

# ARPES: How to make it quantitative?

*P. Aebi, Institut de Physique, Université de Neuchâtel, Switzerland*

**If it doesn't work for Cu, forget it!**

**Does it work for Cu? for HTc s? for CDW s?**

(not so much new results / science, but “naive” questions)

(what are the different problems)

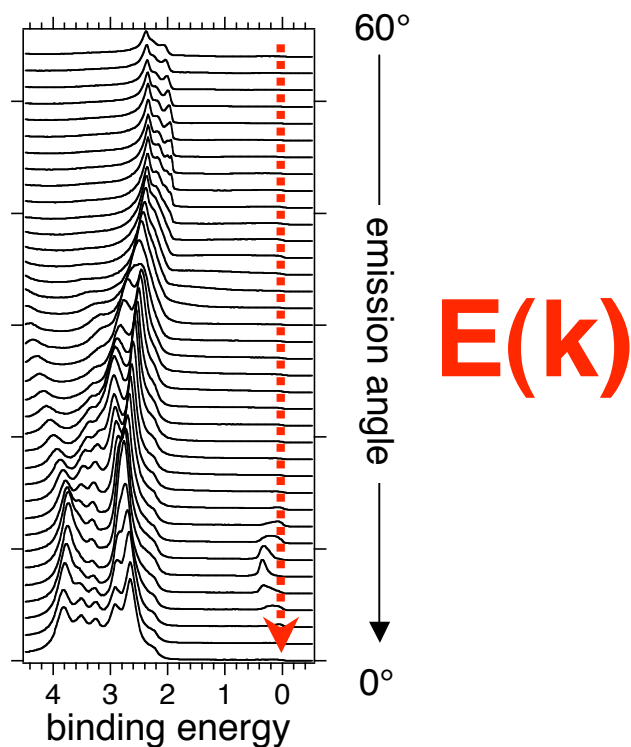
Modular approach:  
separately understand

- physics of initial state ('everybody is interested')
- physics of final state ('nobody is interested')
- physics of coupling (matrix elements) ('nobody is interested')

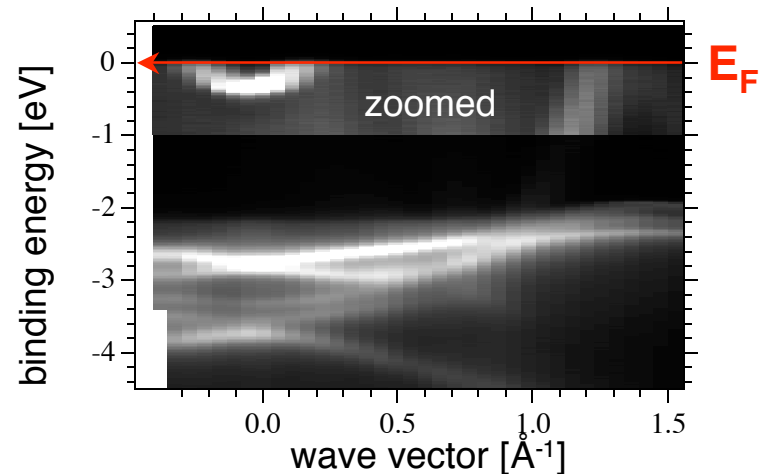
*F. Clerc, M. Bovet, C. Battaglia, L. Despont, H. Cercellier, M.G. Garnier*

# What we would like to do...

Measure spectra



Bandmapping



Interpret line shape as

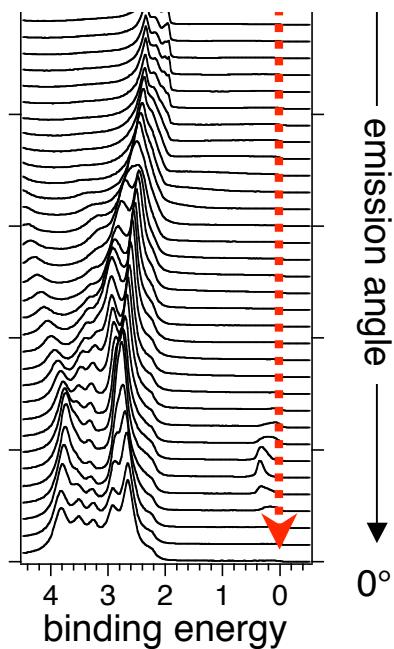
$$A(\vec{k}, \omega) = \frac{1}{\pi} \frac{\Im m \Sigma(\vec{k}, \omega)}{|\omega - \epsilon_{\vec{k}} - \Re e \Sigma(\vec{k}, \omega)|^2 + |\Im m \Sigma(\vec{k}, \omega)|^2}$$

$\Sigma(\vec{k}, \omega)$  **Self Energy**

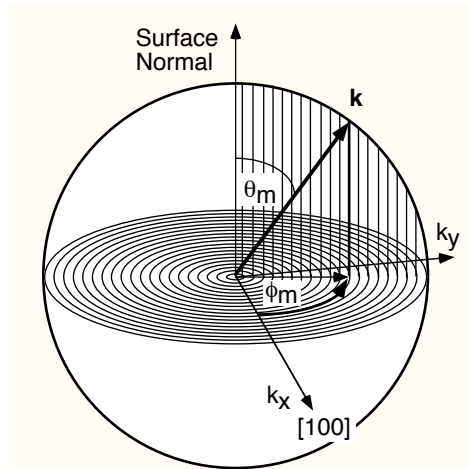
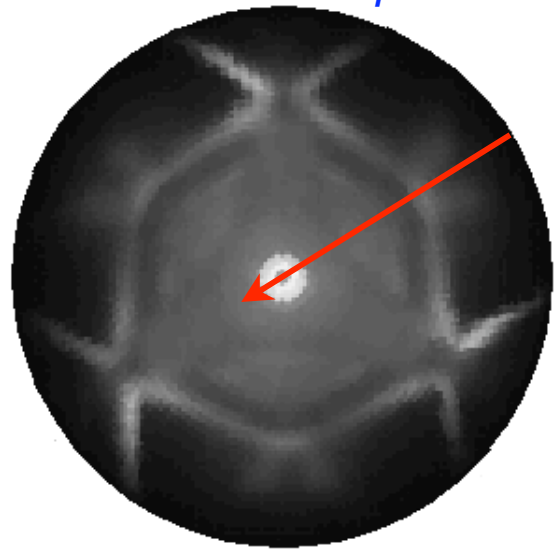
Band dispersion

Peak width: inverse life time

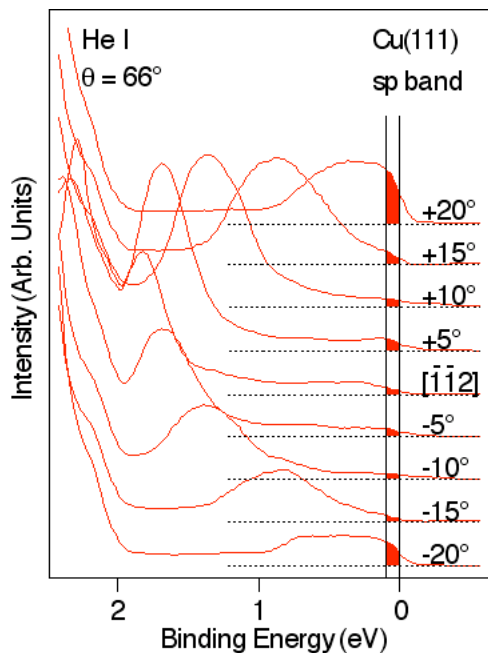
# What we would like to do...



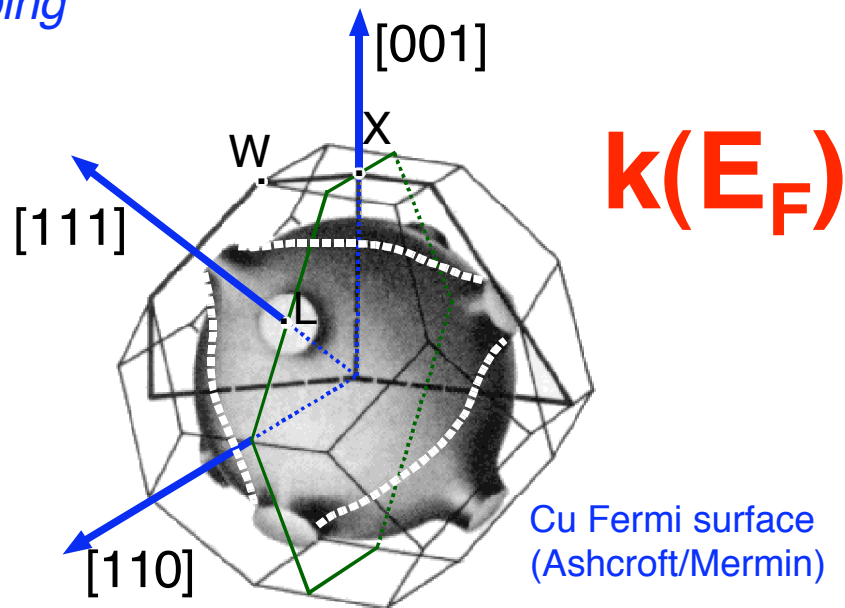
Measure maps...



$E_F$  mapping



and interpret as ...  
... Fermi surface



We know: It is not as simple as that !

Presently, what can we do?

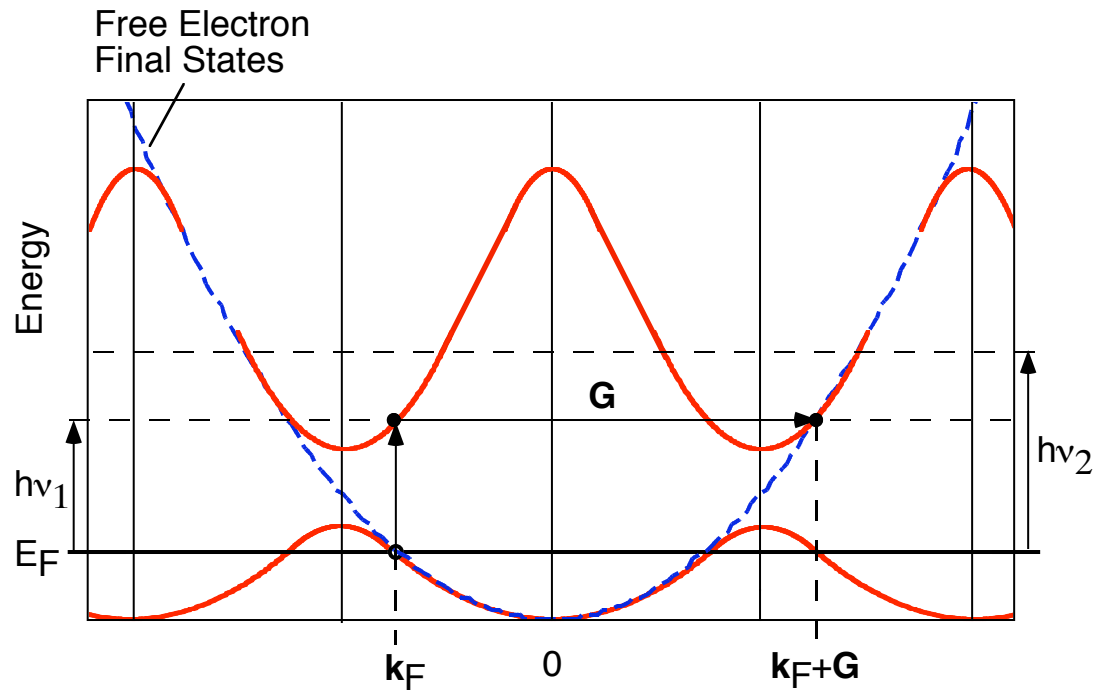
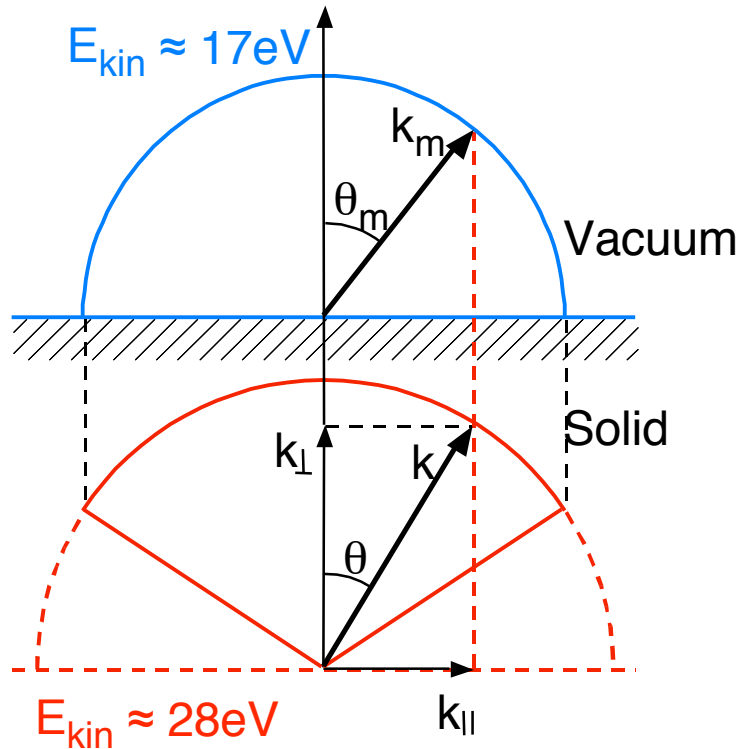
(as experimentalists)

Does it work for Cu?

... almost ...

What can we do? ... consider ...

## Direct transitions / Free electron final state



$$E_{kin}^m = h\nu - \Phi - E_B$$

$$|\vec{k}_{||}| = \frac{1}{\hbar} \sqrt{2mE_{kin}^m} \sin\theta_m$$

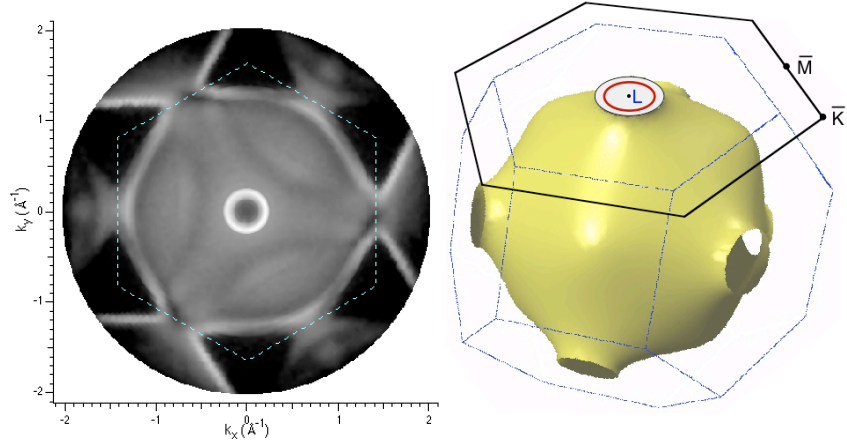
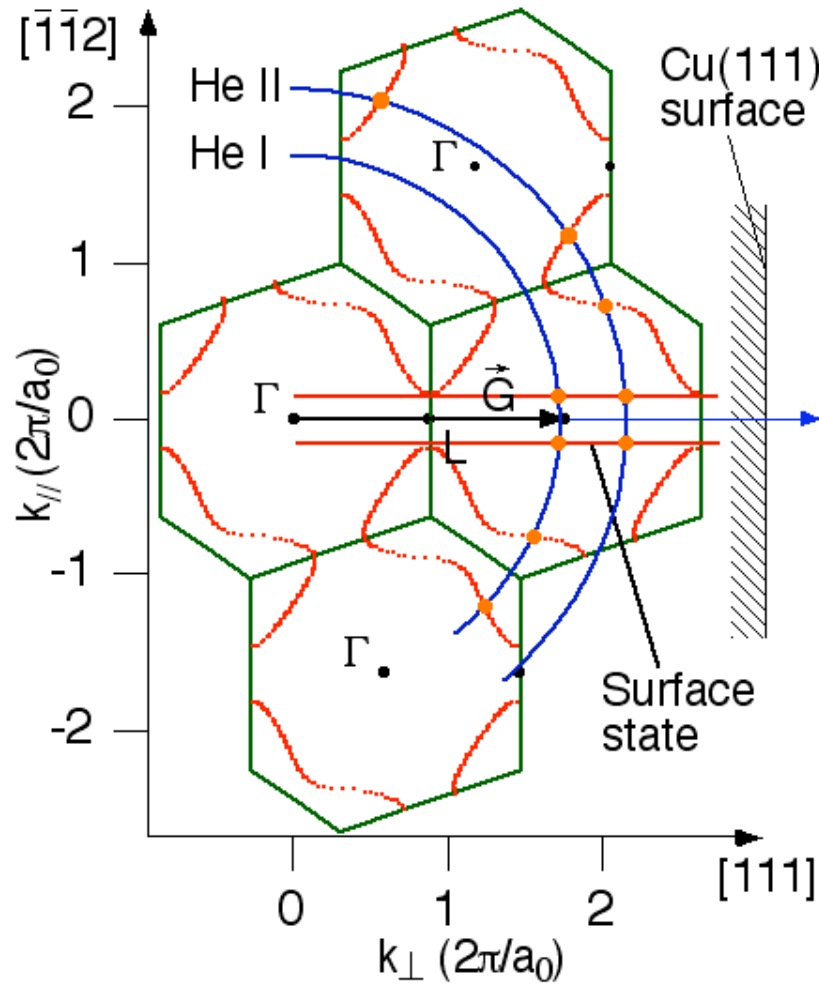
$$|\vec{k}_{\perp}| = \frac{1}{\hbar} \sqrt{2m(E_{kin}^m + V_0)} \cos\theta_m$$

$$\sin\theta = \sin\theta_m \sqrt{\frac{E_{kin}^m}{(E_{kin}^m + V_0)}} \quad \text{Refraction}$$

**Given:  $h\nu$ ,  $\Phi$ ,  $E_B$ ,  $\theta_m$ ; adjust  $V_0$  -->  $k$  is completely determined**

# Fermi surface mapping

Section along  $(\bar{1}10)$  plane in reciprocal space



In the photoemission process:

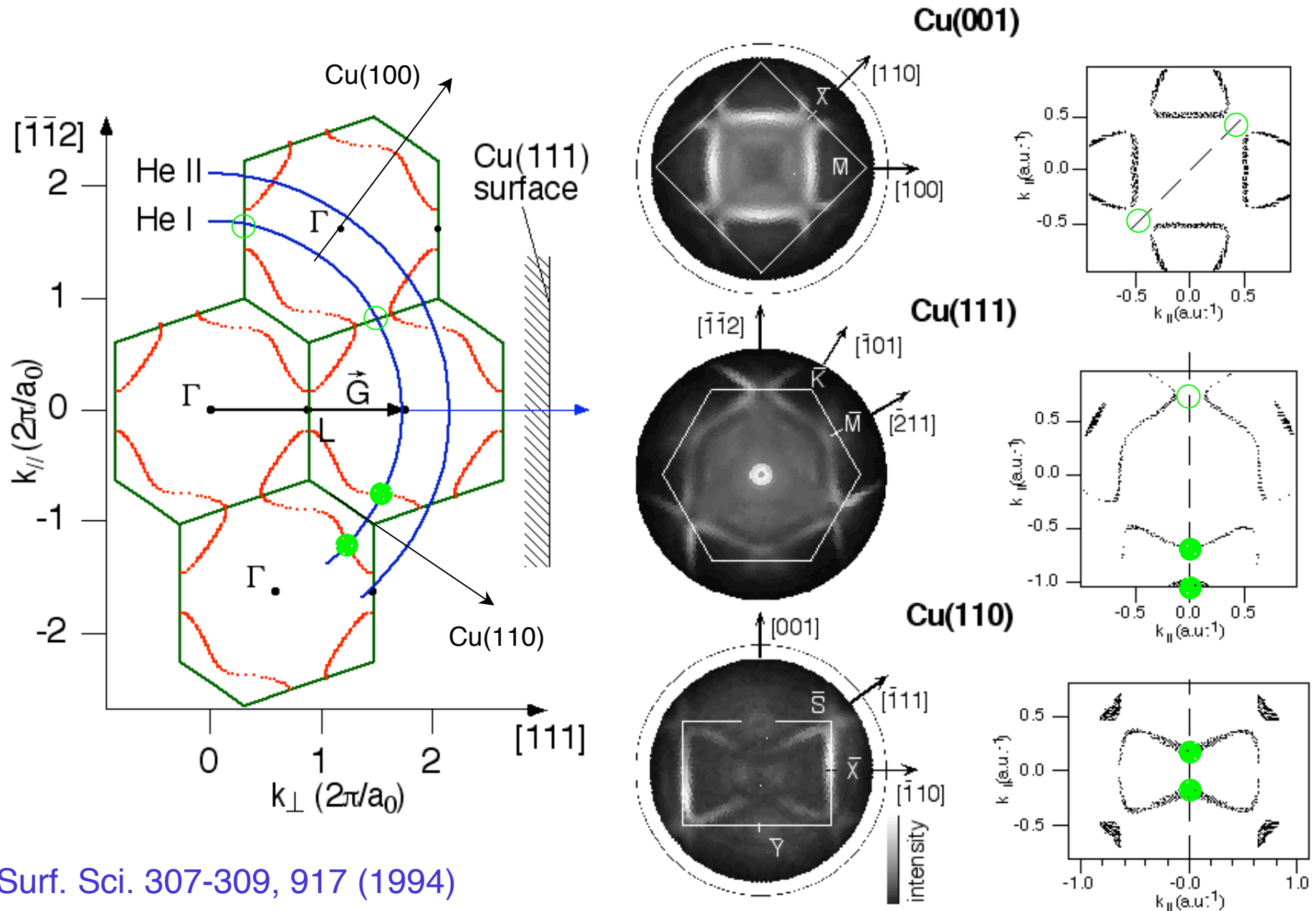
Energy conservation:

$$E_f = E_i + h\nu$$

Momentum conservation:

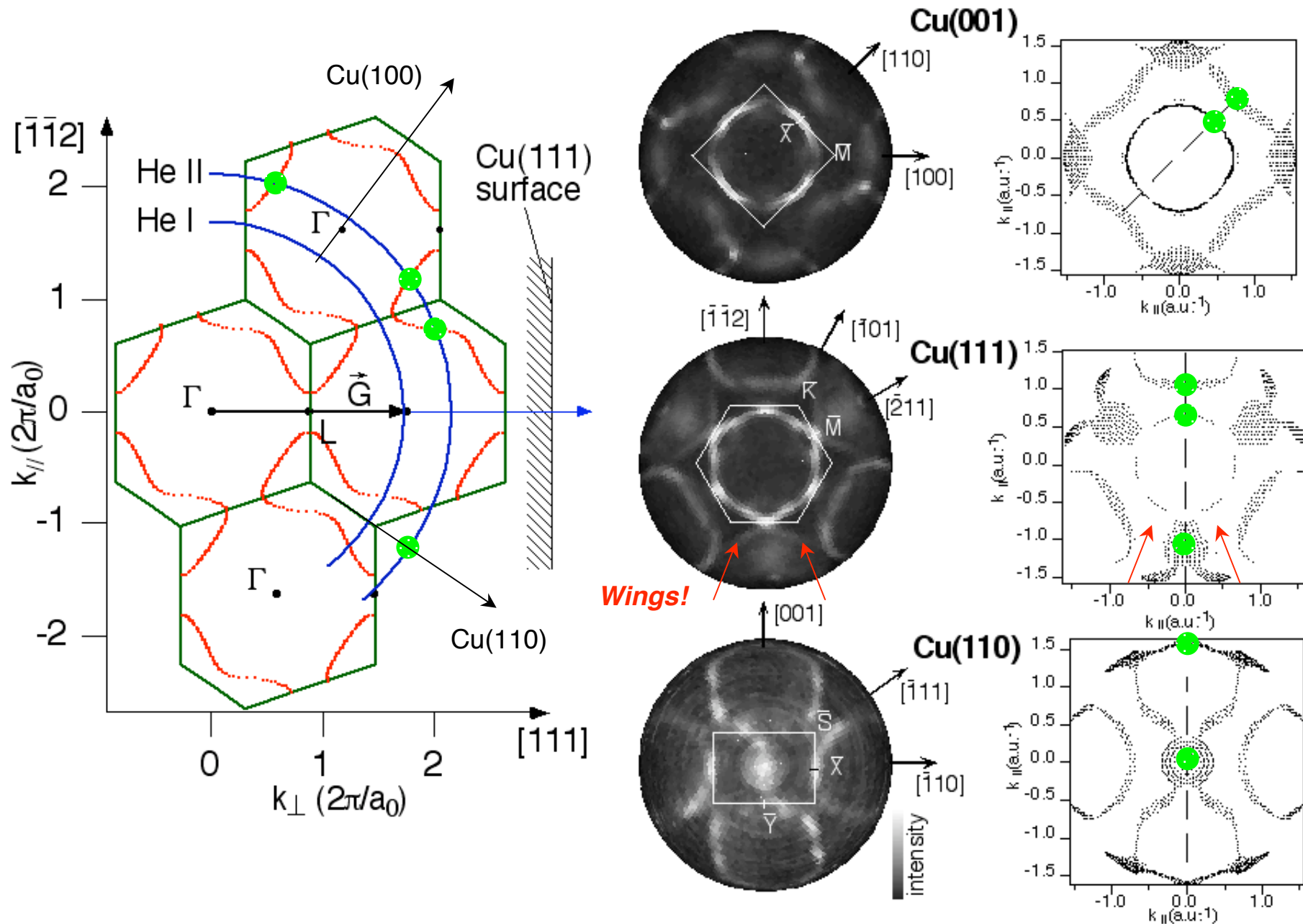
$$\vec{k}_f = \vec{k}_i + \vec{G}$$

# Fermi surface mapping: Cu surfaces He I



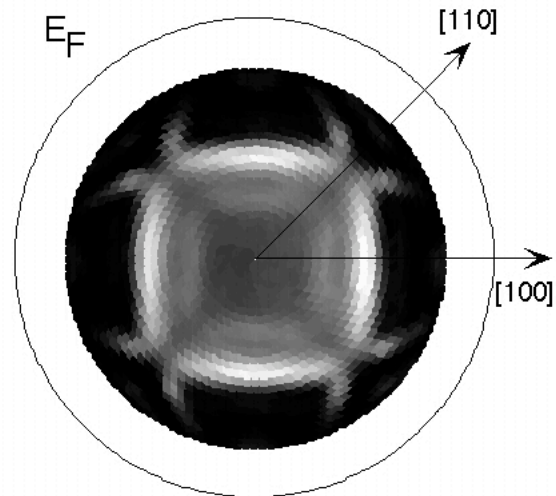
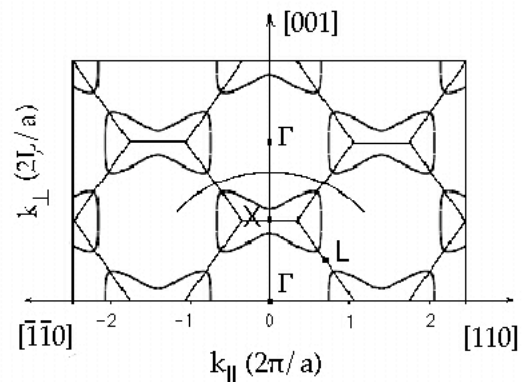
Surf. Sci. 307-309, 917 (1994)

# Fermi surface mapping: Cu surfaces He II

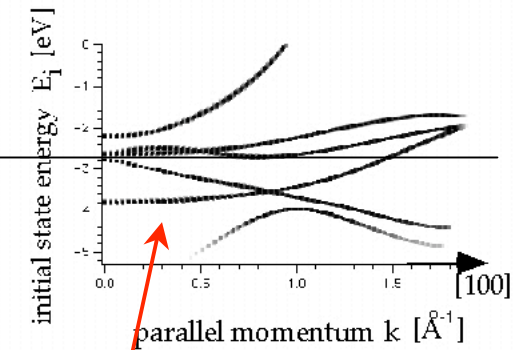
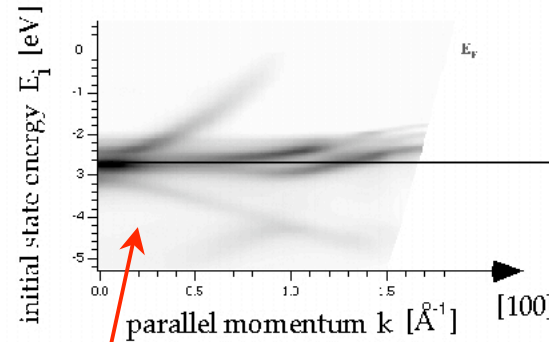
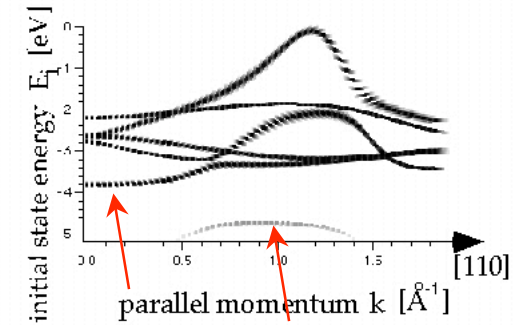
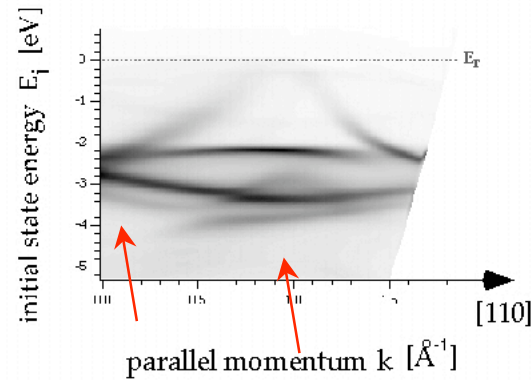




# Band mapping: Cu(001) He I



Cu(001)



Experiment

Theory

Missing band! - matrix elements ?

# One-step model may account for this ...

VOLUME 77, NUMBER 14

PHYSICAL REVIEW LETTERS

30 SEPTEMBER 1996

## A Novel Direct Method of Fermi Surface Determination Using Constant Initial Energy Angle-Scanned Photoemission Spectroscopy

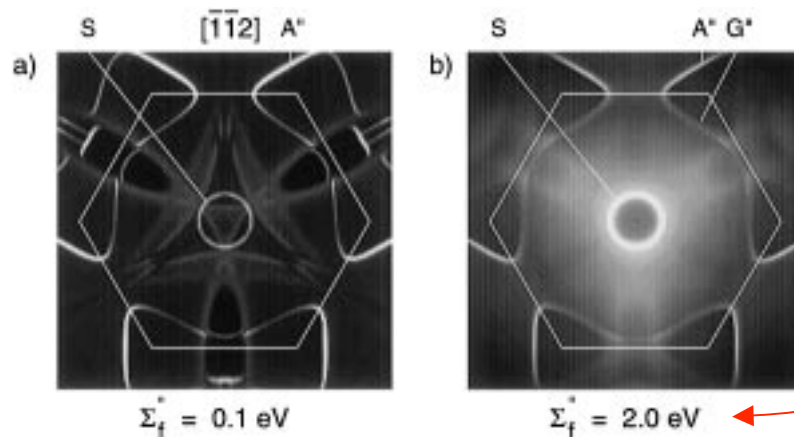
M. Lindroos<sup>1,2</sup> and A. Bansil<sup>1</sup>

<sup>1</sup>Physics Department, Northeastern University, Boston, Massachusetts 02115

<sup>2</sup>Tampere University of Technology, P.O. Box 692, SF-33101, Tampere, Finland

(Received 26 April 1996)

We show that a constant initial energy, angle-scanned (CIE-AS) photoemission spectrum for emission from the Fermi energy ( $E_F$ ) contains Fermi surface (FS) signatures which originate from density of states type *indirect* transitions. Such previously unrecognized FS features in a CIE-AS spectrum would provide a robust and straightforward means of determining Fermi surfaces. Furthermore, the associated photointensity should yield a new window on  $k_{\perp}$  dispersion related issues in materials. Extensive simulations of CIE-AS spectra from low index faces of Cu are presented within the framework of the one-step photoemission model in order to delineate the nature of these new spectral features. [S0031-9007(96)01334-8]



$h\nu = 21.2 \text{ eV}$ , unpolarized,  
would be nice to have it  
for  $h\nu = 64 \text{ eV}$

Final state broadening

**For Cu the situation is not too bad ...**

**BUT:**

**Free electron final state **does NOT explain:****

- DOS features, - indirect transitions,**
- Missing band**

**We need to consider:**

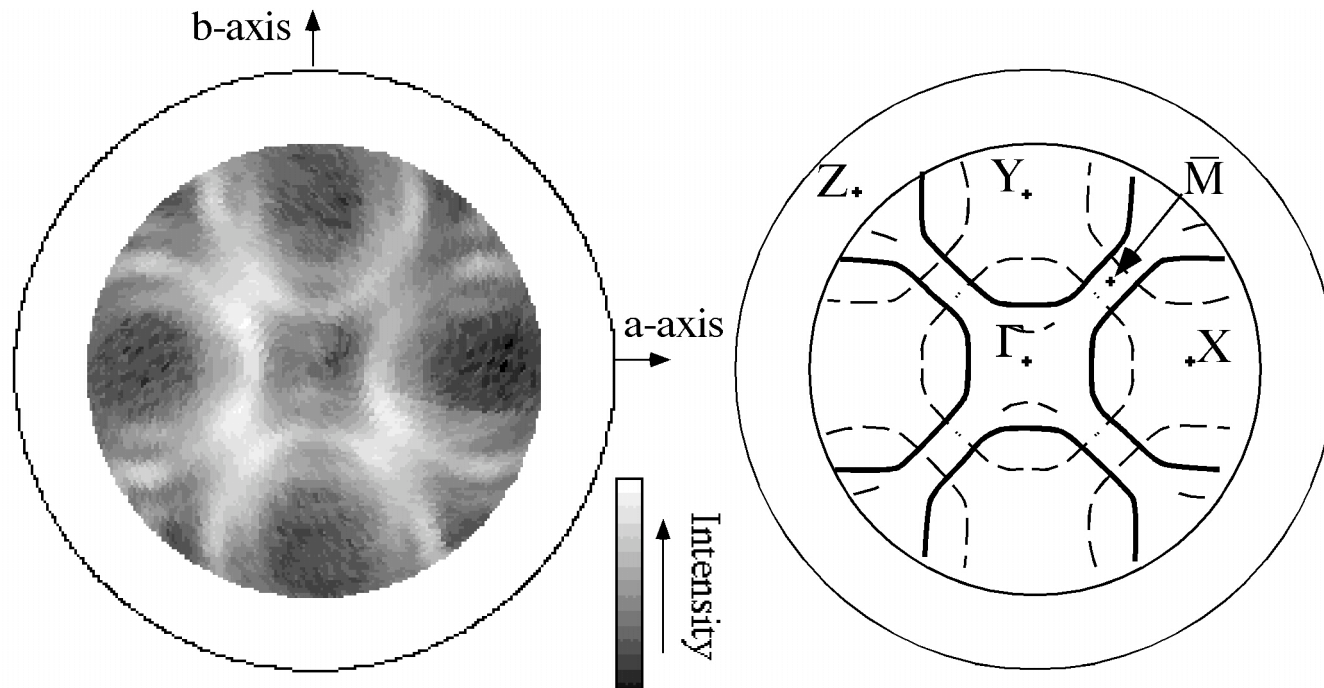
- final state scattering**
- lifetime broadening**
- matrix elements**

Is it because Cu is 3D?

What about 2D?

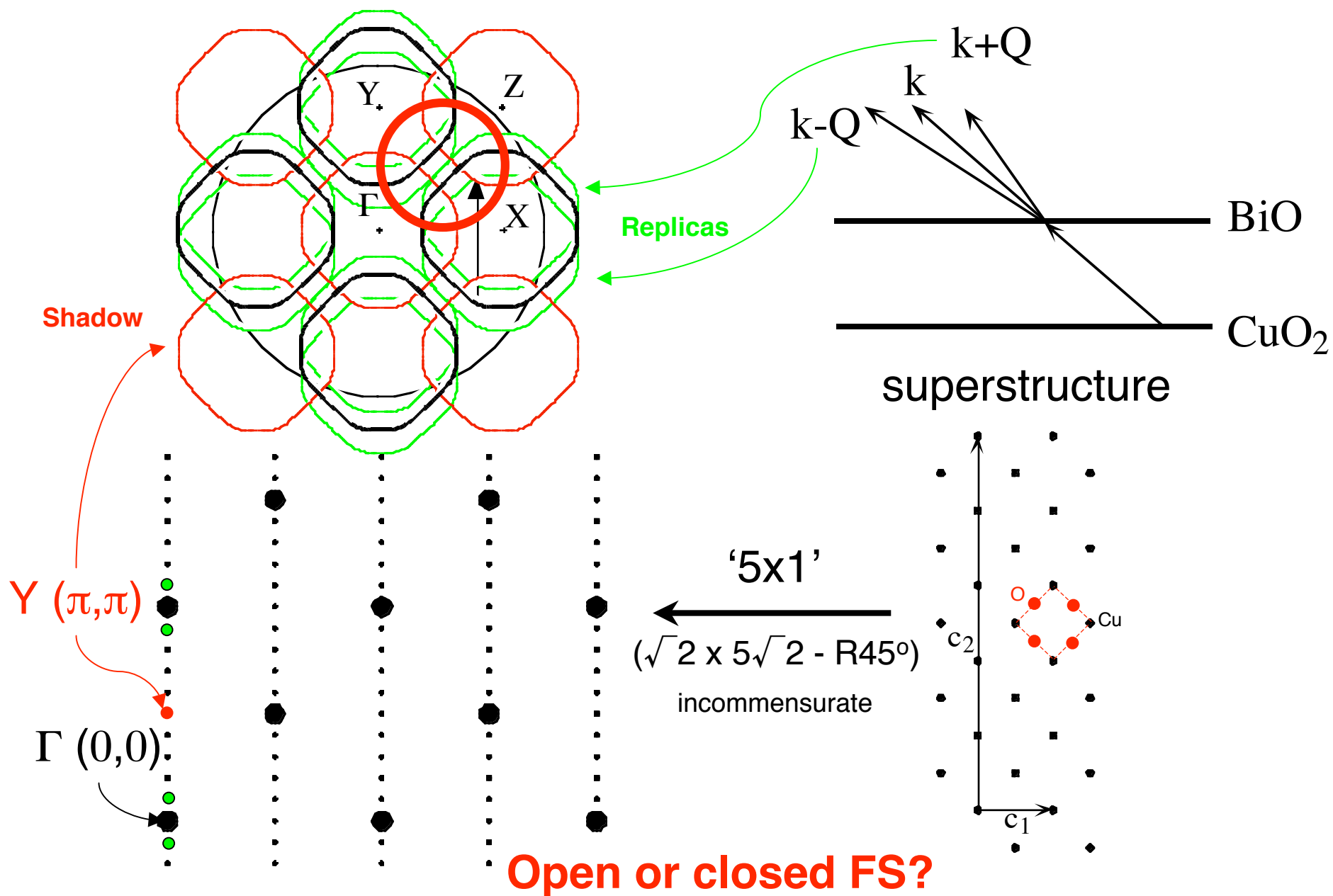
Quasi 2D system, a well-known example ...

## Bi2212: The joys of Fermi surface mapping ...



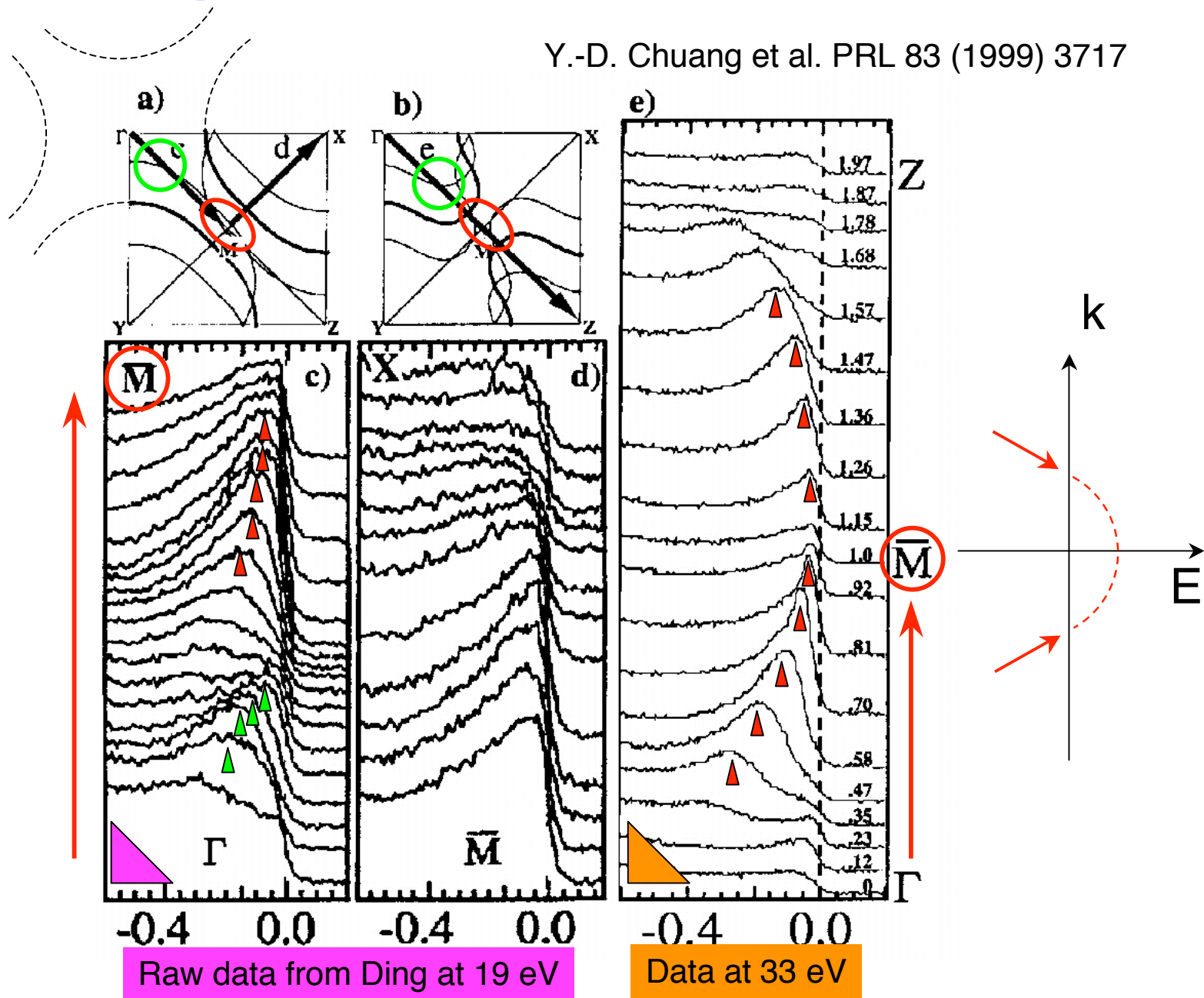
... may turn into pitfalls ....

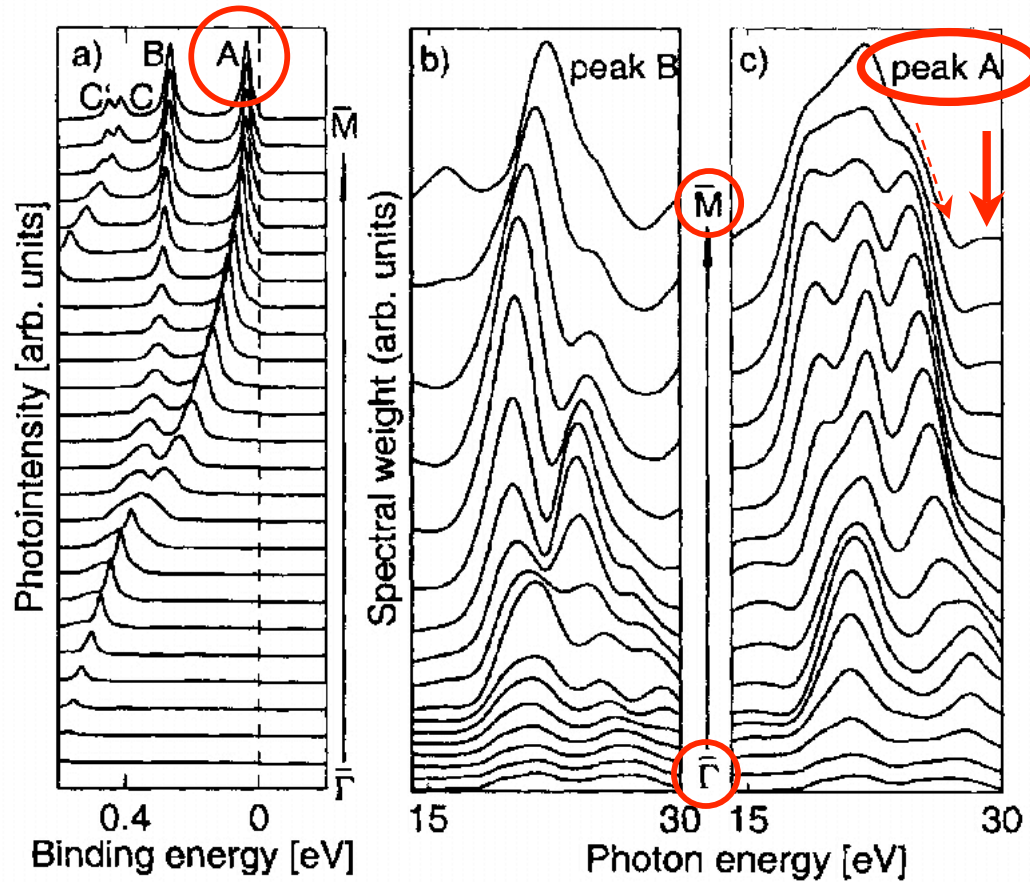
# ... complicated situation due to FS contour manifolds



# Open or closed Fermi surface?

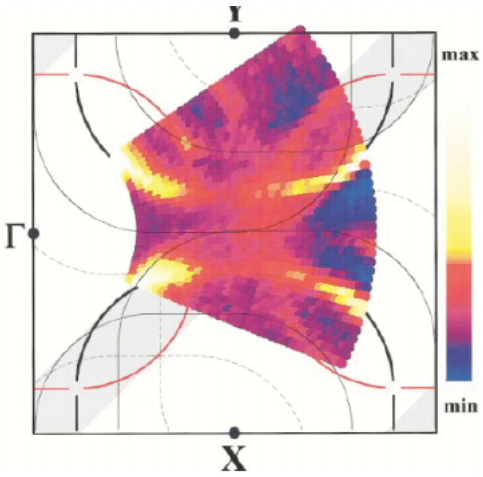
Y.-D. Chuang et al. PRL 83 (1999) 3717





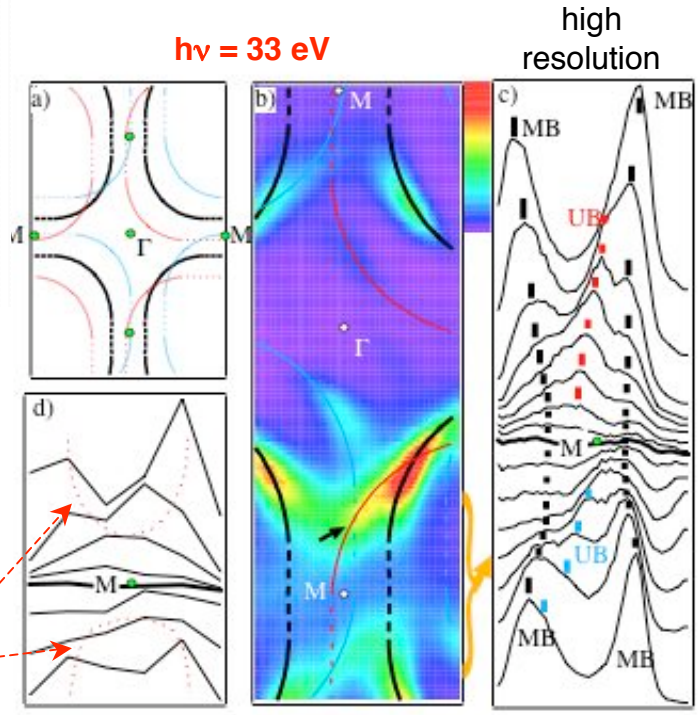
Bansil, Lindroos, PRL 83 (1999) 5154

**Matrix elements  
play  
a crucial role**



**High resolution  
experiments**

simulated  
low  
resolution  
  
apparent  
small  
Fermi surface



Borisenko et al., PRL 84 (2000) 4453

Fretwell et al., PRL 84 (2000) 4449

**Bi2212: the situation is complicated despite its 2D character**

**We need to consider**

- final state scattering ('5x1')-reconstruction
- matrix elements ( $h\nu$  - dependence)

**We should have a modular approach:**

**Module for computing:  
Inverse LEED state  
+ coupling to initial state  
from arbitrary model**

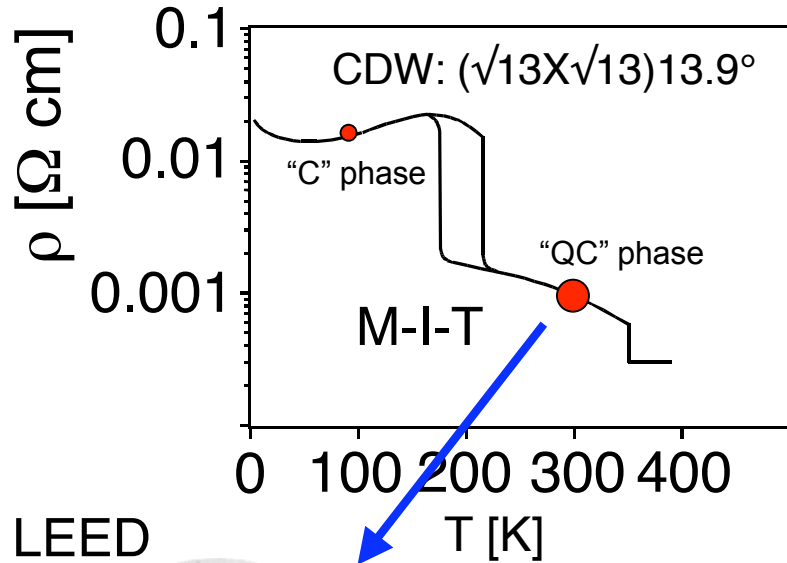
**Many different models deal with initial state physics  
(calculate: wavefunctions, greensfunction,  $A(k,\omega)$ )**

**Final state scattering (LEED, 'conventional')  
(calculate inverse LEED state for known structure)**

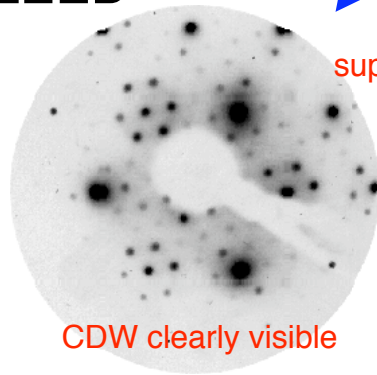


# CDW system 1T-TaS<sub>2</sub>

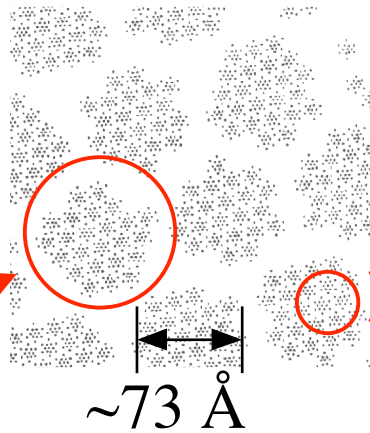
F. J. Di Salvo *et al.*, Solid State Commun. **23**, 825 (1977)



LEED

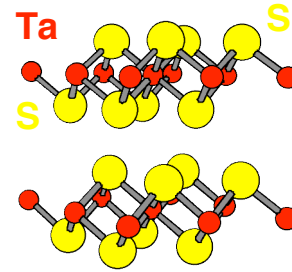


Domains of commensurate CDW



CDW:  $(\sqrt{13} \times \sqrt{13}) 13.9^\circ$

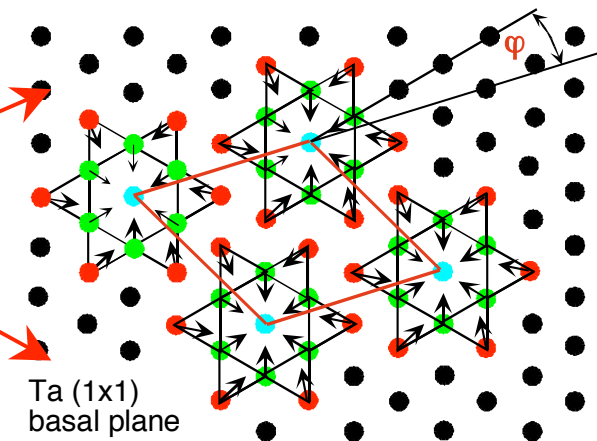
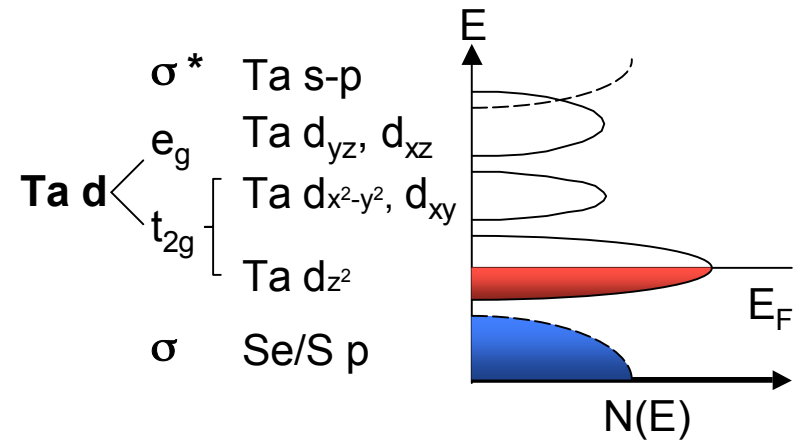
A. Spijkerman *et al.* Phys. Rev. B **56**, 13757 (1997)



<sup>73</sup>Ta [Xe]4f<sup>14</sup>5d<sup>3</sup>6s<sup>2</sup>

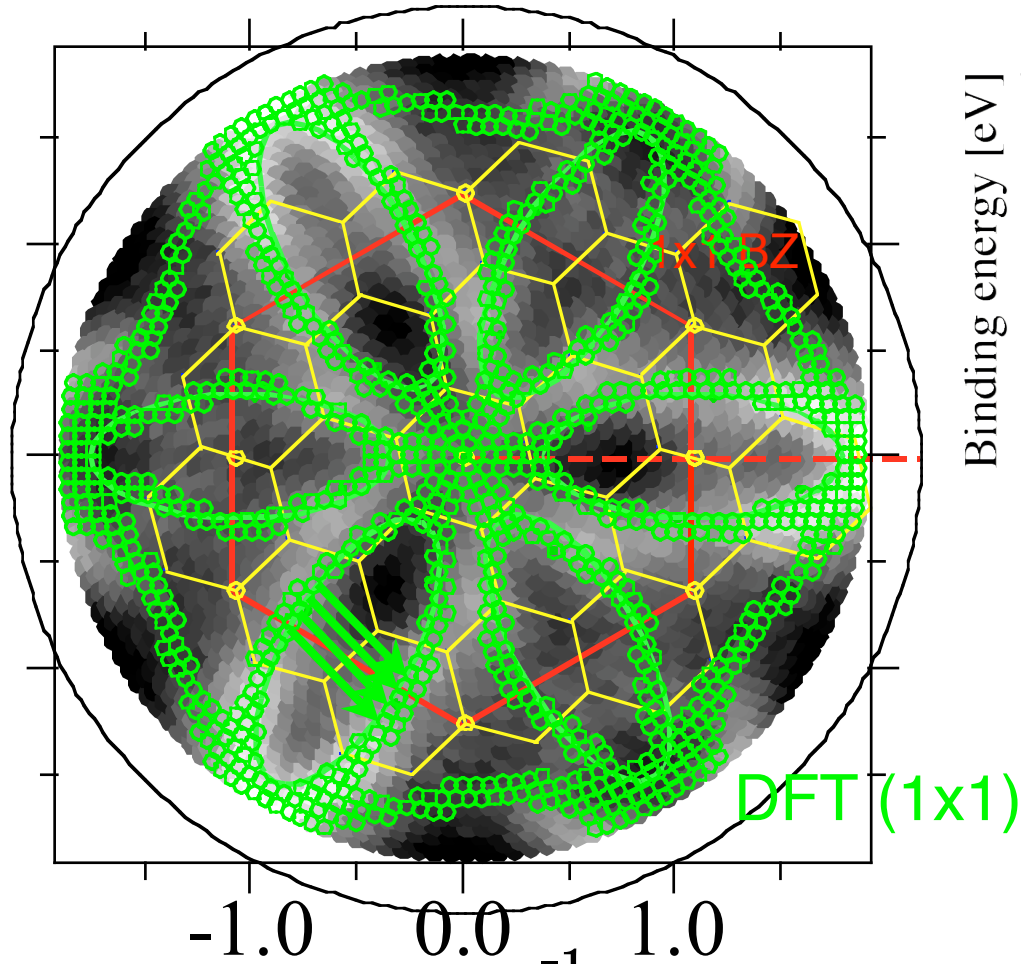
<sup>16</sup>S [Ne] 3s<sup>2</sup>3p<sup>4</sup>

IONIC PICTURE



... what do we see in the experiment ...

## Experiment: FS mapping

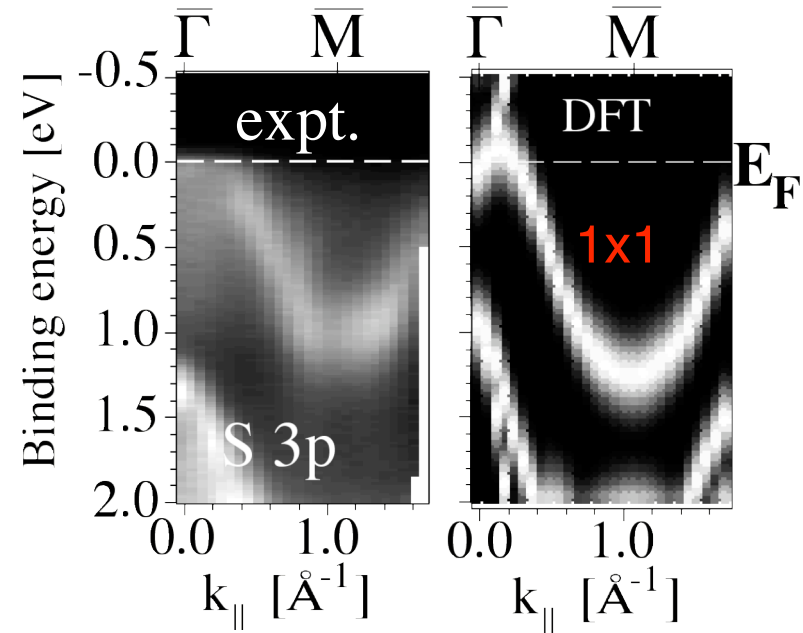


Can we interpret this as  $A(k, \omega)$  ?  
What is ordinary / exotic?

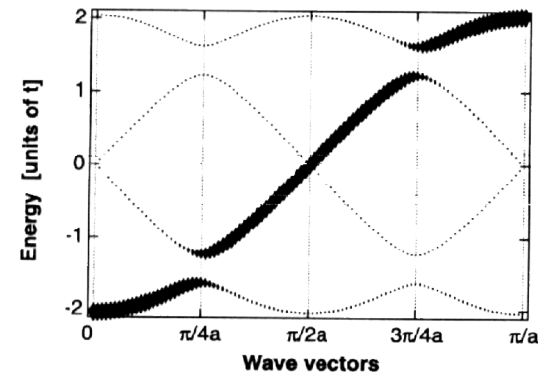
No clear gap opening?

Phys. Rev. B 69, 125117/1-125117/9 (2004)

## Band mapping

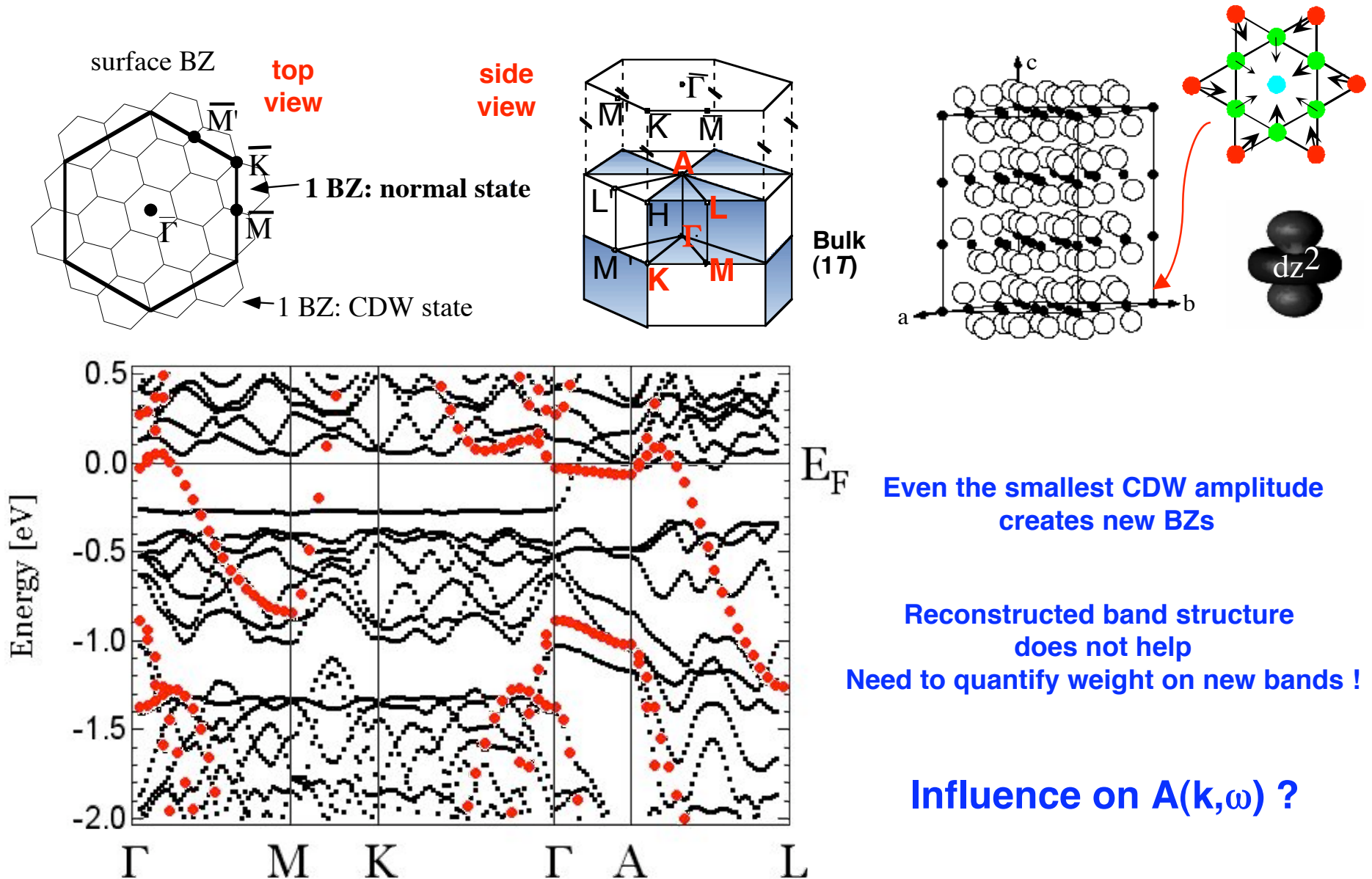


No clear effect of CDW?



*J.Voit et al. Science 290,501 (2001)*

# realistic\* DFT calculation accounting for CDW



\* calculation for expt. XRD structure

Phys. Rev. B 67, 125105 (2003)

# CDWs: the situation is complicated despite its 2D character

## ?How to know?

- what is due to large unit cell (CDW) in initial state
- what is due to large unit cell (CDW) in final state
  - what is due to  $A(k,\omega)$  / quasi particles
- whether low intensity is due to absence of QP or ME

## We should have a modular approach:

Many different models go into initial state physics  
(calculate: wavefunctions, greensfunction,  $A(k,\omega)$ )

### -Module for computing: $A(k,\omega)$ for large unit cell

Influence of potential with variable modulation strength

- Module for: Inverse LEED state for large unit cell
  - + coupling (ME) to initial state

# Experimental information on final states ...

## VLEED experiments !

### Absolute Band Mapping by Combined Angle-Dependent Very-Low-Energy Electron Diffraction and Photoemission: Application to Cu

V. N. Strocov,<sup>1,2,\*</sup> R. Claessen,<sup>1</sup> G. Nicolay,<sup>1</sup> S. Hüfner,<sup>1</sup> A. Kimura,<sup>3</sup> A. Harasawa,<sup>3</sup> S. Shin,<sup>3</sup> A. Kakizaki,<sup>4</sup>  
P. O. Nilsson,<sup>2</sup> H. I. Starnberg,<sup>2</sup> and P. Blaha<sup>5</sup>

the method by application to Cu, and find significant deviation from free-electron-like behavior in the unoccupied states, and from density-functional theory in the occupied states. [S0031-9007(98)07792-8]

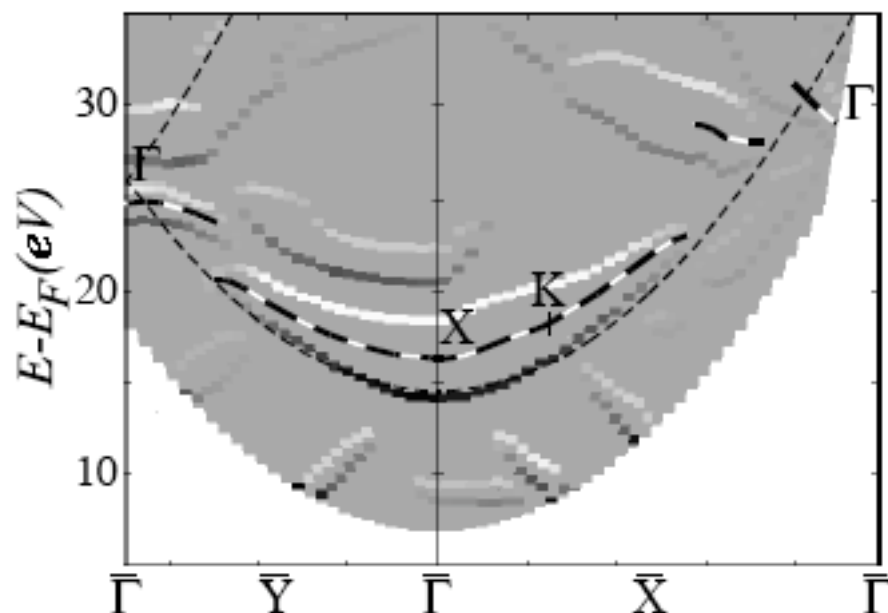
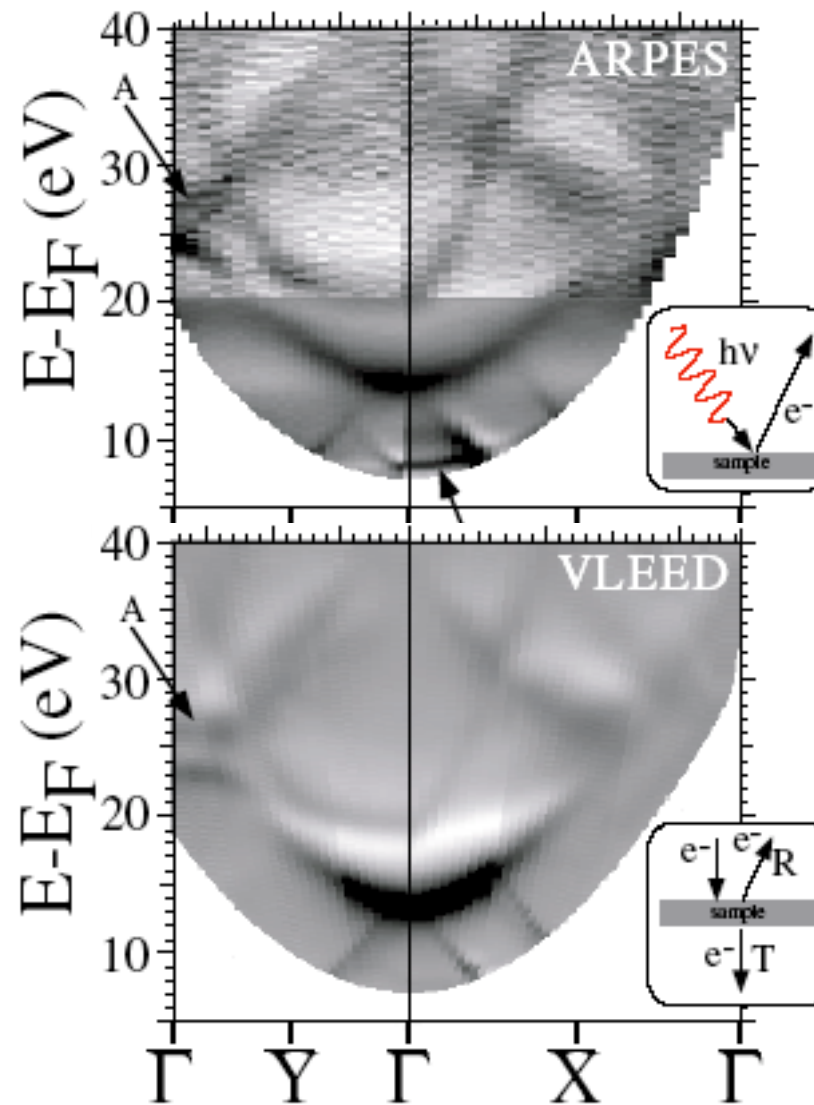
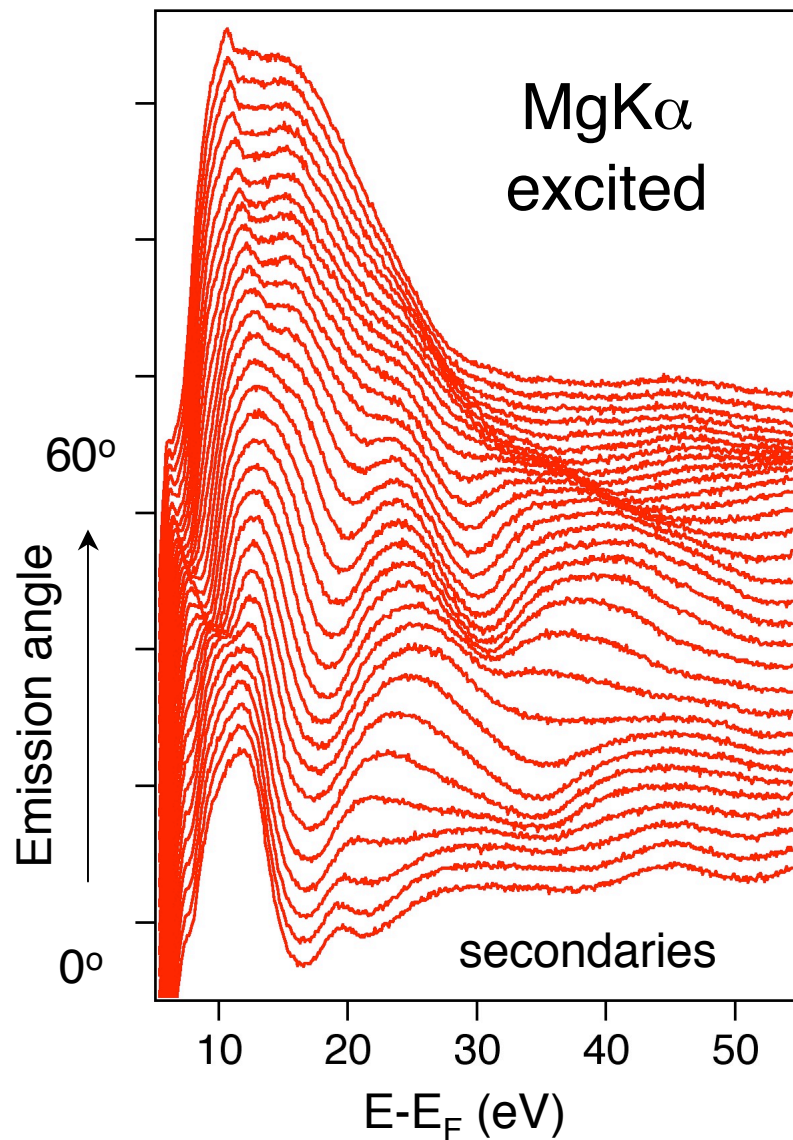


FIG. 3. Experimental upper bands derived from the VLEED  $dT/dE$  extrema. Their shading reflects a logarithmic gray scale proportional to  $-\frac{d^2(dT/dE)}{dE^2}$ , on top of the zero-level gray scale; dark (light) points correspond to  $dT/dE$  minima (maxima). The bold dashed curves show the bands of the final-state energies chosen for the CFS PE experiment, with the high-symmetry points in the  $\Gamma K L U X$  plane indicated; the thin dashed curve is their free-electron approximation. The region below  $E_{\text{vac}} + \frac{\hbar^2 K_{\parallel}^2}{2m} + 2 \text{ eV}$  is clipped.

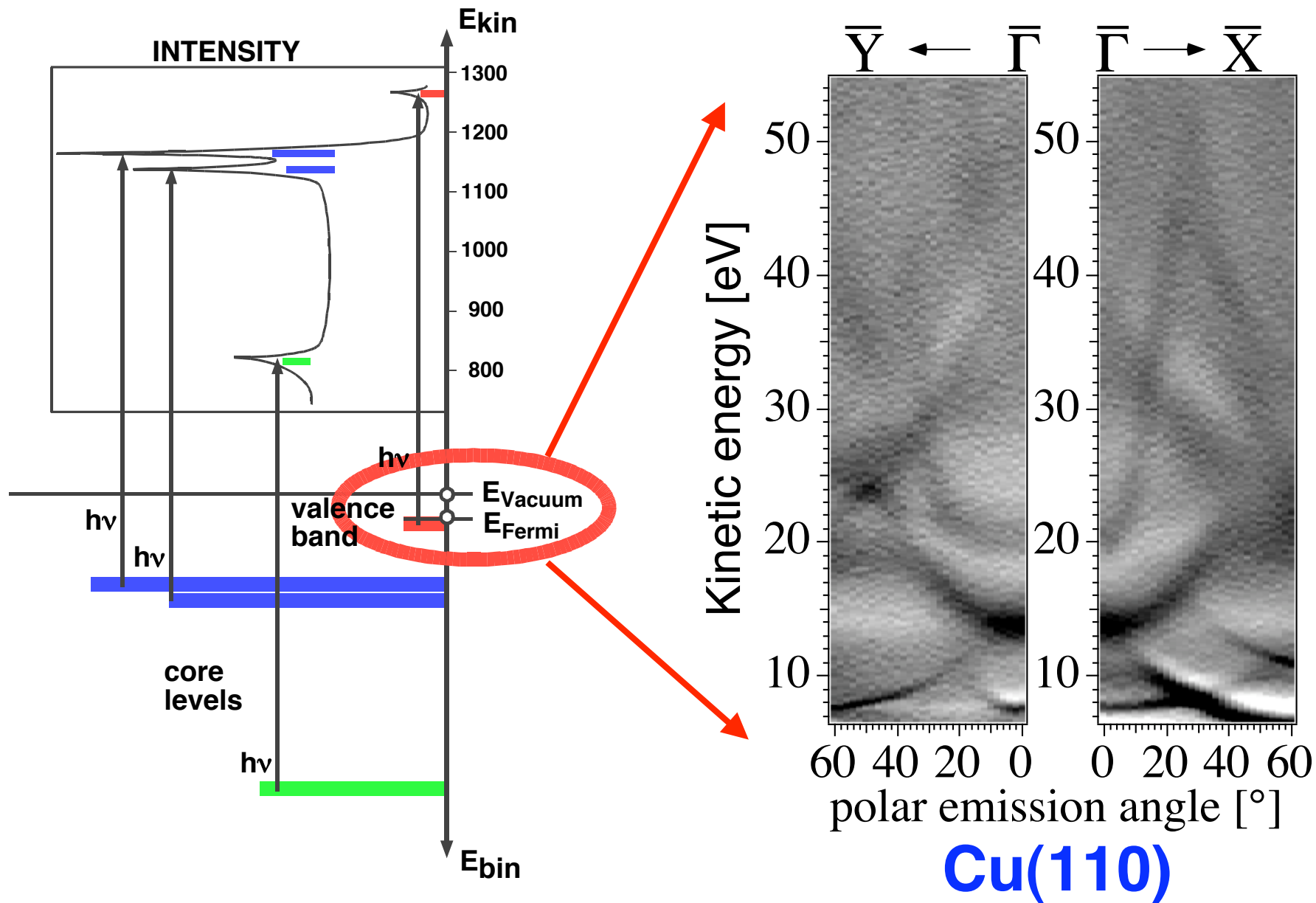
VLEED experiments on Cu(110)

# Experimental information on final states ...

It works with secondary ARPES !



# Photoemission ... also for un-occupied states



# Conclusion / “Wish list”

**Create standard (like in XRD)** democratisation

For final state calculation and Matrix elements,  
**independent** of initial state physics

For *arbitrary* initial state physics (LDA,  $\mu$ -model, etc. )  
have a **standard** for final state calculation and Matrix elements

## Example

### Given:

- known (super)structure, different elements A, B,...
- known LDA bandstructure (generally accessible)  
or have a  $\mu$ -model for physics

### Would like to know:

- what  $h\nu$ , polarization, BZ (geometry) ?  
To see best states A, B,... details of  $\mu$ -model

---

## Photoemission (for quantitative)

Fermi surface- / spectral function- / empty band  
mapping

