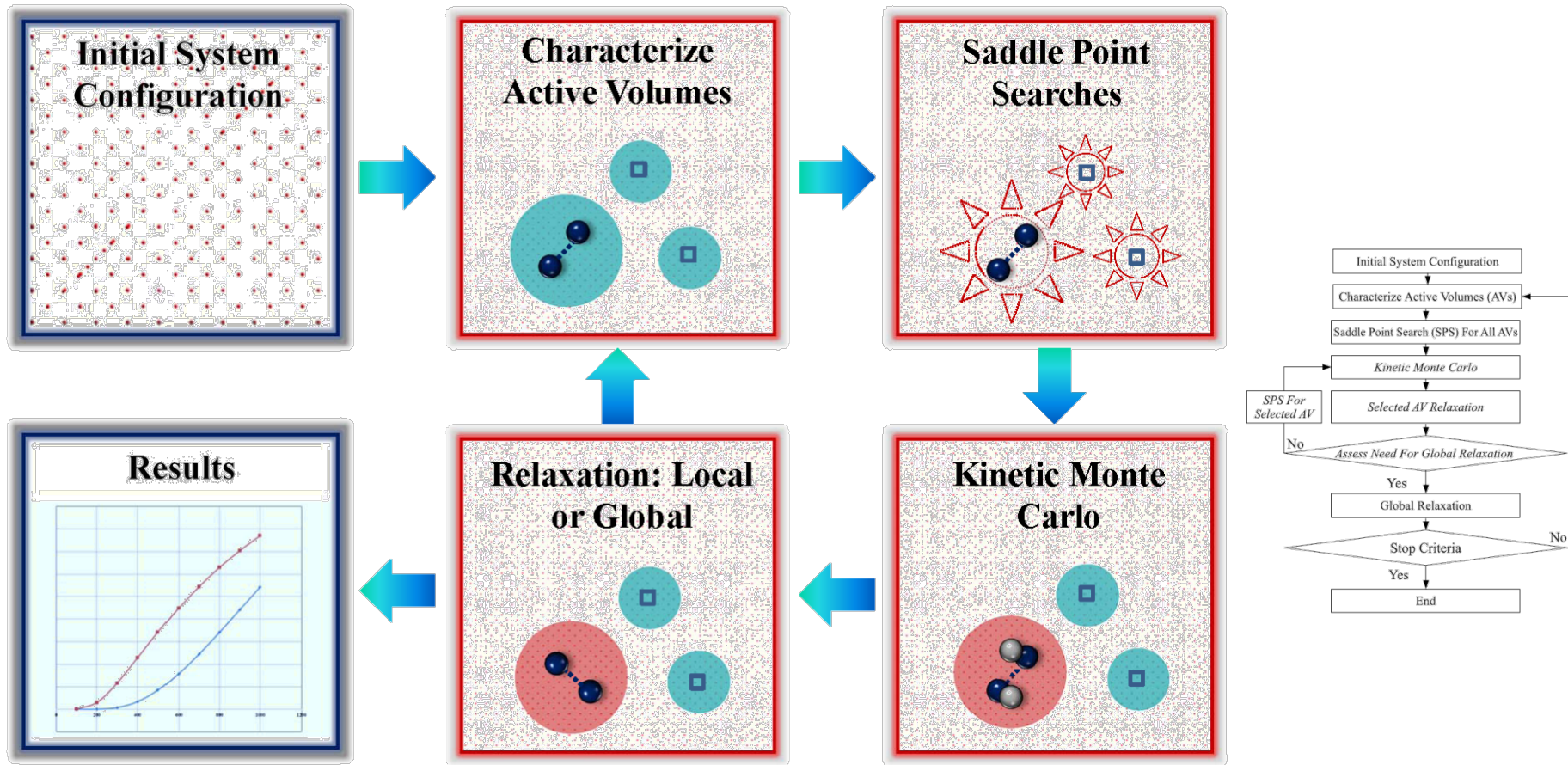
- Difficult to predetermine the diffusion mechanisms and corresponding energy
- Too much simplification: no atomistic configurations of defects
- Does not account for migration mode and energy dependence on configuration
- Simplistic description of defect interactions

*Object KMC is a oversimplified model*

*Atomistic details are crucial to accurately describe defect evolution*



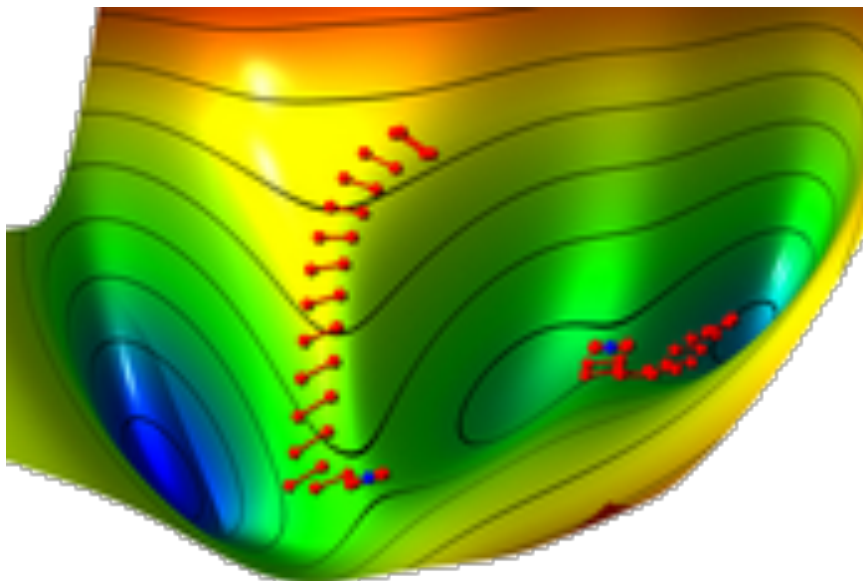
# Self-Evolving Atomistic KMC (SEAKMC) Method



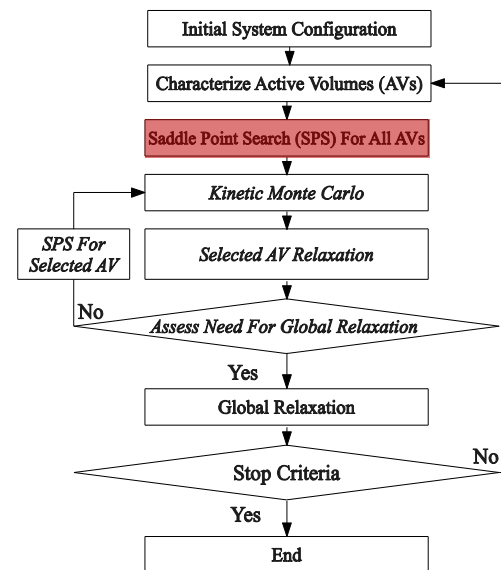
Xu et al. *Phys. Rev. B* 84, (2011) *J. Phys.: Condens. Matter* 24 (2012), *Computational Materials Science* 100, 135(2015) *Computational Materials Science* 100, 124 (2015)

***SEAKMC is a general framework including several techniques, particularly powerful for large systems with complex defects***

# Saddle Point Search Techniques



<http://www.theochem.uni-stuttgart.de/kaestner/dlfind.html>



Calculating Hessian

Partitioned Rational Function Optimizer

Without Calculating Hessian

Minimum Mode Following

Dimer

Lanczos

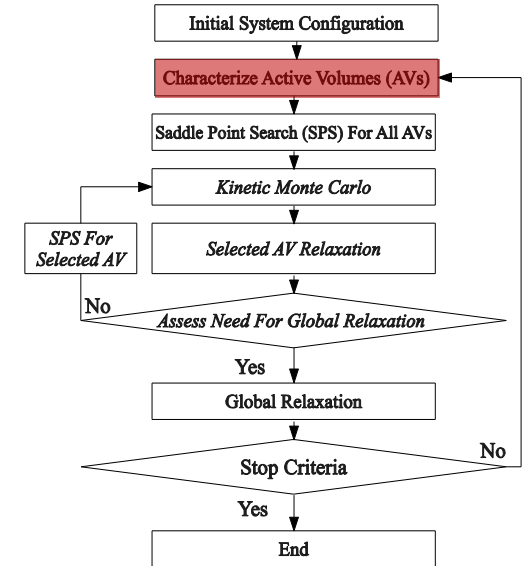
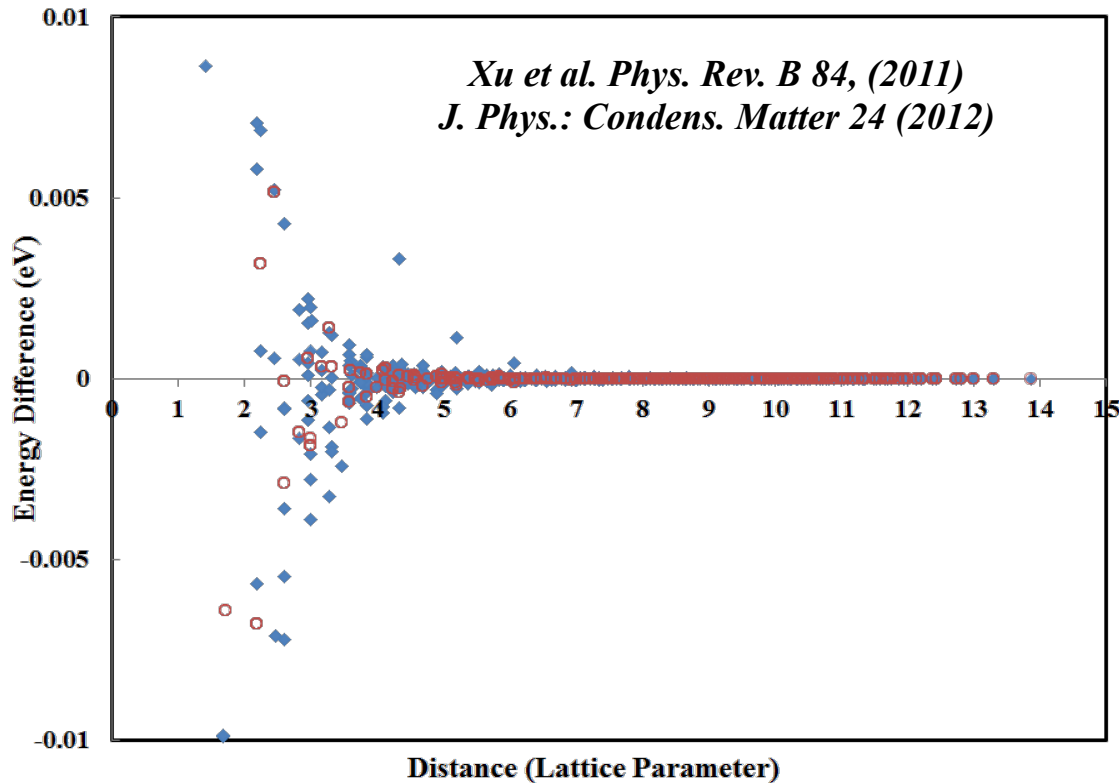
Others

ABC+NEB

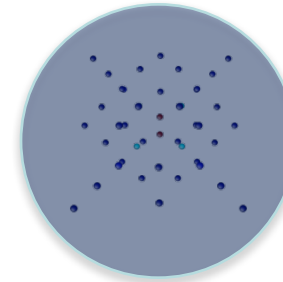
- ❖ Find migration barriers on-the-fly, based on harmonic transition state theory
- ❖ Only need initial configuration; find the saddle point configurations

# Part I: Active Volumes-Concept and Application

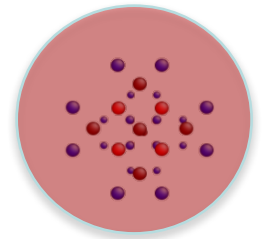
*Point defects are localized so activate volume can be defined based on energy, stress/strain criteria*



*Interstitial*

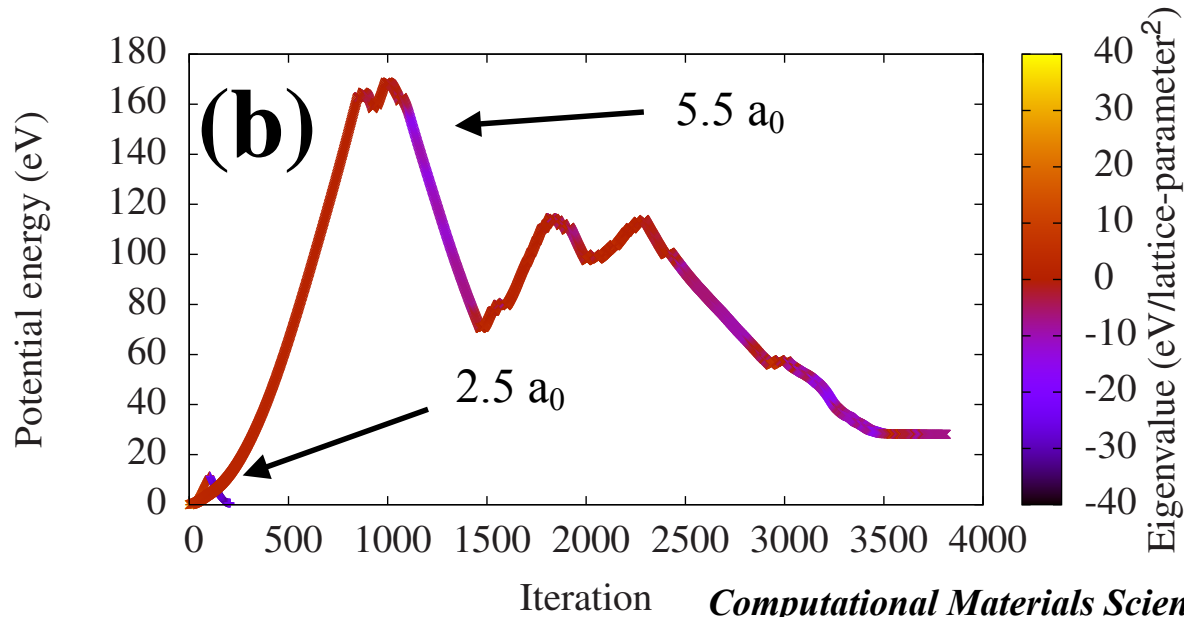
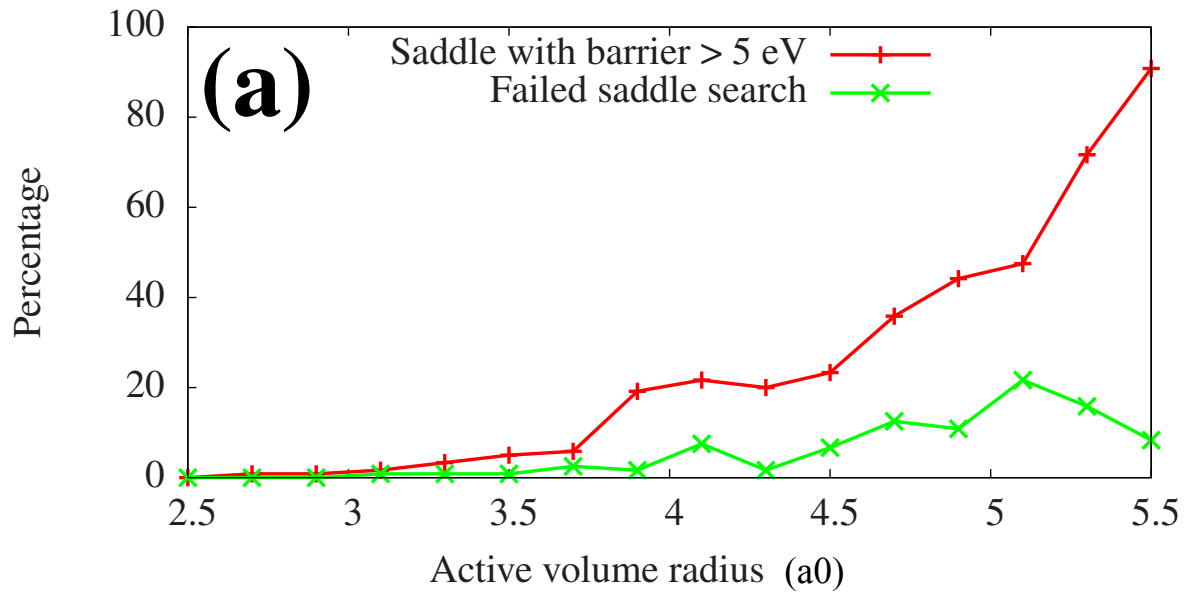


*Vacancy*

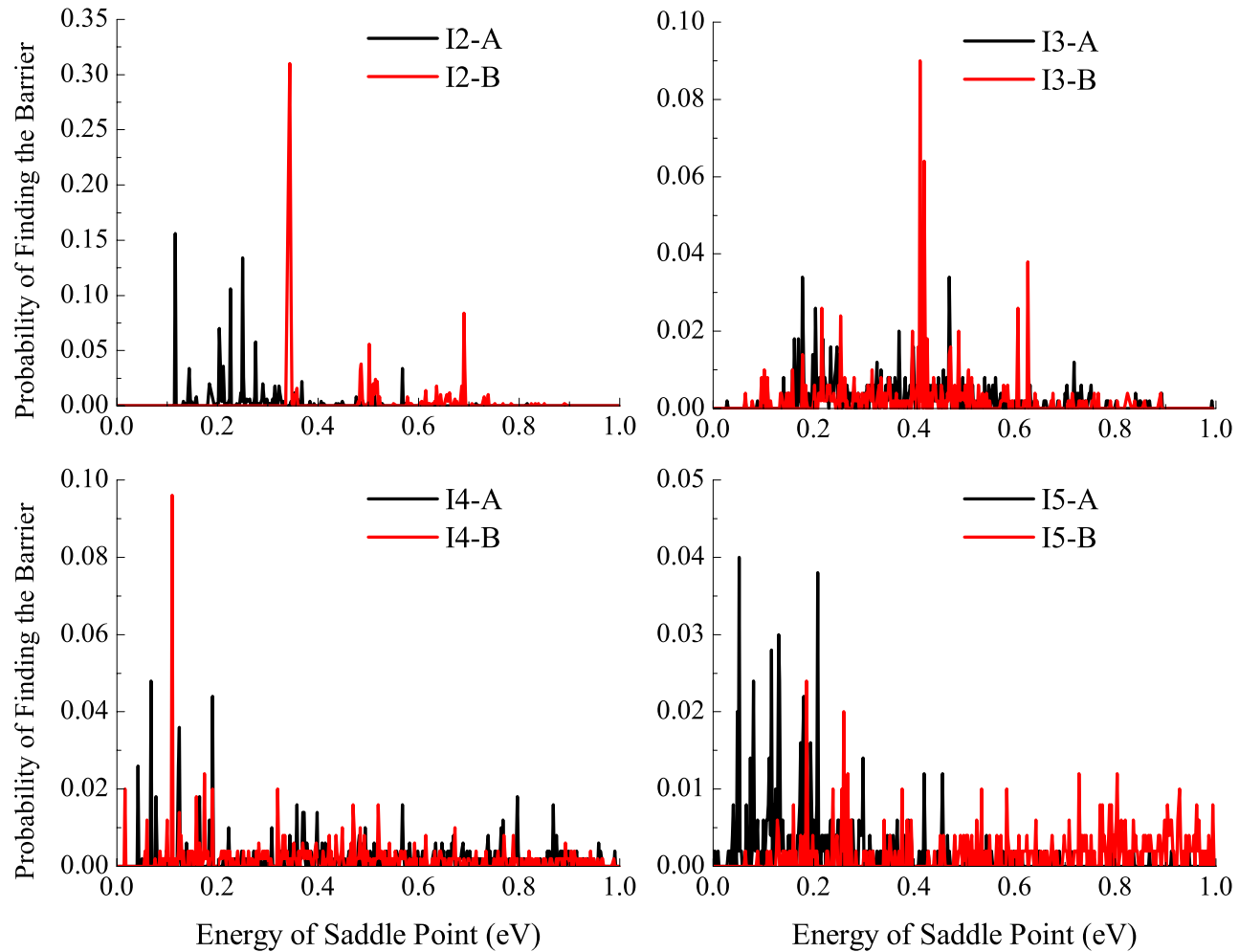


*Saddle point searches are only carried out within the active volumes, significantly reduce the computational cost*

# AV size



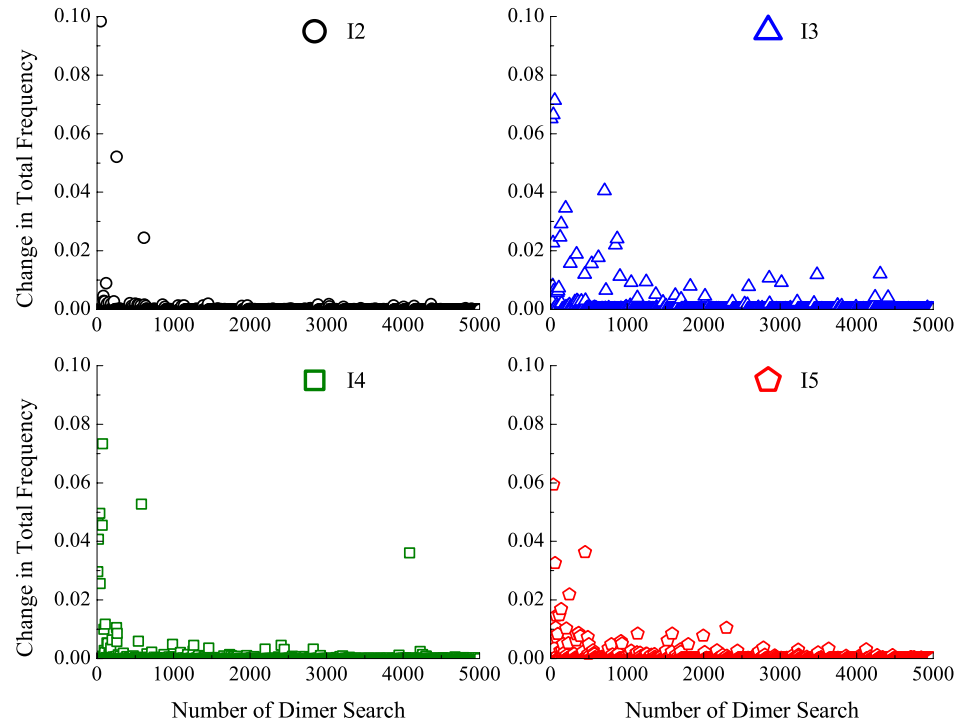
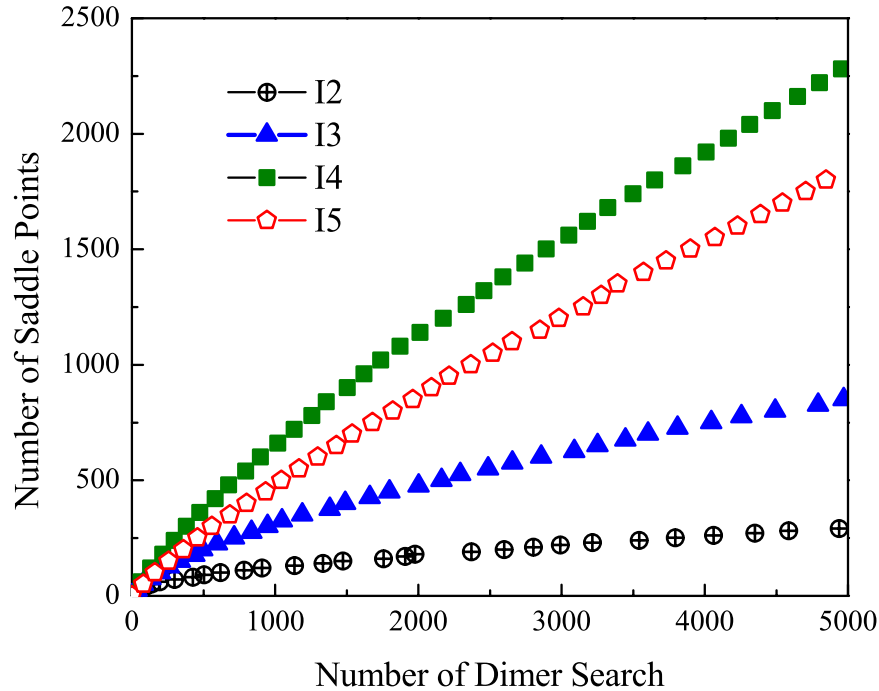
# Saddle Point Searches



*J. Phys.: Condens. Matter 24 (2012)*



# Number of Unique Saddle Points



*J. Phys.: Condens. Matter 24 (2012)*

*For interstitial clusters (complex defects), the number of unique saddle points does not converge.*

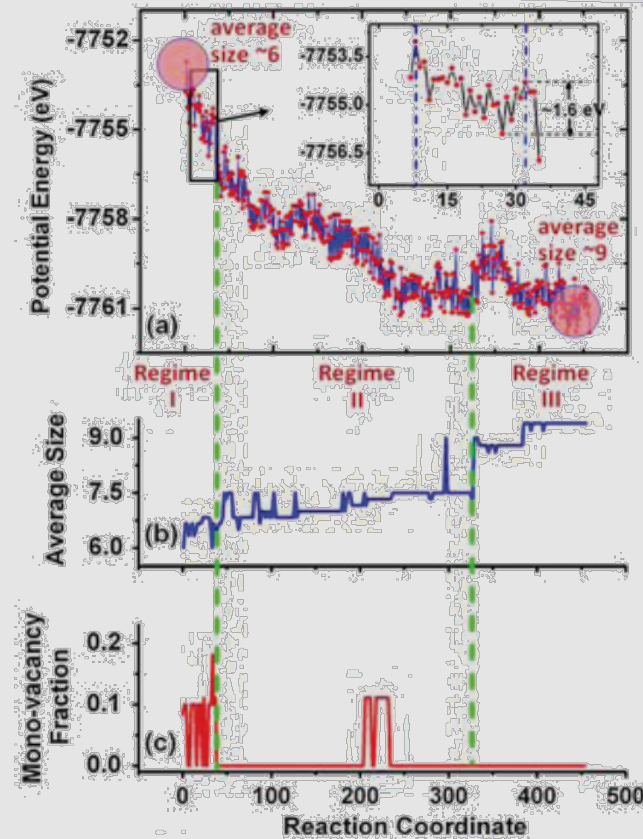
# Vacancy Clustering in Iron

For vacancy clusters grow beyond 6.5 vacancies (system energy is around -7760 eV)

Autonomous Basin Climbing  
+KMC

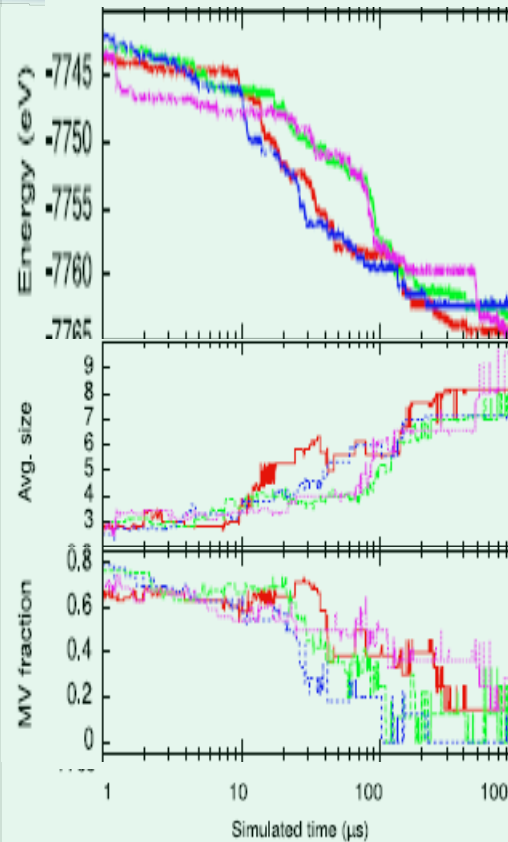
20000 seconds at 150 °C

*Phys. Rev. Letter 106, (2011) 125501*



Kinetic Activation  
Relaxation Technique  
0.5 ms at 50 °C

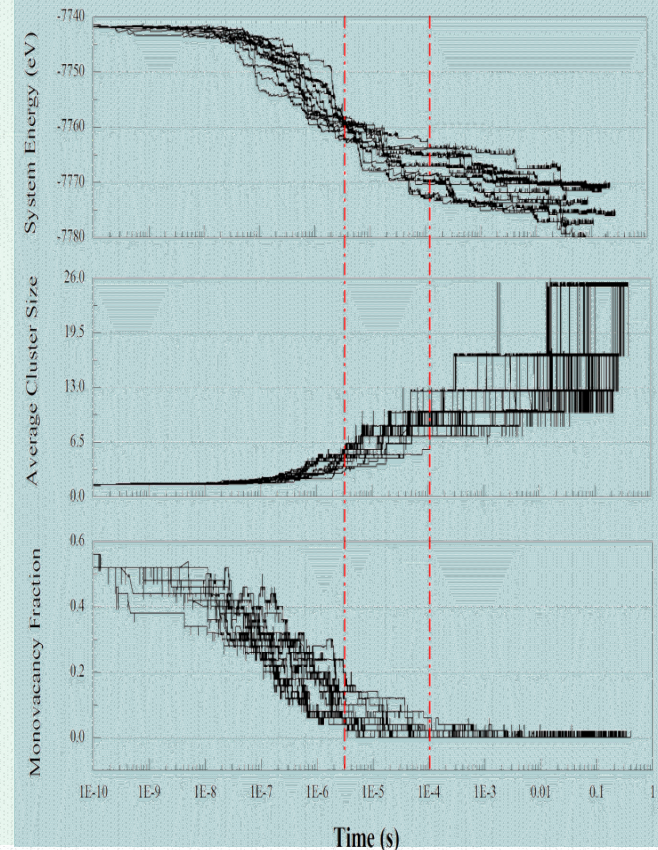
*Phys. Rev. Letter 108, (2012) 219601*



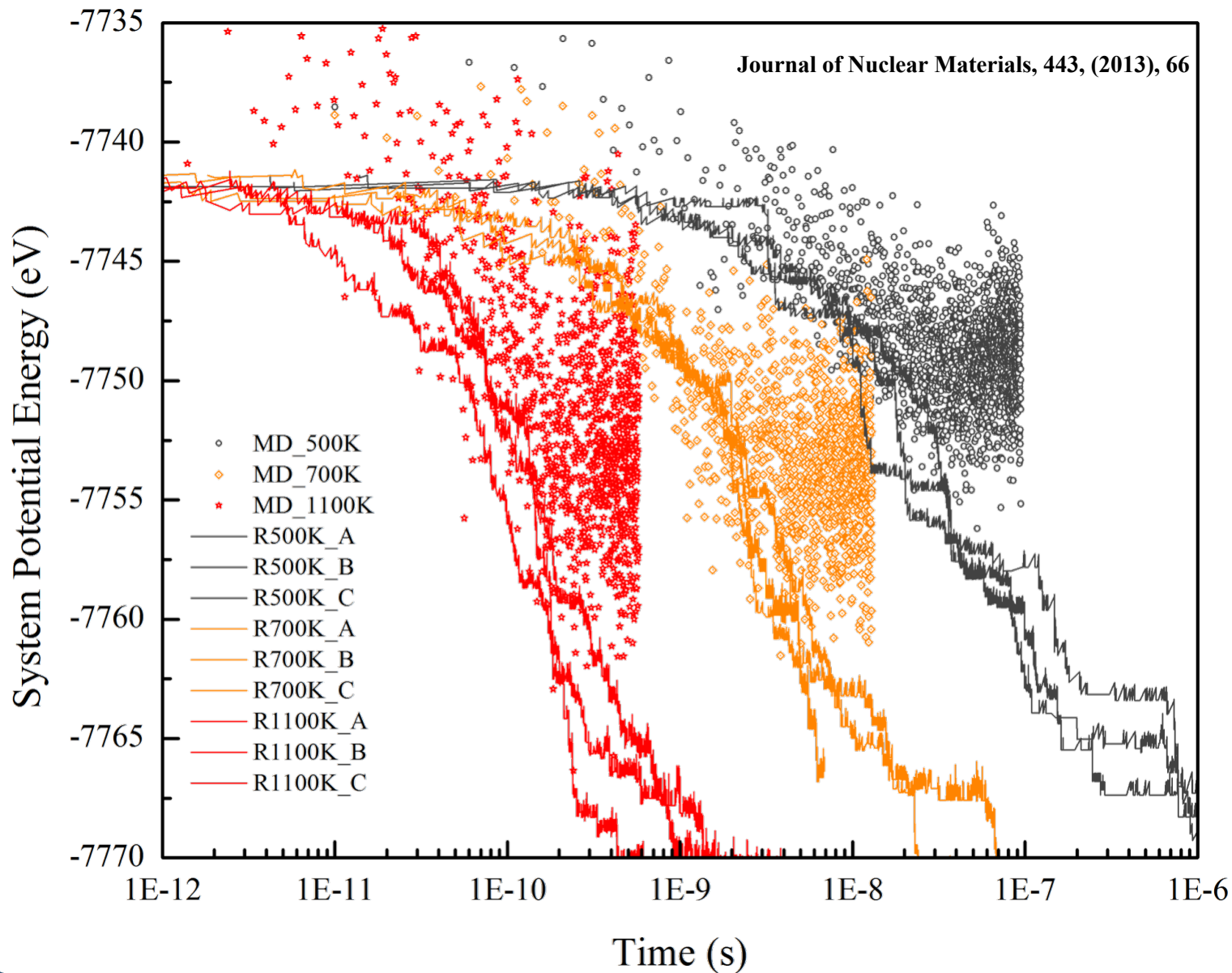
SEAKMC

0.005-0.1 ms at 50 °C

*Journal of Nuclear Materials, 443, (2013), 66*



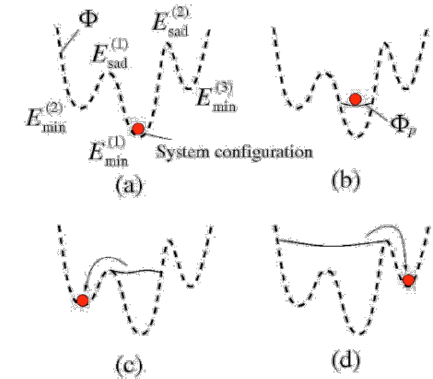
# Vacancy Clustering in Iron: SEAKMC vs MD



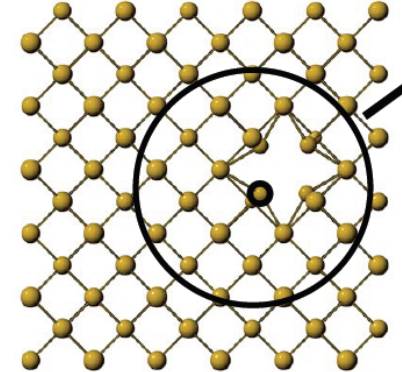
*SEAKMC agrees well with MD at high temperatures*

# Where does the difference come from?

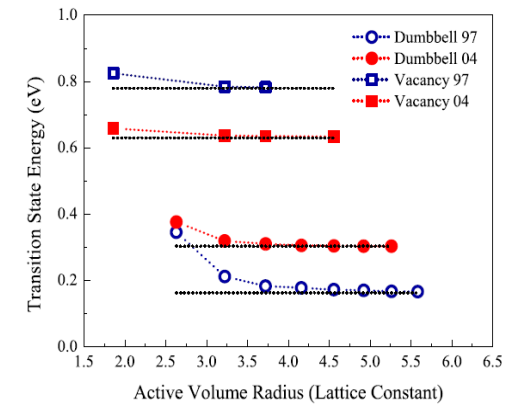
- ABC+KMC
- One saddle point (of minimum energy barrier) is used per KMC step
- Missing low-energy reaction paths
- **kART**
- **Topological classification of configurations based on the 2<sup>nd</sup>/3<sup>rd</sup> nearest neighbors**
- **Basin Filling Methods**
- **SEAKMC**
- **Active volumes are sufficiently large**
- **Nearly complete sampling of saddle points**



*J. Chem. Phys.* 130, (2009) 224504



*Phys. Rev. B* 78, (2008) 153202



*Xu et al. J. Phys.: Condens. Matter* (2012)

*Beland et al, Computational Materials Science* 100, p124 (2015)



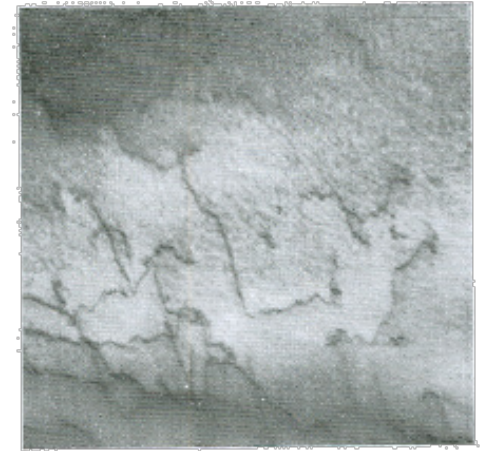
# Interstitial Loops -Unique Signature of Radiation Damage

- Eyre 1962: Discovery of interstitial loops in bcc Fe
- Masters 1964: Two population of loops  $\frac{1}{2} \langle 111 \rangle$  and  $\langle 100 \rangle$  loops
- $\frac{1}{2} \langle 111 \rangle$  and  $\langle 100 \rangle$  loops have very different mobility
- **Eyre-Bullough Mechanism 1965**

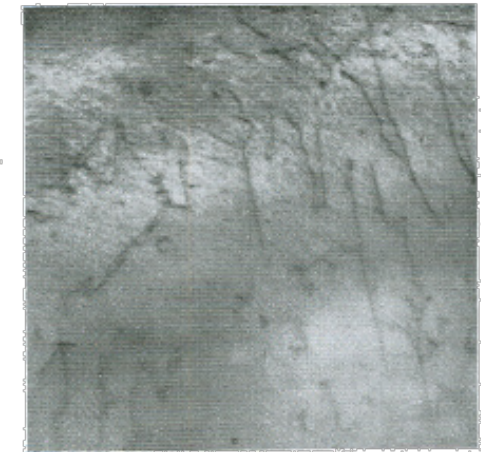
$$\frac{1}{2}[110] + \frac{1}{2}[001] = \frac{1}{2}[111]$$

$$\frac{1}{2}[110] + \frac{1}{2}[1-10] = [010]$$

- Because of the high stacking fault energy,  $\frac{1}{2}\langle 110 \rangle$  loop was not observed experimentally and spontaneously transform into  $\frac{1}{2}\langle 111 \rangle$  loops in simulations. Therefore, Eyre-Bullough mechanism is not applicable.



(a)



(b)

Dislocation arrangements in  $\alpha$ -iron after a dose of  $5 \times 10^{19} \text{ n cm}^{-2}$  followed by deformation. (a) Dislocations pinned by interstitial loops at  $x=10^{19}$ . (b) Loops left by dislocations breaking away from pinning points at  $x=10^{20}$ .

B. Eyre *Phil. Mag.* (1962)



# Recent Atomistic Studies

## Collision cascades

- SIA clusters are formed in cascades, mainly of  $\frac{1}{2}\langle 111 \rangle$  type

## Mutual interaction of dislocation loop

*Marian 2002: proposed a modified Eyre-Bullough Mechanism*

$$\frac{1}{2}[111] + \frac{1}{2}[00-1] = \frac{1}{2}[110]$$

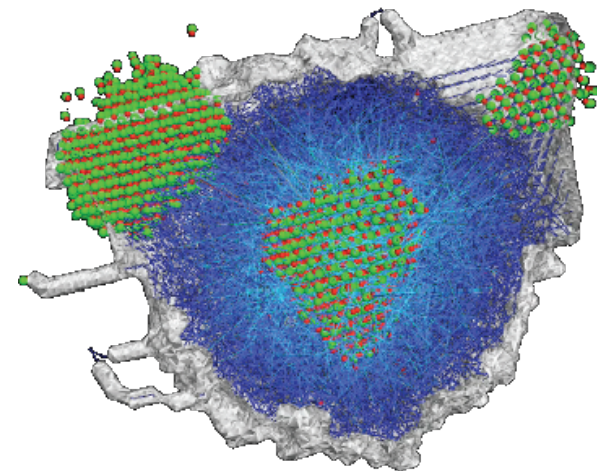
$$\frac{1}{2}[110] + \frac{1}{2}[1-10] = [010]$$

*Terentyev 2008: MD simulations*

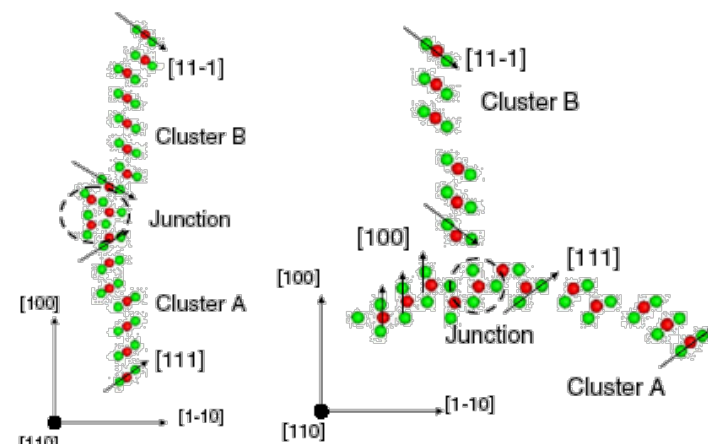
- Only  $\langle 111 \rangle$  loops are observed from mutual interactions

## Loop Stability

*Dudarev 2008: developed a model to include the temperature dependence of an anisotropic elastic self-energies of dislocations in iron*



*A. Calder et al. Phil. Mag. (2010)*



*D. Terentyev et al., J. Nucl. Mater. (2008)*

***The  $\langle 100 \rangle$  loop formation mechanism remains undetermined after fifty years since it was first discovered in 1962***

# Simulation Setup

- **Simulation methods:** SEAKMC and molecular dynamics
- **Interatomic potentials:** A97, A04, M07
- **System size:**  $27a_0 \times 27a_0 \times 27a_0$
- **Temperature:** From 0 K to 1200K
- **Interaction angle:** acute and obtuse
- **Interstitial cluster(IC) size:** 19,37,61
- **Active volume size:**  $4.5-7.5 a_0$

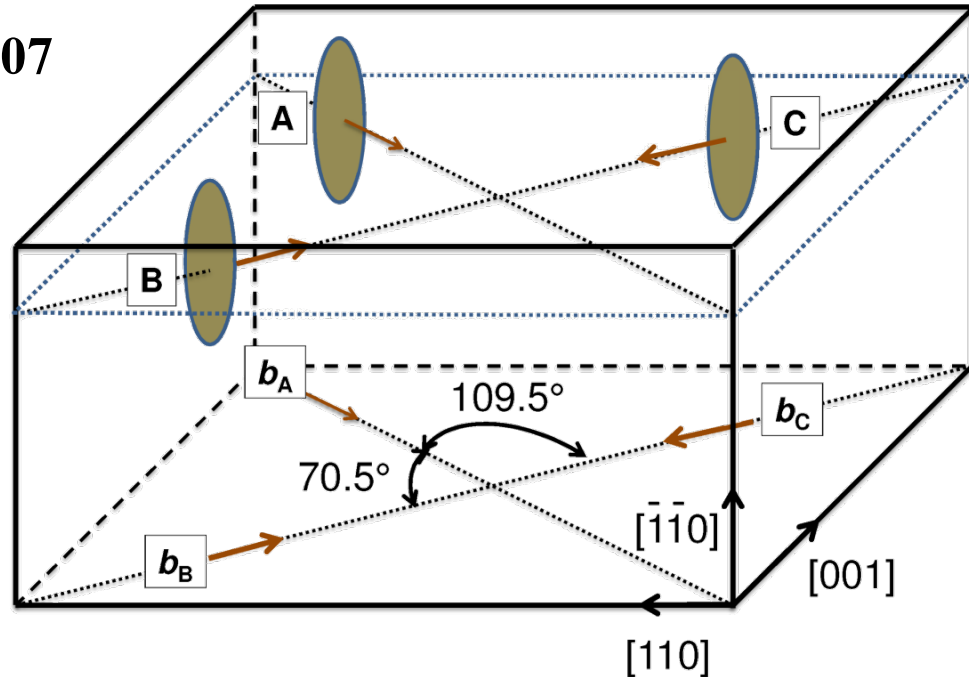
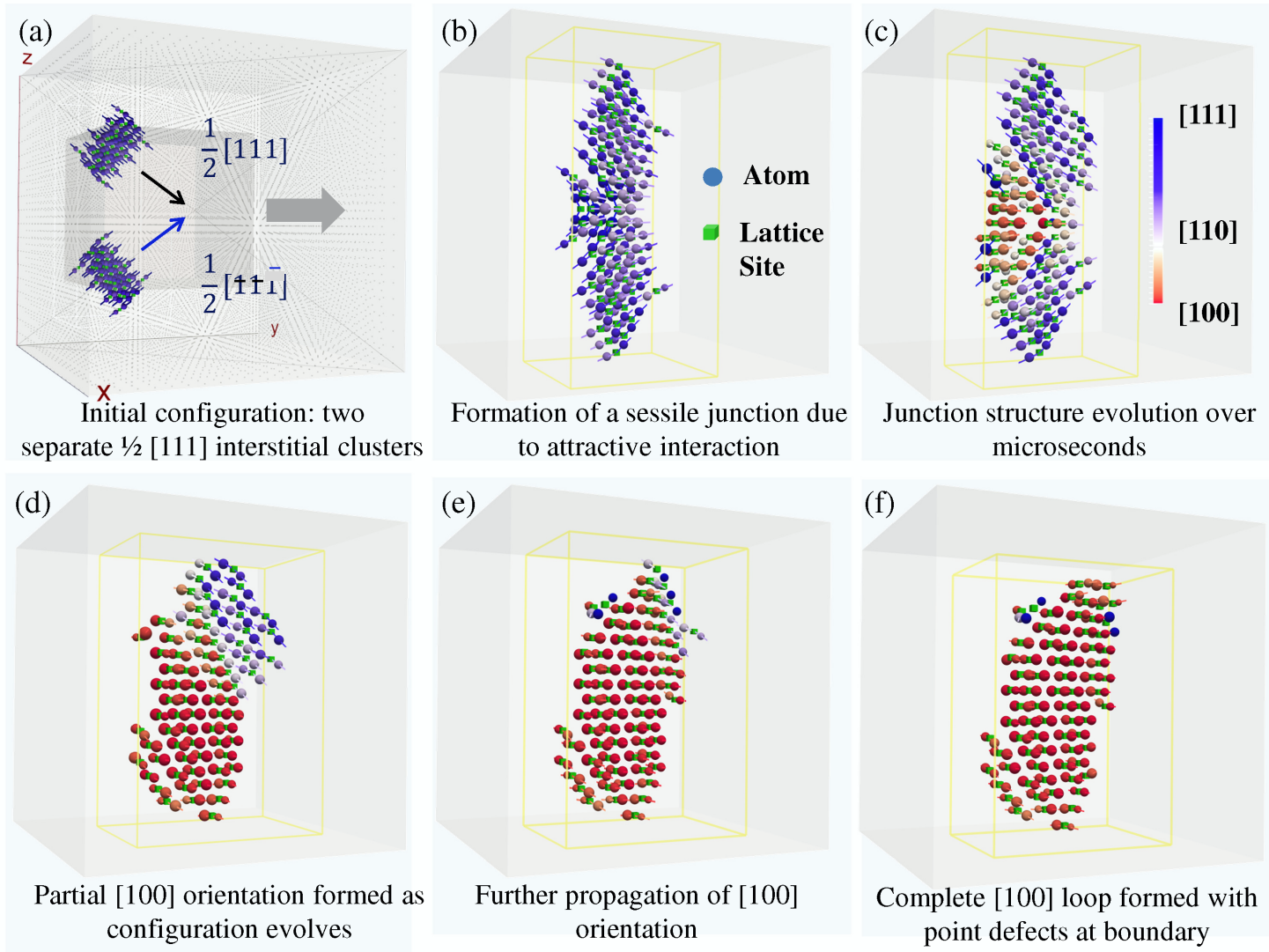


Illustration of  $\langle 111 \rangle$  type interstitial clusters moving in a  $\{110\}$  plane with their angle of intersection projected onto the corresponding base plane

# [100] Loop Formation Process from SEAKMC



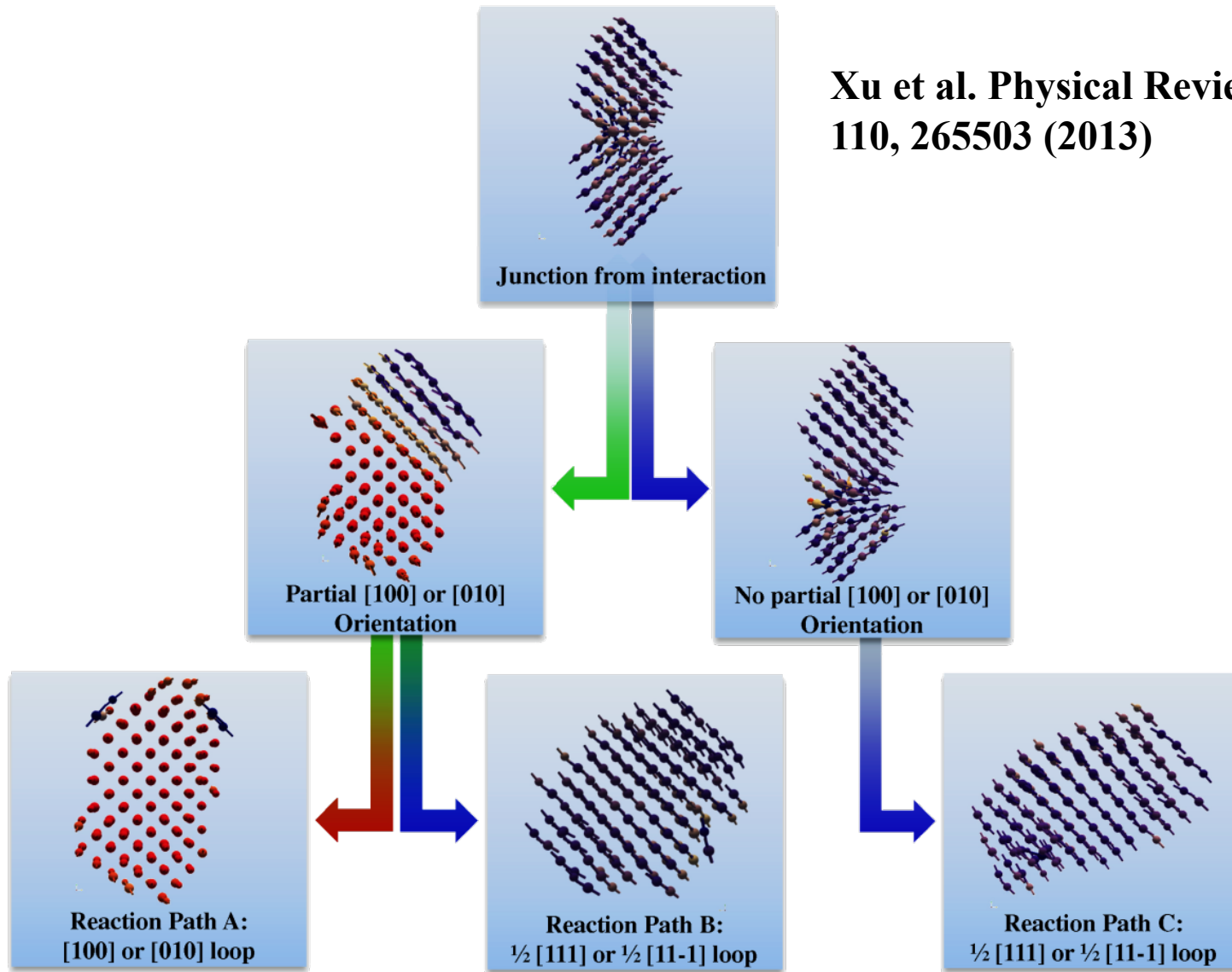
Xu et al. Physical Review Letters, 110, 265503 (2013), Journal of Alloys and Compound (2015)

*Never previously observed, distinctly atomistic process*

*Different from all previous proposed mechanisms*

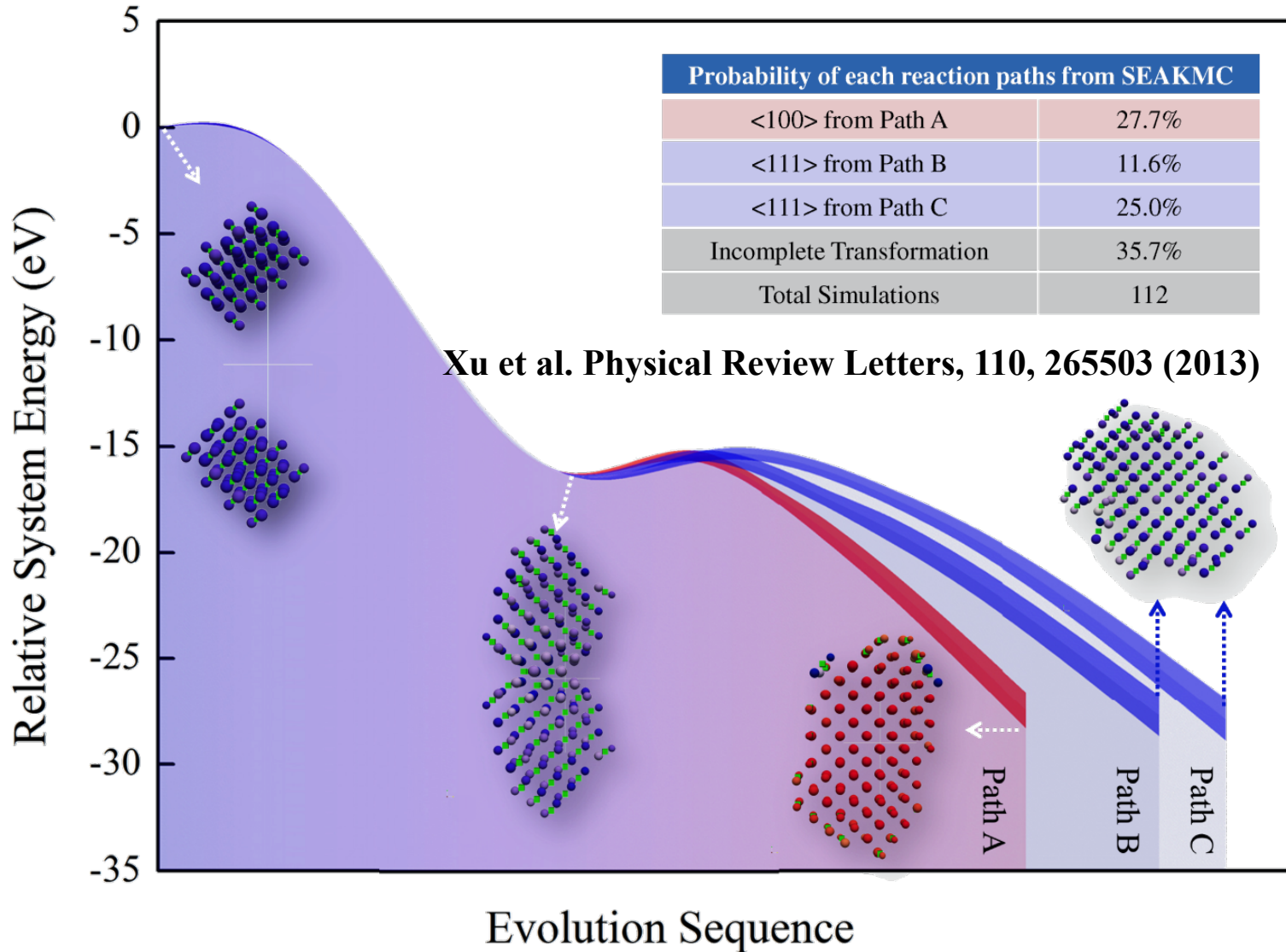
# Stochastic Process in Nature

Xu et al. Physical Review Letters,  
110, 265503 (2013)



*Different configurations may form from the same initial structure*

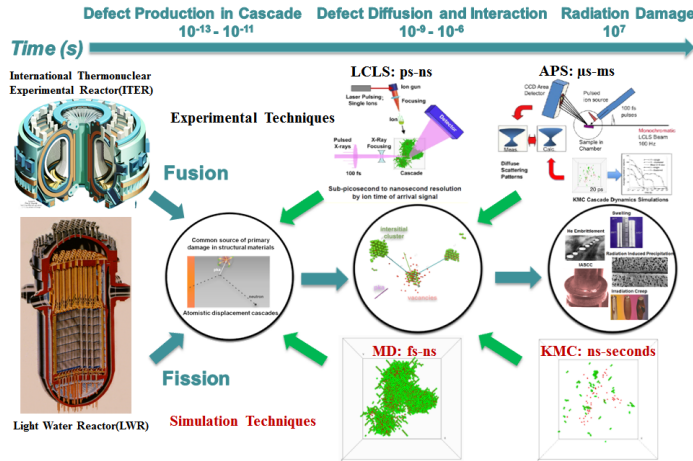
# Energetics of the Evolution Process



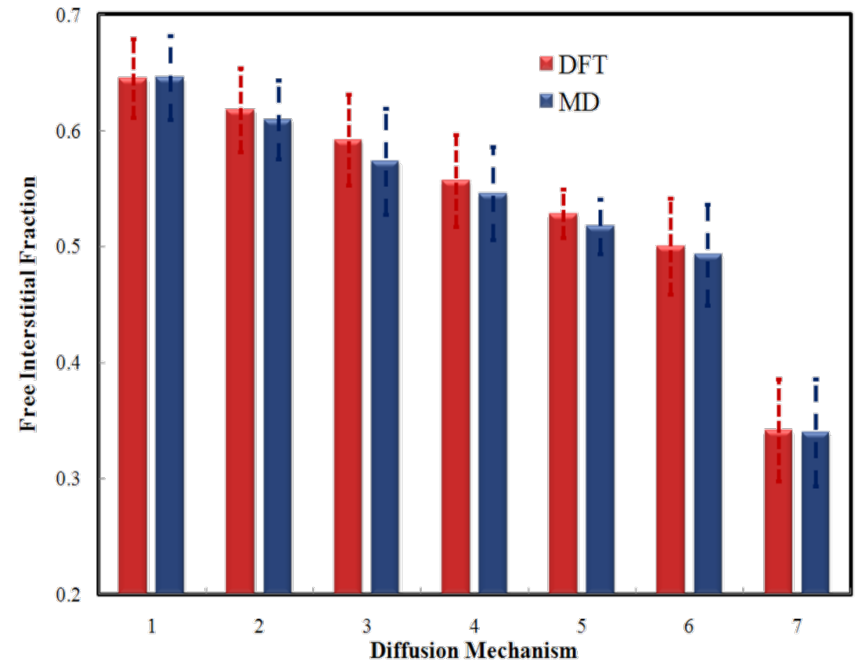
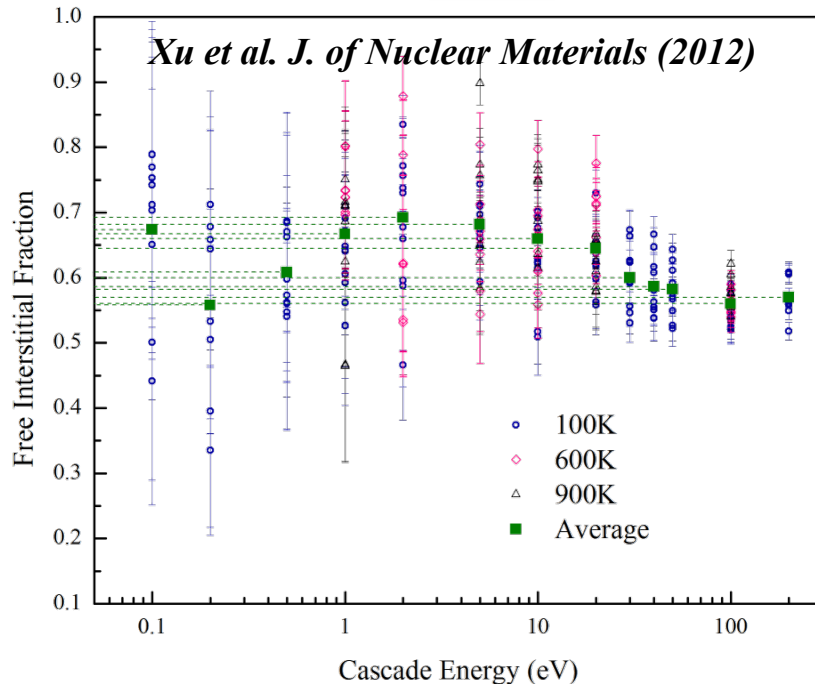
*MD employs high temperature to speed up the process, significantly increasing the stability of <111> loop due to its larger entropy*



# Cascade Annealing-Comparison of OKMC and SEAKMC



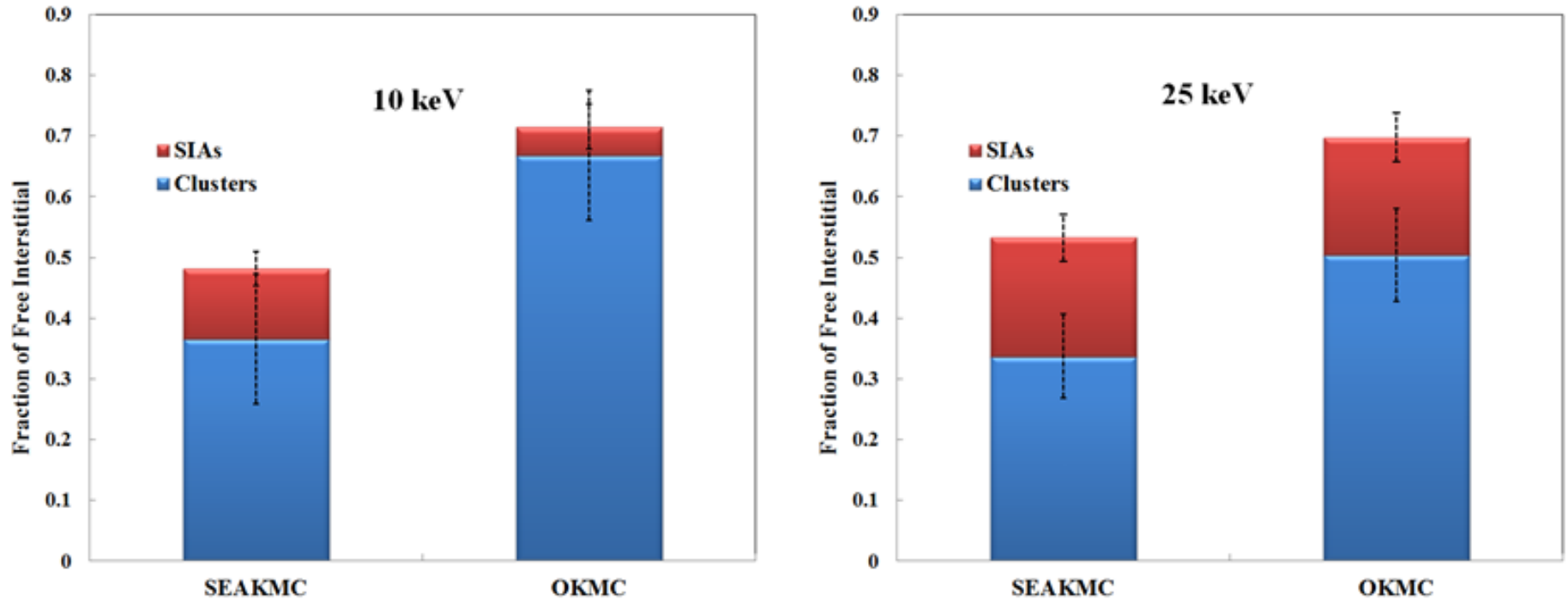
- Initial structure from MD cascade simulations
- Cascade energy is 10 keV and 25 keV
- System size: 128,000 and 250,000 , with an absorbing boundary condition
- Annealing temperature : 650 K



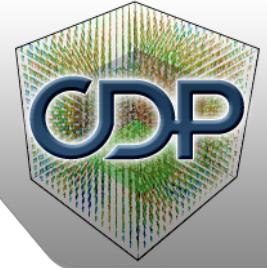
*Parameter-free SEAKMC provides different defect survival fractions*

# Comparison of OKMC and SEAKMC-Continued

Simulation were perform under the same condition using both methods



*Parameter-free SEAKMC provides different defect survival fractions*  
*SEAKMC can help OKMC to increase the accuracy of the simulations*



# Challenges

**On-the-fly KMC methods have made significant progresses.**

- *How to efficiently determine saddle points if a large number of atoms is involved in the transition states*
- *How to ensure sufficient sampling of saddle points for complex defects?*
- *How to validate the accuracy of on-the-fly KMC methods?*

**Thank you very much for your attention!**