

# Velocity pulsations in continuous turbidity currents: observations from the field, laboratory experiments and Direct Numerical Simulation

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# Two-Phase Continuum Models for Geophysical Particle-Fluid Flows



**Geoflo13:** Lillooet Lake



**Geoflo16:** Lillooet Lake + Xiaolangdi Reservoir + DNS + lab + linear stability analysis

# A global collaboration..



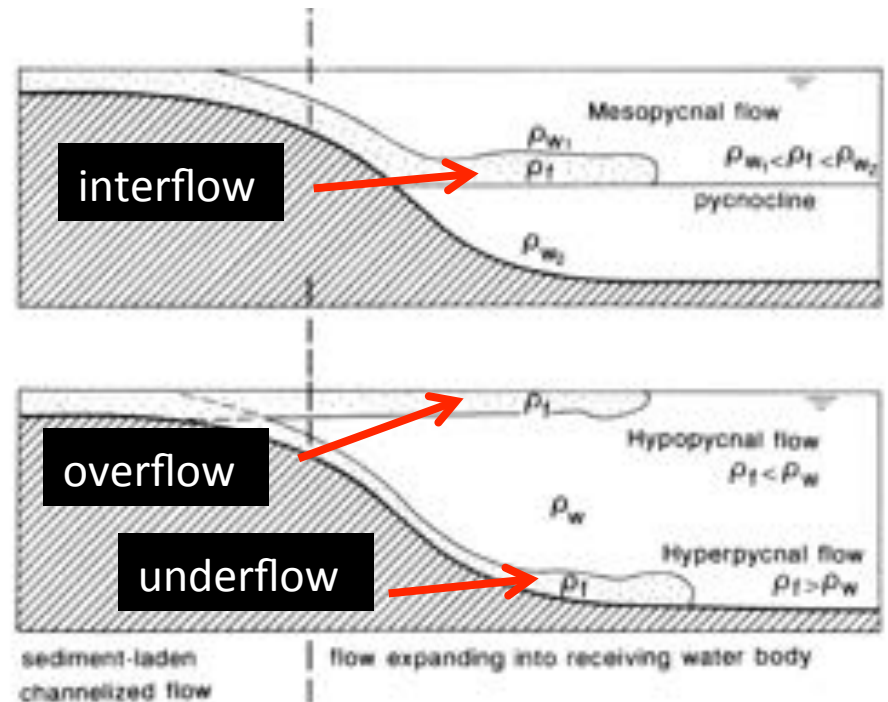
# Turbidity currents

- Gravity current driven by a density difference caused by **suspended sediment**

## Surge



## Continuous



from Mulder & Alexander (2001)

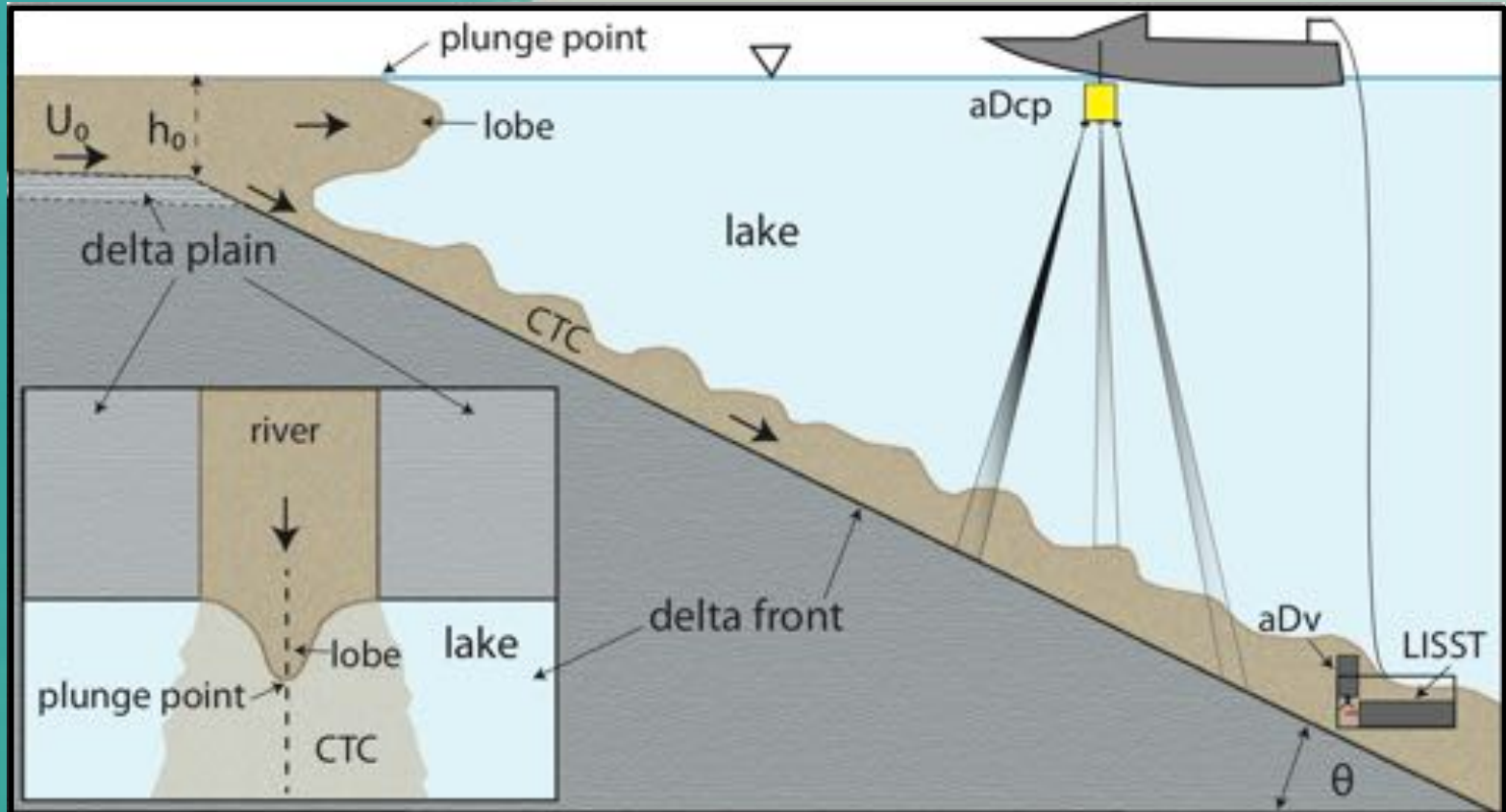


# Research Objectives

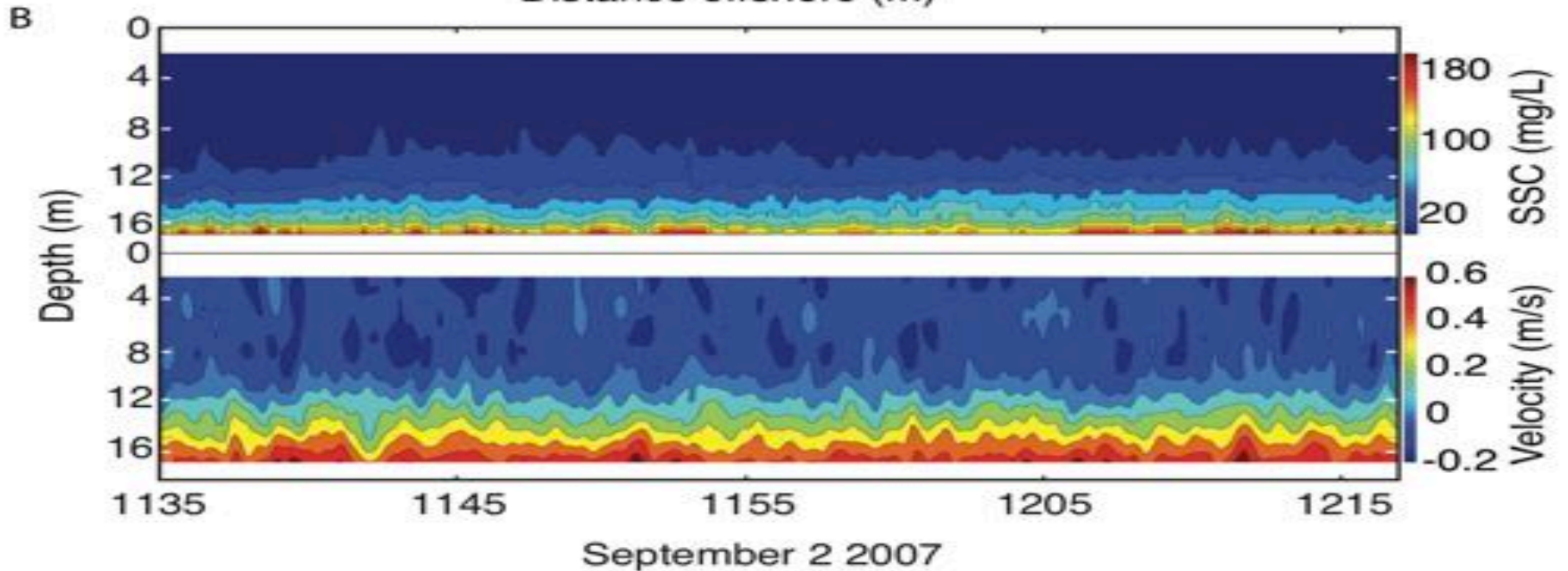
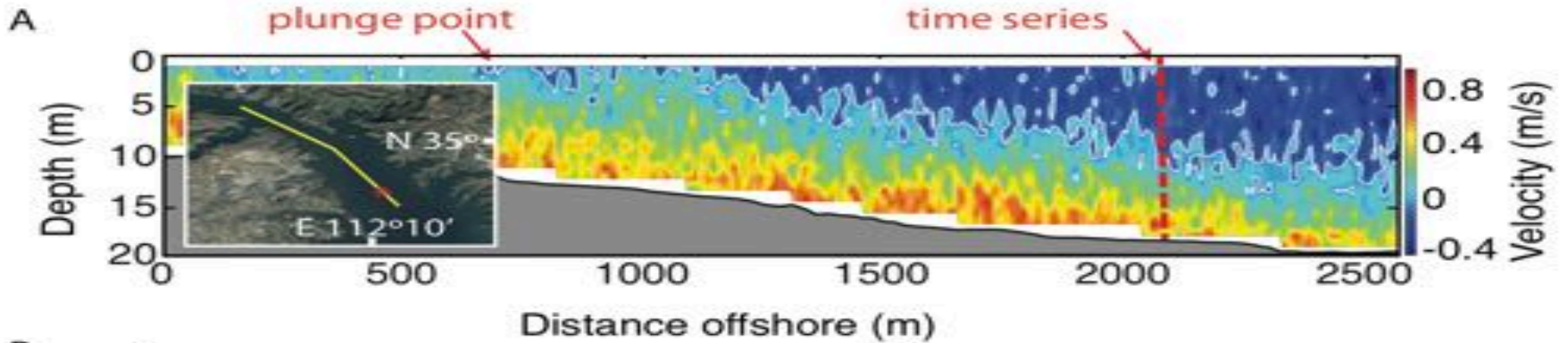
- Primary objective: to examine the **cause(s) of pulsing** in continuous, natural turbidity currents in the field using laboratory experiments, numerical simulations and linear stability analysis of stratified shear flows
- Stratified shear layer instability: large-amplitude, wave-like structures such as **Kelvin–Helmholtz (KH)** (*Brown and Roshko, 1974*), **Holmboe (H)** (*Smyth and Winters, 2003; Smyth et al., 2007*) and **Taylor-Caulfield (TC)** (*Taylor, 1931; Caulfield et al., 1995; Carpenter et al., 2013; Guha and Lawrence, 2014*).

# Field Methods

- Transects and time series: velocity, temperature, suspended sediment concentration and particle size in **Lillooet Lake** and **Xiaolangdi Reservoir**

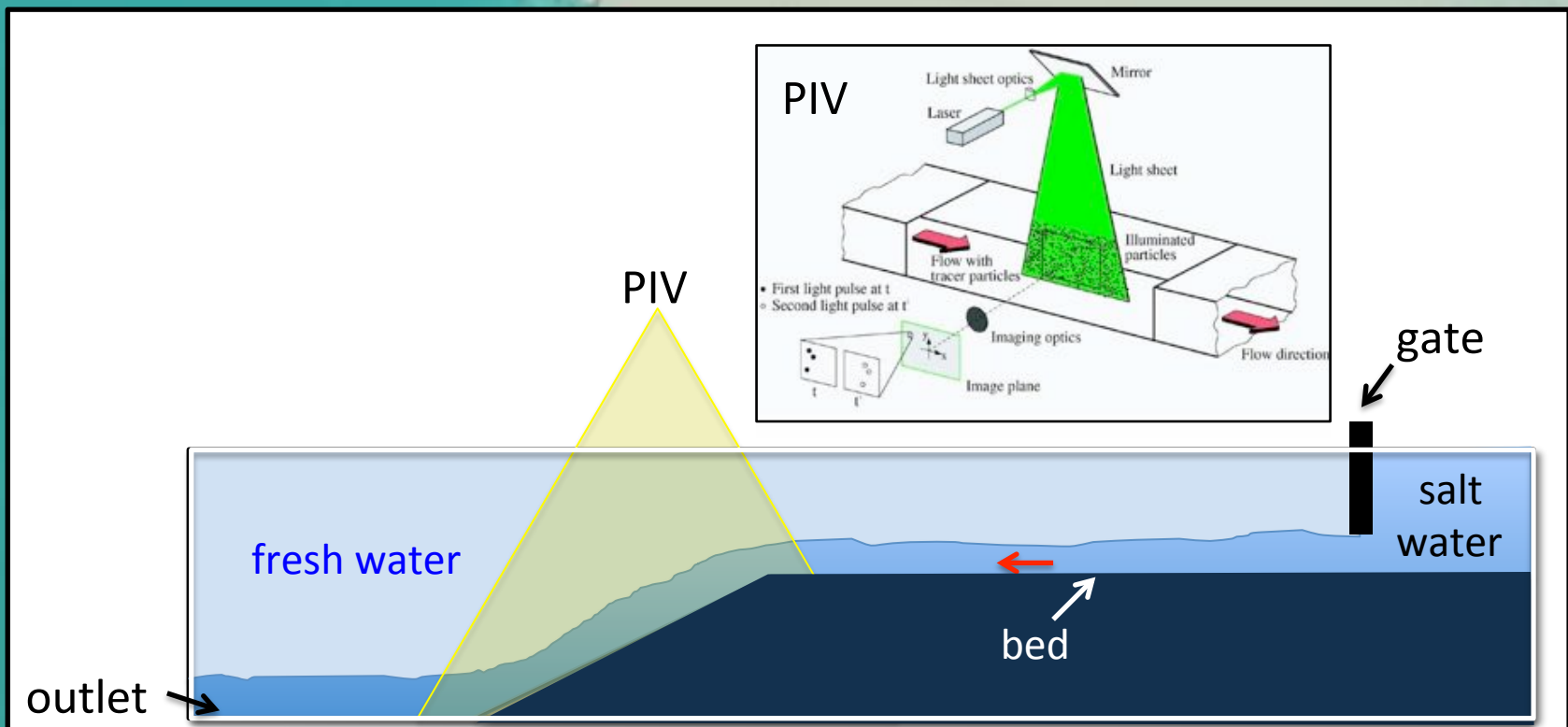


# Field Results



# Laboratory Methods

- Saline **gravity current** experiments: 6 m long open glass-wall tank with an internal channel
- Velocity: Particle Imaging Velocimetry (PIV)





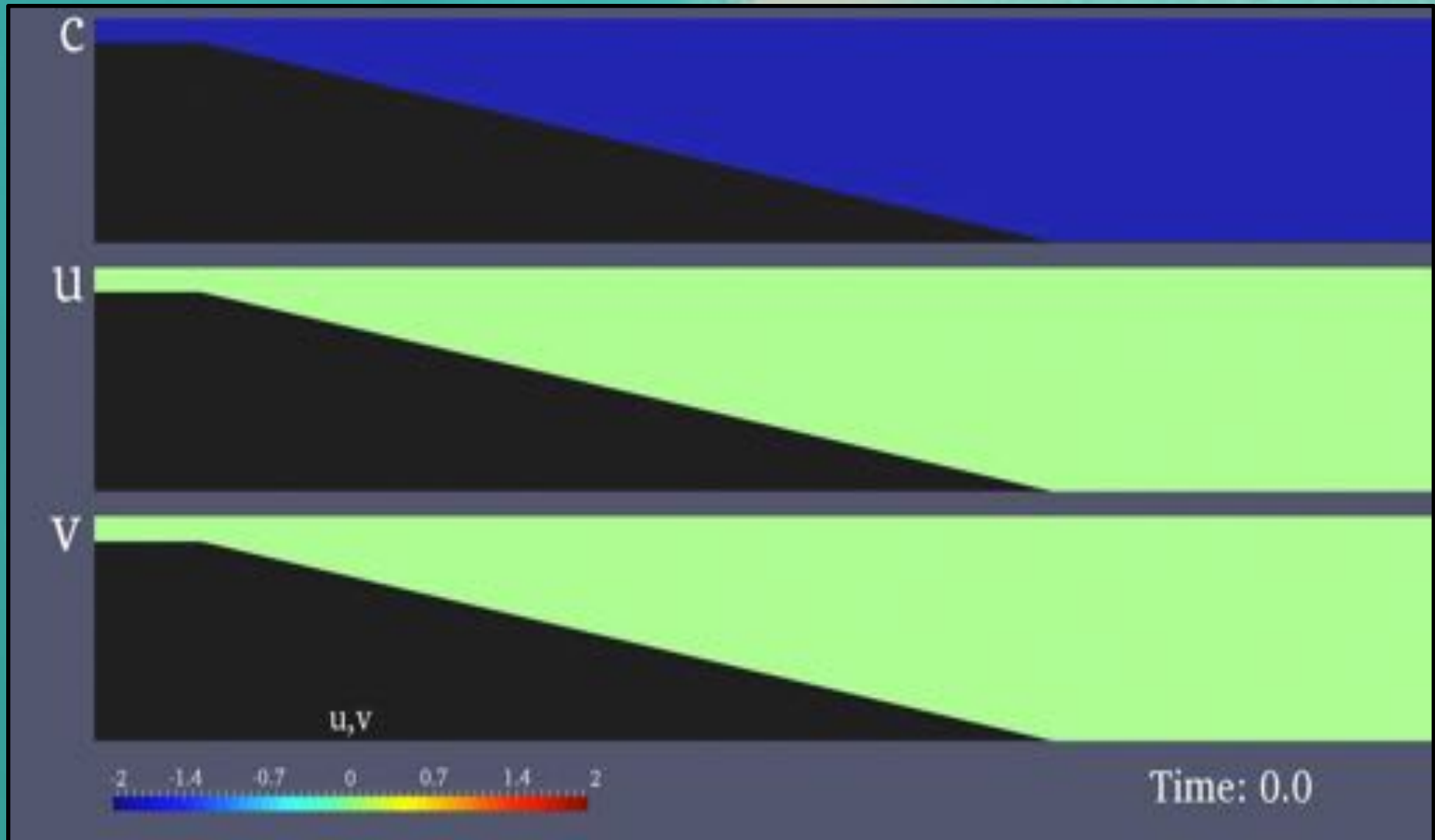
# Laboratory Results



# DNS Methods

- Software **TURBINS** (e.g., Nasr-Azadani and Meiburg, 2014): direct numerical simulations (DNS) of continuous two-dimensional gravity and turbidity currents
- **Simulations:** combination of straight and segmented bed slopes; gravity and turbidity currents with settling velocities consistent with sand ( $150\mu\text{m}$ ) and silt-clay ( $30\mu\text{m}$ )
- This study: **gravity currents** - similar to silt-clay turbidity currents and saline gravity currents

# DNS Results



# Linear Stability Analysis

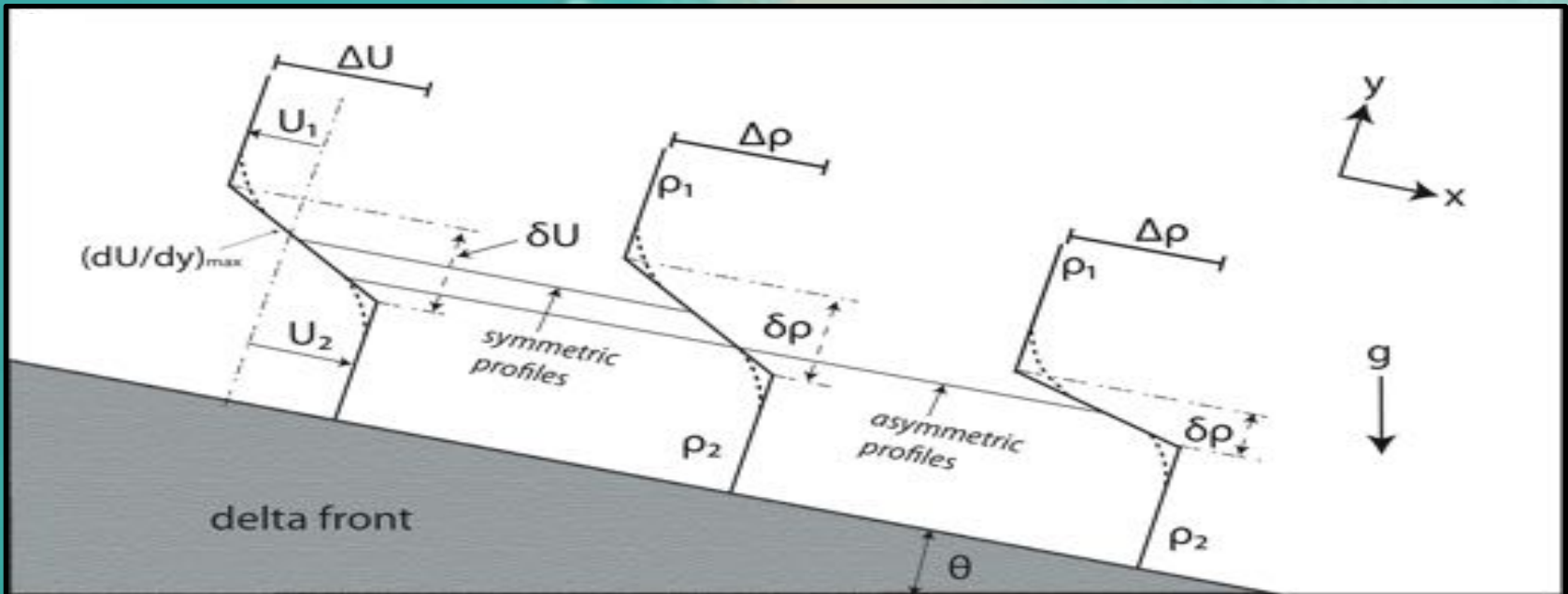
- Linear stability analysis: evolution of stratified shear layers is based on the **Taylor-Goldstein (TG)** equation (e.g., Lawrence et al., 2013):

$$w'' + \left[ \frac{N^2}{(U - c)^2} - \frac{U''}{U - c} - k^2 \right] w = 0$$

- Analytical solutions: possible assuming **piecewise** velocity and density profiles
- Velocity and density profiles: expressed non-dimensionally by the **bulk Richardson Number (J)**, **wave number ( $\alpha$ )**, and the **scale ratio (R)** of shear layer thickness to density layer thickness



# Linear Stability Analysis



$$J_L = g' h / \Delta U^2 \quad \text{where:} \quad g' = g \Delta \rho / \rho_2 \quad h = \Delta U / (dU / dy)_{\max}$$

$$\alpha = kh \quad \text{where:} \quad k = 2\pi / \lambda$$

$$R = \delta U / \delta \rho$$

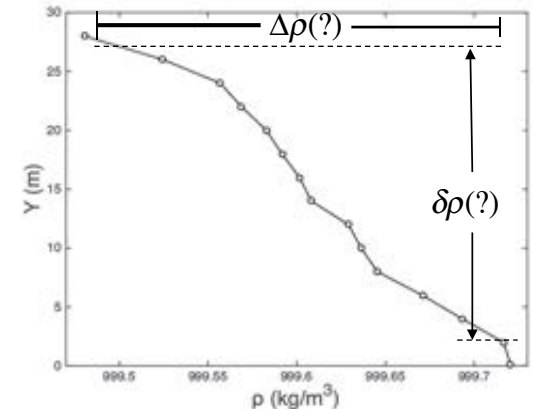
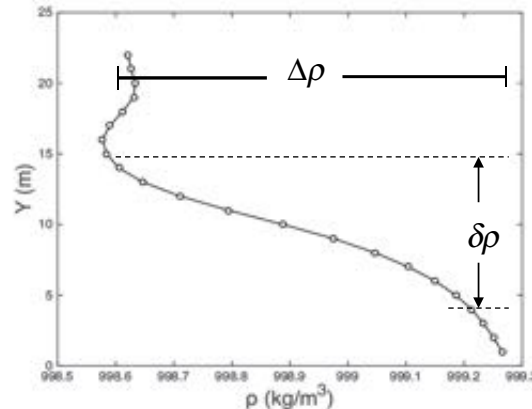
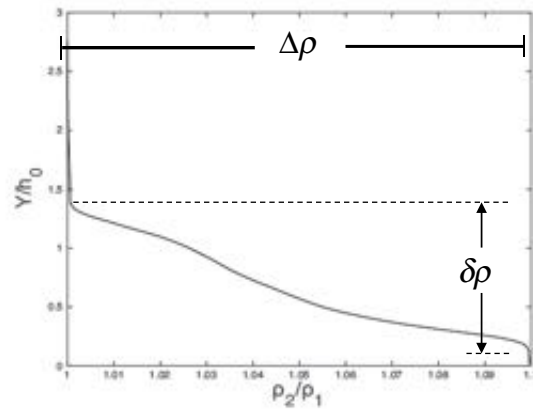
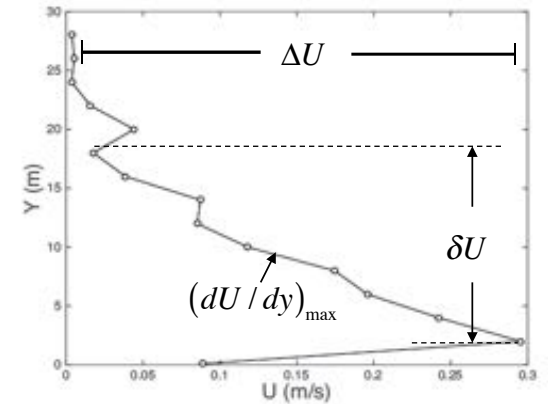
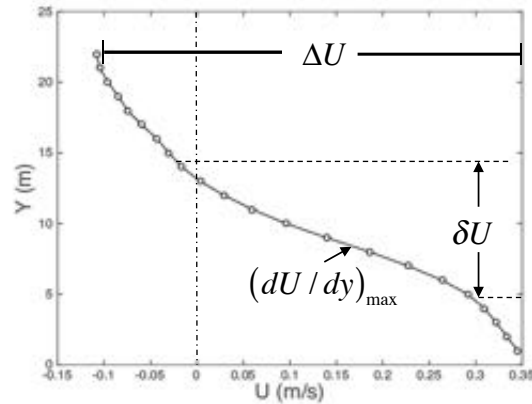
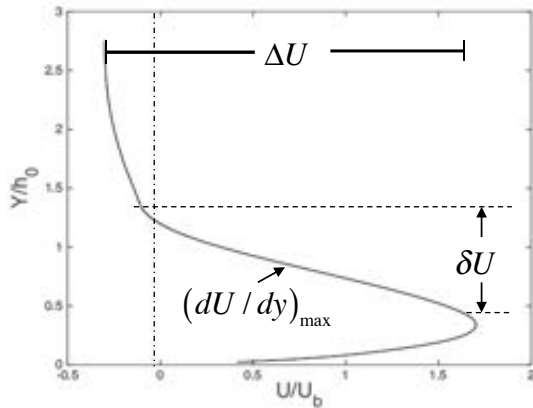
Based on: Lawrence et al. (1991, 2013), Negretti et al. (2008), Khavasi et al. (2013)

# Velocity and Density Profiles

DNS

Lillooet Lake  
08-22-2001

Lillooet Lake  
08-13-2008



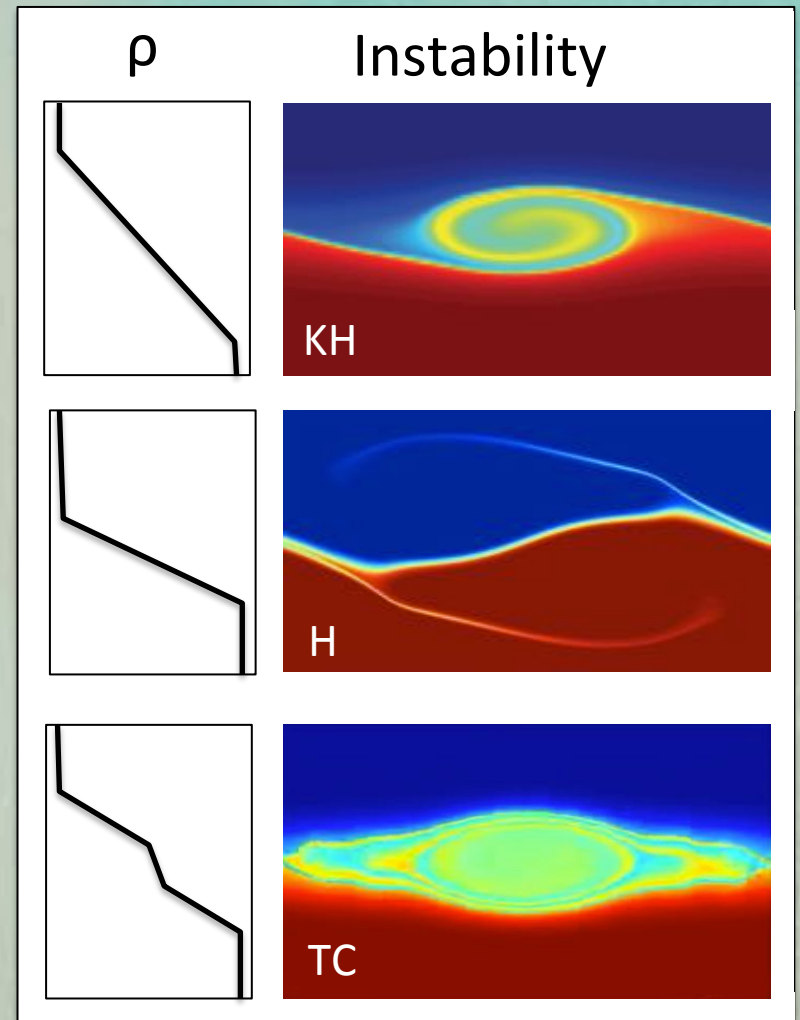
R = 0.8

R = 1

R = 0.6(?)

# Stratified Shear Layer Instabilities

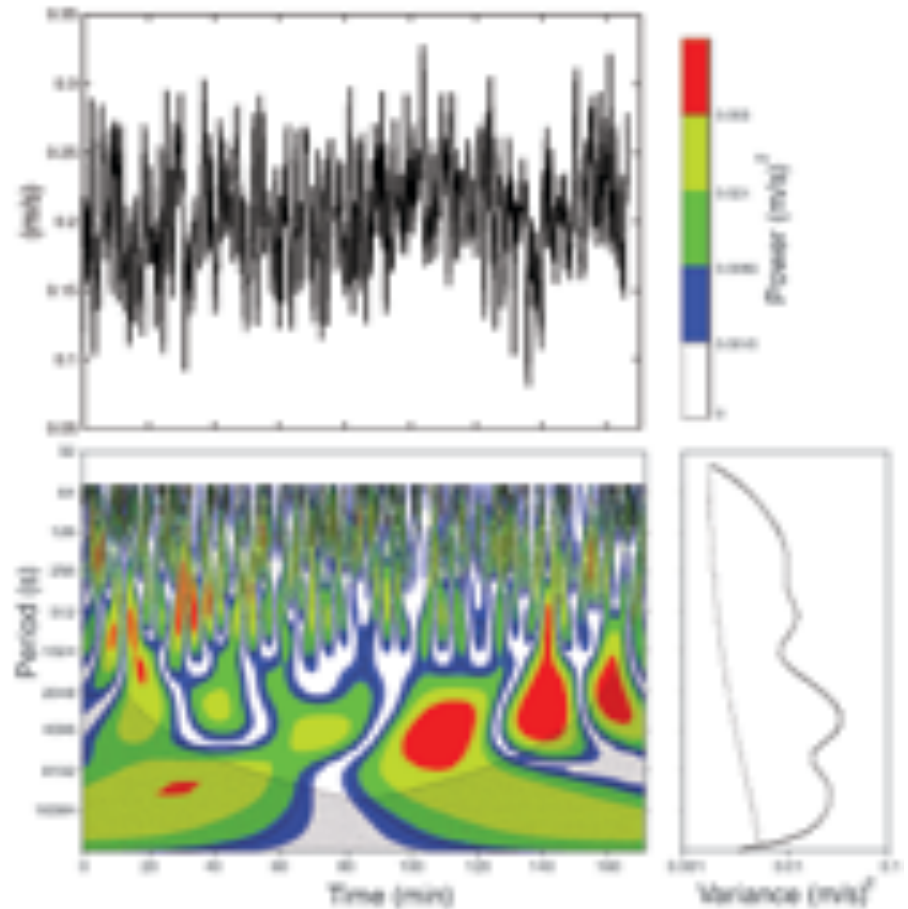
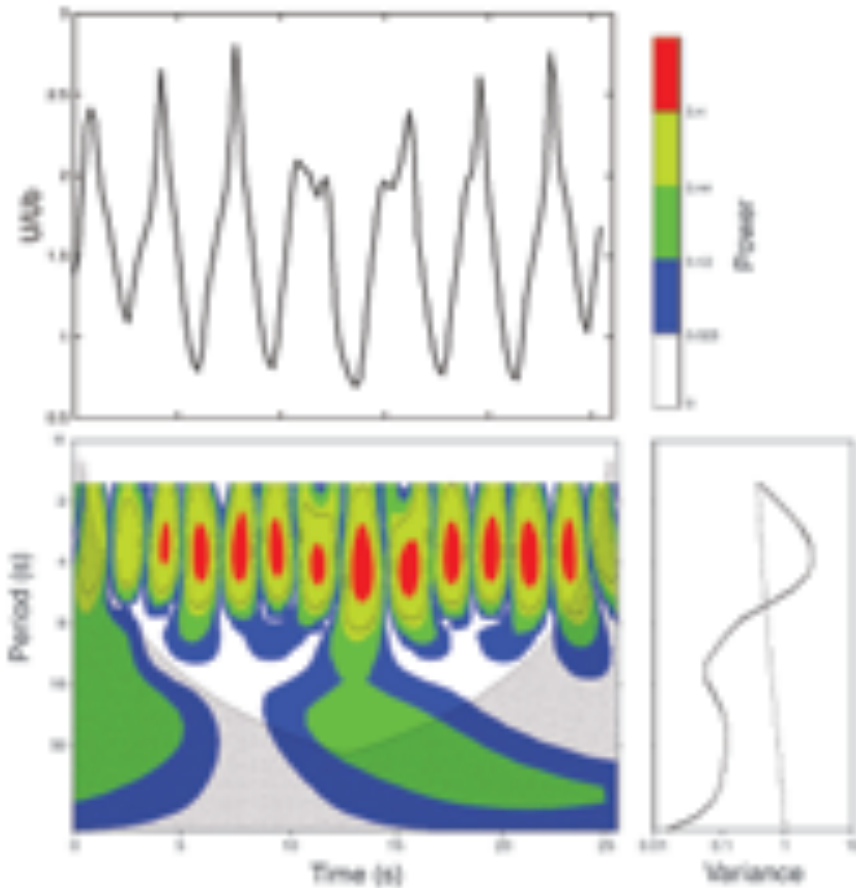
- **Kelvin-Helmholtz**
  - Two vorticity waves
  - Overturning billows
- **Holmboe**
  - Vorticity and gravity waves
  - Positive and negative cusps
- **Taylor-Caulfield**
  - Two gravity waves
  - Intermediate density layer



# Wavelet Analysis

DNS

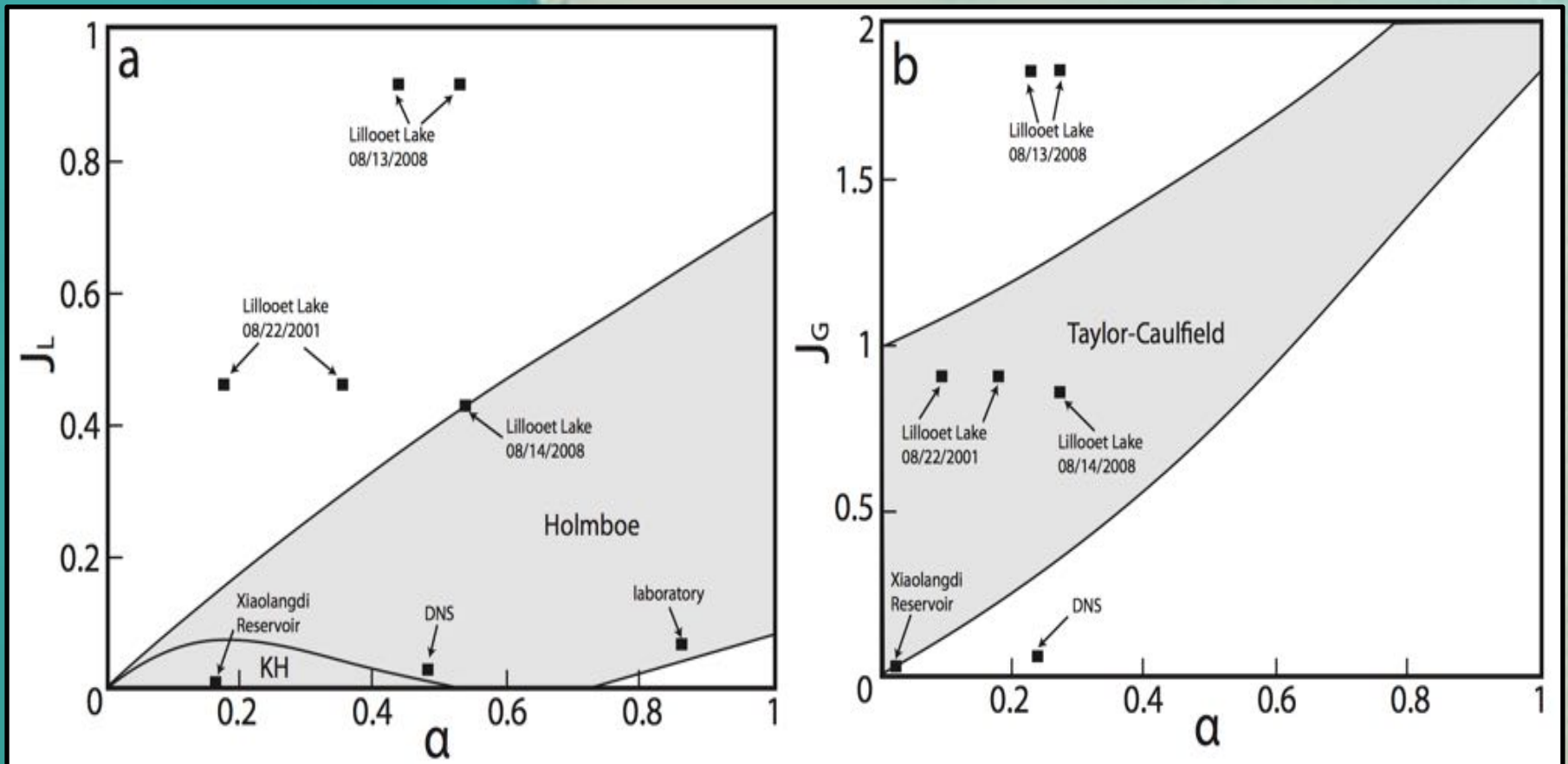
Xiaolangdi Reservoir





# Stability diagrams

Horizontal flow:  $\theta = 0$

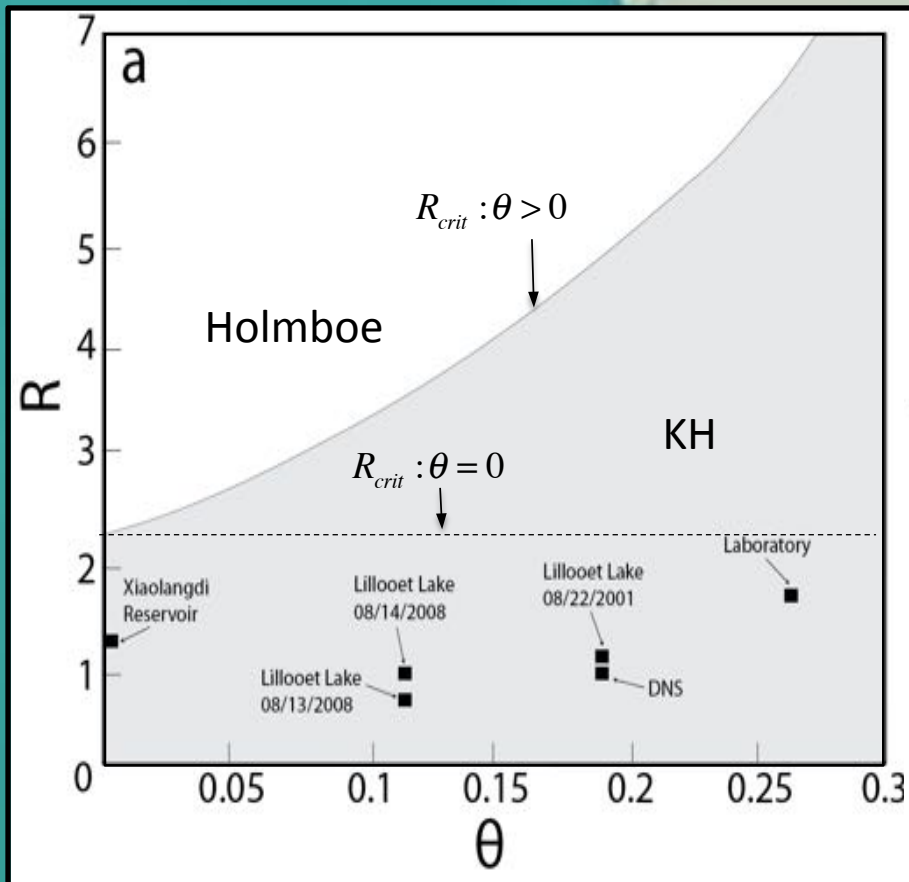


Based on: Lawrence et al. (1991, 2013)

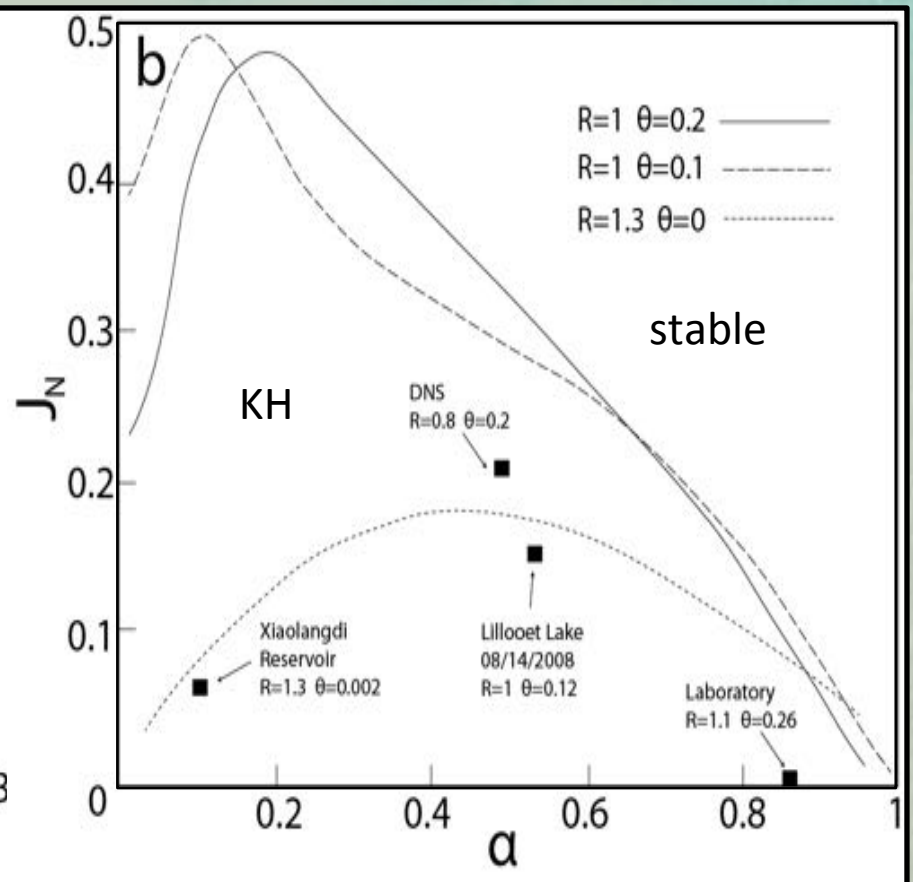
Based on: Guha and Lawrence (2014)

# Stability diagrams

Inclined flow:  $\theta > 0$



Based on: Khavasi et al. (2013)



Based on: Negretti et al. (2008)

# Conclusions

- **Causes of velocity pulsing**
  - Laboratory and DNS currents: KH instability
  - Stability analysis for horizontal flow: KH, H and TC instabilities
  - Stability analysis for inclined flow: primarily KH instability, H and TC instabilities at large values of bulk Richardson number?
- **Continuous turbidity currents**
  - Caulfield et al. (1995): “all three instabilities (*KH*, *H*, *TC*) can be observed simultaneously at markedly different wavelengths and phase speeds for extended periods of time, even though linear theory may predict significantly different growth rates”



Danke!