

#### The brain at the edge



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Dresden June 18, 2014

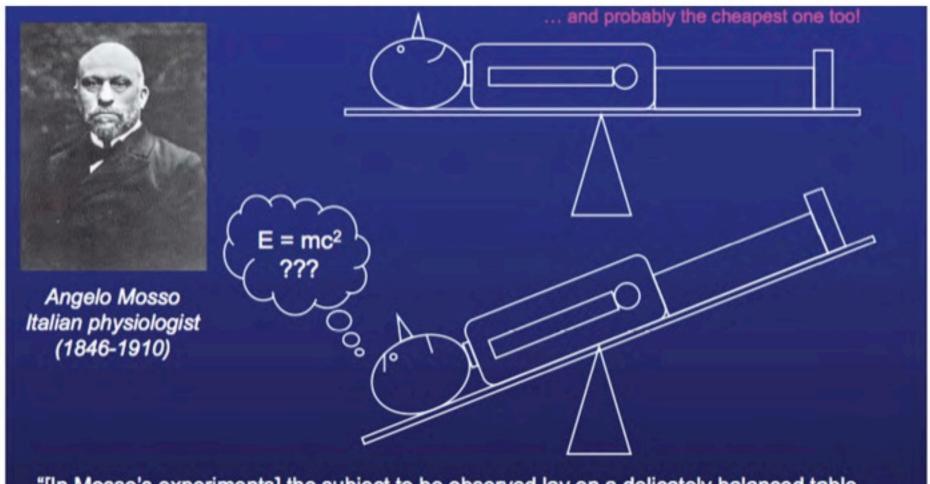


#### Emc<sup>3</sup> Lab

Estudios Multidisciplinarios en Ciencias del Cerebro y sistemas Complejos



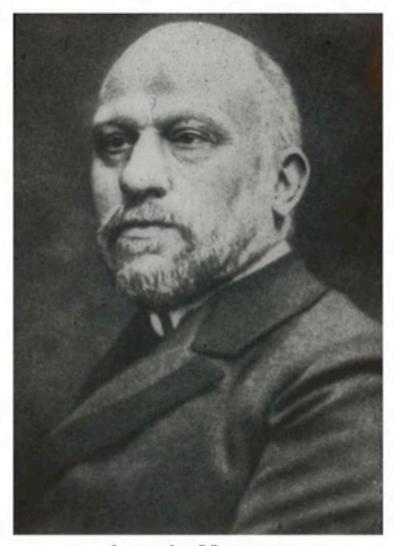
## The first brain critical experiment (~1880)



"[In Mosso's experiments] the subject to be observed lay on a delicately balanced table which could tip downward either at the head or at the foot if the weight of either end were increased. The moment emotional or intellectual activity began in the subject, down went the balance at the head-end, in consequence of the redistribution of blood in his system."

- William James, Principles of Psychology (1890)

#### The first connection between blood flow and mental activity



Veber den Kreislauf des Blutes in Menschlichen Gehirn (Concerning the circulation of the blood in the human brain) Verlag von Viet & Company: Leipzig, 1881

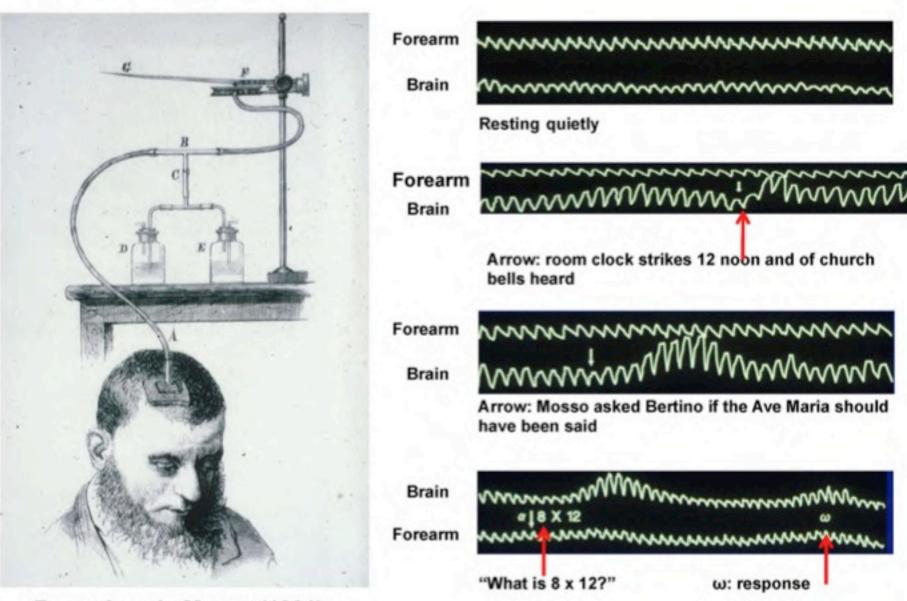


Inventor of the first device to measure muscle force

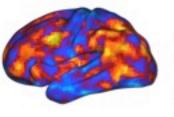
Angelo Mosso 30 May 1846 - 24 November 1910



#### 1878 Experiment with Bertino



From: Angelo Mosso (1881)



## Now we know better why Mosso was unsuccessful in his critical experiment...

- The brain exhibits large spontaneous activity ("brain noise")
- This activity evolves on the (so-called) Resting State Networks (RSN)
- •Even "not doing anything" the brain uses 30% of the body energy ~ 30 Watts
- •When "does something" a few places increase 1 2 % that number

What is the origin and mechanism of that "noise"?

Answer: critical dynamics

#### Two recent reviews

(download from www.chialvo.net/Publications)



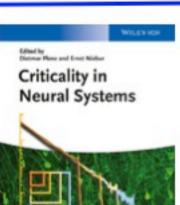
#### **REVIEW ARTICLE**

PUBLISHED ONLINE: XX MONTH XXXX | DOI: 10.1038/NPHY51803

#### **Emergent complex neural dynamics**

Dante R. Chialvo1,2\*

A large repertoire of spatiotemporal activity patterns in the brain is the basis for adaptive behaviour. Understanding the mechanism by which the brain's hundred billion neurons and hundred trillion synapses manage to produce such a range of cortical configurations in a flexible manner remains a fundamental problem in neuroscience. One plausible solution is the involvement of universal mechanisms of emergent complex phenomena evident in dynamical systems poised near a critical point of a second-order phase transition. We review recent theoretical and empirical results supporting the notion that the brain is naturally poised near criticality, as well as its implications for better understanding of the brain.



#### Critical Brain Dynamics at Large Scale

Dante R. Chialvo

Some general properties expected near the critical point of a continuous phase transition:

- Long range correlations in space and time.
- Correlation length scales with system size
- Anomalous scaling of the variance of the fluctuations
- Variance of the order parameter peaks at the critical point (susceptibility)
- Scaling in the clusters size distribution
- Scaling of avalanches sizes

## Long range correlations in space and time.

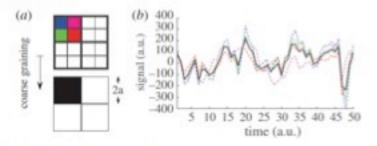
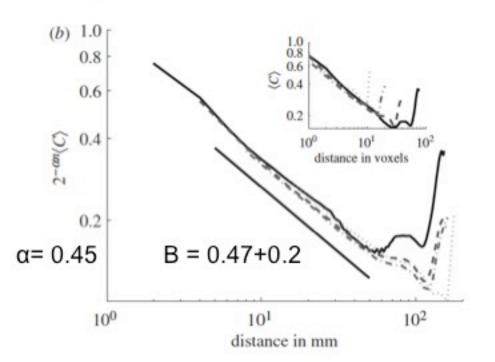


Figure 6. (a) Example of coarse graining in two dimensions where there are four boxes B within a block-box B'. (b) The four dashed-coloured signals from the four original boxes B are averaged to produce the solid-black coarse-grained signal of B'.

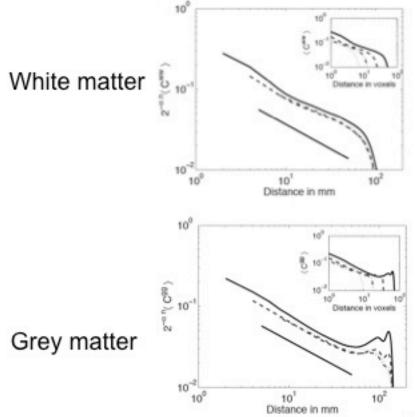




#### Self-similar correlation function in brain resting-state functional magnetic resonance imaging

Paul Expert<sup>1,2</sup>, Renaud Lambiotte<sup>1</sup>, Dante R. Chialvo<sup>4</sup>, Kim Christensen<sup>1,2</sup>, Henrik Jeldtoft Jensen<sup>1,3,\*</sup>, David J. Sharp<sup>5</sup> and Federico Turkheimer<sup>5</sup>

<sup>1</sup> Institute for Mathematical Sciences, 53 Prince's Gate, Exhibition Road, Imperial College London, London SW7 2PG, UK



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Simple example of a apparently complex dynamic

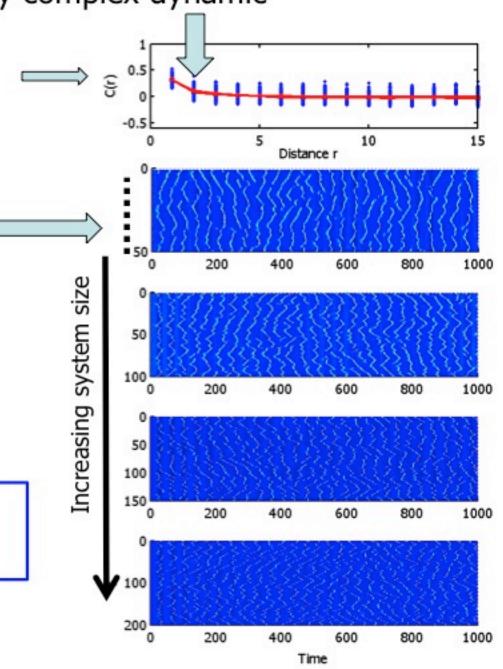
with finite correlation length

1- Estimate the (average) two point correlation function of all pairs (as a function of Euclidean distance between the pair)

2- Repeat for increasing system's size



In this example the correlation length is a constant: is the trivial "wave length"



one bird



two birds

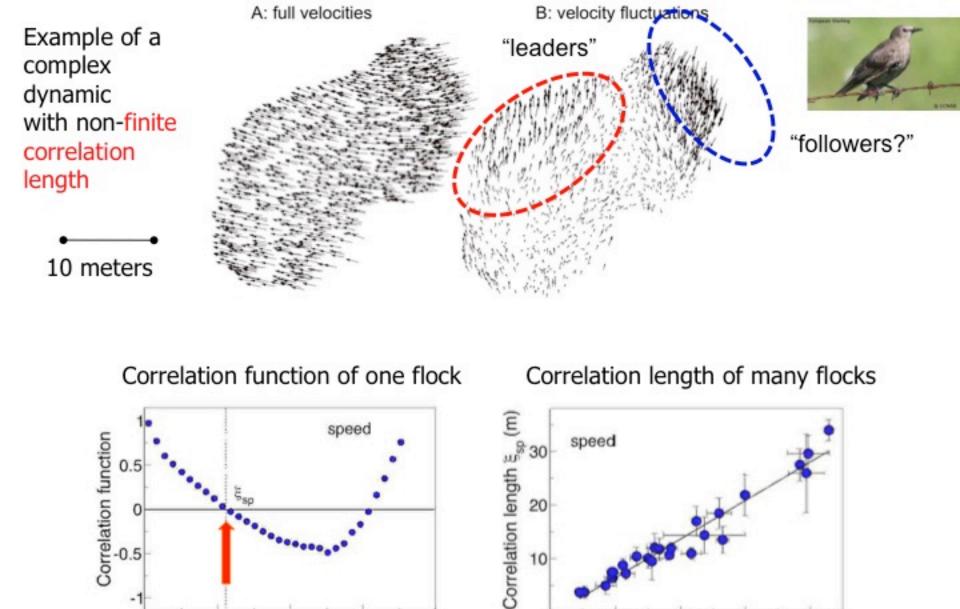




Too many birds



300000 starlings in the spring (real time.)

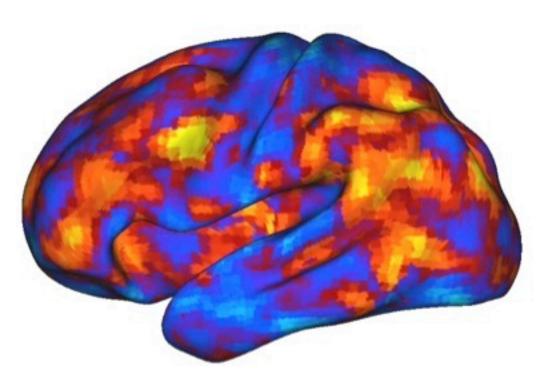


From Andrea Cavagna et al, Scale-free correlations in bird flocks, arXiv:0911.4393, (2010); Also in PNAS (2010)

Flock size L (m)

Distance r (m)

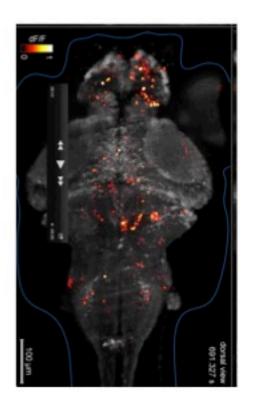
### Example of another complex dynamics



fMRI data from a healthy subject during resting state, shown about 13 times faster than real time (BOLD signal with the mean substracted).

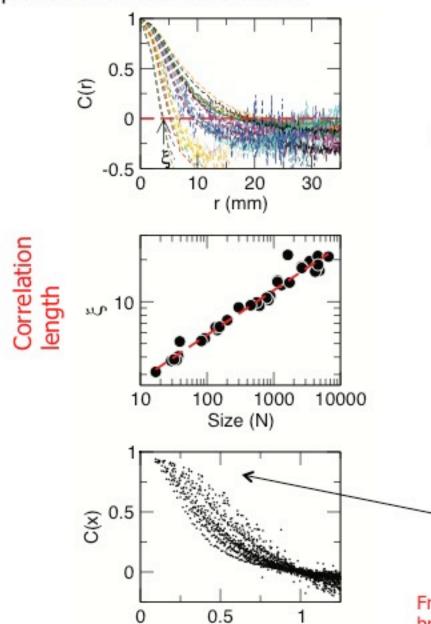


Head



Tail

Whole-brain functional imaging at cellular resolution using light-sheet microscopy. Misha B Ahrens et al , Nature Methods. (2013) Compute the average two point correlation for blobs, plot as a function of distance



Rescaled  $x = (r/\xi)$ 

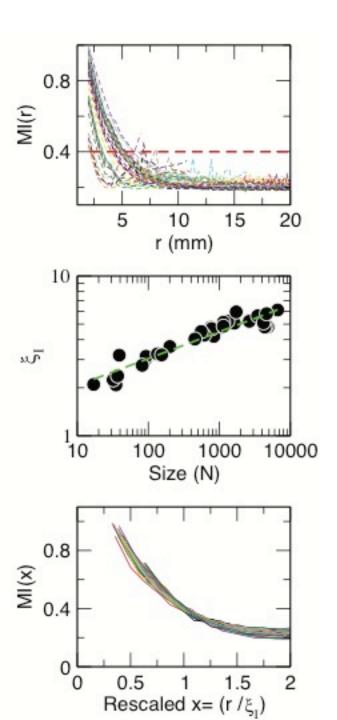
#### Correlation length diverges with cluster size

Big, intermediate and small "blobs" behaves all in the same way

The bottom line: Two places 4 mm appart on a blob of 20 voxels are as correlated as those 40 mm appart on a blob of 4000 voxels

Rescaled C(x) is not very good and worst for less spherical blobs, as expected

Fraiman D. & Chialvo DR. What kind of noise is brain noise. Frontiers in Fractal Physiology. (2012)



Doing the same for Mutual Information

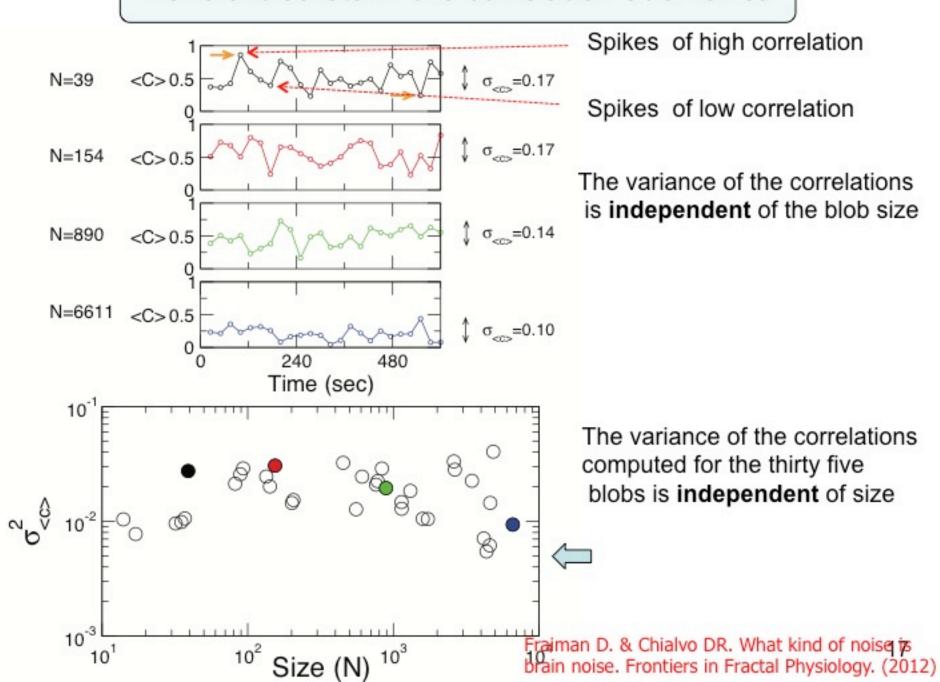
$$MI(X;Y) = H(X) - H(X \mid Y)$$

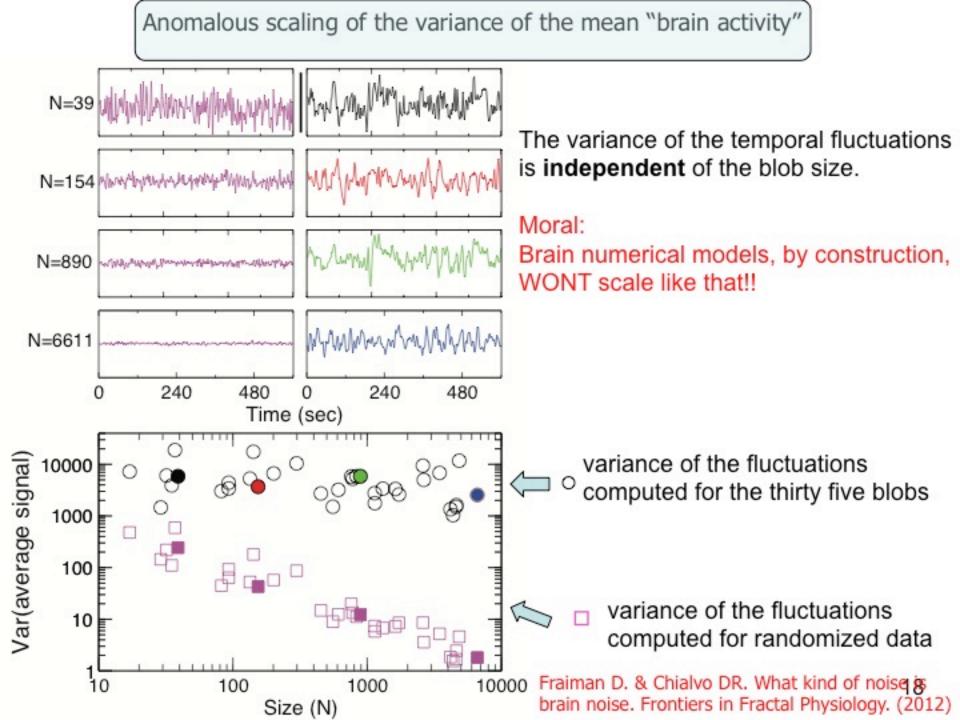
Mutual information MI(r) as a function of distance r averaged over all time series of each of the thirty five blobs.

Mutual information diverges with cluster size.

Rescaled mutual information

#### Transient bursts in the correlation at all sizes





Some general properties expected near the critical point of a continuous phase transition:

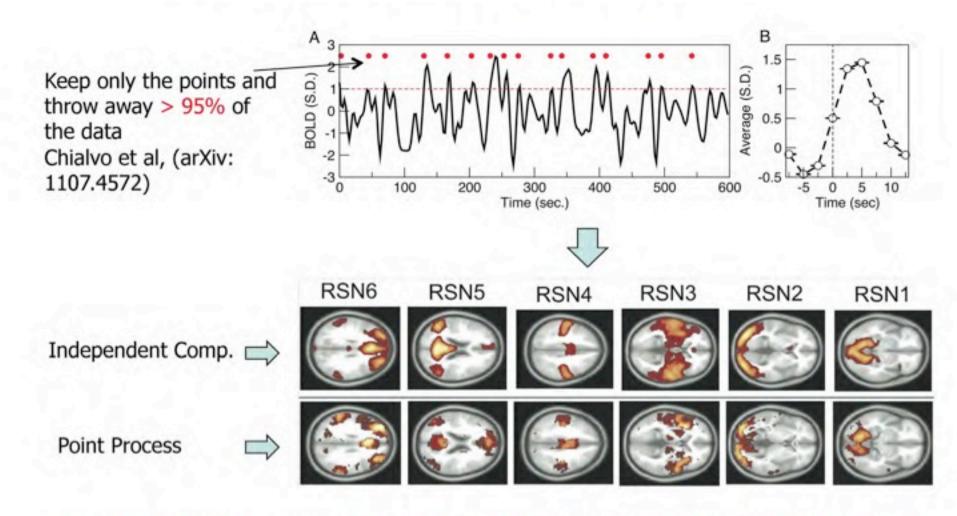
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# We need to resample the dynamics

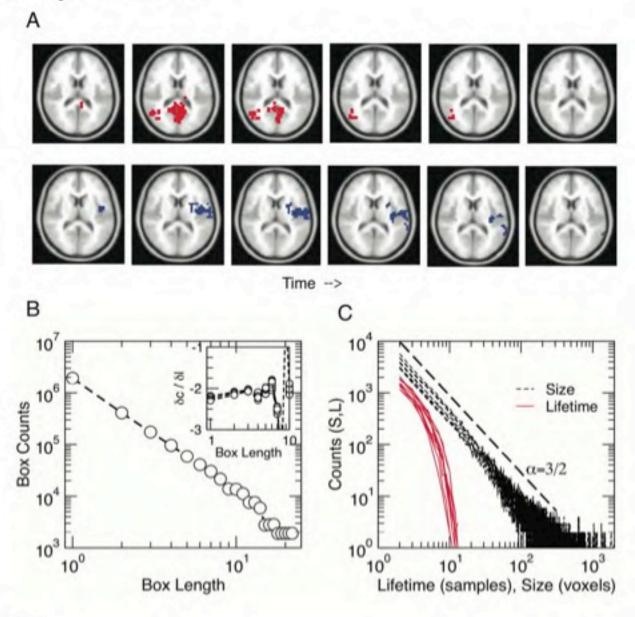
Let call Poincare

#### (Compresing and resampling thanks to Poincare)



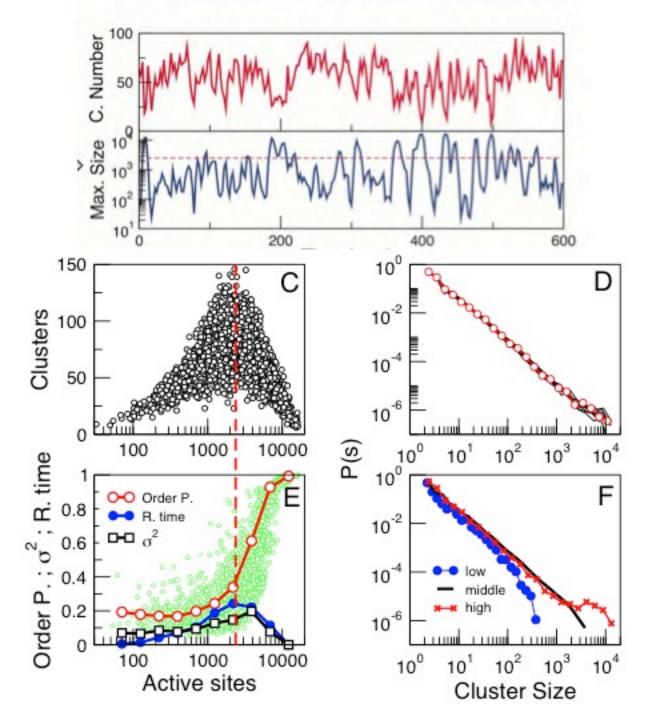
Moral: Despite the huge data reduction (> 95%) a few points holds more of the information.

## Earthquakes in your head



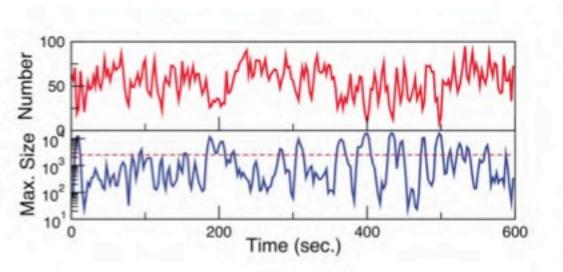
Some general properties expected near the critical point of a continuous phase transition:

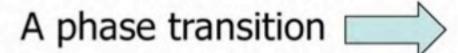
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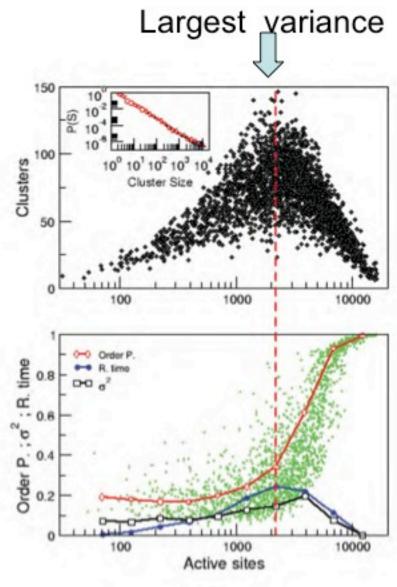


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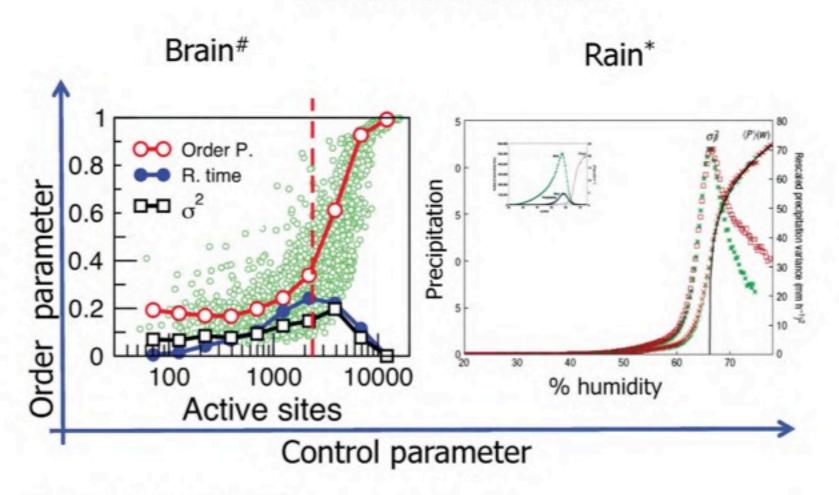




Some general properties expected near the critical point of a continuous phase transition that are seen in fMRI brain data:

- ✓ Long range correlations in space and time.
- ✓ Correlation length scales with system size.
- Anomalous scaling of the variance of the fluctuations
- ✓ Scaling of avalanches sizes
- ✓ Scaling in the clusters size distribution
- ✓ Variance of the order parameter peaks at the critical point (susceptibility)

#### The end of Brain SOC?



<sup>\*</sup>Peters & Neelin, Nature Phys. (2006).

<sup>#</sup> Tagliazucchi et al, Frontiers (2012).

### Lets do some modeling



#### Modeling the connectome

Brain Organization into Resting State Networks Emerges at Criticality on a Model of the Human Connectome

Ariel Haimovici, Enzo Tagliazucchi, Pablo Balenzuela, and Dante R. Chialvo Phys. Rev. Lett. 110, 178101 (2013) – Published April 22, 2013



Ariel Haimovici

Physics 6, 47 (2013)



#### Viewpoint

#### The Critical Brain

#### Dietmar Plenz

Section on Critical Brain Dynamics, National Institute of Mental Health, NIH, Bethesda, MD 20892, USA

Published April 22, 2013

A model describing the brain as a system close to a phase transition can capture the global dynamics of brain activity observed in fMRI experiments.

Subject Areas: Biological Physics

## Mapping the brain: MegaProjects (\$\$\$)

- 1. Human Connectome Project, USA.
- 2. BRAIN (Brain Research through Advancing Innovative Neurotechnologies), USA.
- 3. Human Brain Project, Europe.
- 4. Brainnetome Project, China.
- ---These projects all focus on determining "connections"...(brain as a "circuit")
  --- Our work shows that connections are
- insufficient to understand the brain

## A related problem to help our thinking traffic





solid



gas

structure



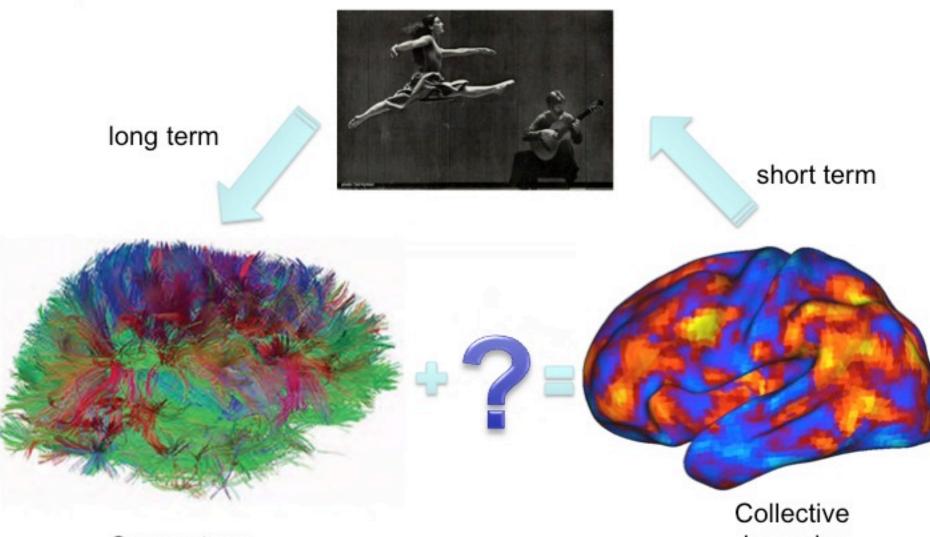
Individual Non-linear dynamics

"phases"

"Streetome"

## The problem:

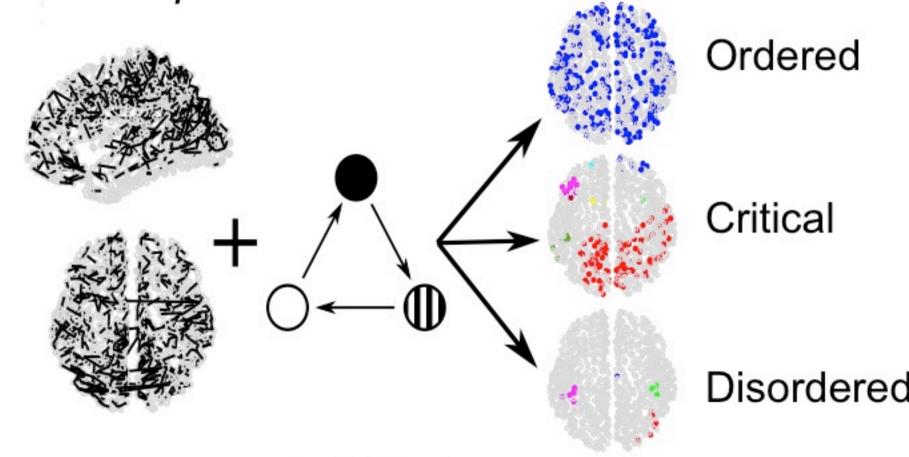
**Behaviors** 



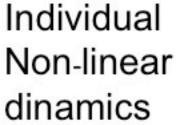
Connectome

dynamics

## The solution: A simple model



Structure

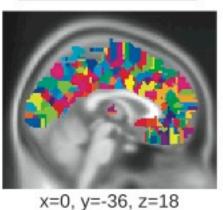


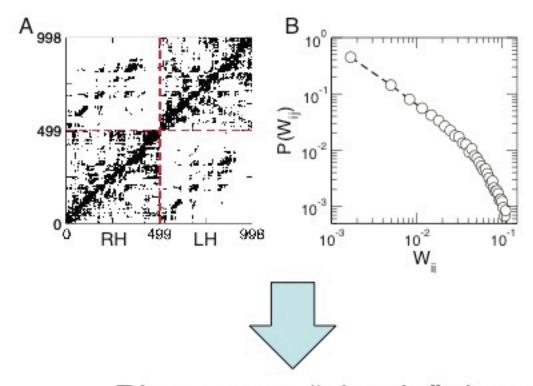


phases

## The structure: the human connectome



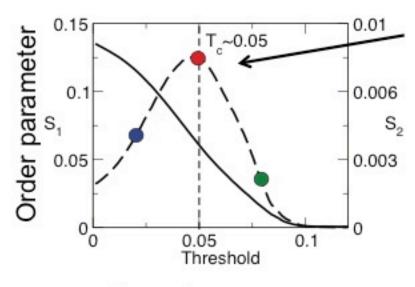




Plus some "simple" dynamics actually (if universality applies almost any nonlinear one

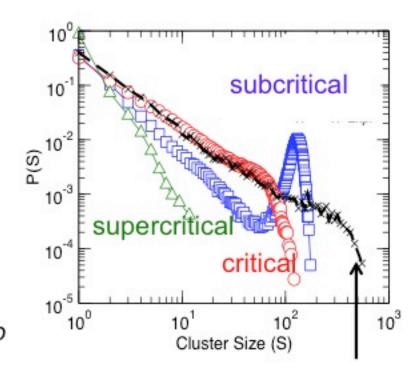
-Haimovici A, et al. Brain organization into resting state networks emerges from the should give the same result... connectome at criticality. PRL (2013).

## The model's collective dynamic exhibit different phases



Control parameter

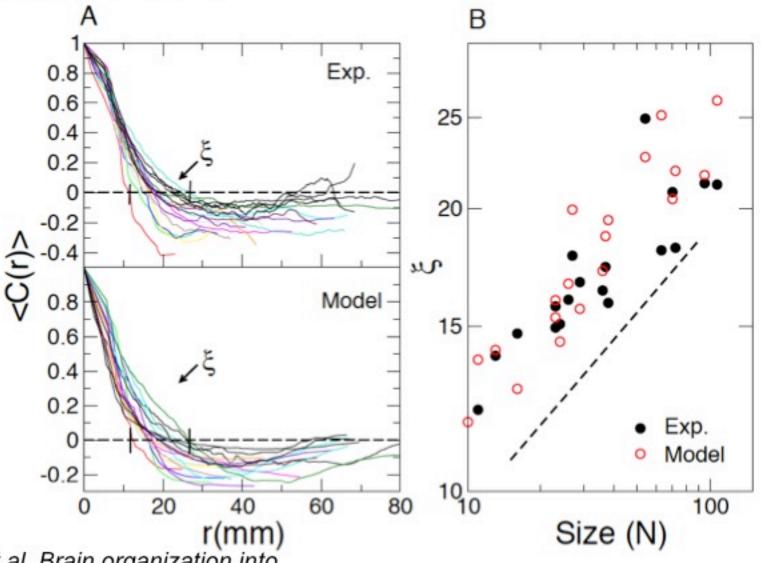
#### Phase transition



-Haimovici A, et al. Brain organization into resting state networks emerges from the connectome at criticality. PRL (2013).

The experimental dynamics is replicated only at criticality

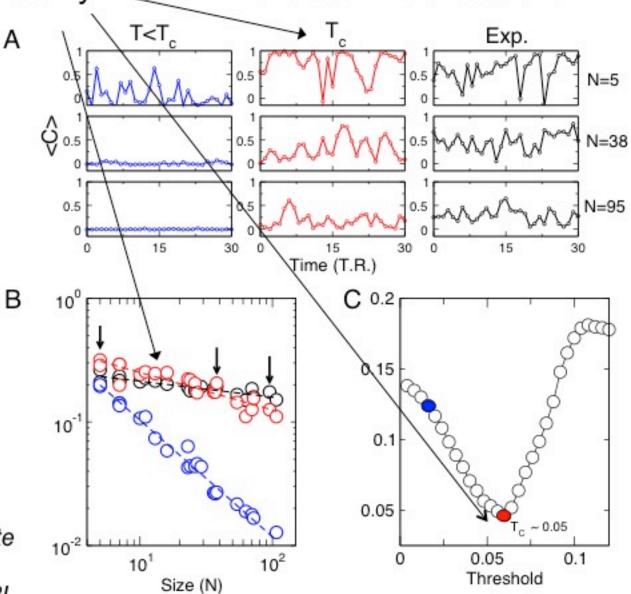
#### Divergence of correlations



-Haimovici A, et al. Brain organization into resting state networks emerges from the connectome at criticality. PRL (2013).

The experimental dynamics is replicated only at criticality

Anomalous scaling of short term correlations

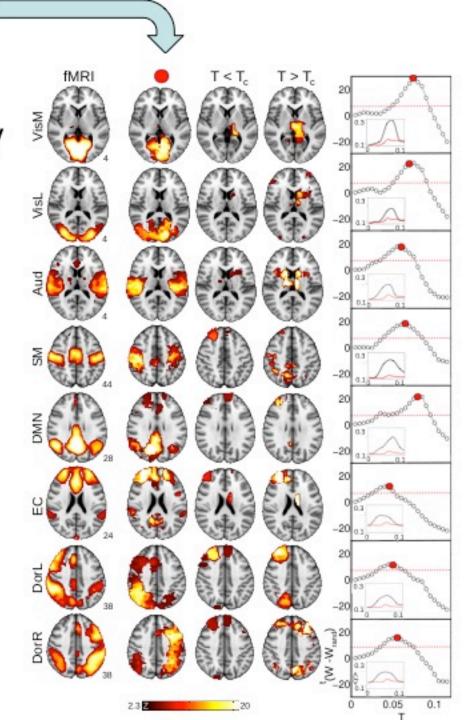


-Haimovici A, et al. Brain organization into resting state networks emerges from the connectome at criticality. PRL (2013).

The experimental dynamics is replicated only at criticality

(resting state networks)

-Haimovici A, et al. Brain organization into resting state networks emerges from the connectome at criticality. PRL (2013).



#### Summary

- 1- Some general properties expected near the critical point of a continuous phase transition are seen in fMRI brain data:
- ✓ Long range correlations in space and time.
- ✓ Correlation length scales with system size
- ✓ Anomalous scaling of the variance of the fluctuations
- ✓ Variance of the order parameter peaks at the critical point (susceptibility)
- ✓ Scaling in the clusters size distribution
- ✓ Scaling of avalanches sizes
- 2- A model based on the brain connectivity replicates the observations ONLY at criticality
- 3- Despite 1 & 2 no theory is at hand to formally explain how the brain does it...