

Kondo excitons and spin-dependent optical phenomena in charged quantum dots

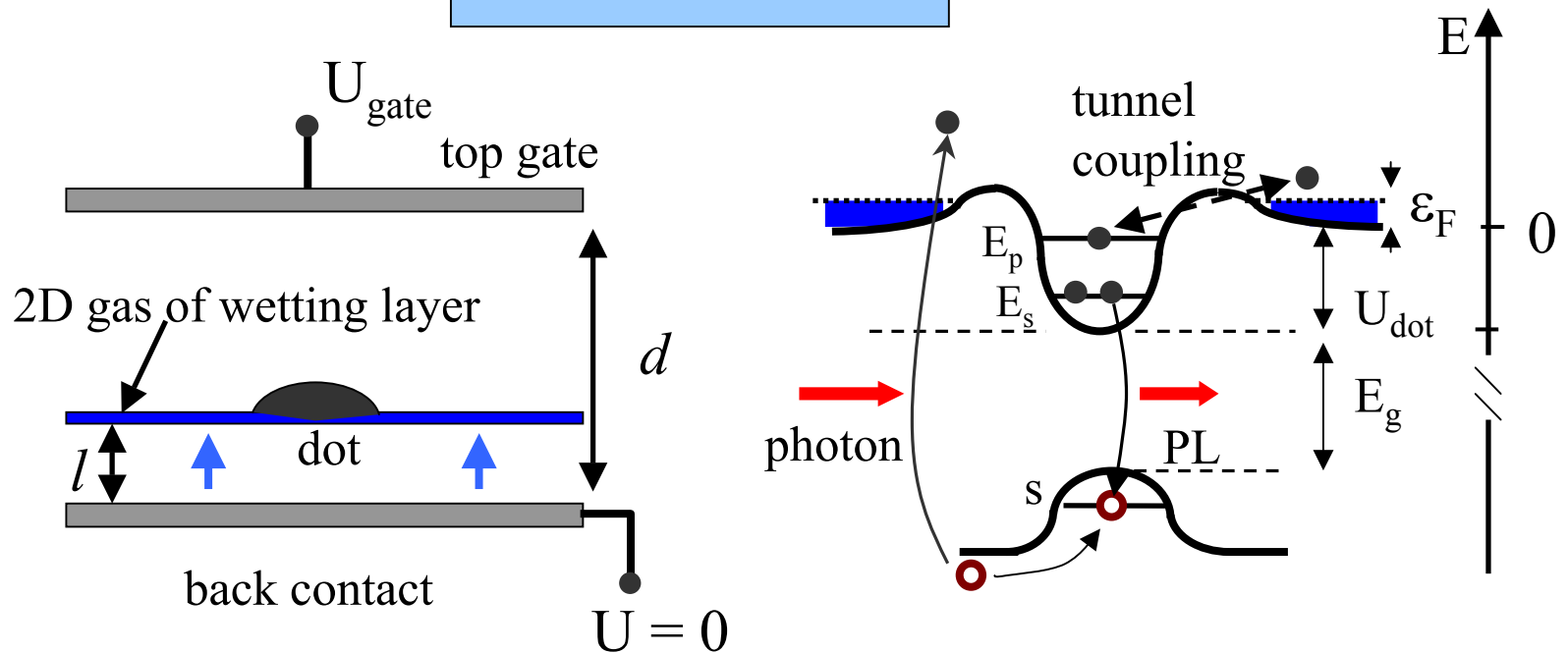
Alexander Govorov

Department of Physics and Astronomy,
Ohio University, Athens, Ohio

Khaled Karrai, Munich University, Germany

Richard J. Warburton, Heriot-Watt University, Edinburgh, UK

Model

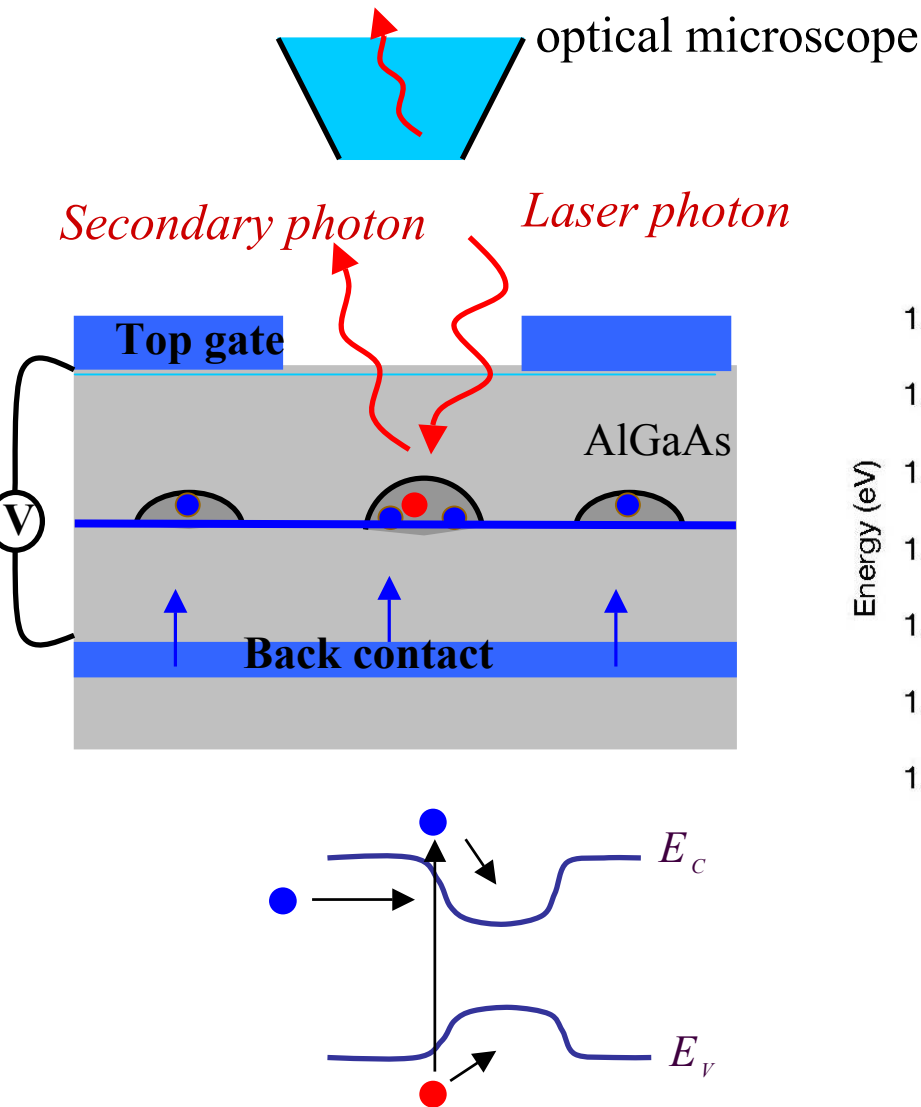


Anderson Hamiltonian:

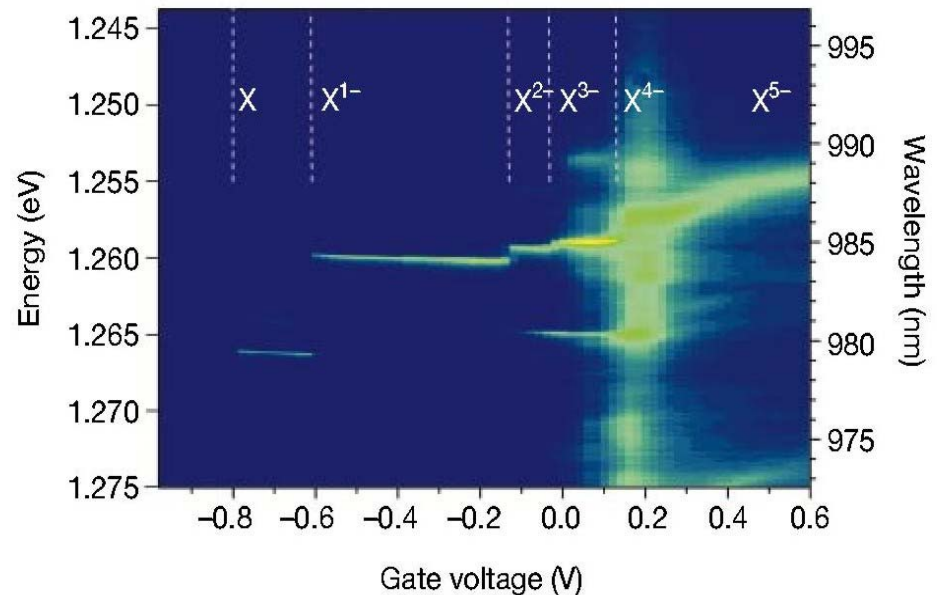
$$\hat{H} = \hat{H}_{\text{single-particle}} + \hat{H}_{\text{Coulomb}}^{\text{intra-dot}} + \hat{H}_{\text{hybridization}}$$

$$\hat{H}_{\text{hybridization}} = \sum_{k,\sigma} V_k [a_{p,\sigma}^+ \hat{c}_{k,\sigma} + \hat{c}_{k,\sigma}^+ a_{p,\sigma}]$$

Neutral and Charged excitons in quantum dots



Single-dot spectroscopy

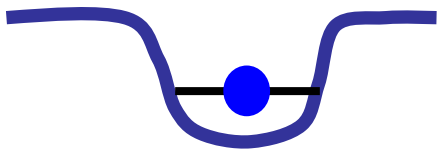


R. Warburton, K. Karrai et al.,
Nature - 2000

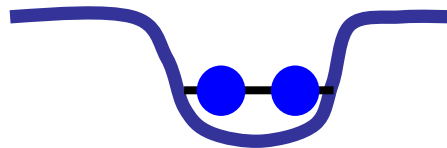
Neutral and charged excitons in quantum dots

X^{n-} ($n+1$ electrons and one hole)

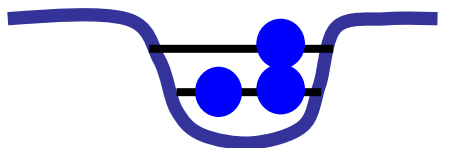
X^0



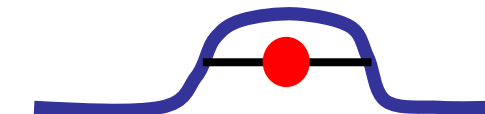
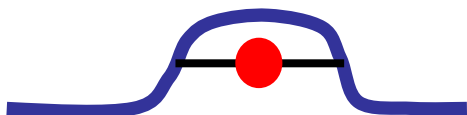
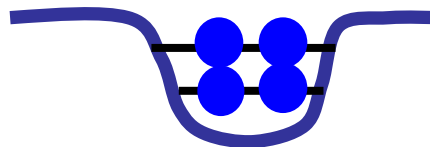
X^{1-}



X^{2-}

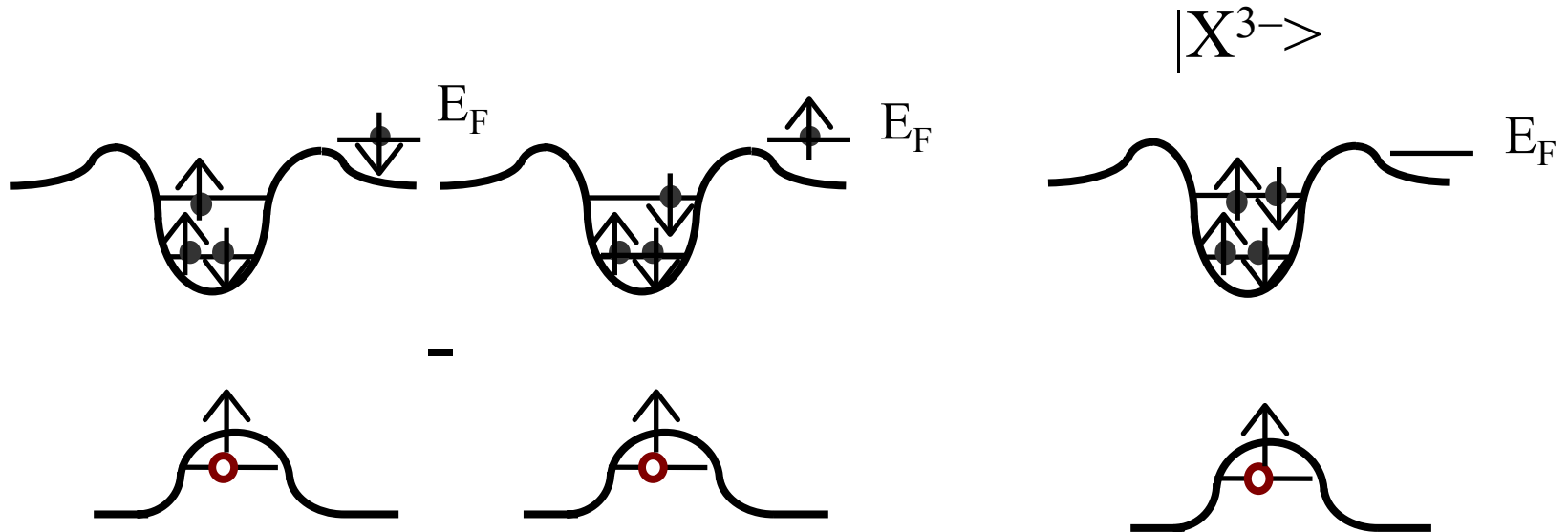


X^{3-}



Zero bandwidth model

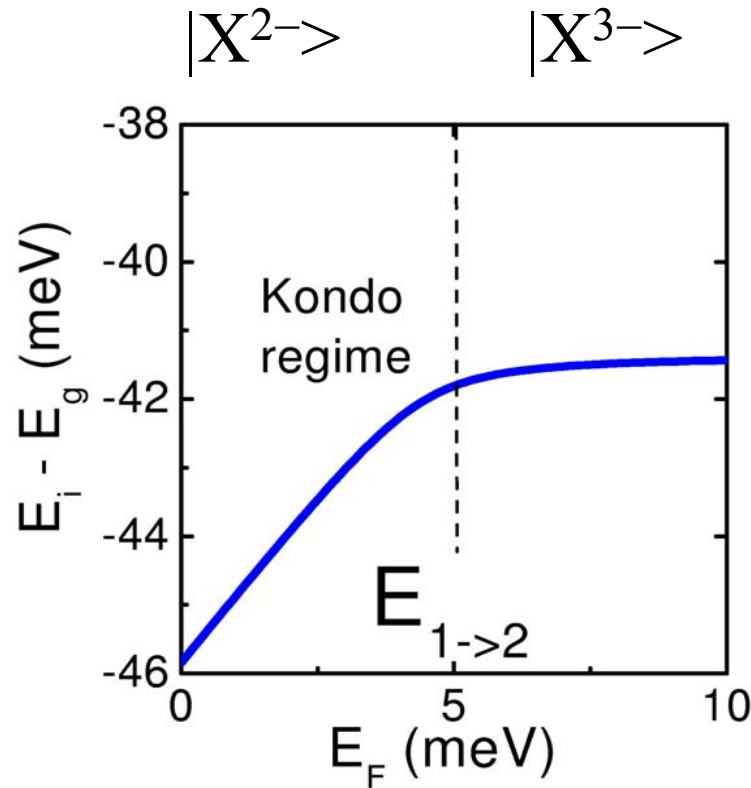
$|X^{2-}\rangle$, Kondo exciton



Ground state: $S_{electrons} = 0$

$$|\Psi_{initial}\rangle = a_1 |X^{2-}\rangle + a_2 |X^{3-}\rangle$$

Initial state energy



Harmonic-oscillator functions with

$$\hbar\omega_x = 20 \text{ meV}$$

$$\hbar\omega_y = 25 \text{ meV}$$

$$U_{dot} = 64 \text{ meV}$$

$$I_{PL}(\omega) = \text{Re} \int_0^{\infty} e^{-i\omega t} \langle i | \hat{V}_{opt}^+(t) \hat{V}_{opt}^+(0) | i \rangle dt$$

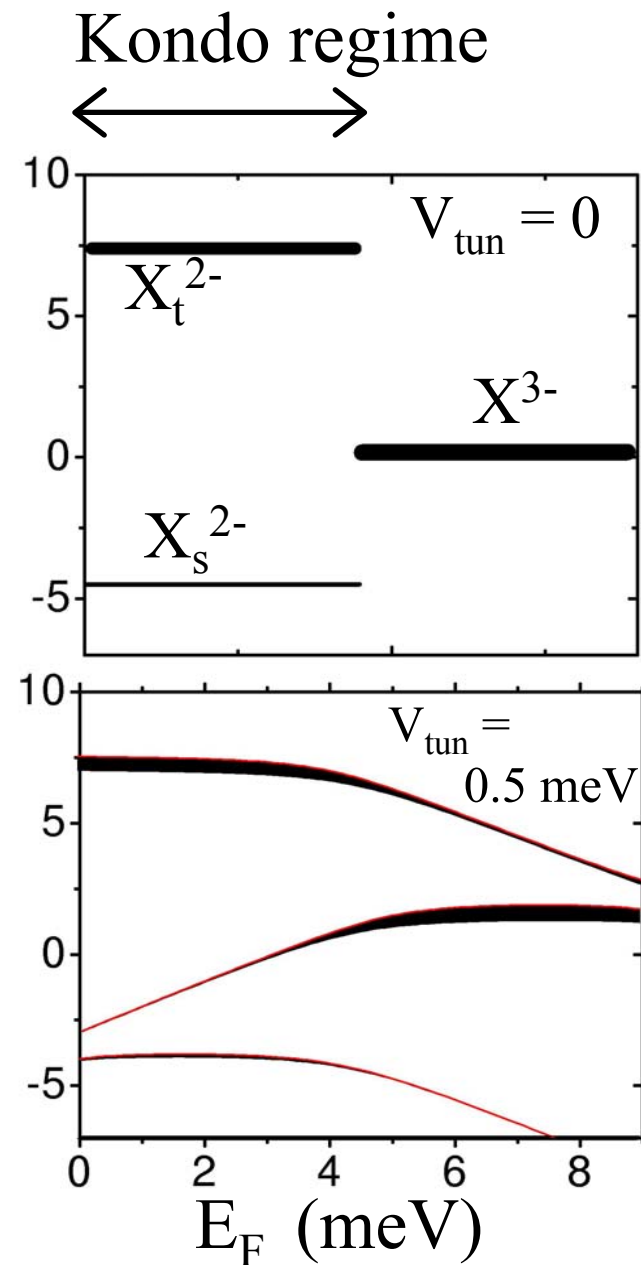
R.J. Warburton et al., Nature – 2000

F. Findeis et al., Phys. Rev. B - 2001

X_s^{2-} singlet final state: $\frac{1}{\sqrt{2}} \begin{pmatrix} \uparrow\downarrow & \uparrow\downarrow \\ \downarrow\uparrow & \downarrow\uparrow \end{pmatrix} \ominus \begin{pmatrix} \uparrow\uparrow & \downarrow\downarrow \\ \downarrow\downarrow & \uparrow\uparrow \end{pmatrix}$
X_t^{2-} triplet final states: $\frac{1}{\sqrt{2}} \begin{pmatrix} \uparrow\downarrow & \uparrow\downarrow \\ \downarrow\uparrow & \downarrow\uparrow \end{pmatrix} \oplus \begin{pmatrix} \uparrow\uparrow & \downarrow\downarrow \\ \downarrow\downarrow & \uparrow\uparrow \end{pmatrix}, \quad \begin{pmatrix} \uparrow\uparrow \\ \downarrow\downarrow \end{pmatrix}$
X^{3-} final state: $\begin{pmatrix} \uparrow\downarrow \\ \uparrow\downarrow \\ \uparrow\downarrow \end{pmatrix}$

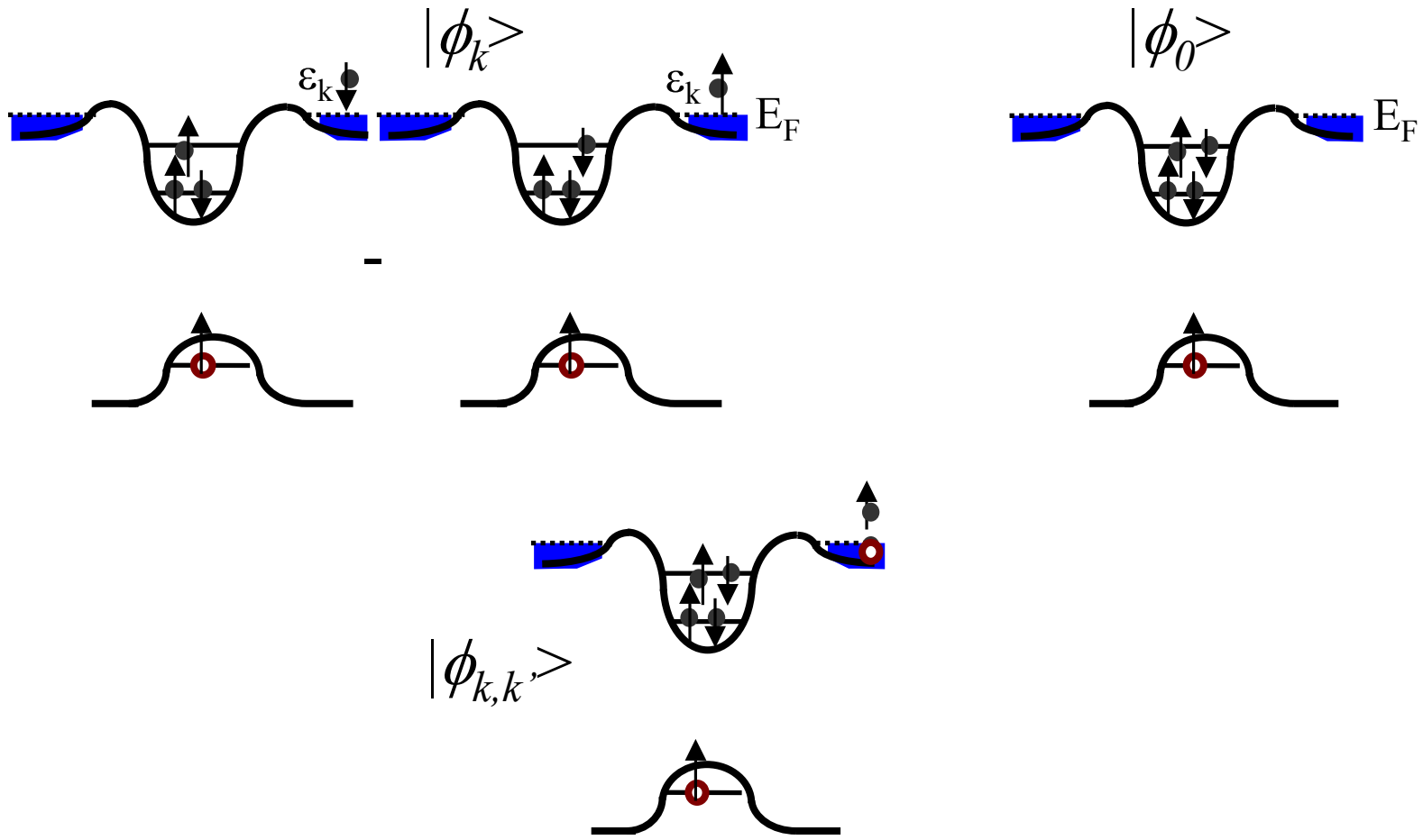
The emission energy depends on $E_F(U_{gate})$

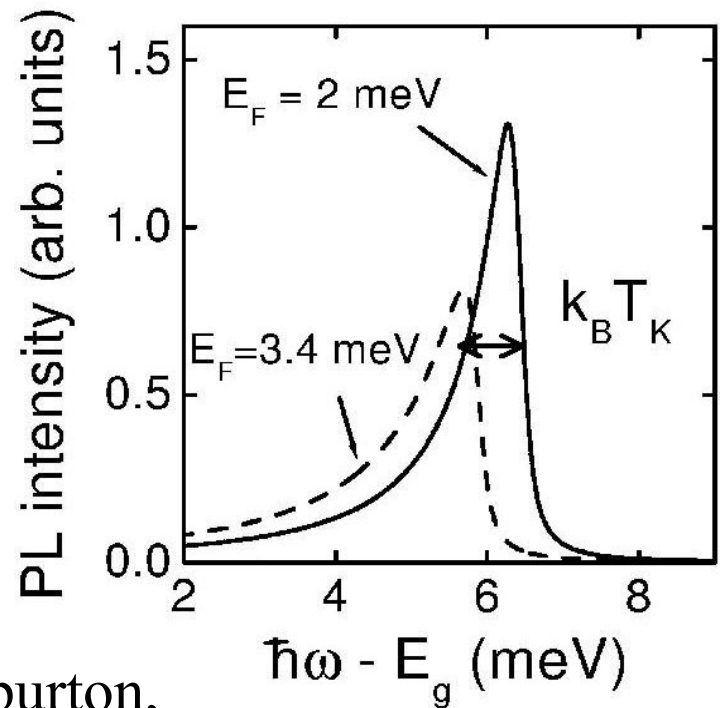
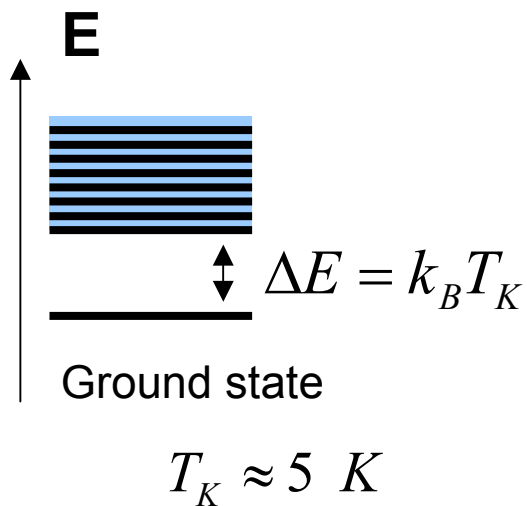
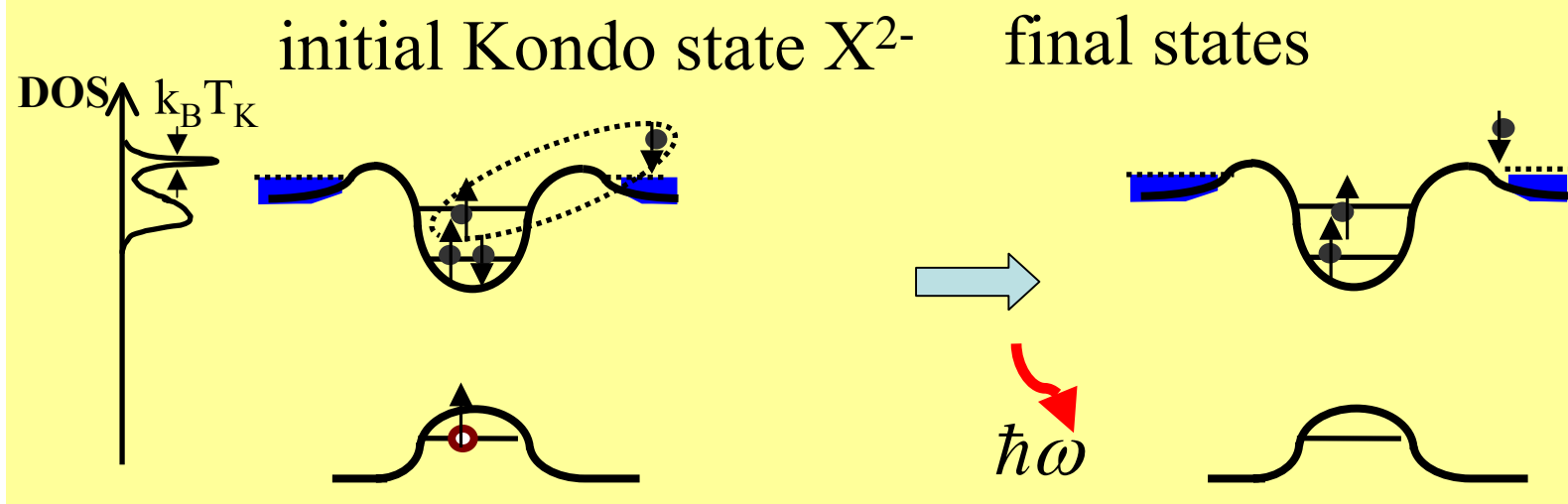
Emission energy, $E - E_g$ (meV)



Finite bandwidth

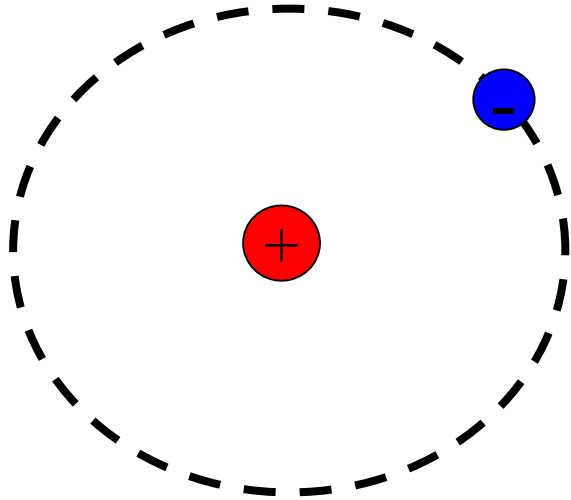
$$|\Psi_{initial}\rangle = \overset{\text{model}}{A_0}|\phi_0\rangle + \sum_{k>k_F} A_k |\phi_k\rangle + \sum_{\substack{k>k_F \\ k'<k_F}} A_{k,k'} |\phi_{k,k'}\rangle$$





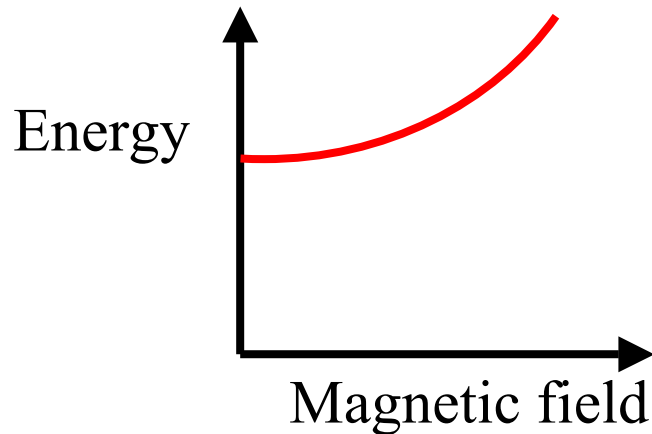
A.O. Govorov, K. Karrai, and R. Warburton,
PRB RC- 2003

Magnetic field effects



Excitons in 3D

$$a_0^* \approx 100 \text{ \AA} \gg a_0$$

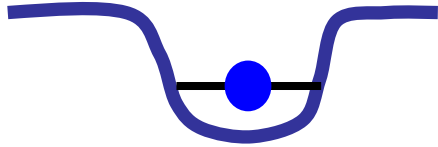


$$E_{exc} = E_{exc}(0) + \alpha B^2$$

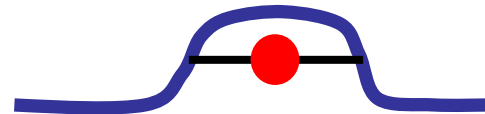
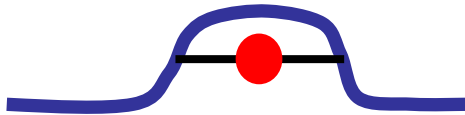
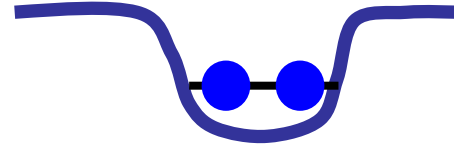
$$\alpha \propto (a_0^*)^2$$

Neutral and charged excitons in quantum dots

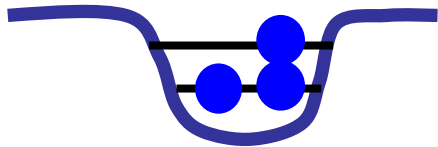
X^0



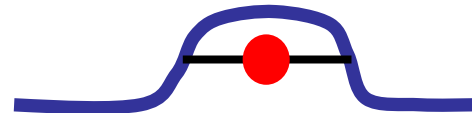
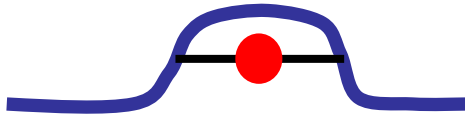
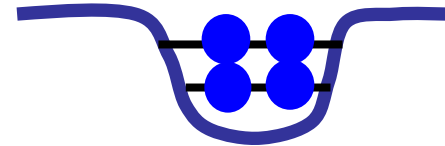
X^{1-}



X^{2-}



X^{3-}



Experimental data

Diamagnetic
behavior

X^{1-}

X^{2-}

X^{3-}

PL energy (eV)

1.265

1.260

-9 -6 -3 0 3 6 9

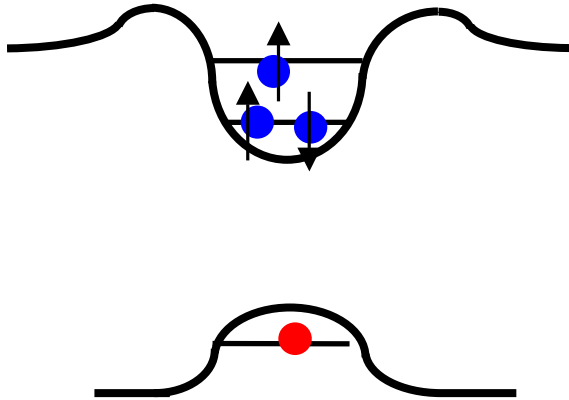
B (tesla)

?????

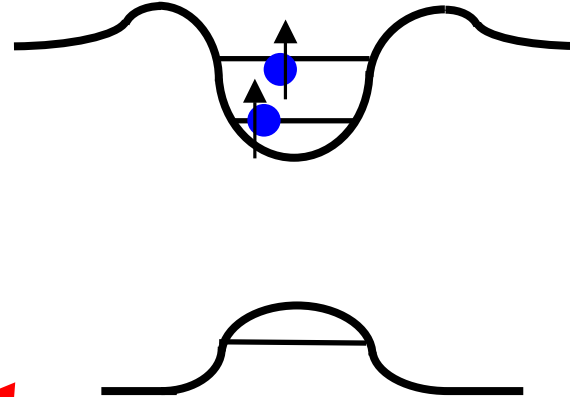
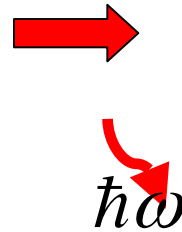
R.J. Warburton, B. Urbaszek, E.J. McGhee, C. Schulhauser, A. Högele, K. Karrai, A.O.Govorov, J.M. Garcia, B.D.Gerardot, and P.M. Petroff, *Nature*, 2004.

X^{2-} - exciton

Initial state



final state

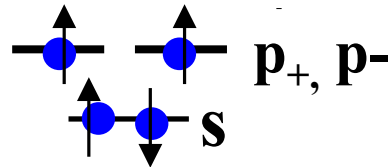


The final state is stable:
Spin blockade

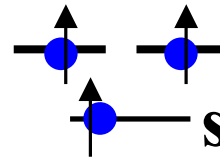
X^{3-} - exciton in a symmetric dot

$B=0$
 $S=1$
 (Hund's rule)

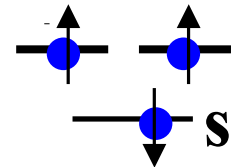
Initial state



Final states



$S=3/2$

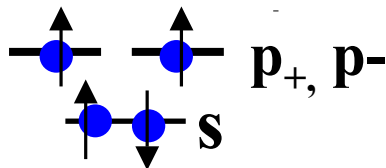


$S=1/2$



$\hbar\omega$

Initial state



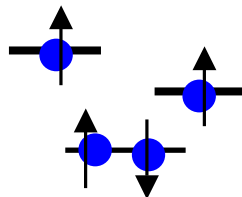
$B=0$

$S=1$ (Hund's rule)



B

Initial state

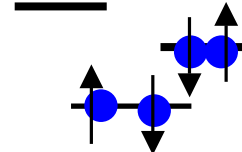


$B < B_{\text{crit}}$
 $S=1$



B

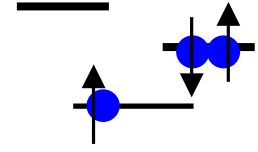
Initial state



$B > B_{\text{crit}}$
 $S=0$



Final state

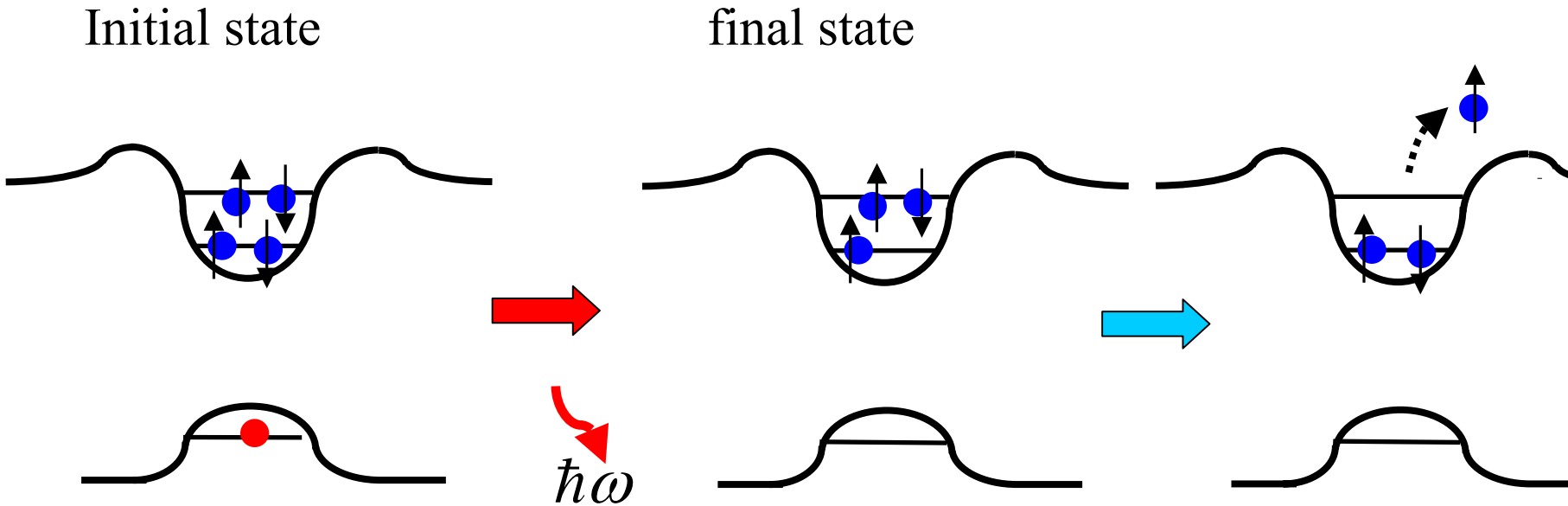


$\hbar\omega$



$B > B_{\text{crit}}$
 $S=1/2$

Exciton X^{3-}

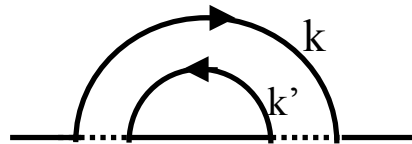
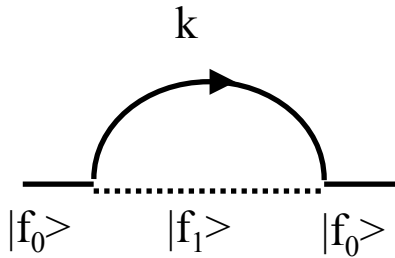
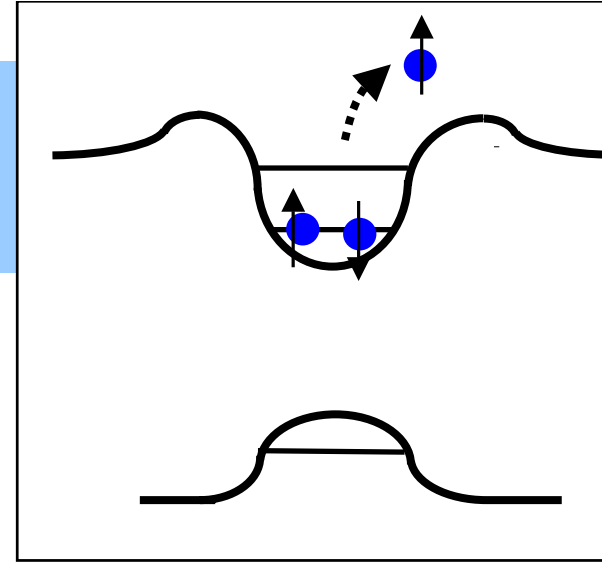


**The final state is not stable
Intra-band Auger-like process**

Coulomb coupling with the d-shell:

A. Wojs and P. Hawrylak, Phys. Rev. B – 1997.

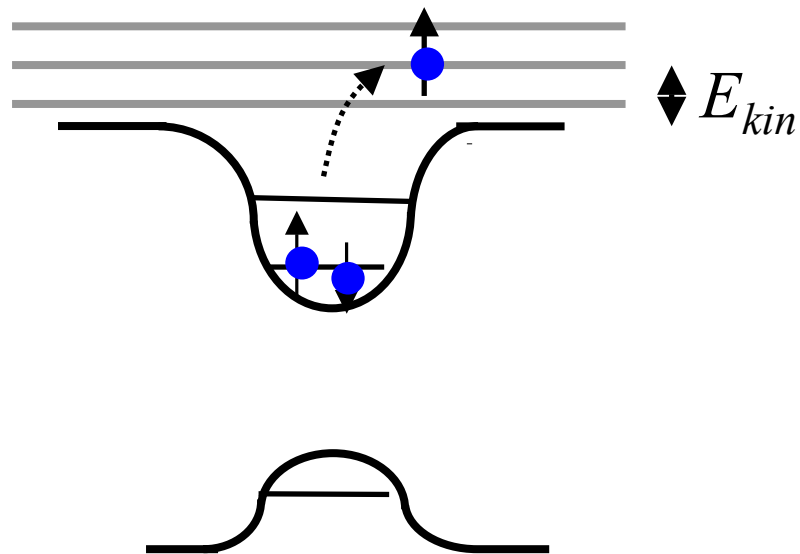
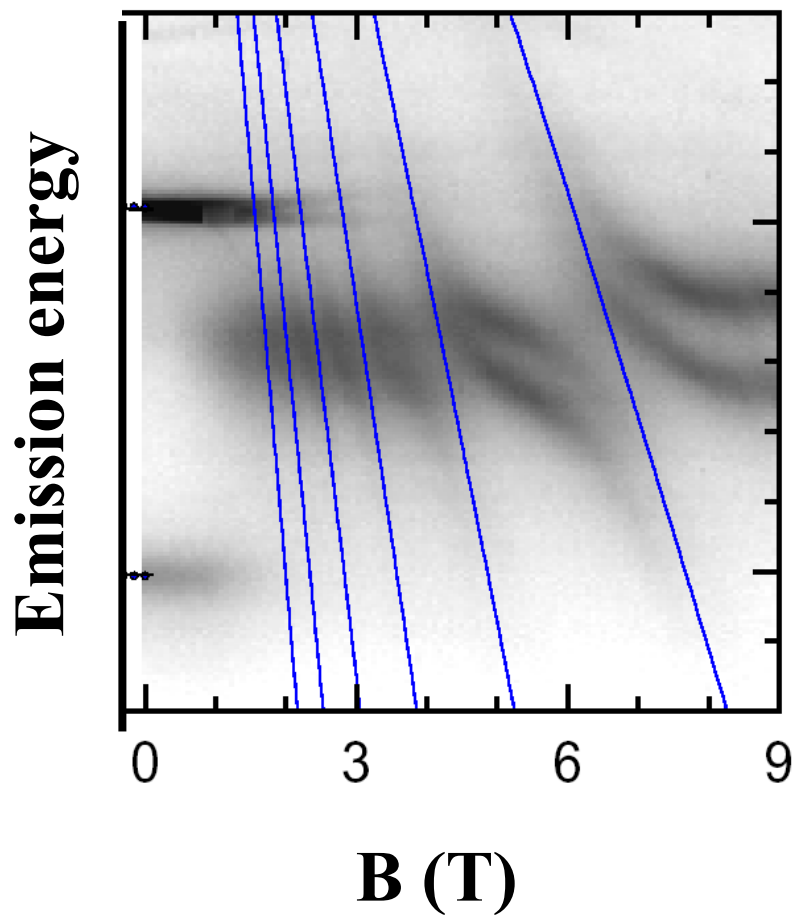
$$\hat{H} = \hat{H}^{\text{intra-dot}} + \hat{H}_{\text{hybridization}}$$



$$I_{PL}(\omega) \propto \text{Re}\left[\frac{-i}{\tilde{\omega} - \Sigma_a - i0}\right]$$

$$\Sigma_a = \int_0^\infty \frac{W_\varepsilon^2 (1 - f_\varepsilon) \rho(\varepsilon) d\varepsilon}{\tilde{\omega} - \delta E_a + \varepsilon - \int_0^\infty \frac{W_\varepsilon^2 f_{\varepsilon'} \rho(\varepsilon') d\varepsilon'}{\tilde{\omega} - \delta E_a + \varepsilon - \varepsilon'}}$$

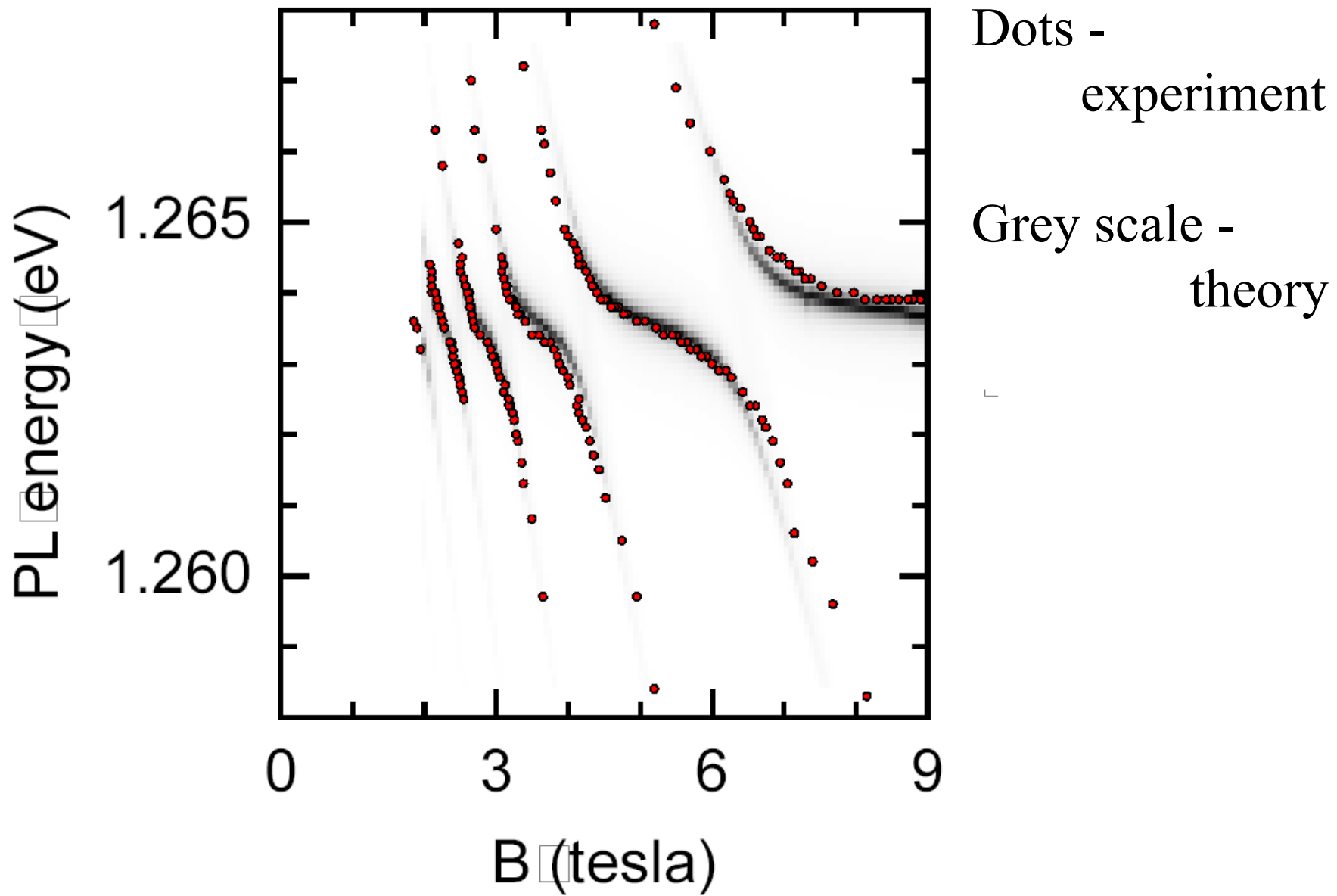
A. Govorov, R.J. Warburton, and K. Karrai, Physica E, 2004



Anticrossing condition:

Excess kinetic energy

$$E_{kin} = E_0 - E_1 = \hbar\omega_c \left(n + \frac{1}{2}\right)$$

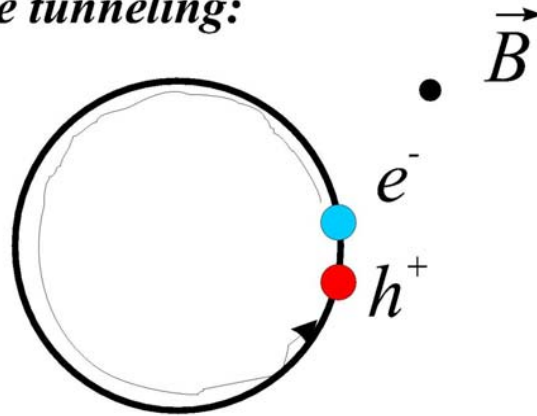


Exciton in ring-like dots

1D ring

Electron-to-hole tunneling:

$$\sum_i q_i = 0$$



$$\Phi = \pi R^2 B > \Phi_0/2$$

$$\Delta E_{exc}(B) = \delta E_{exc}(0) \exp[-2\pi^2 V_0 / \epsilon_0] \cos[2\pi\Phi/\Phi_0]$$

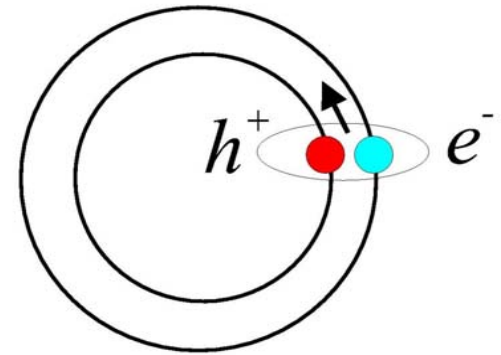
A.V. Chaplik, JETP Lett. - 1995

R.A. Römer and M. E. Raikh,

Phys. Rev. B-2000

quasi-1D ring

Polarized exciton: rotating dipole



$$\Delta\Phi = 2\pi(R_1^2 - R_2^2)B > \Phi_0/2$$

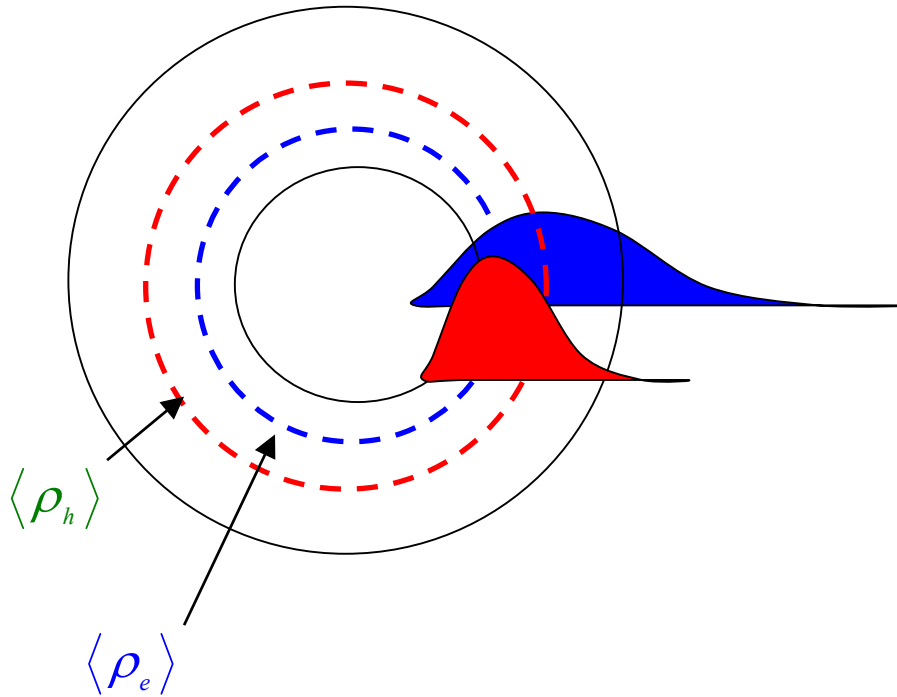
$$\Delta E_{exc}(B) = f(\Delta\Phi)$$

A.V. Kalameitsev, and V. Kovalev,

and A.O. Govorov,

JETP Lett. - 1998

Models of semiconductor nano-ring

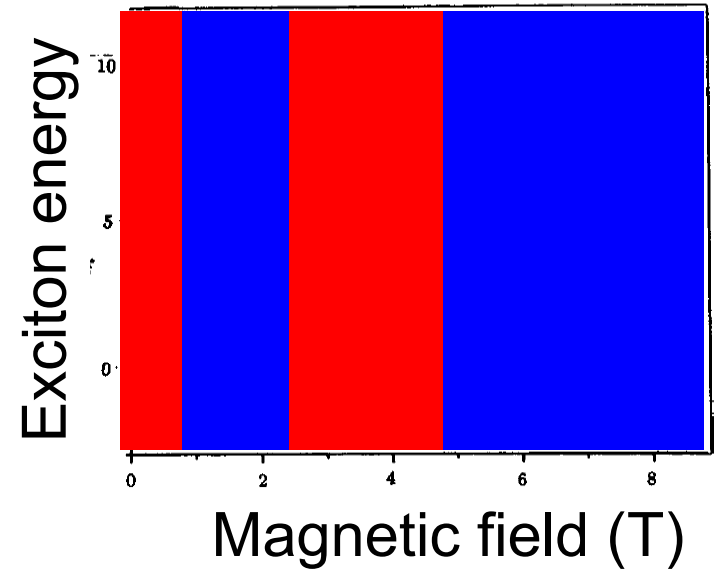
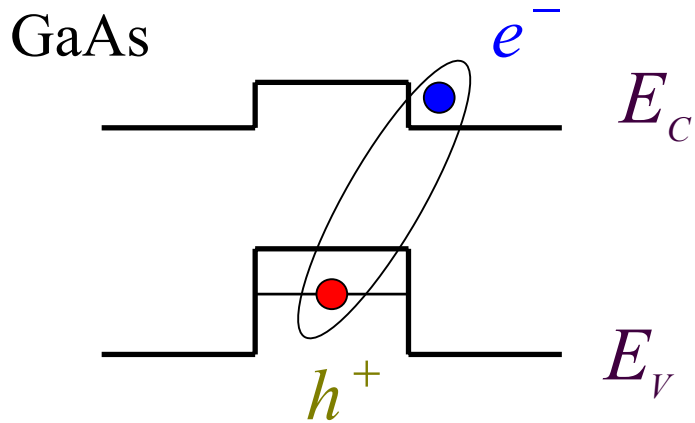
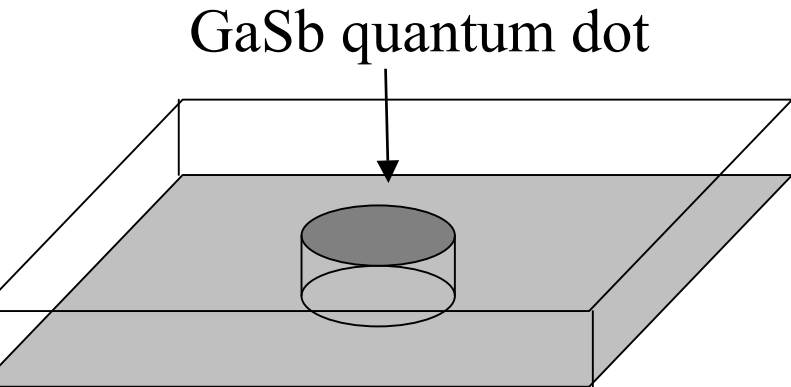


$$U_{e(h)} = \frac{m_{e(h)} \Omega_{e(h)}^2}{2} (\rho - R_0)^2$$

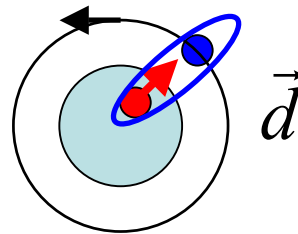
$$m_e \Omega_e \neq m_h \Omega_h$$

A.O. Govorov, S. E. Ulloa, K. Karrai,
and R. J. Warburton, PRB RC - 2002.

Type-II quantum dots



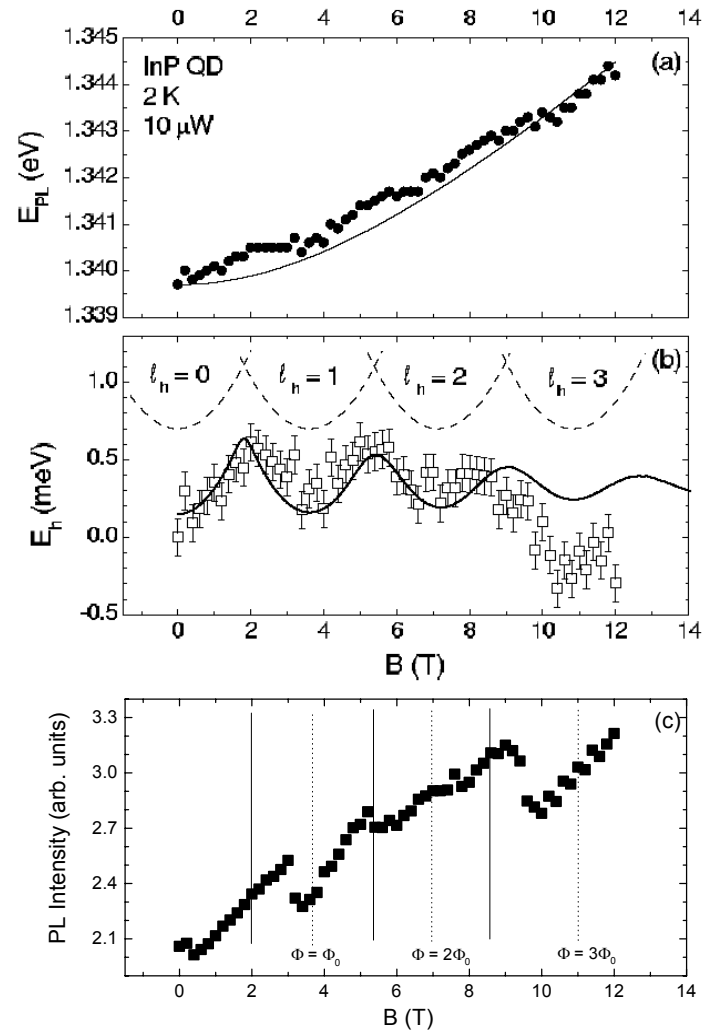
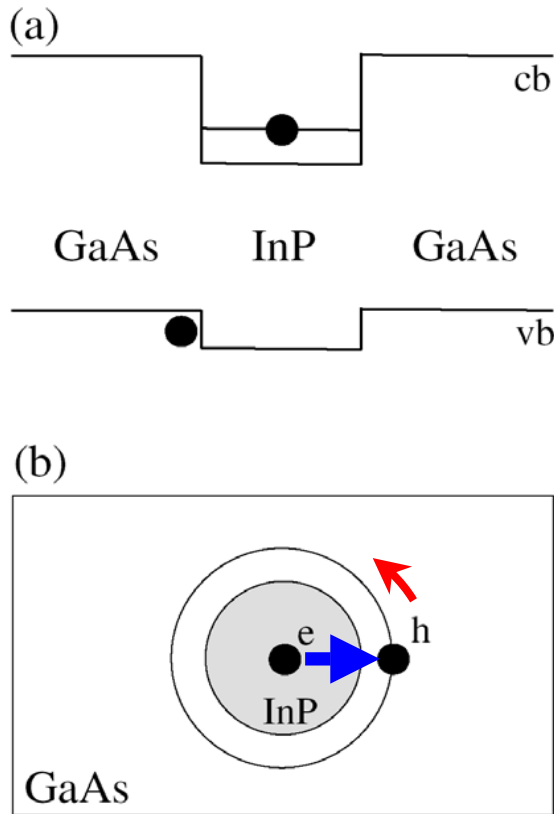
Top view



$$\phi = \pi(R_e^2 - R_h^2)B \approx \phi_0$$

A.V.Kalameitsev, and V.Kovalev, and A.O.Govorov, JETP Lett. - 1998

Experiment with type-II quantum dots



E. Ribeiro, A.O. Govorov, G. Medeiros-Ribeiro, and W. Carvalho Jr
 Phys. Rev. Lett. (2004) .

X^{1-}

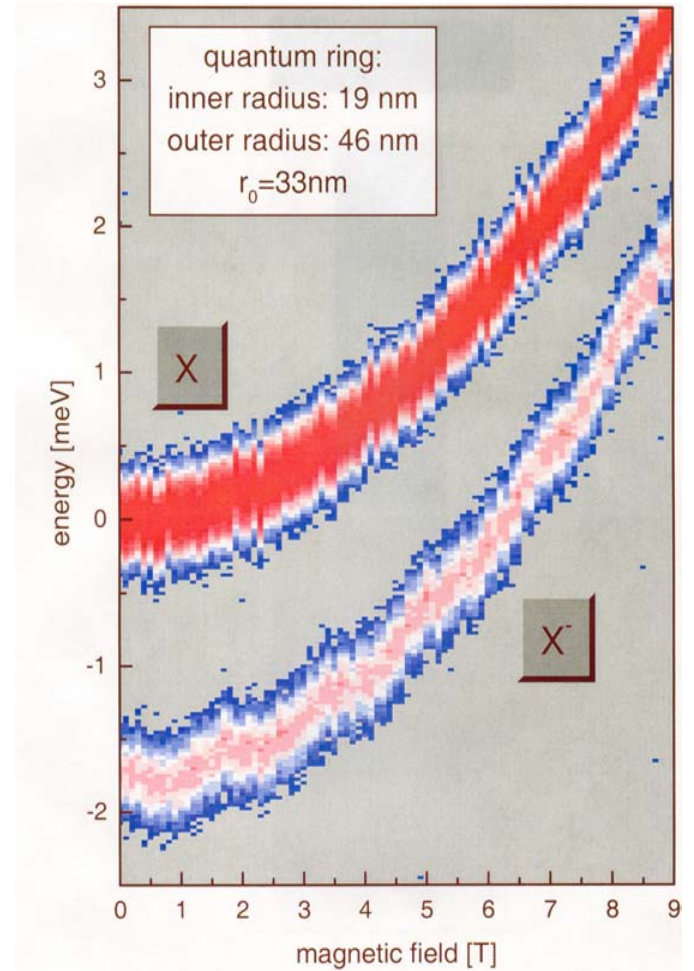
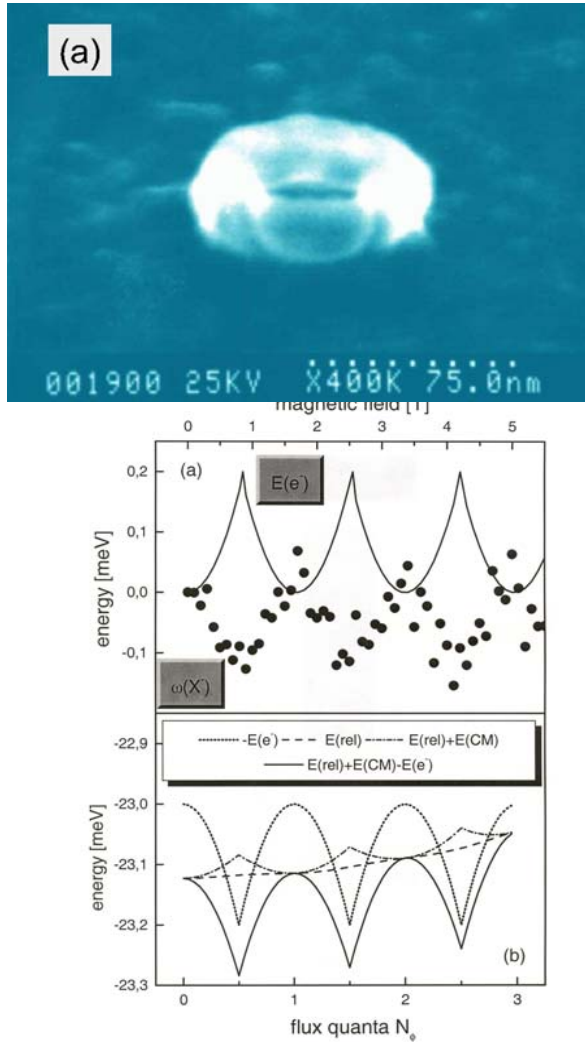
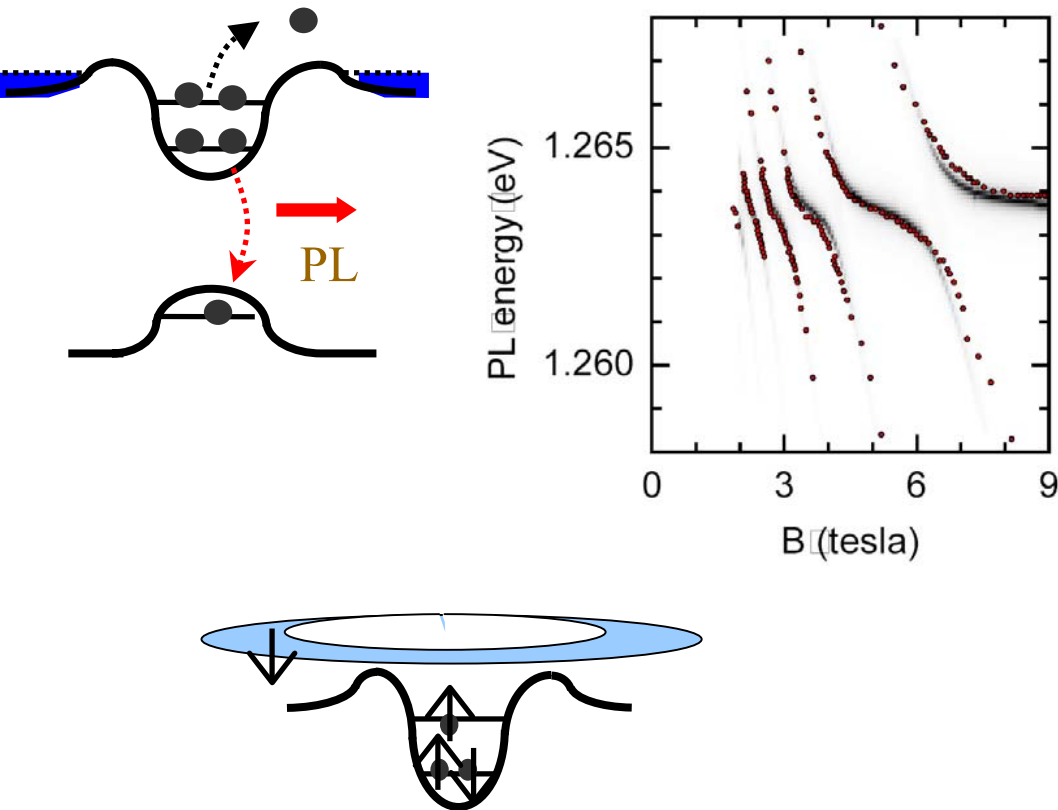


Fig. 2 M. Bayer et al

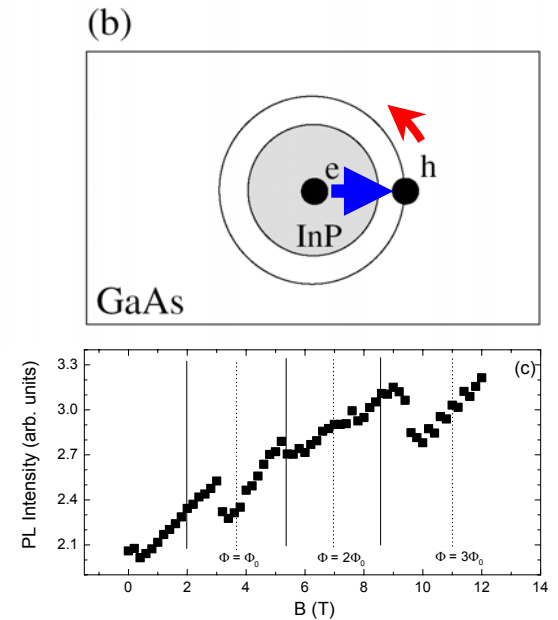
M. Bayer, M. Korkusinski, P. Hawrylak, T. Gutbrod, M. Michel, and A. Forchel ,
Phys. Rev. Lett. - 2003

Conclusions

Quantum dots as an open system
Hybridization with extended states



a neutral exciton
“traps” magnetic
flux quanta



Thanks to:

Sergio E. Ulloa

G. Medeiros-Ribeiro

E. Ribeiro

Alexander Kalameitsev