

# Simulation of charge transfer in DNA using QM/MM methods

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T. Kubar, B. Woiczikowski, M. Elstner  
TU Braunschweig

R. Guttierrez, R. Caetano, B. Song, G. Cuniberti  
TU Dresden

# Acknowledgements

TU Braunschweig:



B. Woiczikowski



T. Kubar

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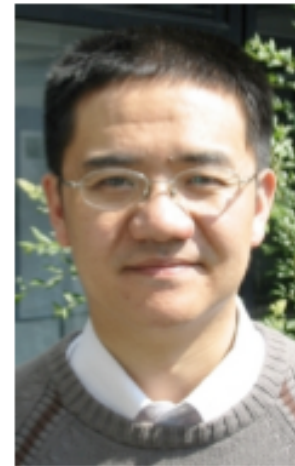
## Dresden group



G. Cuniberti



R. Gutiérrez



B. Song

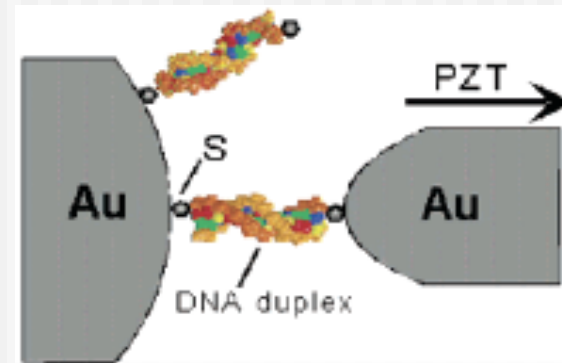


R. Caetano

# Conduction and charge transfer in DNA

## Physical experiments:

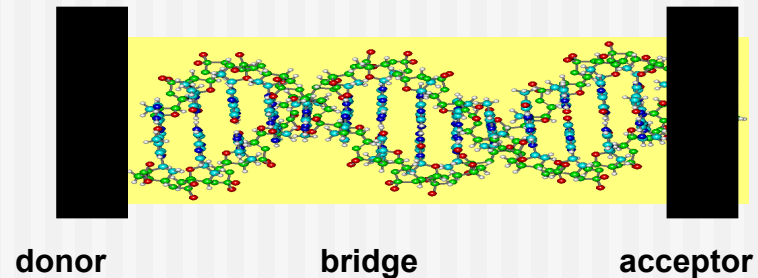
- DNA contacted by gold leads
- Current measurements



*B. Xu et al., Nano Lett. 4, 1105 (2004)*

## Chemical experiments:

- Charge carrier injection
- long range transfer over several 100 nm



- conduction?
- Transport mechanism?

# Theoretical description

## Theoretical Physics:

- tight binding Hamiltonian+ Landauer theory

$$H = \sum_i \varepsilon_i c_i^\dagger c_i + \frac{1}{2} \sum_{ij} T_{ij} (c_i^\dagger c_j + c_j^\dagger c_i)$$

$$G_D(E) = (E - H_D^{\text{KS}} - \Sigma_L - \Sigma_R)^{-1}$$

$$T(E, V) = \text{tr}[\Gamma_L G_D^r \Gamma_R G_D^a]$$

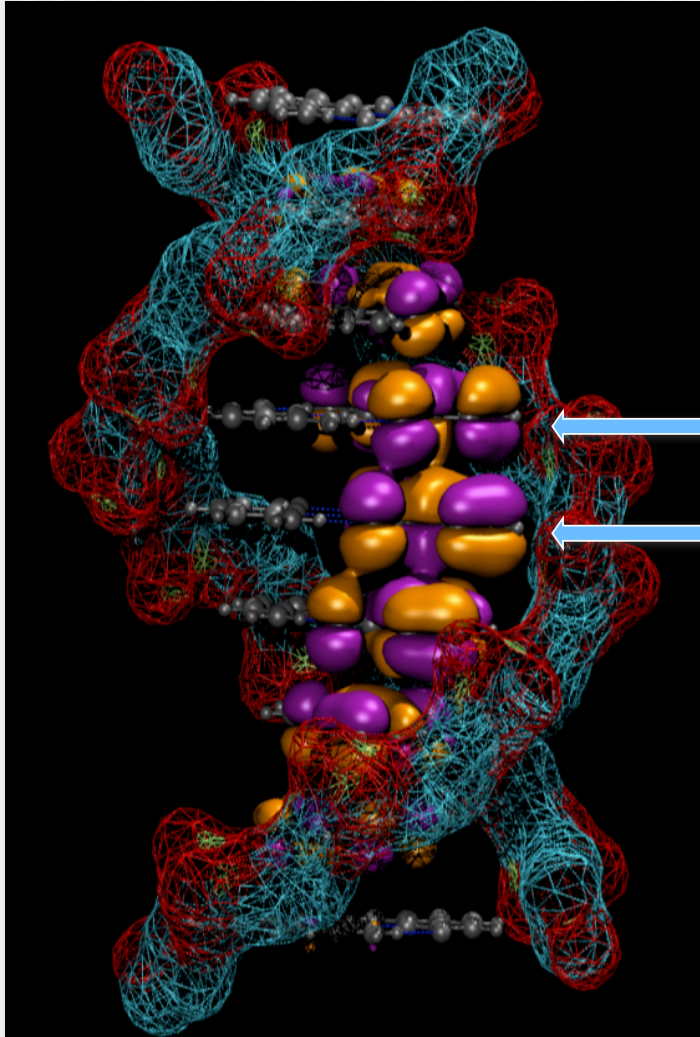
$$I(V) = \frac{2e}{h} \int_{\mu_1(V)}^{\mu_2(V)} T(E, V) dE$$

## Theoretical Chemistry:

- superexchange: coherent tunneling
- thermal induced hopping

$$k = \frac{2\pi}{h} |T_{ij}|^2 \times \text{FC}$$

# Model



Base i

$\epsilon_i$  = ionisation potential

Base j

$T_{ij}$   $\rightarrow$  charge transfer matrix elements

Marcus theory:

$$\Delta G = \epsilon_i - \epsilon_j$$

$$H_{DA} = T_{ij}$$

$$k_{DA} = \frac{2\pi}{\hbar} |H_{DA}|^2 \frac{1}{\sqrt{4\pi\lambda k_B T}} \exp\left[-\frac{(\Delta G^0 + \lambda)^2}{4\lambda k_B T}\right]$$

# Parameter determination

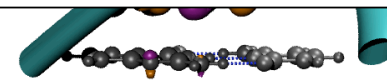
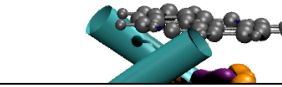
Parameters:  $\epsilon_i$  and  $T_{ij}$

calculat  
DNA ba

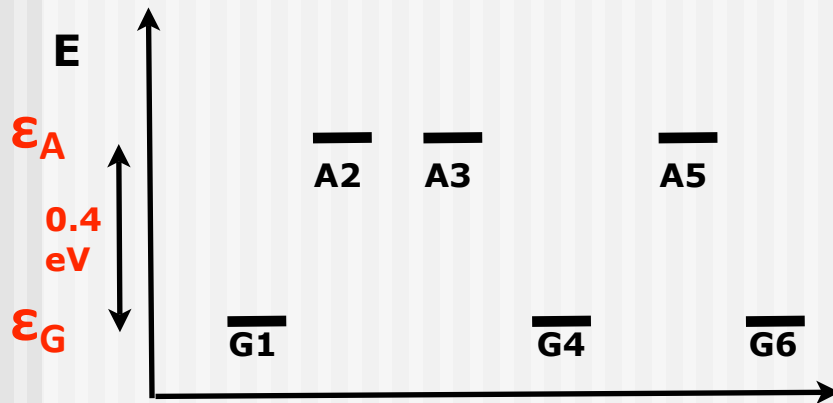
$\epsilon_i$  : HO  
 $T_{ij}$ : calc

=> sta

what about dynamics and solvent effects?



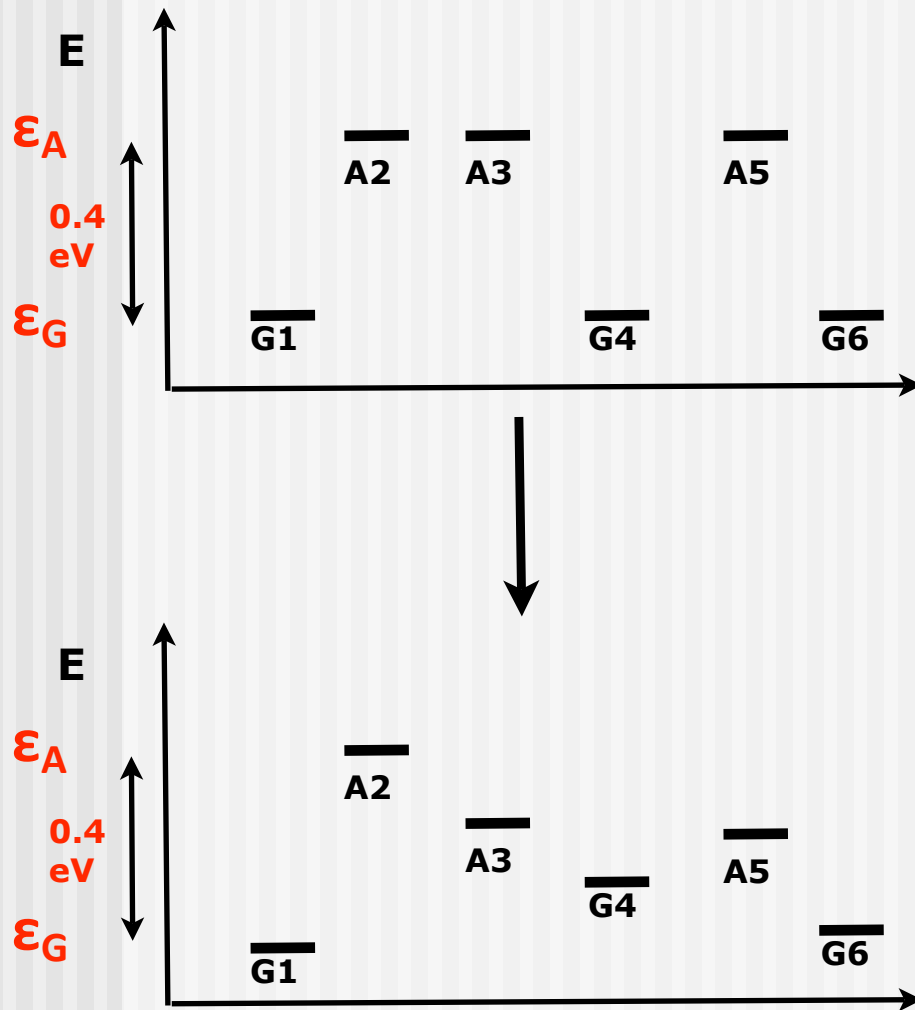
$\epsilon_i$   
 $T_{ij}$



**$A_n$ -bridges:**

$n = 1-4$ : superexchange  
 $n > 4$  : thermal induced hopping

# Effect of solvent and dynamics

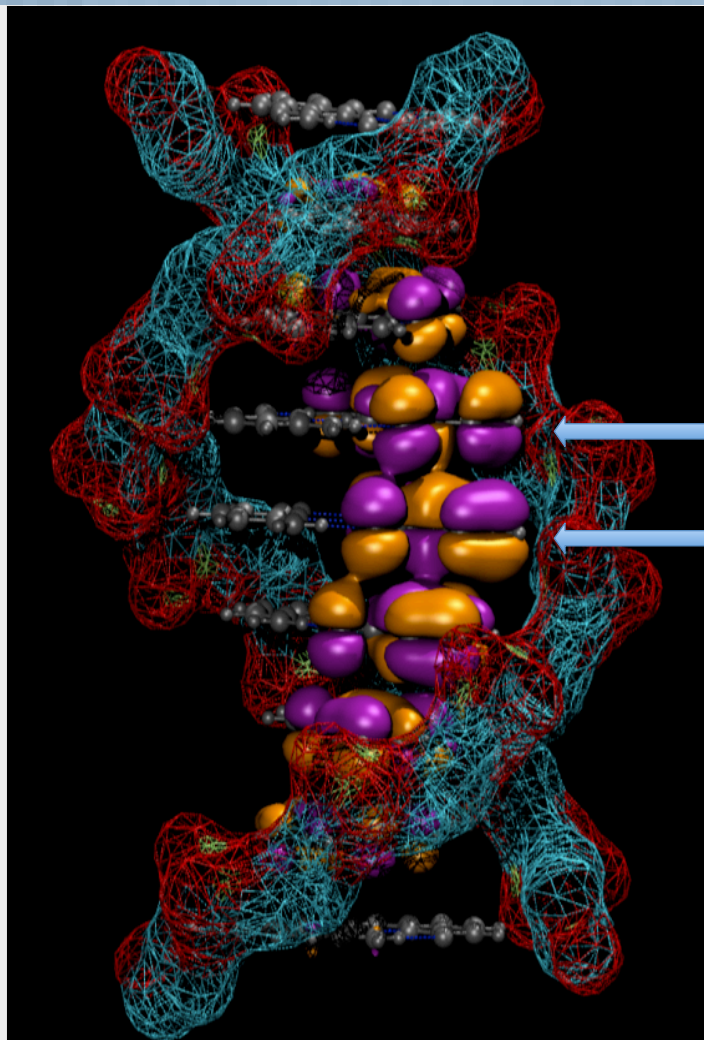


- calculate parameters 'on the fly' along classical MD trajectories

- include the interaction with DNA backbone, counterions and water using a QM/MM scheme

- for sufficient sampling, use a fast QM method: SCC-DFTB

## CT parameters from DFT



$$\epsilon_i = \langle \varphi_i | H | \varphi_i \rangle$$

$$T_{ij} = \langle \varphi_i | H | \varphi_j \rangle$$

site i

$\epsilon_i$ : energy of electron/hole on site i

site j

$T_{ij}$ : transfer integral from site i to j

Calculate  $\varphi_i$  and H from DFT/DFTB  
along classical MD trajectories → include:

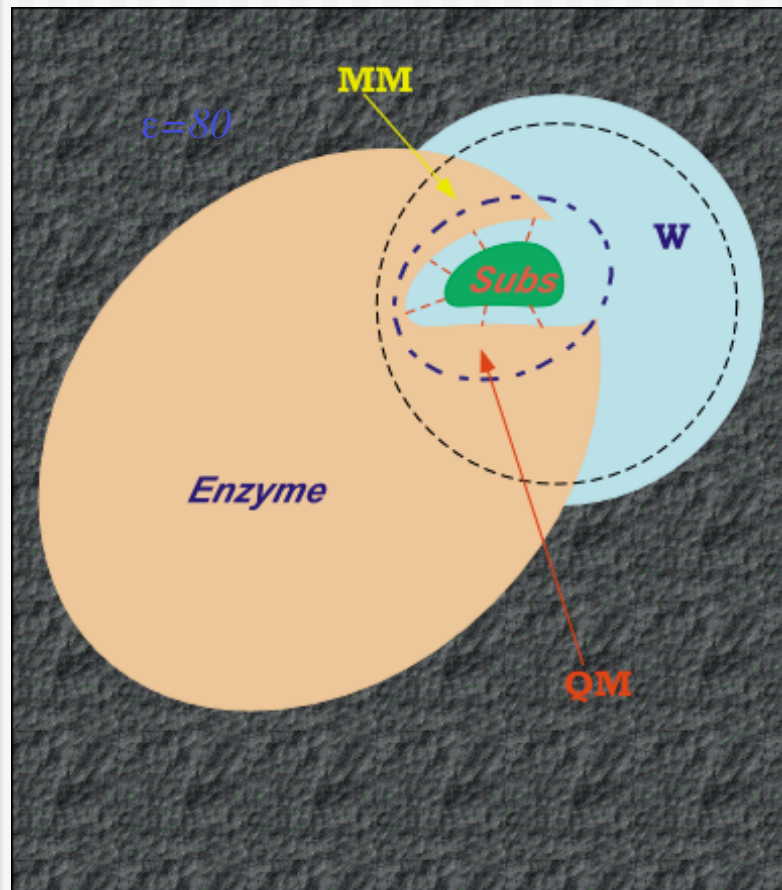
- **dynamical changes in parameters**
- **solvent effects**

Kubar et al., *J. Phys. Chem. B* **2008**, *112*, 7937

Kubar & Elstner, *J. Phys. Chem. B* **2008**, *112*, 8788



## Combined QM-MM Methods



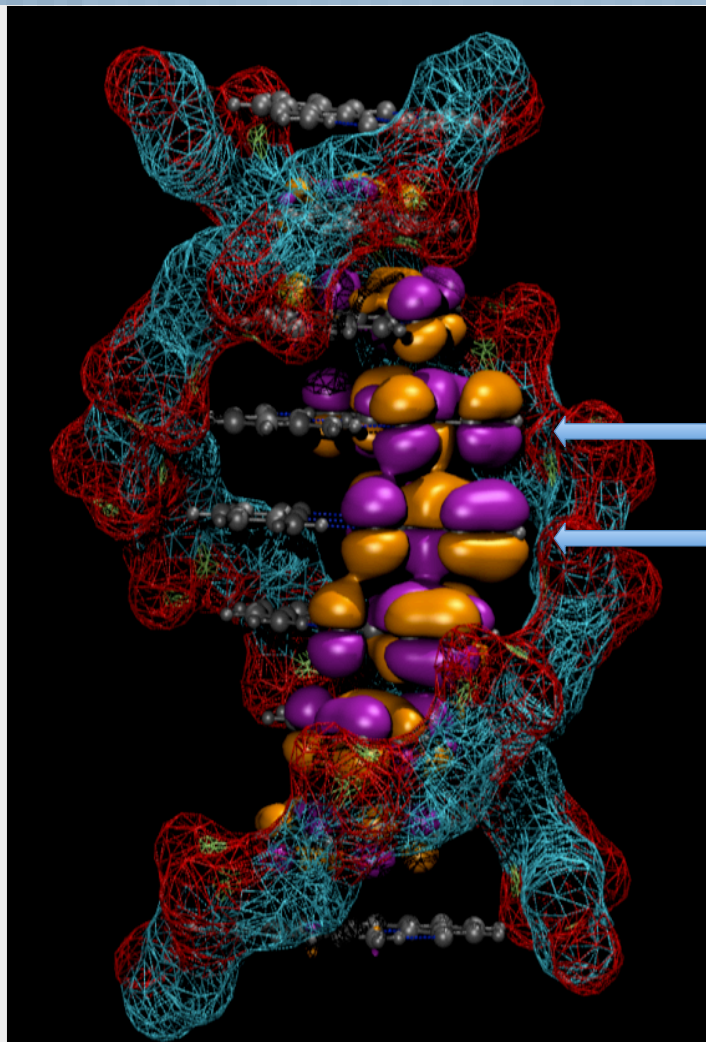
Quantum Mechanics (QM)

Molecular Mechanics (MM)

Polarization of the  
QM region through  
MM point charges

$$E = \langle \Psi | \hat{H}^{QM} + \hat{H}_{el}^{QM/MM} | \Psi \rangle + E_{van}^{QM/MM} + E^{MM}$$

## CT parameters from DFT



$$\epsilon_i = \langle \varphi_i | H | \varphi_i \rangle$$

$$T_{ij} = \langle \varphi_i | H | \varphi_j \rangle$$

site i

$\epsilon_i$ : energy of electron/hole on site i

site j

$T_{ij}$ : transfer integral from site i to j

Calculate  $\varphi_i$  and H from DFT/DFTB  
along classical MD trajectories → include:

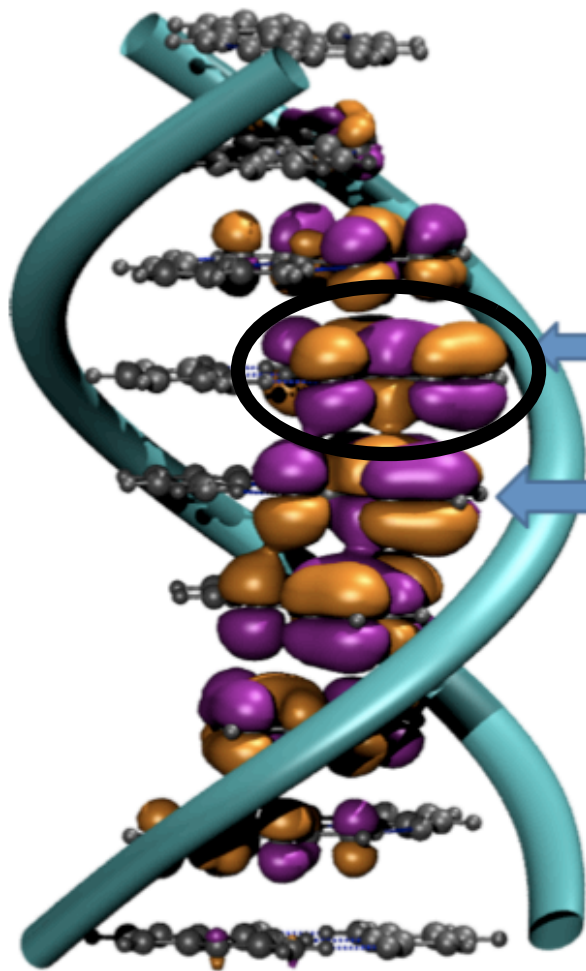
- **dynamical changes in parameters**
- **solvent effects**

Kubar et al., *J. Phys. Chem. B* **2008**, *112*, 7937

Kubar & Elstner, *J. Phys. Chem. B* **2008**, *112*, 8788

# Fragment Orbitals

Senthilkumar et al., JACS 127, 14894



Fragment orbitals (FO) in LCAO  
ansatz:

$$\phi_i = \sum_{\mu} c_{\mu}^i \eta_{\mu}$$

$$\phi_j = \sum_{\nu} c_{\nu}^j \eta_{\nu}$$

$T_{ij}, S_{ij}$

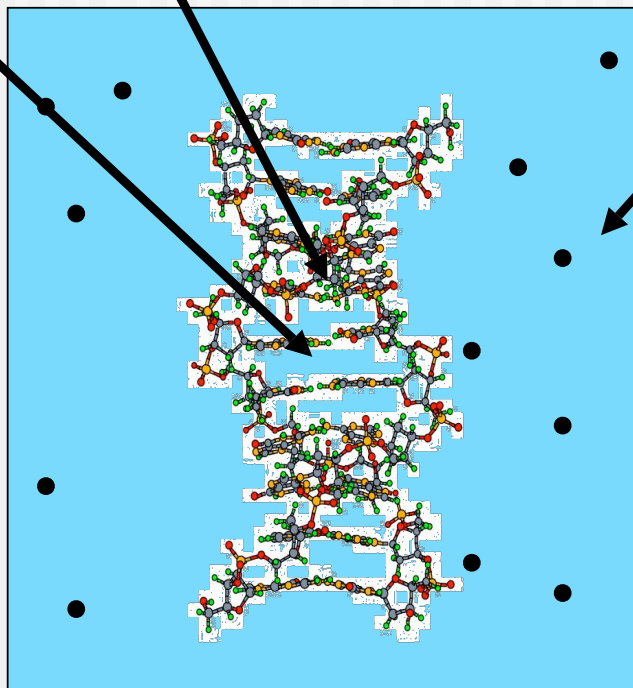
$$T_{ij} = \sum_{\mu\nu} c_{\mu}^i c_{\nu}^j \langle \eta_{\mu} | H | \eta_{\nu} \rangle$$

$$= \sum_{\mu\nu} c_{\mu}^i c_{\nu}^j H_{\mu\nu}$$

# Couple to solvent degrees of freedom: SCC-DFTB QM/MM Hamiltonian

$$H_{\mu\nu} = H_{\mu\nu}^0 + \frac{1}{2} S_{\mu\nu} \sum_{\gamma} \Delta q_{\gamma} (\gamma_{\alpha\gamma} + \gamma_{\beta\gamma}) + \frac{1}{2} S_{\mu\nu}^{\alpha\beta} \sum_A Q_A (1/R_{\alpha A} + 1/R_{\beta A})$$

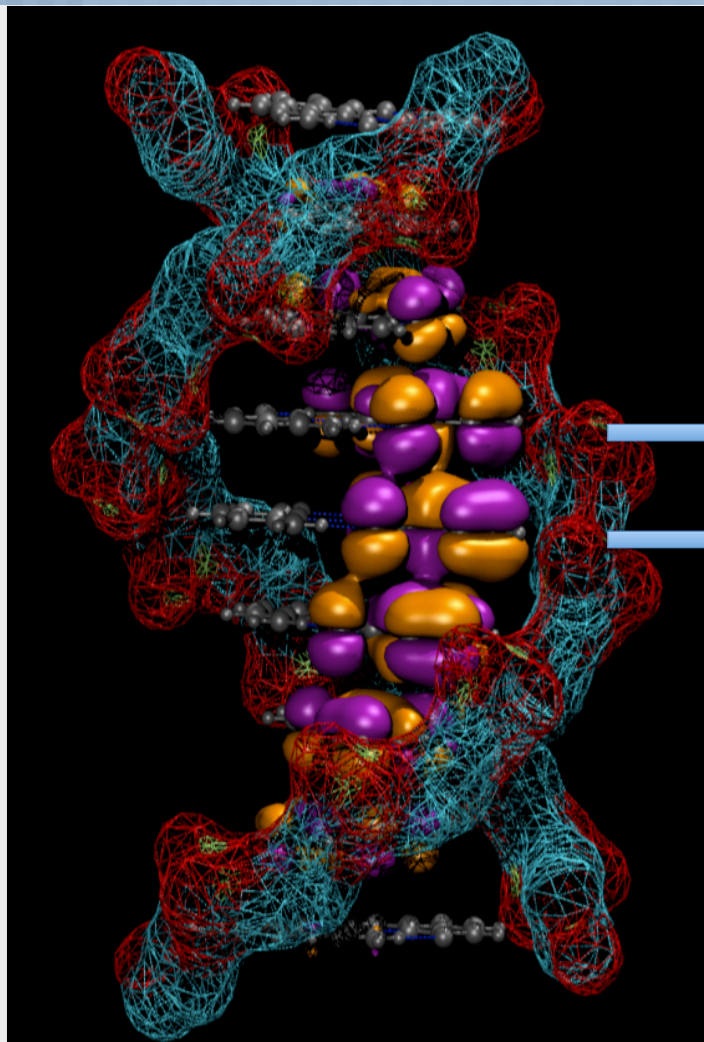
interaction  
between  
QM atoms



$Q_A$ : MM charges  
polarizing QM  
region:  
backbone, waters,  
counterions

$$T_{ij} = \sum_{ij} c_{\mu}^i c_{\nu}^j H_{\mu\nu} \quad \text{includes the effect of environment}$$

# Coarse grained Hamiltonian



site i

site j



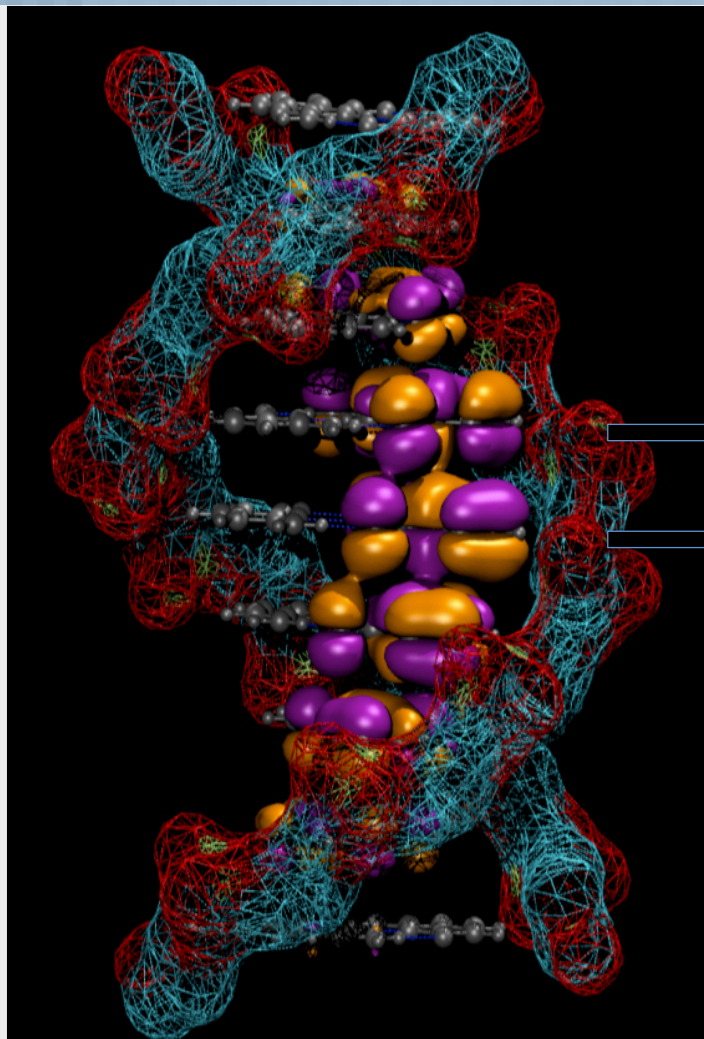
$$H = \sum_i \epsilon_i a_i^+ a_i + \sum_{ij} T_{ij} a_i^+ a_j$$

Time dependent  
parameters  
 $\epsilon_i(t)$  and  $T_{ij}(t)$   
contain dynamical and  
solvation effects

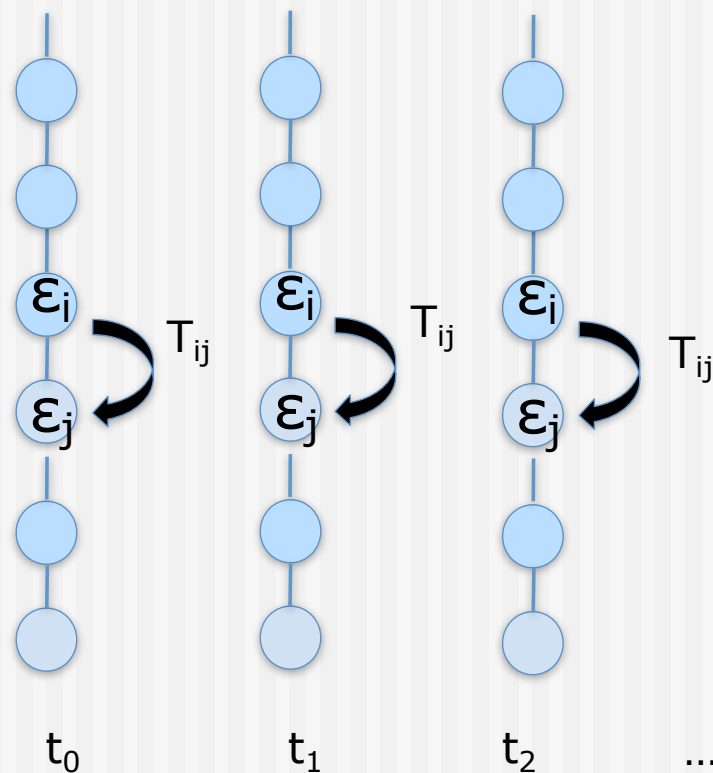
Kubar et al., *J. Phys. Chem. B* **2008**, *112*, 7937

Kubar & Elstner, *J. Phys. Chem. B* **2008**, *112*, 8788

## CT parameters along a QM/MM MD simulation

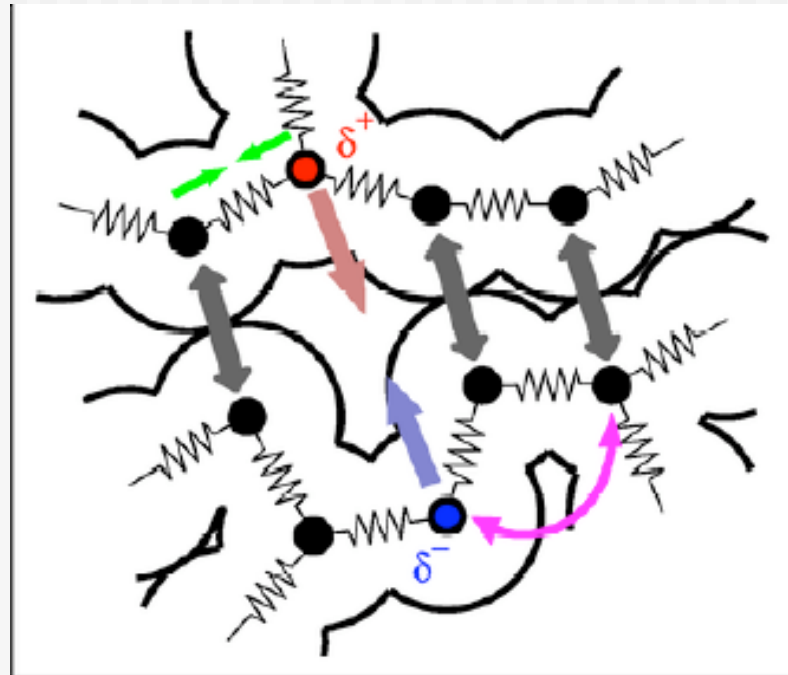


Coarse grained  
Hamiltonian



Time dependent parameters  
 $\epsilon_i(t)$  and  $T_{ij}(t)$  contain dynamical and  
solvation effects

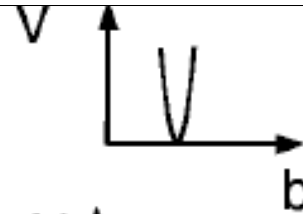
# Empirical Force Fields: **Molecular Mechanics** (MM)



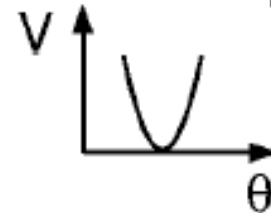
© Grubmüller



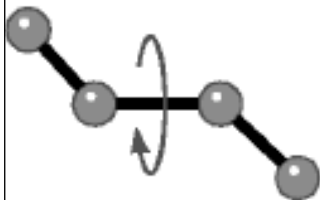
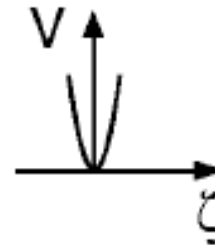
$$V_B = \sum_{\text{Bindungen}} \frac{1}{2} K_b (b - b_0)^2$$



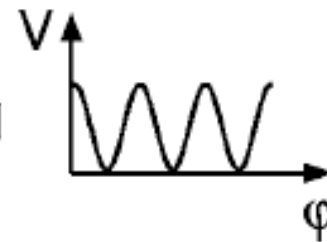
$$V_a = \sum_{\text{Winkel}} \frac{1}{2} K_\theta (\theta - \theta_0)^2$$



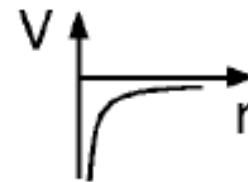
$$V_{imp} = \sum_{\text{Extraplanarwinkel}} \frac{1}{2} K_\zeta (\zeta - \zeta_0)^2$$



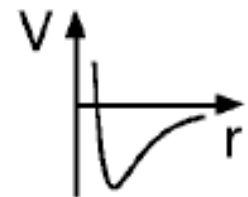
$$V_D = \sum_{\text{Dihedralwinkel}} K_\varphi [1 + \cos(n\varphi - \delta)]$$



$$V_q = \sum_{\text{Paare}(i,j)} q_i q_j / (4\pi\epsilon_0\epsilon_r r_{ij})$$



$$V_{vdW} = \sum_{\text{Paare}(i,j)} C_{12}(i,j)/r_{ij}^{12} - C_6(i,j)/r_{ij}^6$$

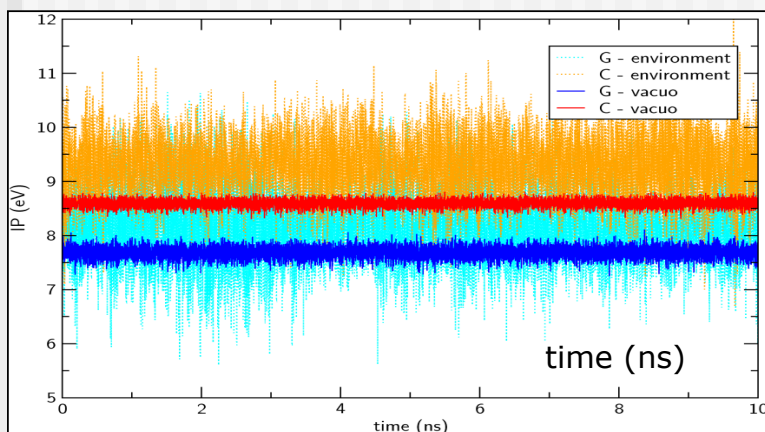


Quelle: Grubmüller  
MPI Göttingen



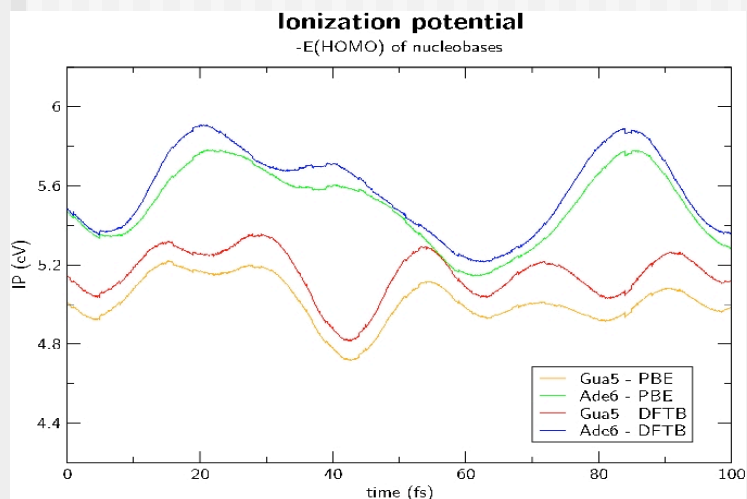
# Fluctuations of $I_p$

$$H_{\mu\nu} = H_{\mu\nu}^0 + \frac{1}{2} S_{\mu\nu} \sum_{\gamma} \Delta q_{\gamma} (\gamma_{\alpha\gamma} + \gamma_{\beta\gamma}) + \frac{1}{2} S_{\mu\nu}^{\alpha\beta} \sum_A Q_A (1/R_{\alpha A} + 1/R_{\beta A})$$



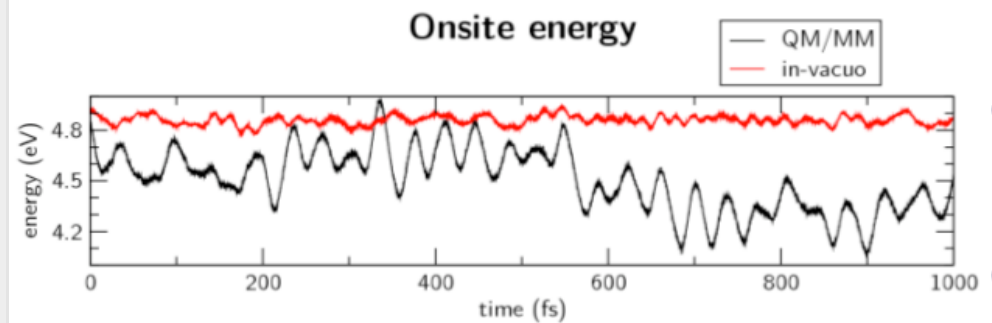
- due to solvent: **0.4 eV**

- 'gas phase' : **0.1 eV**  
(QM/MM term switched off)



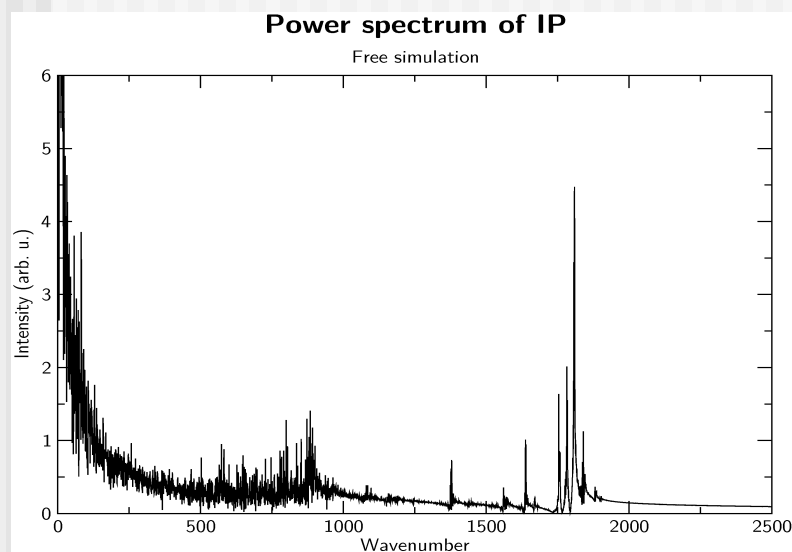
- large fluctuations
- A and G states can have same energy

# Characteristic modes



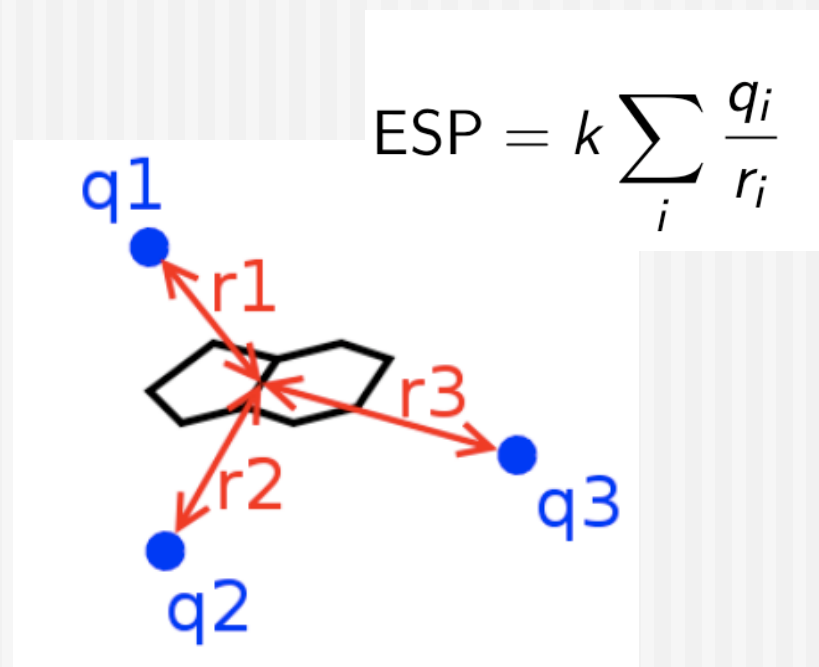
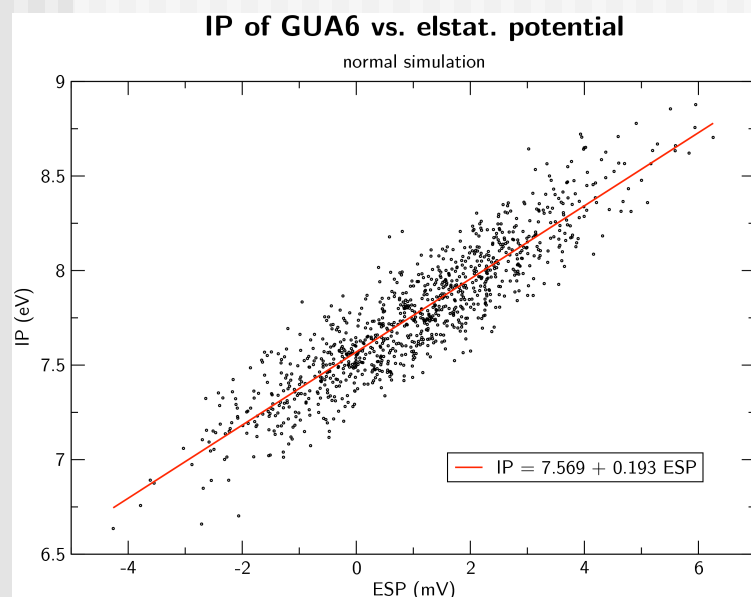
characteristic modes

- water: 40 fs
- bases: 20 fs



- internal base modes: 20 fs      1600 cm<sup>-1</sup>
- 'water modes': 40 fs      800 cm<sup>-1</sup>
- water+counterions: 1ps
- ...

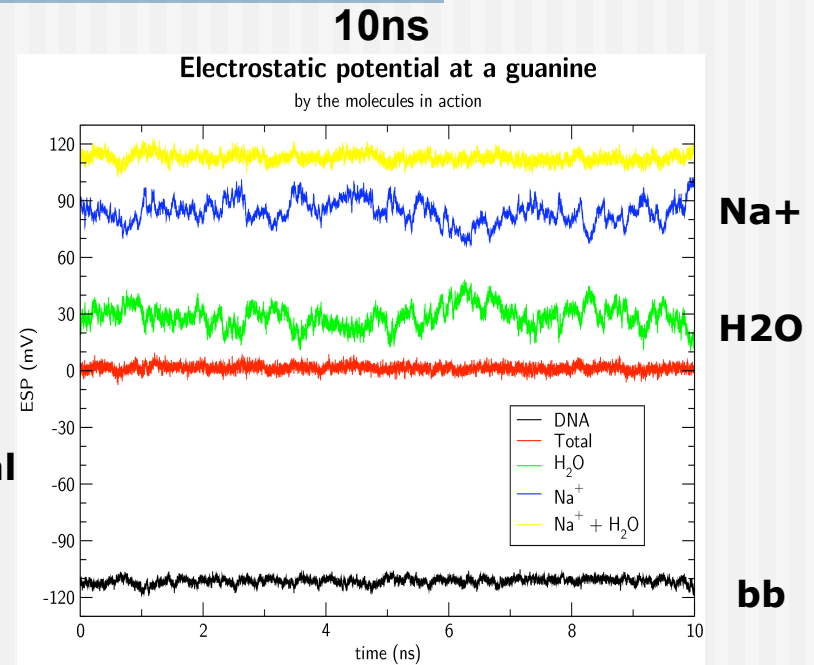
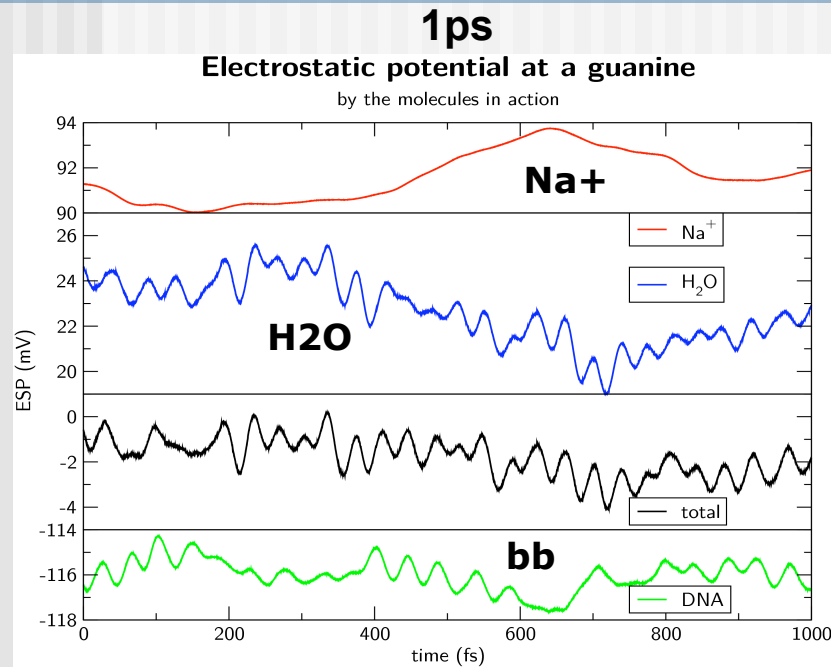
# Correlation of Ip with MM electrostatic potential



Strong correlation of electrostatic potentials with IPs:

→ we can decompose the potential to analyze the components from backbone, waters and ions

# Electrostatic potential of MM atoms at a Guanine

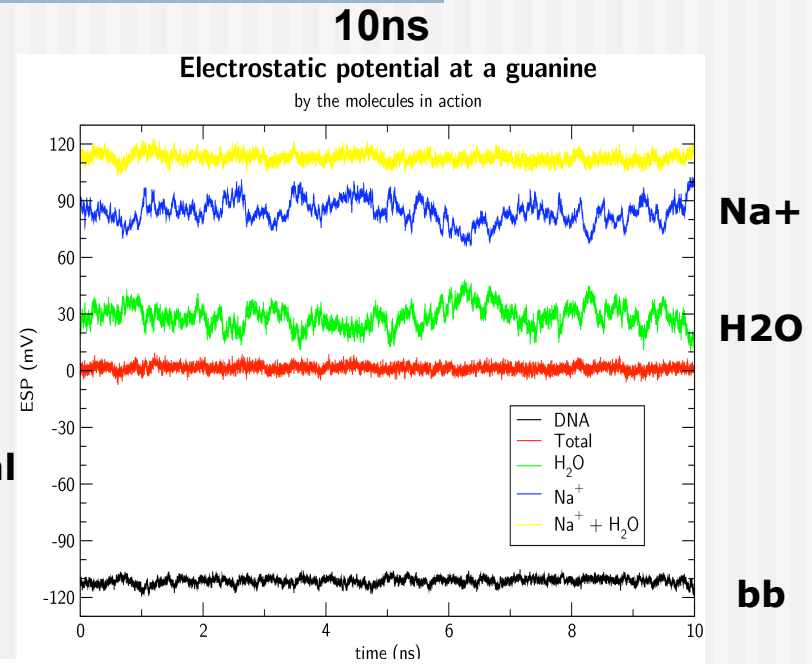
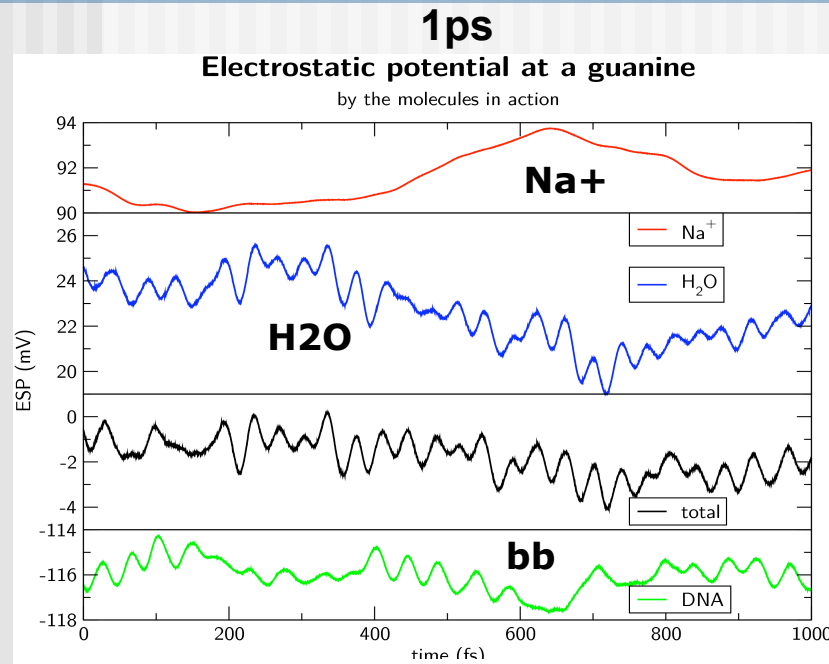


**=> fluctuations of the solvent introduce 40 fs mode,**

i.e. solvent introduces the fluctuations of the IP in the order of 0.4 eV

**ion motion on ps-time-scale**

# Electrostatic potential of MM atoms at a Guanine



**TABLE 3: Correlation Coefficient of the Individual Components of Electrostatic Potential**

$\rho_{x,y}$	water	ions	water + ions	total
DNA	-0.08	-0.16	-0.44	0.18
water		-0.85	0.22	0.19
ions			0.33	0.26
water + ions				0.81

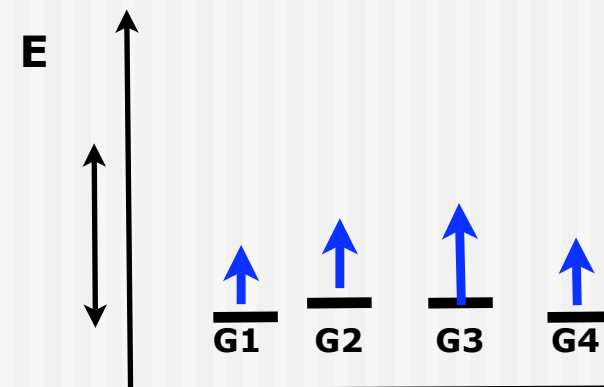
s?

# Results: Ip of neighboring sites correlated

=> motion of water and ions determine Ip fluctuation to large degree

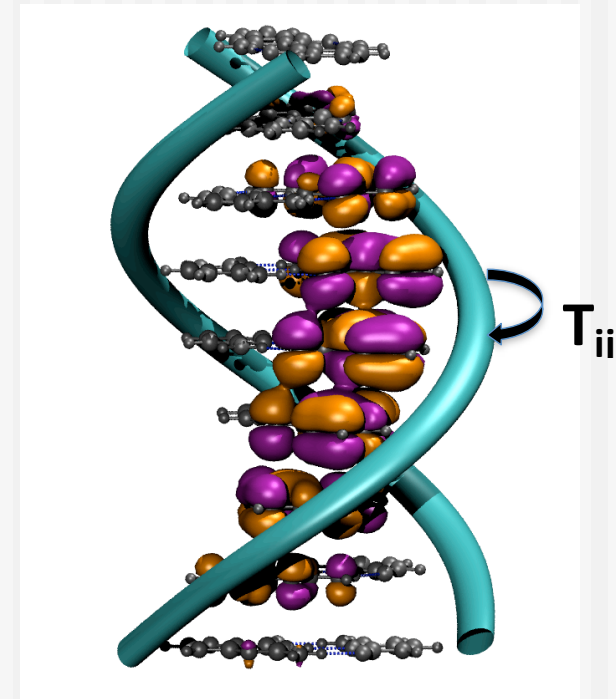
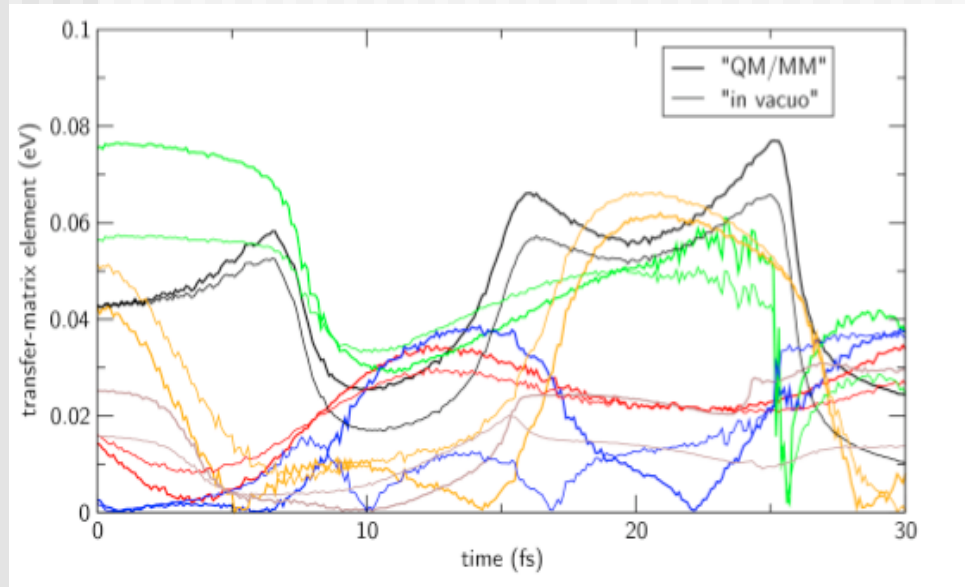
correlation of fluctuation of neighboring sites

$\rho_{\epsilon_i, \epsilon_j}$	G3	G4	G5	G6	G7	G8	G9
G3	1	0.66	0.33	-0.03	-0.22	-0.33	-0.37
G4		1	0.65	0.26	0.00	-0.17	-0.30
G5			1	0.60	0.29	0.07	-0.11
G6				1	0.67	0.43	0.20
G7					1	0.71	0.45
G8						1	0.72
G9							1



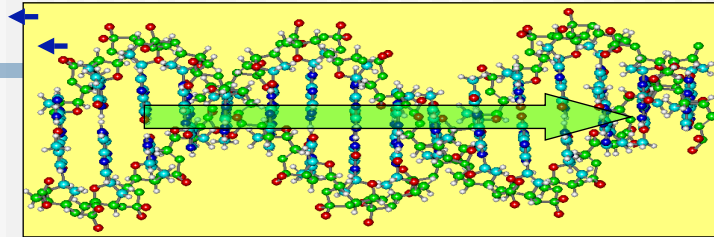
- concerted motion of neighboring sites (3-4) may have important implications or CT and transport
- and this is due to solvent environment

# Fluctuations of $T_{ij}$



- large fluctuations
  - small impact of environment on  $T_{ij}$
  - vanishing correlation between  $T_{ij}$ !
- ➔ no 'collective modes'?

# Charge transport in Physics and Chemistry



conductivity experiments  
coherent transport?

'chemical experiments'  
hole hopping: charge transfer

$$H = \sum_i \epsilon_i a_i^+ a_i + \sum_{ij} T_{ij} a_i^+ a_j$$

$$G_D(E) = (E - H_D^{\text{KS}} - \Sigma_L - \Sigma_R)^{-1}$$

$$T(E, V) = \text{tr}[\Gamma_L G_D^r \Gamma_R G_D^a]$$

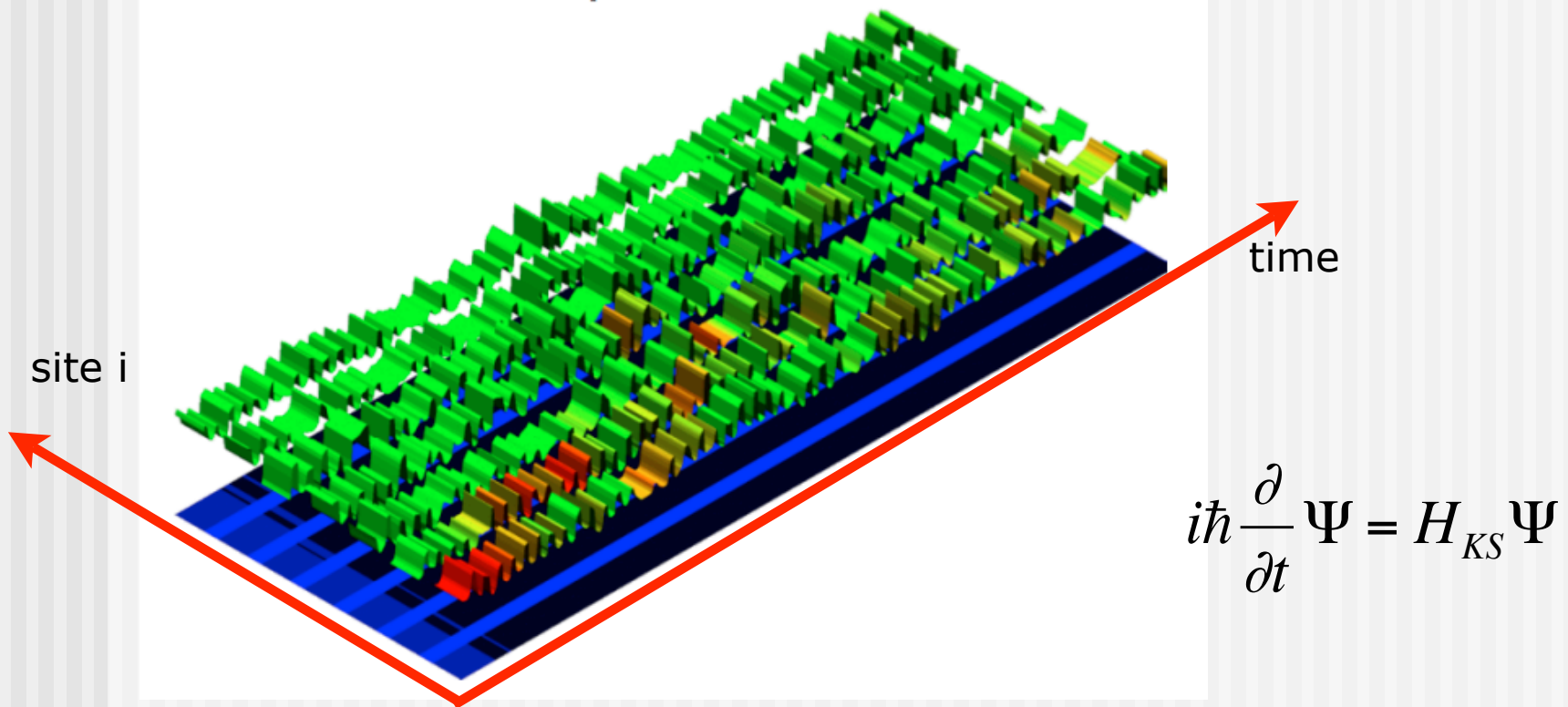
$$I(V) = \frac{2e}{h} \int_{\mu_1(V)}^{\mu_2(V)} T(E, V) dE$$

$$\Psi = \sum_i c_i \phi_i \quad \text{hole WF}$$

$$i\hbar \dot{\mathbf{c}} = \mathbf{H} \mathbf{c} \quad \text{solve TDKS}$$



# hole propagation



coupled eq. of motion for hole and atoms:  
classical MD for atoms  
TDKS for hole wavefunction

# CT in DNA: A-bridges

Giese et al. Nature 2002

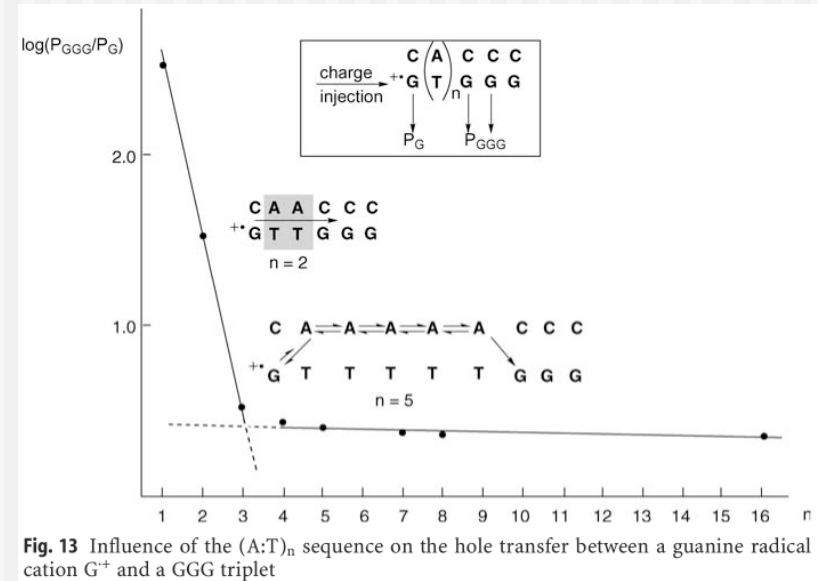
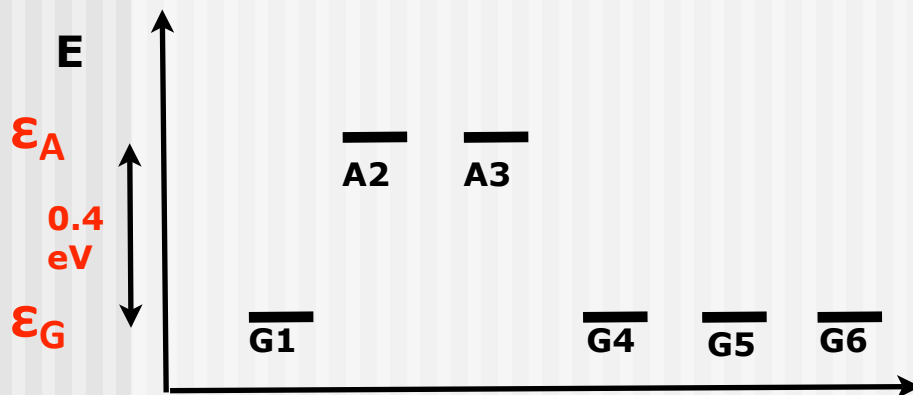
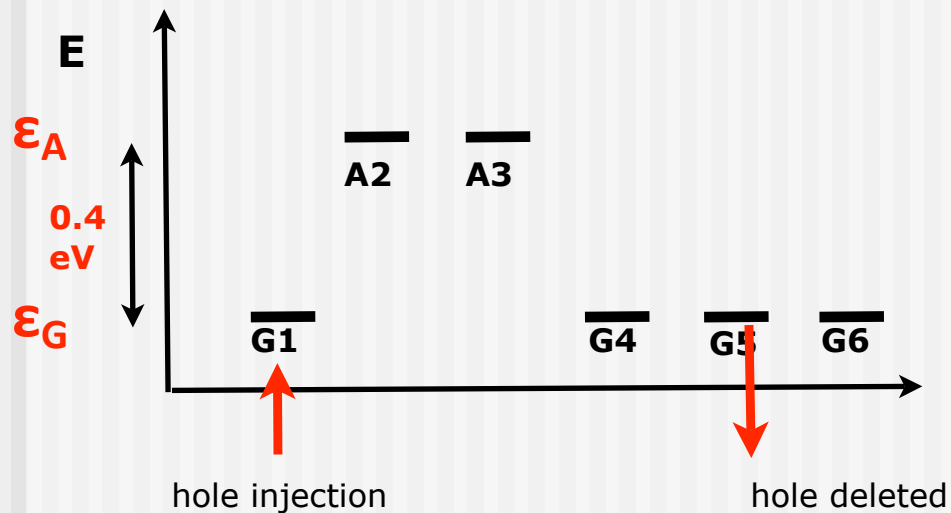


Fig. 13 Influence of the  $(A:T)_n$  sequence on the hole transfer between a guanine radical cation  $G^+$  and a GGG triplet

- exponential decay for short bridges
- algebraic for long A-tracts

# Tunneling through A bridges



Experiments by Giese et al.,  
superexchange tunneling for  
 $G(A)_nGGG$   
for  $n=1-4$

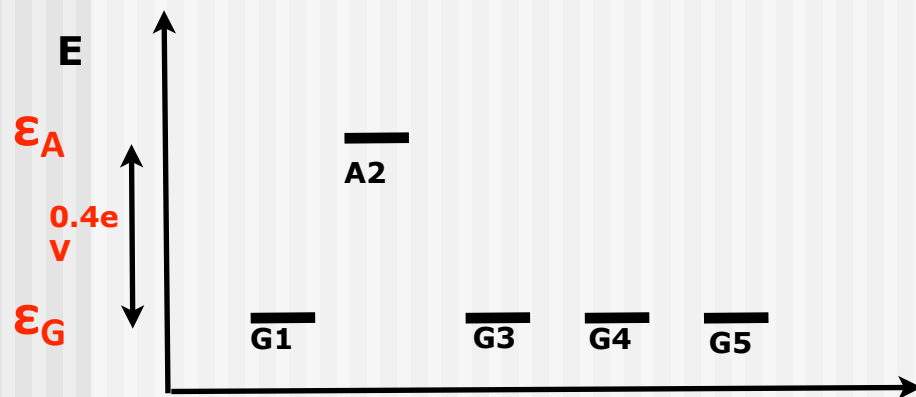
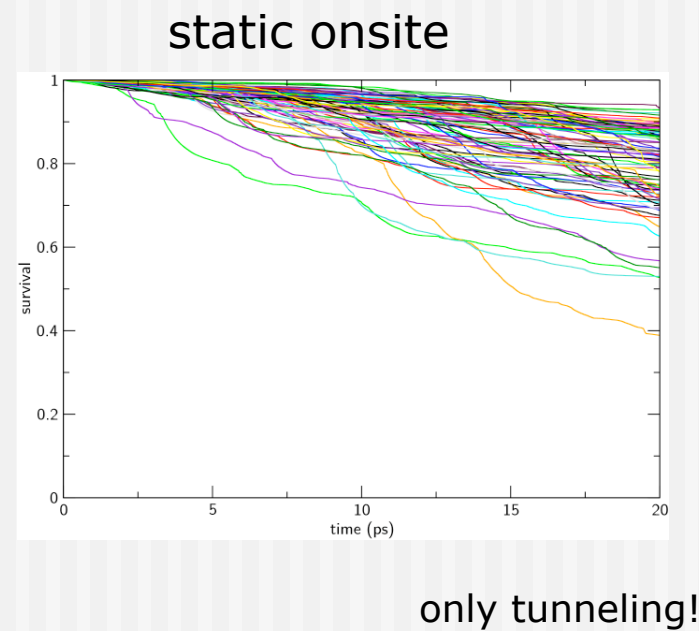
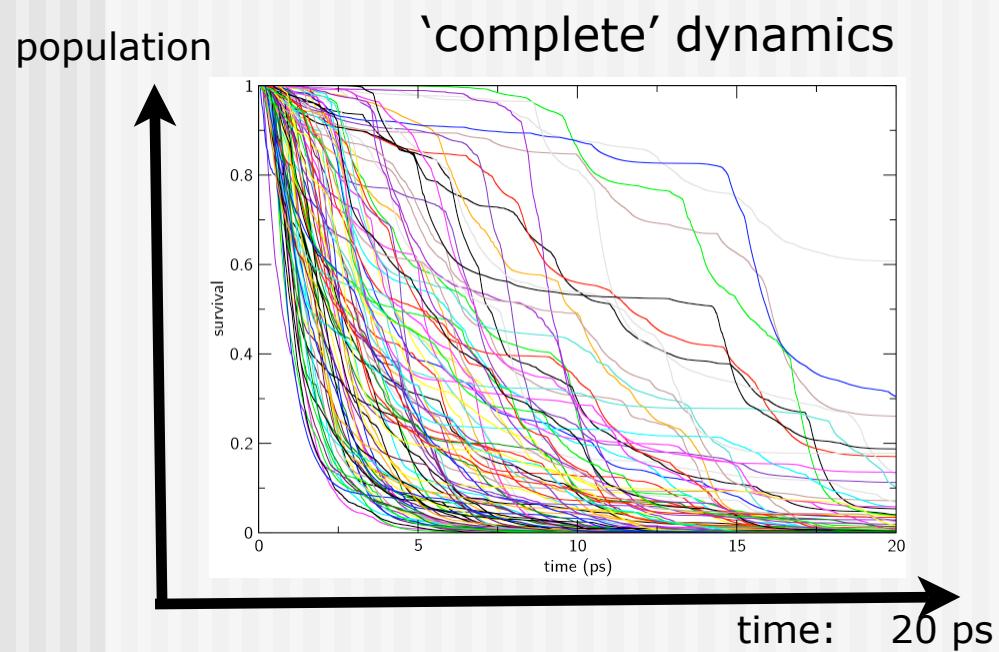
**always static calculations!**

MD simulations for  $G(A)_nGGG$  ( $n=1-4$ )

- sampling: average several trajectories over 20 ps hole motion
- calculate survival probability (eliminate hole at  $G6$ )

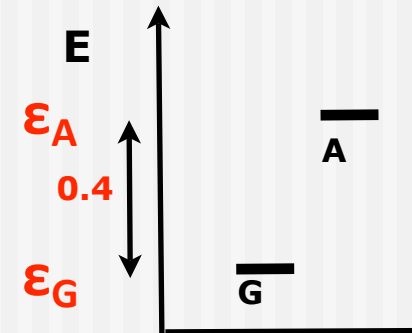
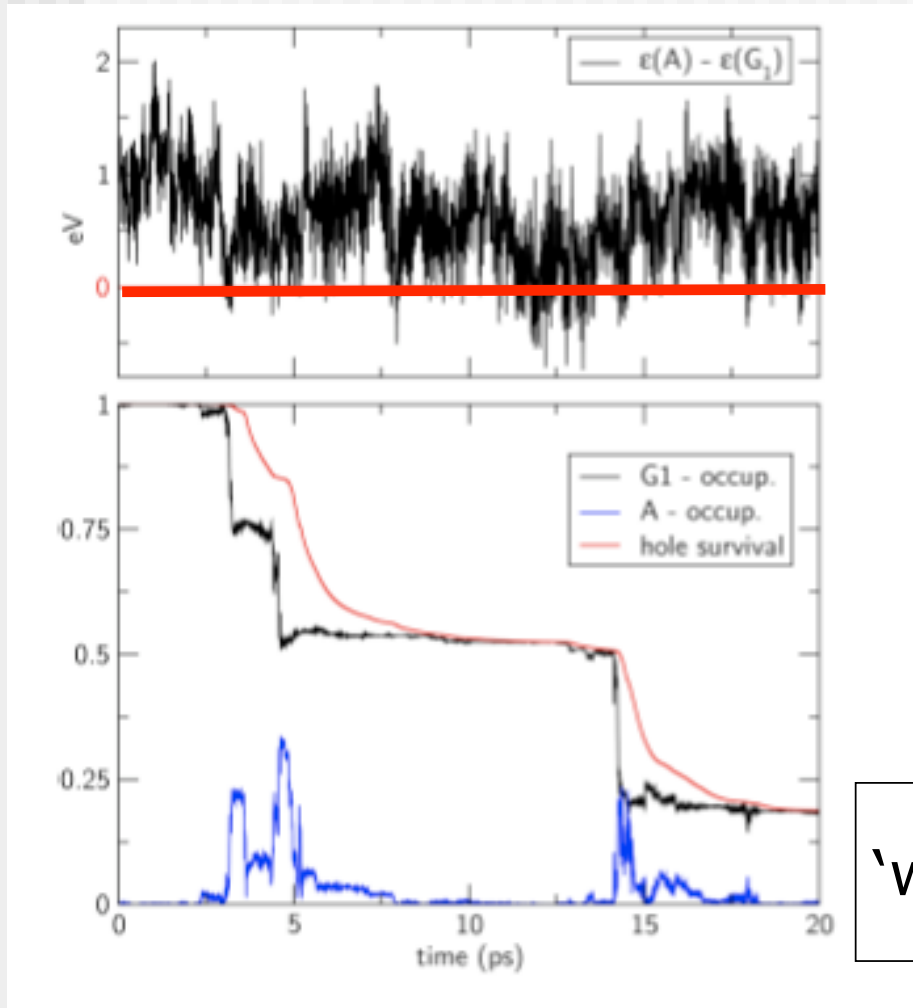
**=> very different picture, since barriers not constant**

# CT in GAGGG: 100 trajectories



Kubar et al. submitted

# CT in DNA: GAGGG



$$\epsilon_A - \epsilon_G$$

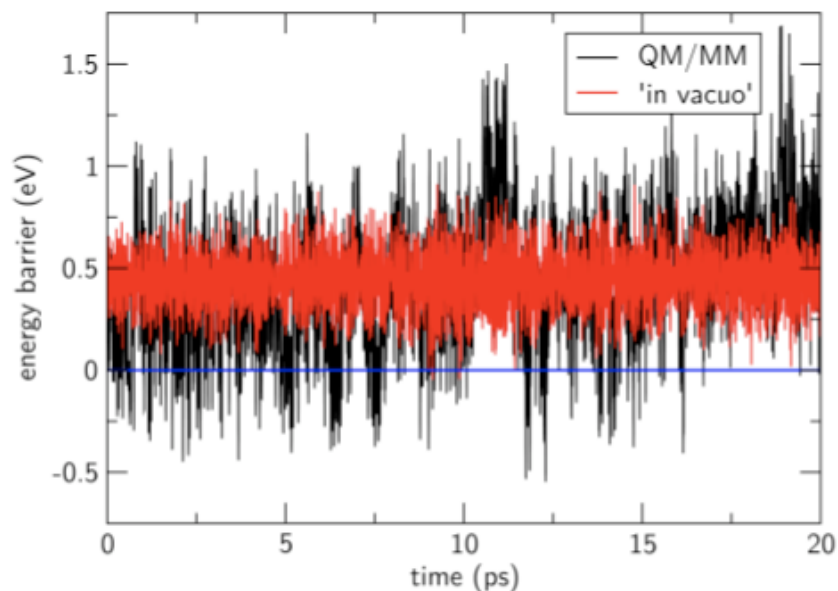
Energy difference between A and G

populations is transferred when:

- energy difference is small
- couplings do not vanish

'water modes' drive the CT!

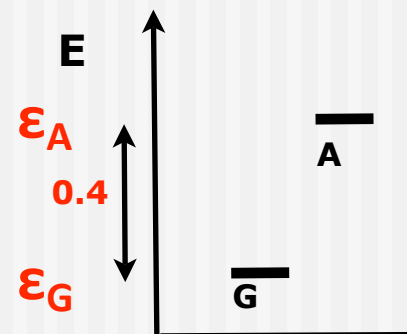
# CT in GAGGG: role of solvent



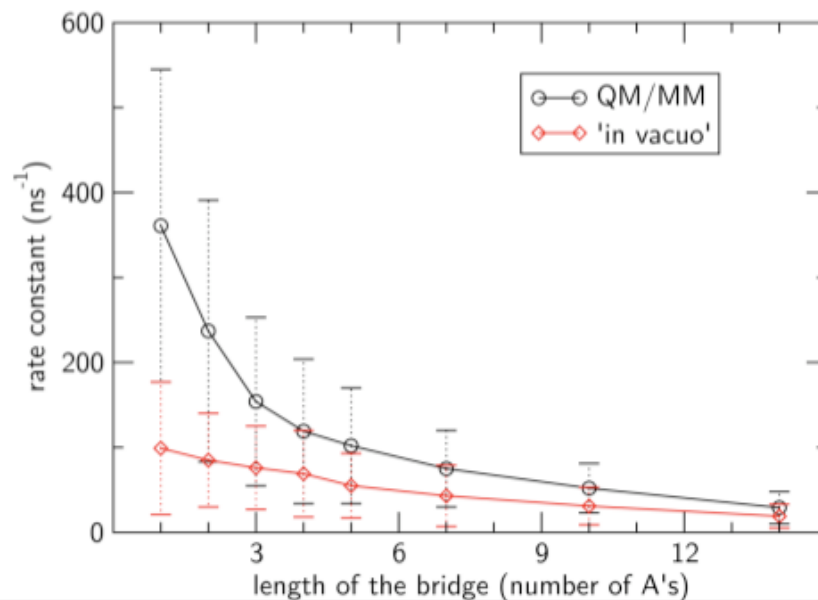
$$\epsilon_A - \epsilon_G$$

energy difference  
between A and G

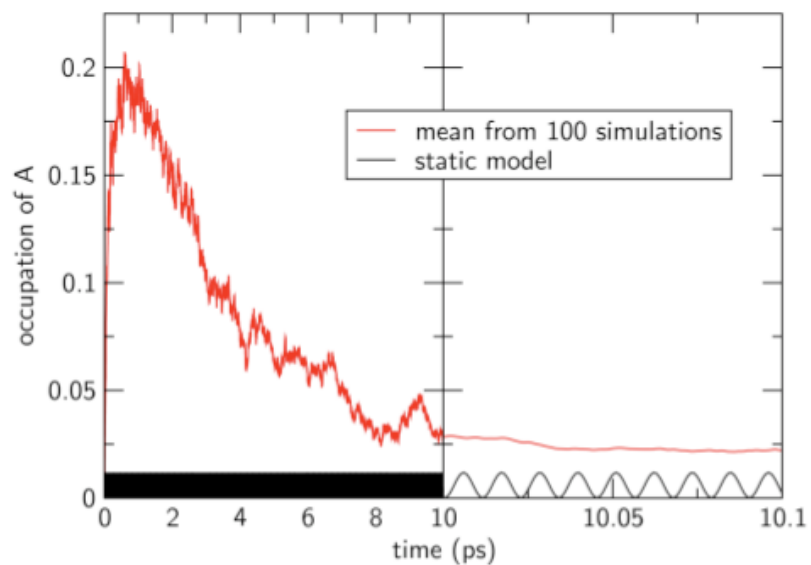
black: with solvent  
red: without solvent



'water modes' drive the CT!

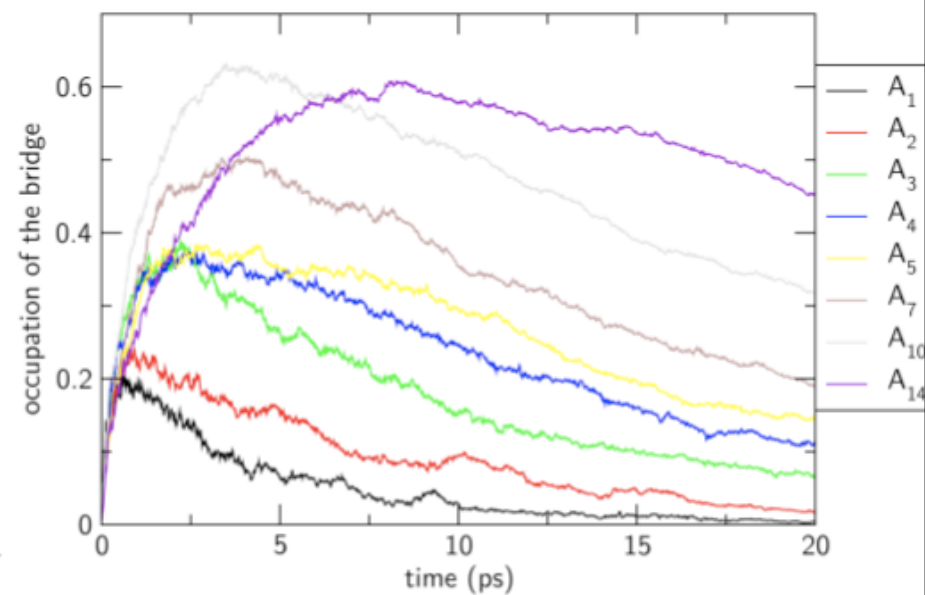


## CT in $\text{GA}_n\text{GGG}$ : bridge occupation



bridge occupation  
in **GAGGG**:

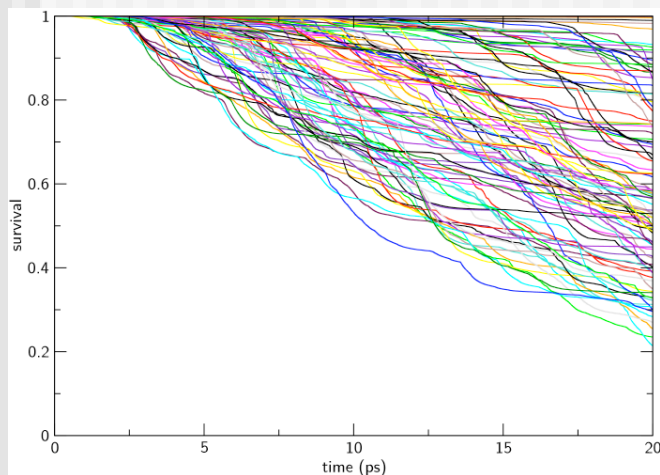
- $\varepsilon_i$  kept fixed
- dynamic model



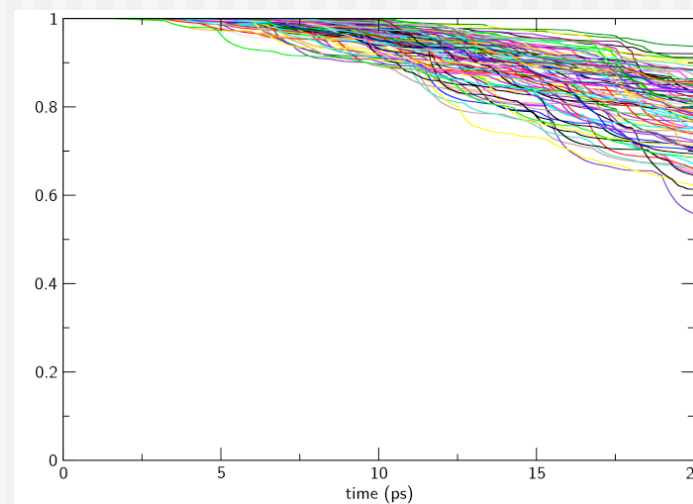
bridge occupation  
in  **$\text{GA}_n\text{GGG}$** :

# CT in DNA: GA<sub>14</sub>GGG

'complete' dynamics



fluctuating onsite, but taken from onsite pdf



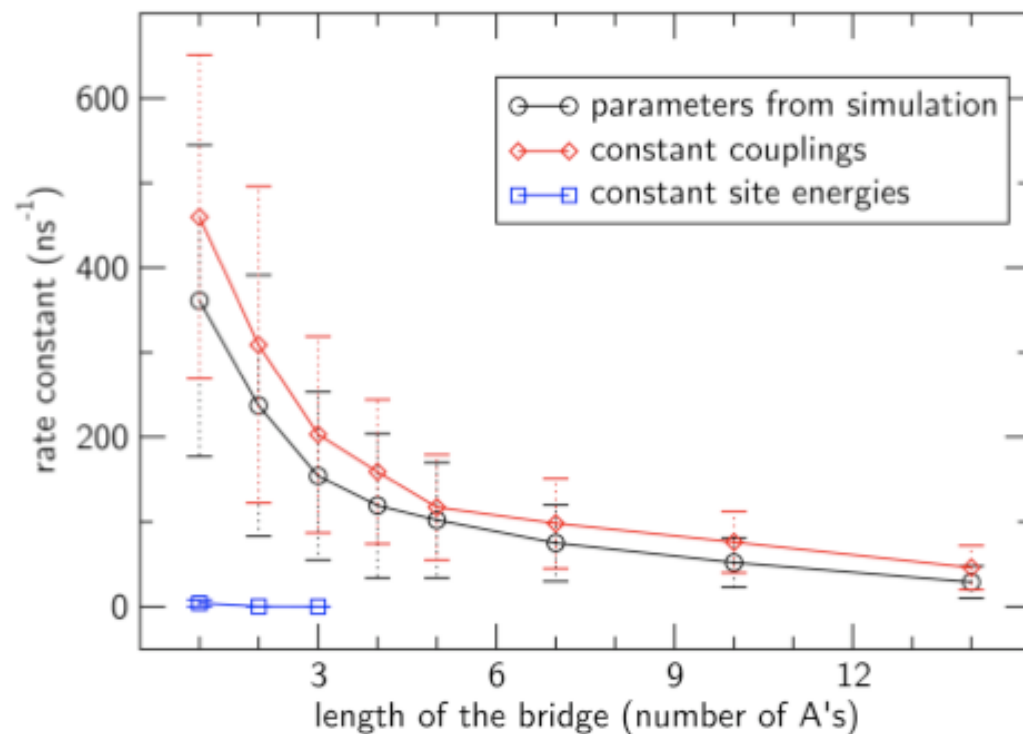
correlated motion of neighboring sites

Kubar et al. submitted

$\rho_{\epsilon_i, \epsilon_j}$	G3	G4	G5	G6	G7	G8	G9
G3	1	0.66	0.33	-0.03	-0.22	-0.33	-0.37
G4		1	0.65	0.26	0.00	-0.17	-0.30
G5			1	0.60	0.29	0.07	-0.11
G6				1	0.67	0.43	0.20
G7					1	0.71	0.45
G8						1	0.72
G9							1



## CT in $\text{GA}_n\text{GGG}$ : role of couplings



time course of couplings can be substituted by their 'averages':

no special CT promoting modes?

# CT in DNA: A-bridges

Giese et al

calc.

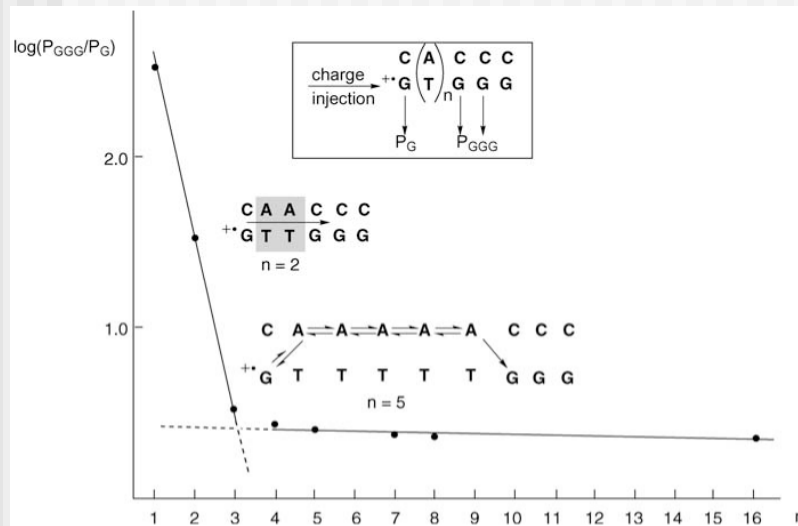
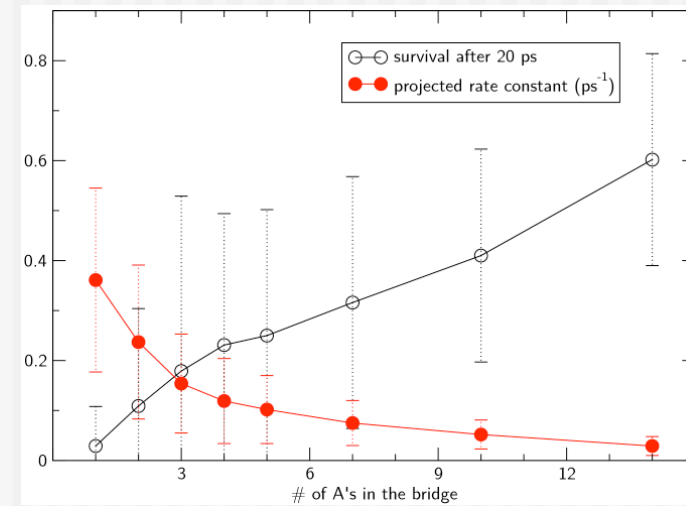


Fig. 13 Influence of the (A:T)<sub>n</sub> sequence on the hole transfer between a guanine radical cation G<sup>+</sup> and a GGG triplet

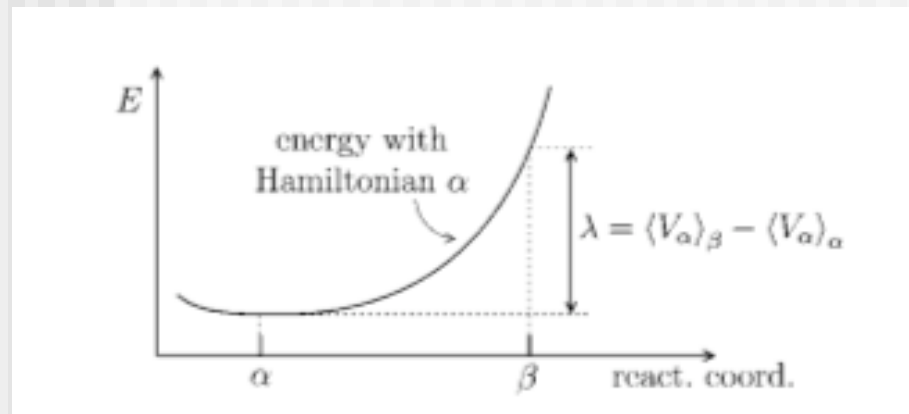


- exponential decay for short bridges
- algebraic for long A-trackts
- => still missing: proper account of solvation

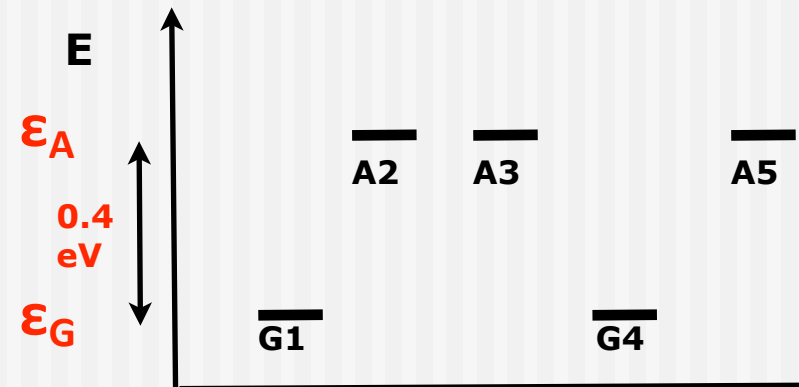
Kubar et al. submitted

## CT in DNA: solvation

$$k = \frac{2\pi}{\hbar} |H_{DA}|^2 \frac{1}{\sqrt{4\pi\lambda k_B T}} \exp\left[-\frac{(\Delta G_0 + \lambda)^2}{4\lambda k_B T}\right]$$



Reorganization energy in Marcus theory



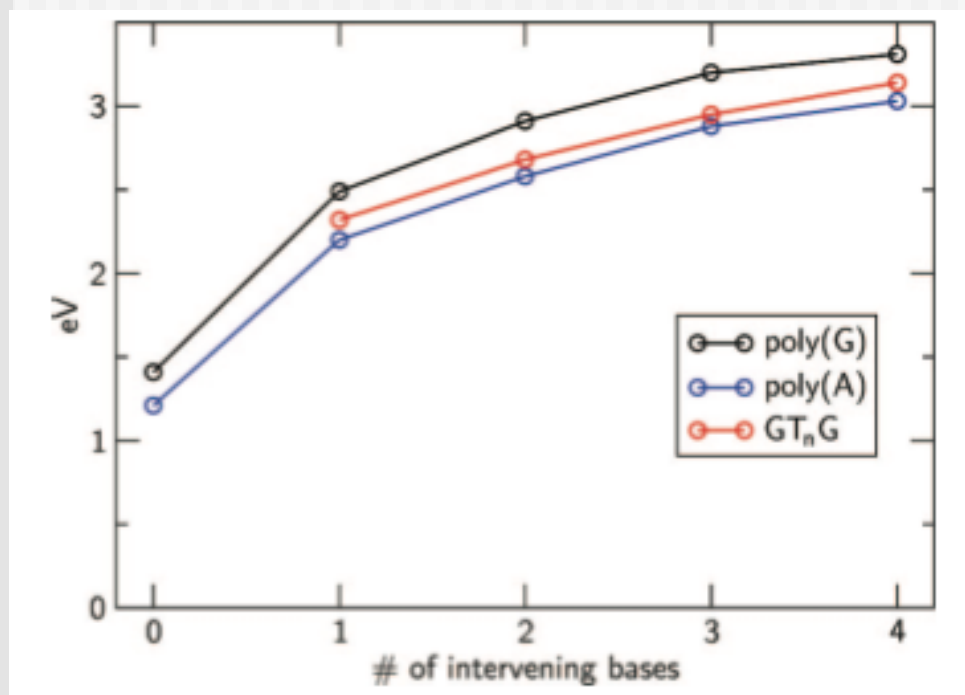
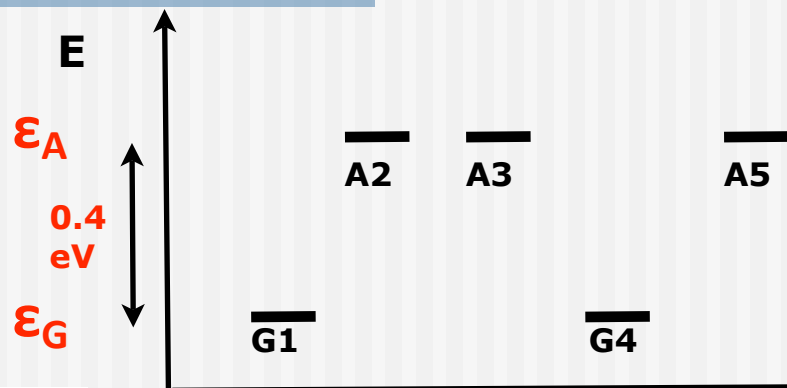
- put hole-charge on base  $\alpha$ , equilibrate the system with MD: ensemble  $\alpha$
- put hole-charge on base  $\beta$ , equilibrate the system with MD: ensemble  $\beta$

compute average energy of hole on  $\alpha$ , using the ensemble  $\beta$

# CT in DNA: solvation

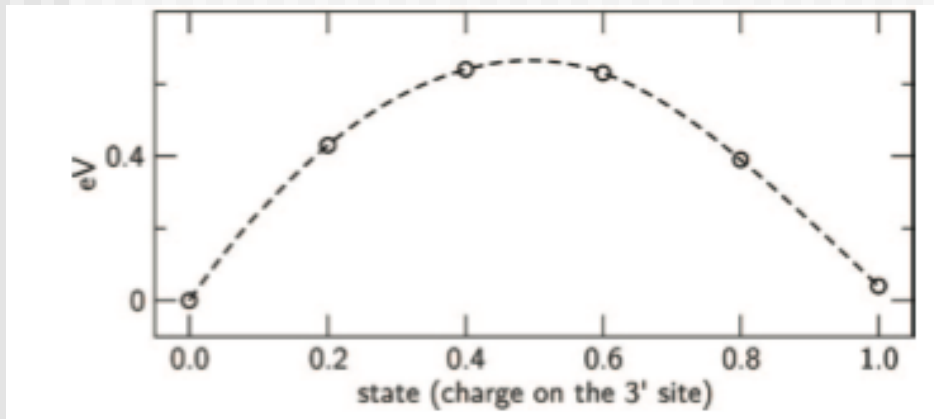
Reorganization energy in Marcus theory

$$k = \frac{2\pi}{\hbar} |H_{DA}|^2 \frac{1}{\sqrt{4\pi\lambda k_B T}} \exp\left[-\frac{(\Delta G_0 + \lambda)^2}{4\lambda k_B T}\right]$$

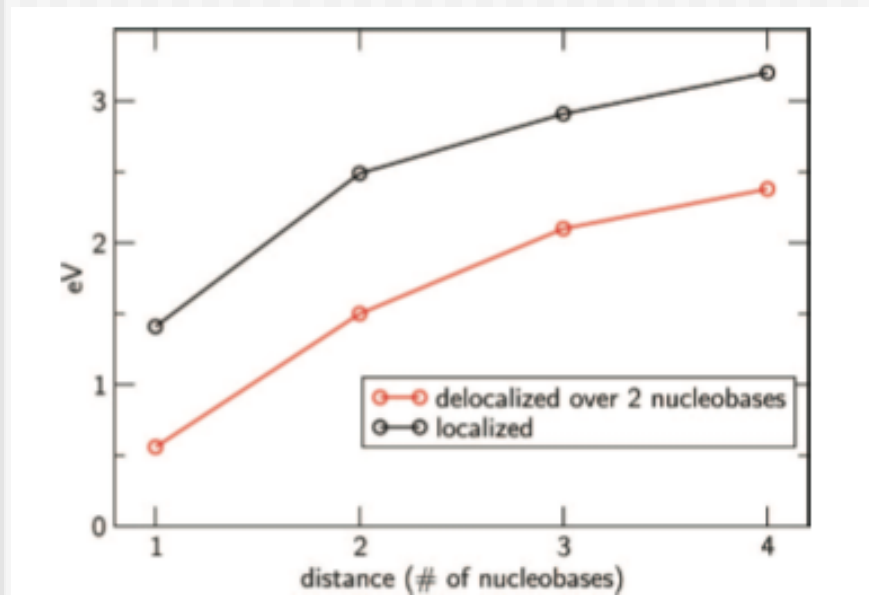


## CT in DNA: solvation

delocalization????



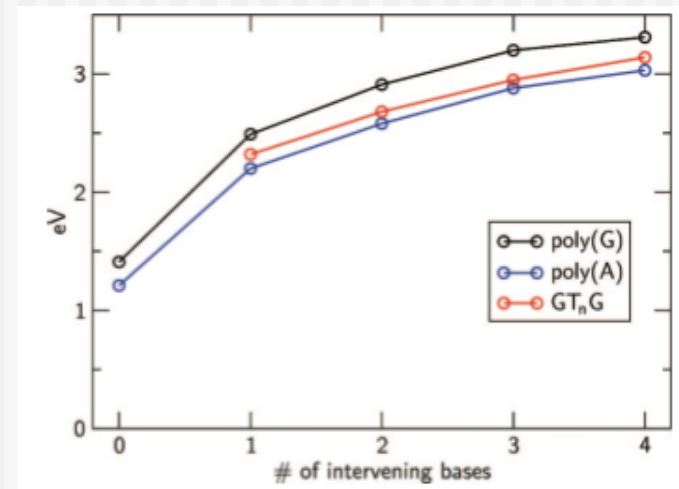
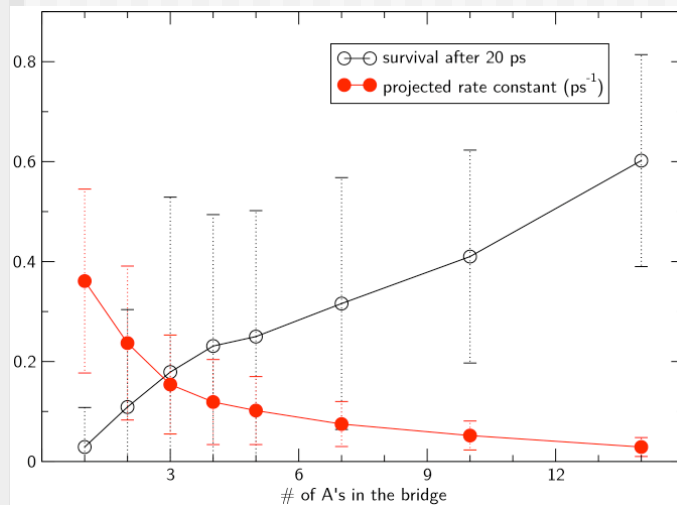
energy to delocalize  
hole between 2 bases:  
0.6 eV



reorganization  
energy to relocate  
delocalized hole:

$\approx 0.8$  eV less than  
for localized hole

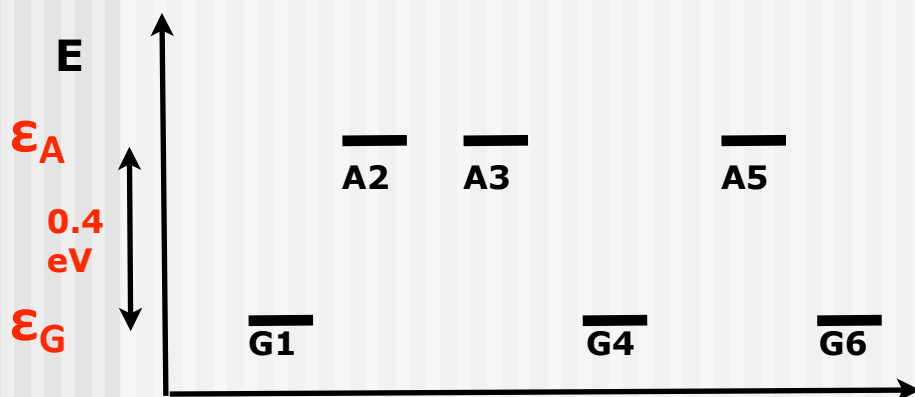
## CT in DNA: A-bridges



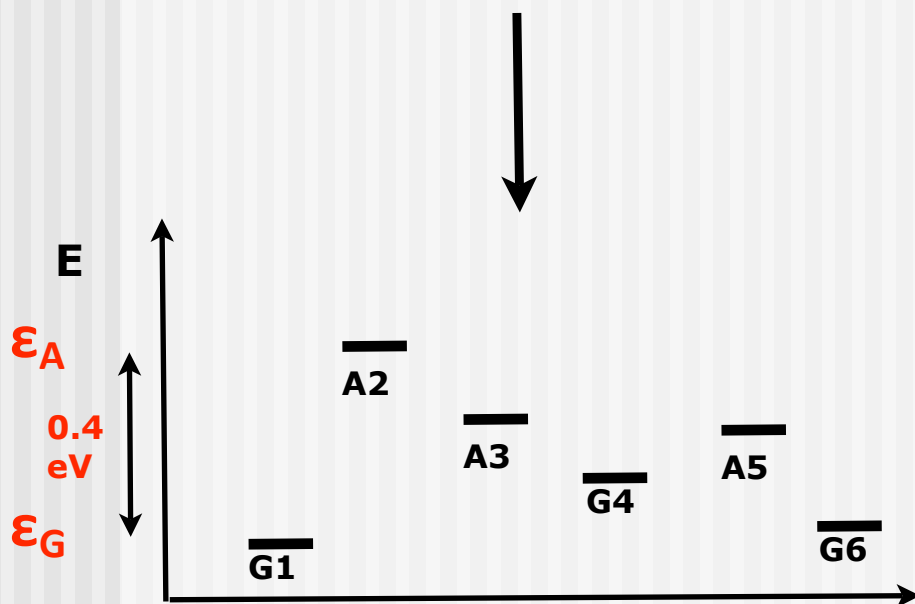
- exponential decay for short bridges
- distance dependent reorganization energy causes exponential dependence

=> still missing: proper account of solvation

## Effect of solvent and dynamics: new mechanistic picture



- static picture not really meaningful
- onsite fluctuations drive the CT
- correlation between sites important
- fluctuations of  $T_{ij}$  less important, contrary to the many proposals!

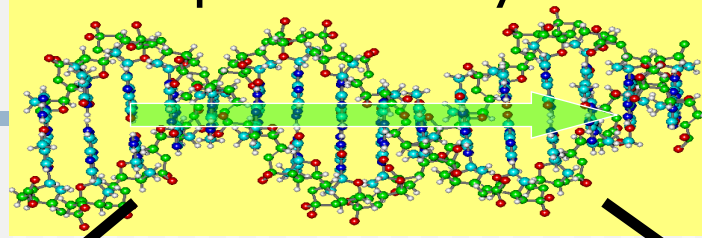


- New model: 'conformal gating'
- 'water modes' drive CT!
- solvent neglected so far, but important factor to determine absolute rates!

=> **coarse grained SCC-DFTB model**

Kubar et al. submitted

# Charge transport in Physics and Chemistry



conductivity experiments

'chemical experiments'

hole hopping; charge transfer

$$H = \sum_i \varepsilon_i a_i^+ a_i + \sum_{ij} T_{ij} a_i^+ a_j$$

$$G_D(E) = (E - H_D^{\text{KS}} - \Sigma_L - \Sigma_R)^{-1} \quad \text{Green functions}$$

$$T(E, V) = \text{tr}[\Gamma_L G_D^r \Gamma_R G_D^a]$$

$$I(V) = \frac{2e}{h} \int_{\mu_1(V)}^{\mu_2(V)} T(E, V) dE$$

Landauer theory

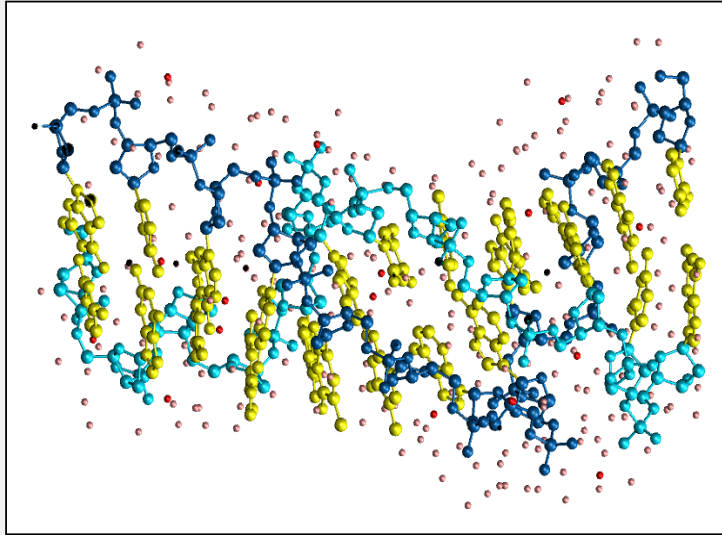
Observables

Woiczikowski et al.,  
JCP accepted

Gutierrez et al.,  
PRL accepted



## The basis: classical MD simulation of DNA in water



- 50 ns MD
- AMBER 9
- Parm99+BSC0
- DNA fully solvated, TIP3P
- Periodic boundary cond.
- Ewald summation

compute

$$H = \sum_i \varepsilon_i a_i^+ a_i + \sum_{ij} T_{ij} a_i^+ a_j$$

$$G_D(E) = (E - H_D^{\text{KS}} - \Sigma_L - \Sigma_R)^{-1}$$

$$T(E, V) = \text{tr}[\Gamma_L G_D^r \Gamma_R G_D^a]$$

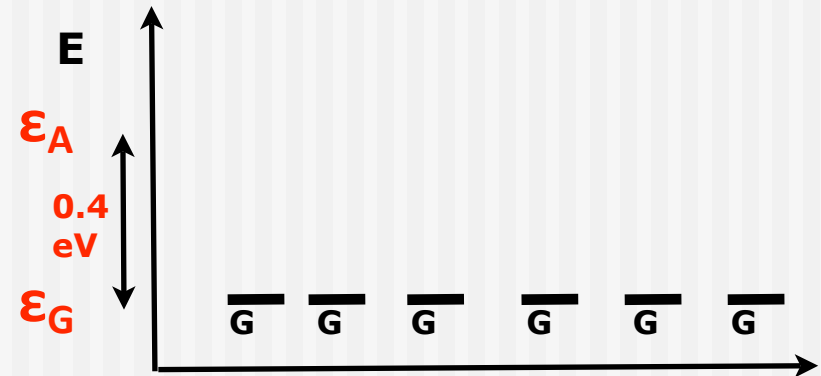
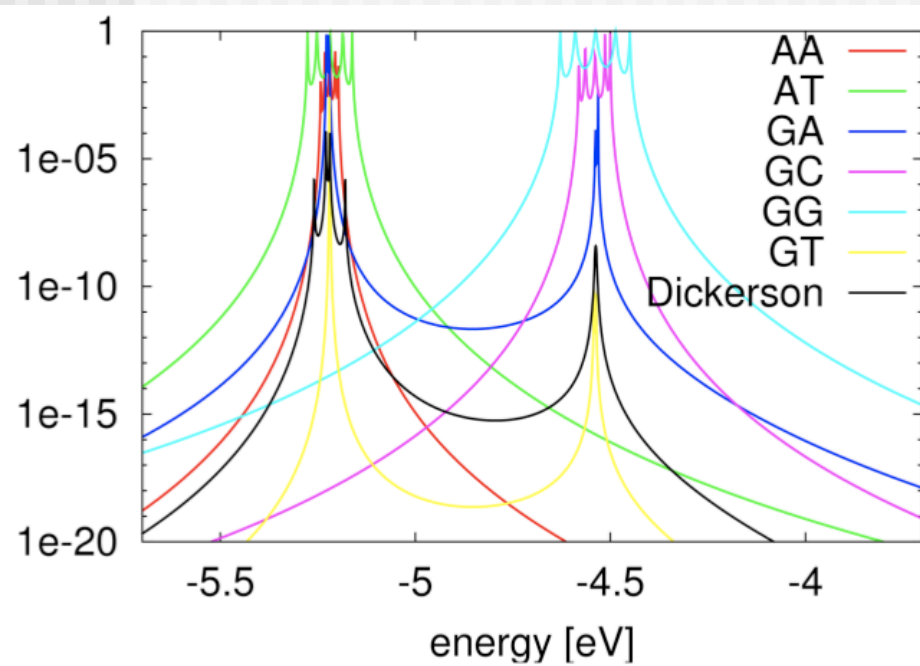
for every time-step,

for: pG, pA,  
p(AT), p(GA) ...

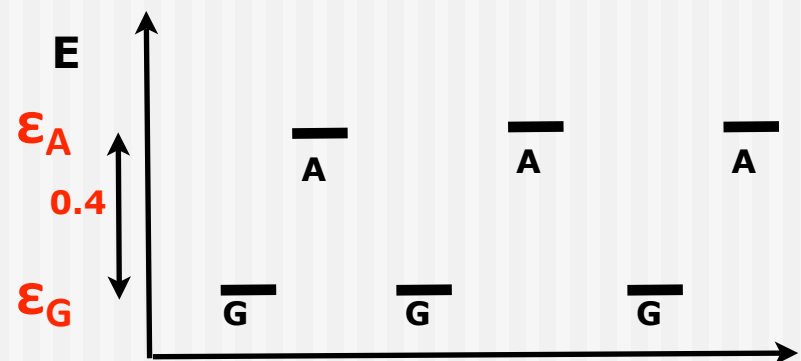
**and then do what? average?**

# the reference: ideal B-DNA structures

transmission

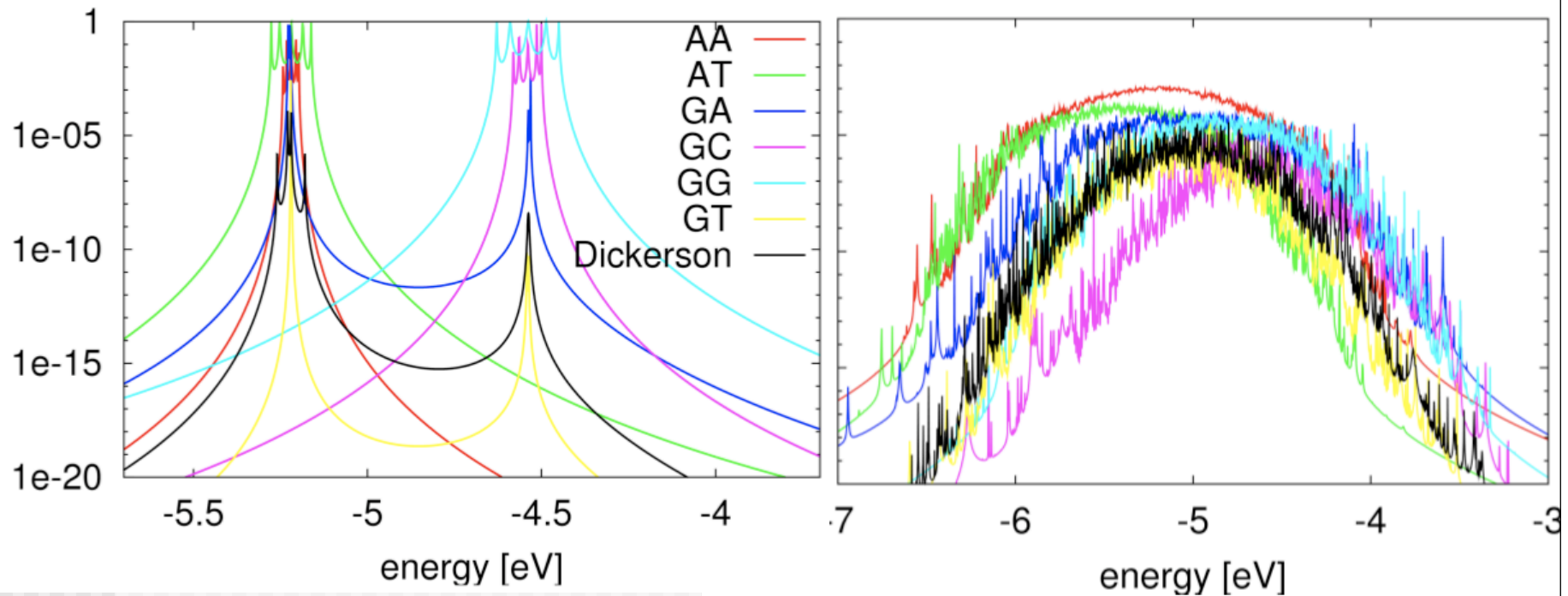


pG: 'good' (conducting) **sequence**



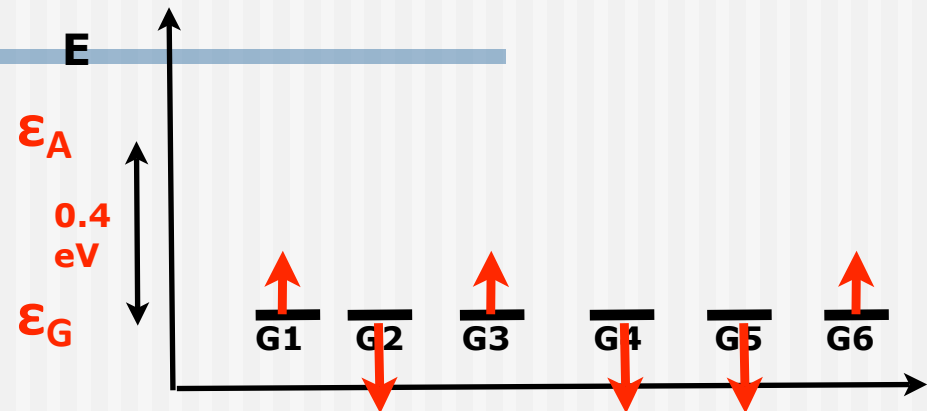
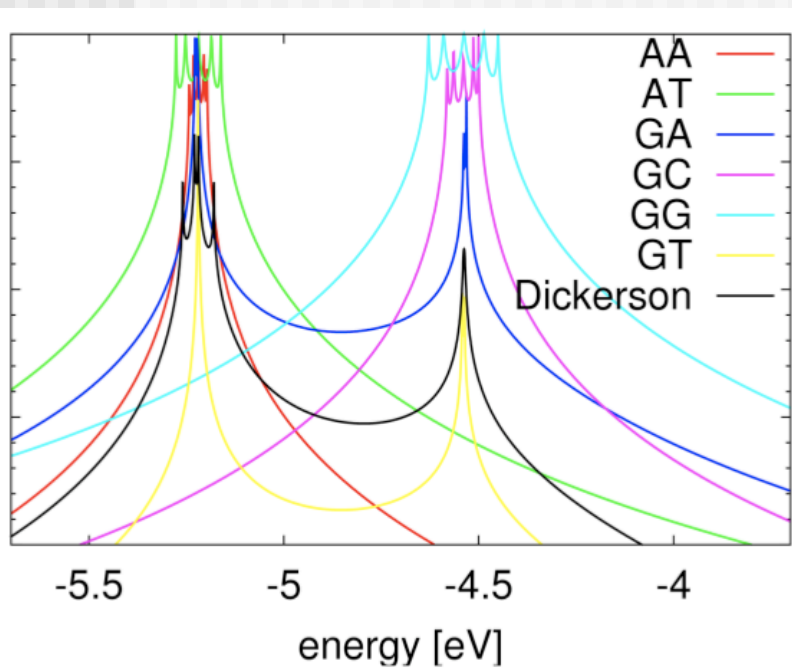
pGA: 'bad' (conducting) **sequence**

## and in water

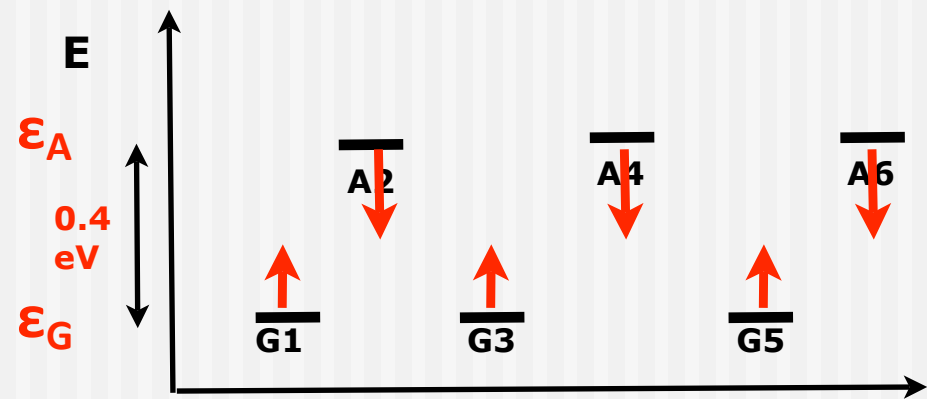


- transmission of 'good sequences' **reduced** by 5 orders of magnitude:  
*dynamical disorder*
- transmission of 'bad sequences' **increased** by 5 orders of magnitude  
*dynamics introduces CT active conformations*

# effect of fluctuations



pG: **'good'** (conducting) **sequence**

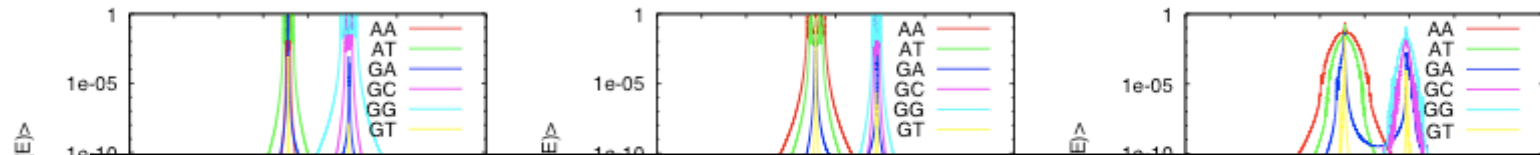


pG: **'bad'** (conducting) **sequence**

$\epsilon = \text{const}$   
(B-DNA)

$\langle \epsilon \rangle$

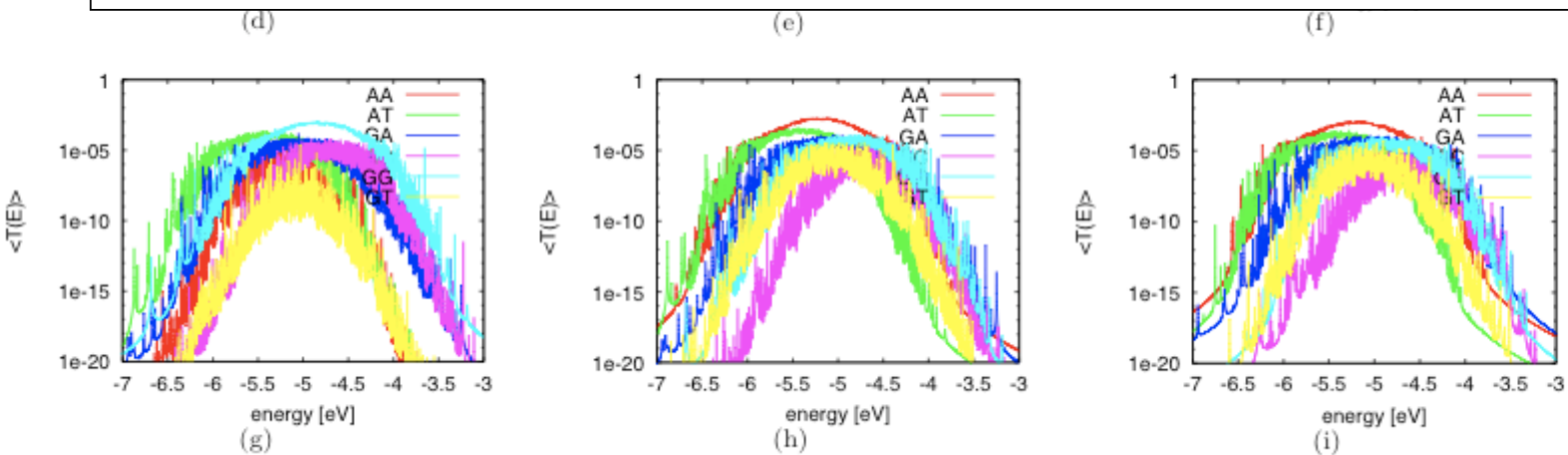
$\epsilon(t)$



- substitution of  $T_{ij}(t)$  by  $T_{ij} = \text{const}$ . does not change the picture

- the transmission is dominated by the fluctuation of the onsite  $\epsilon(t)$ :

=> it is all about the solvent

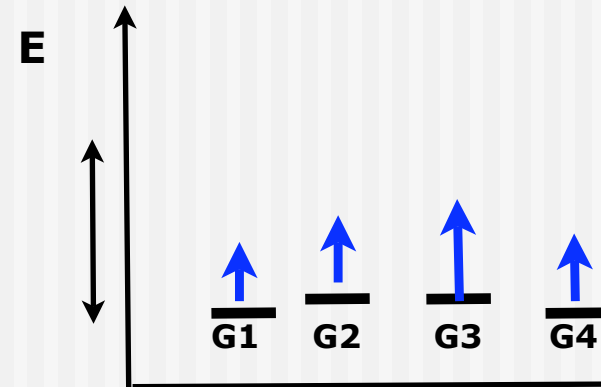
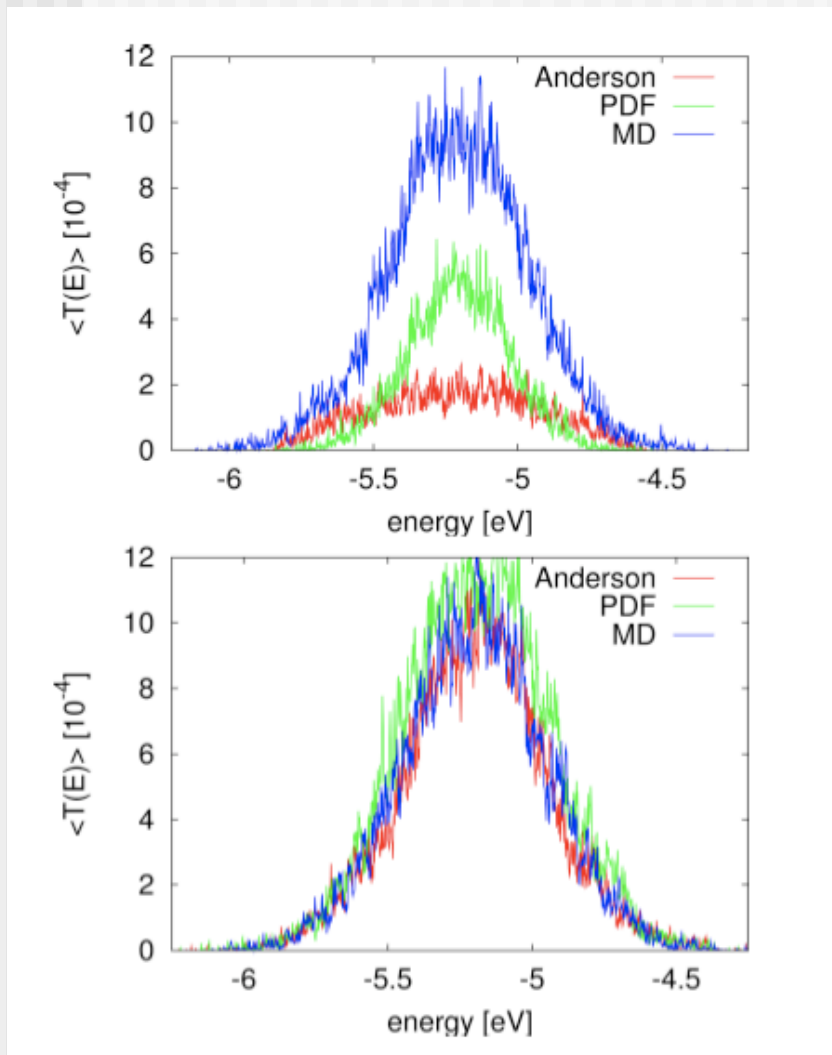


$T_{ij} = \text{const}$   
(B-DNA)

$\langle T_{ij} \rangle = \text{const}$

$T_{ij}(t)$

# How important is the correlation between the sites?

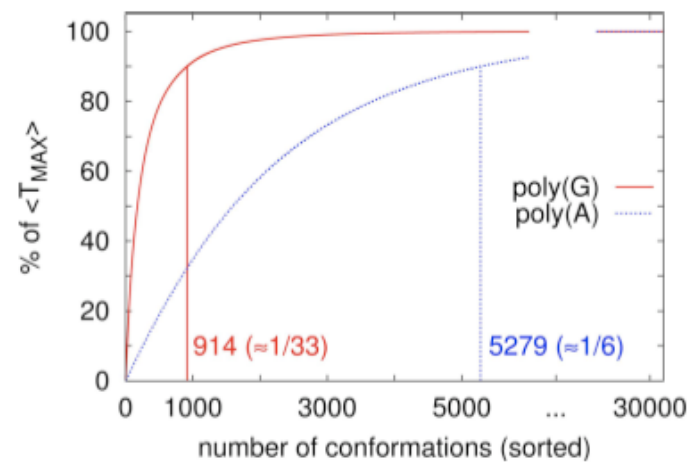
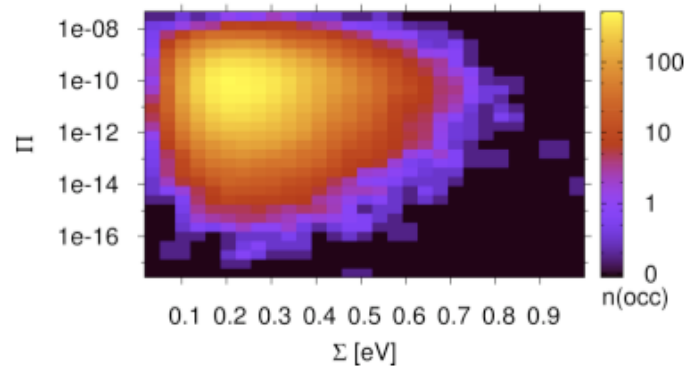
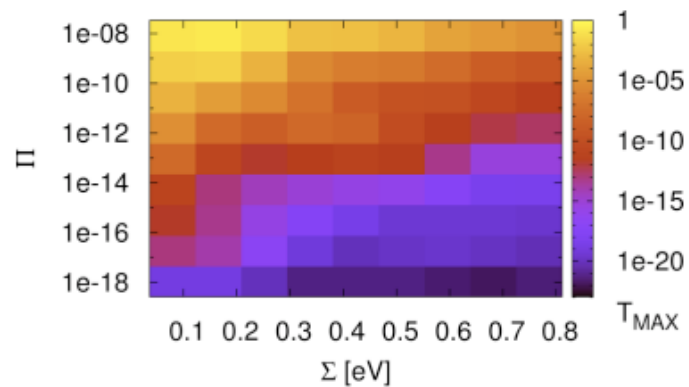


- 1) MD
- 2) draw the parameters from the distribution as generated by MD
- 3) statistical model

# CT active conformations

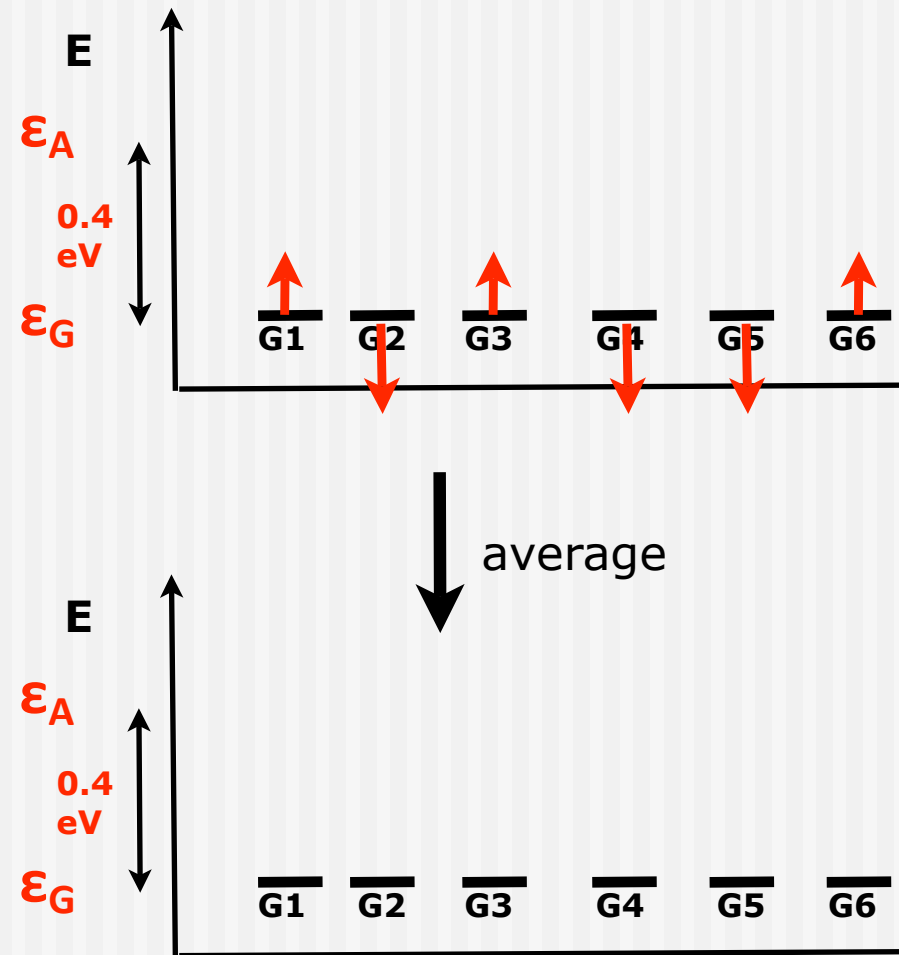
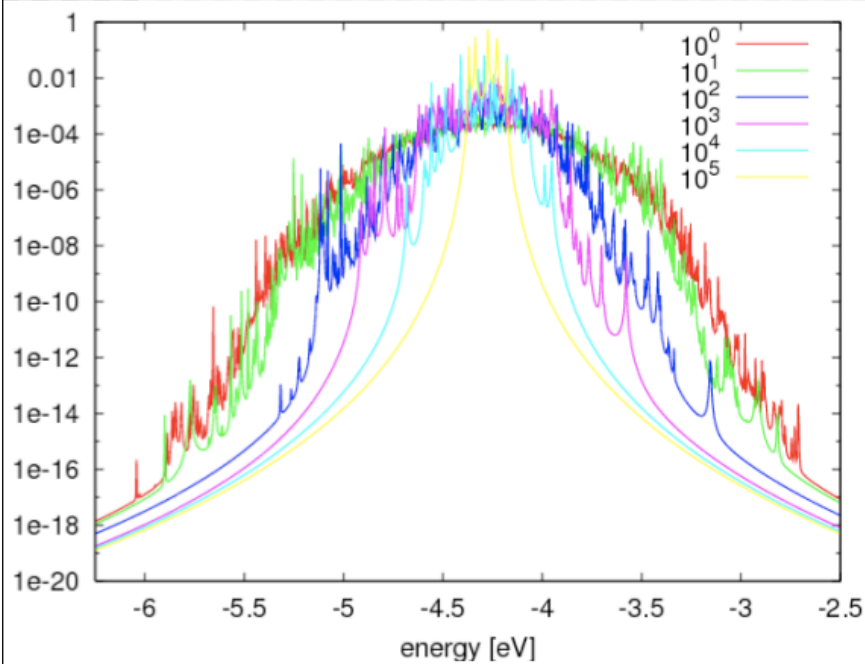
$$\Sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (\epsilon_i - \langle \epsilon \rangle_N)^2} = \sqrt{\langle \epsilon^2 \rangle_N - \langle \epsilon \rangle_N^2}$$

$$\Pi = \prod_{i=1}^{N-1} T_{i,i+1}$$



# how to average the CT parameters?

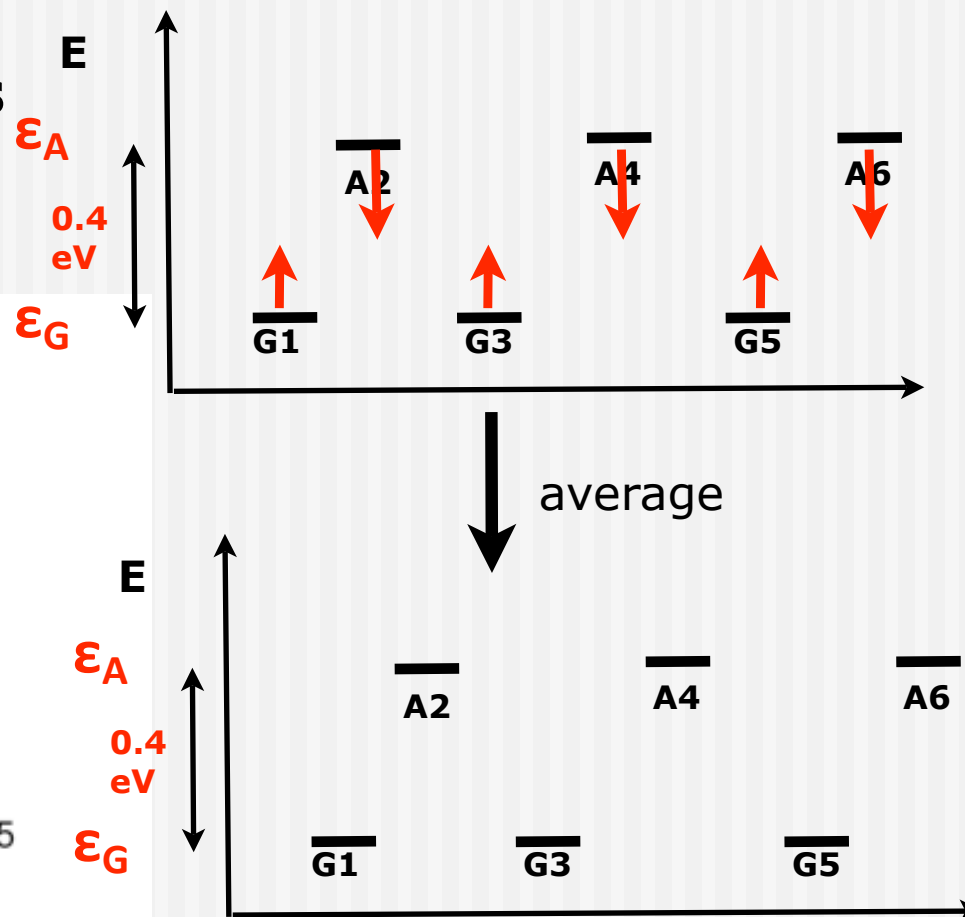
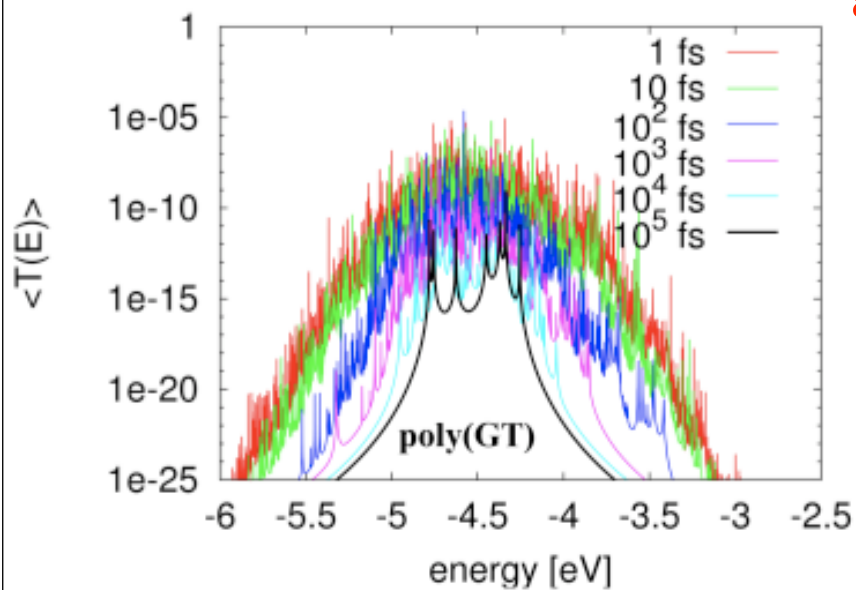
pA:  
transmission **increases**  
with averaging time



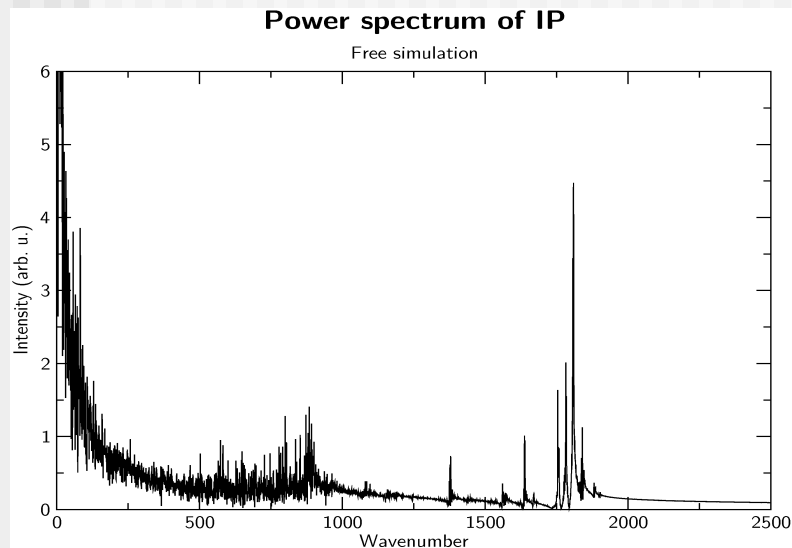


# how to average the CT parameters?

pGT:  
transmission **decreases**  
with averaging time



## so, what are the relevant time-scales?



- internal base modes: 20 fs      1600 cm<sup>-1</sup>
- 'water modes': 40 fs      800 cm<sup>-1</sup>
- water+counterions: 1ps
- ...

cf. Yuri Berlin's talk:  $T_{elec}$  and  $T_{ionic}$

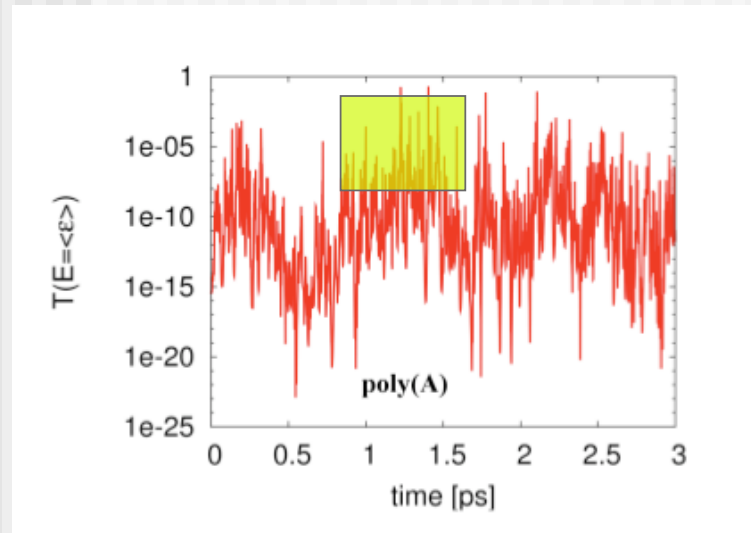
$T_{elec} \ll T_{ionic}$  : statistical analysis (as above)

$T_{ionic} \ll T_{elec}$  : self-averaging of CT parameters

Landauer and Büttiger 1982

so, what are the relevant time-scales?

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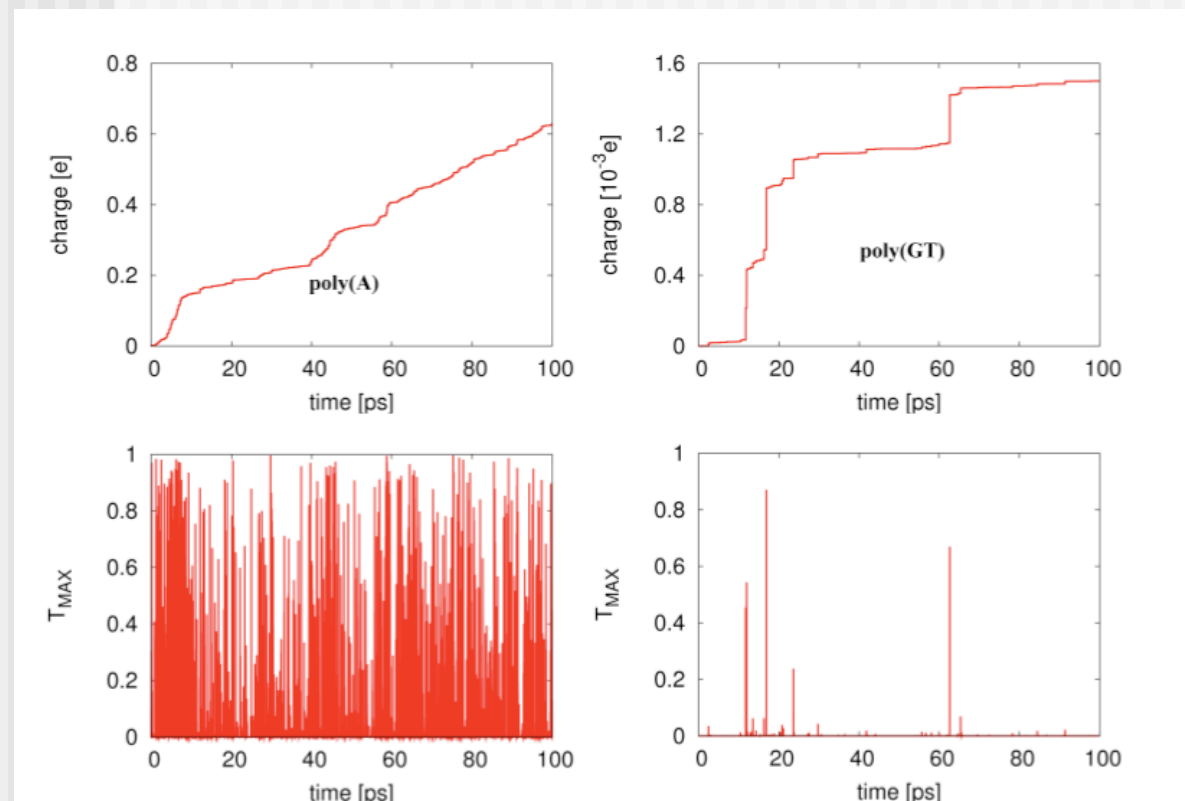


ps time-scale suggests:

CT active conformations  
persistent for several 100fs

average over fluctuations only in  
CT-active windows?

## Integration of Landauer-current...



CT-active conformations in ps-time-scale

- 'fraction of electron' is transferred on ps-time-scale

=> probability, that an electron is transferred during an CT-active state with ps-persistence is about 0.1!

# Acknowledgements

TU BS:



B. Woiczikowski



T. Kubar

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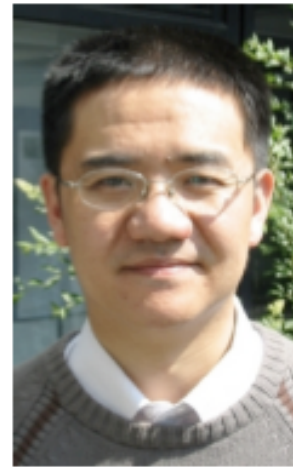
## Dresden group



G. Cuniberti



R. Gutiérrez



B. Song



R. Caetano