

Opportunities and Challenges from Electron Spectroscopy for Realistic Correlated Electron Theory

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Solid State Commun. 123, 469 (2002)

J. Phys. Soc. Jpn. 74, 34 (2005).

*** Work at UM

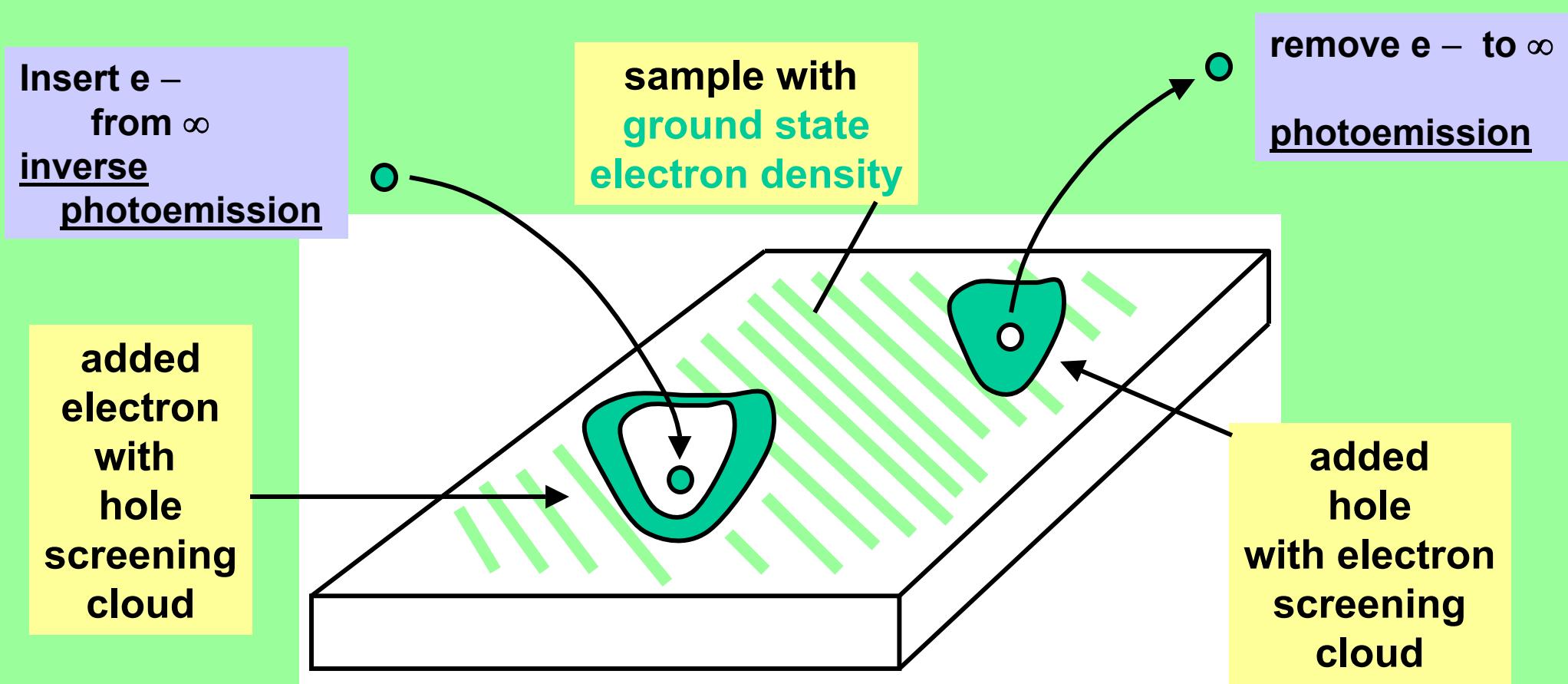
Supported by the U.S. NSF.

electron removal (and addition) to study single-particle behavior of many-body system

Spectroscopy of energy and momentum dependence of spectral weight

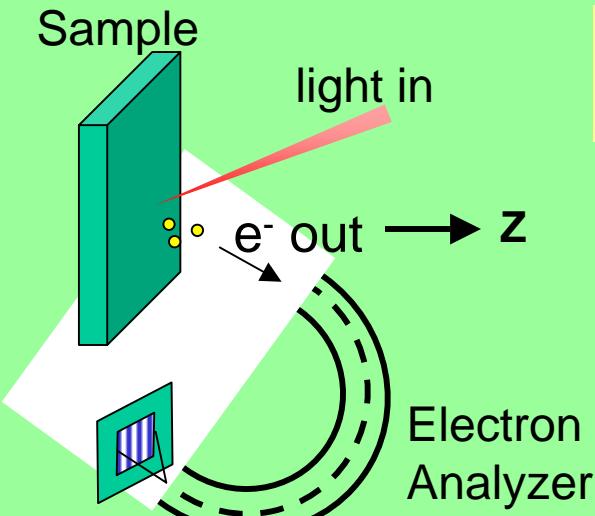
$$\rho(\mathbf{k}, \omega) = (1/\pi) \operatorname{Im} [1/(\omega - \varepsilon_{\mathbf{k}} - \Sigma(\mathbf{k}, \omega))]$$

of single particle Green's function



Both processes together give unbound hole/electron pair
the RIGHT WAY TO DEFINE INSULATOR GAP!

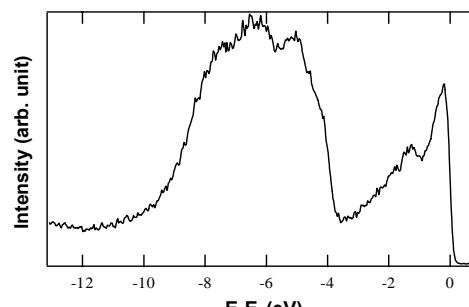
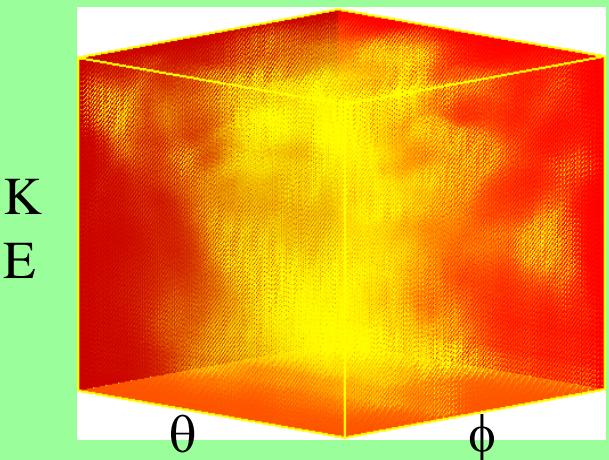
Photoemission spectroscopy (and its inverse) to measure $\rho(k, E)$ or k-summed $\rho(E)$



Angle variation moves on spherical k-space surfaces.

Vary photon energy to change k_z

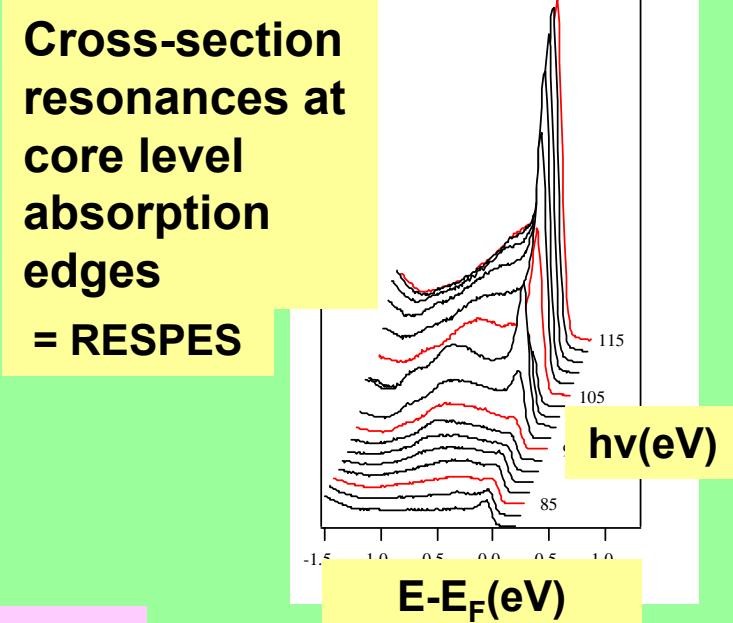
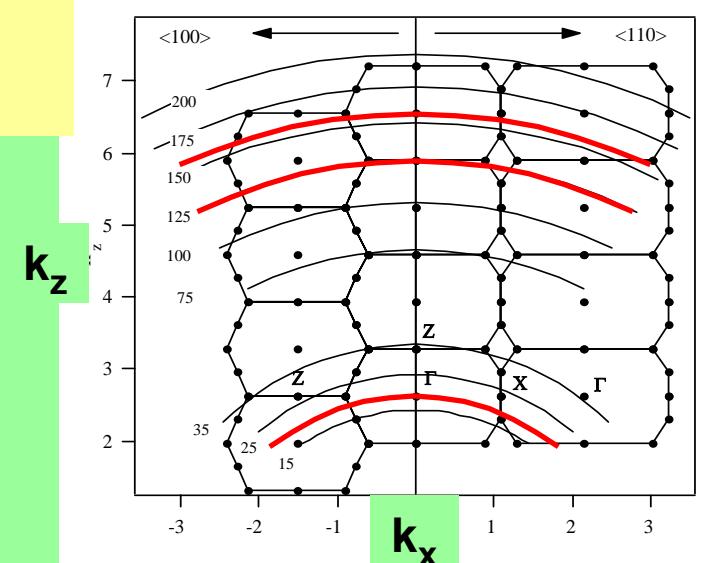
Full electronic structure
@ fixed photon energy
—3D data set—



Angle integrated
or k-summed

angles, energy $\Rightarrow k_x \ k_y$

High photon energy—
more bulk sensitive

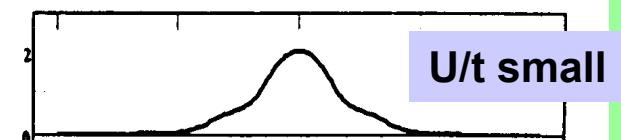


Mott-Hubbard metal-insulator transition

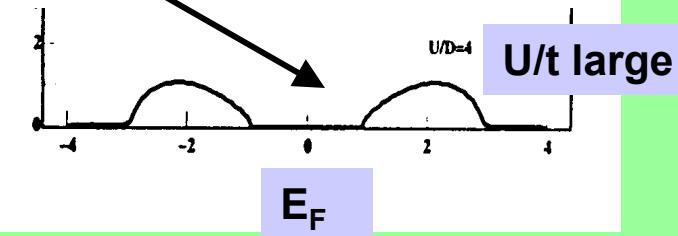
Kin En t



Hubbard model

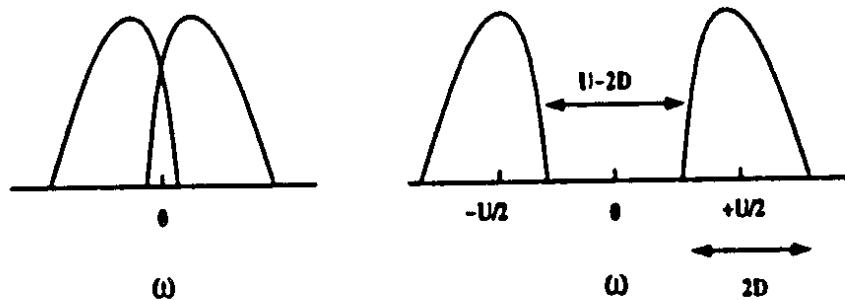


Gap in electron addition/removal spectrum due to U gives insulator!



Mott-Hubbard metal-insulator transition

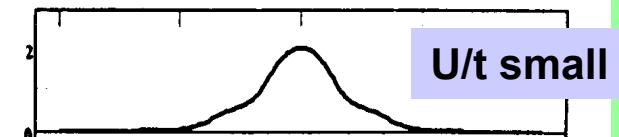
Old gap collapse picture



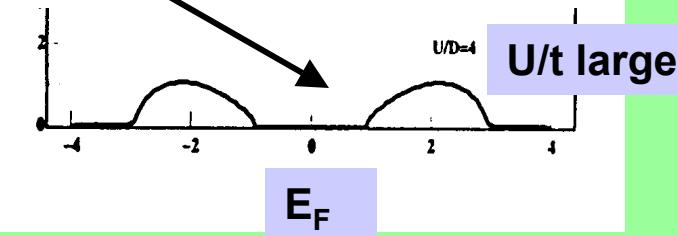
Kin En t



Hubbard model



Gap in electron addition/removal spectrum due to U
gives insulator!

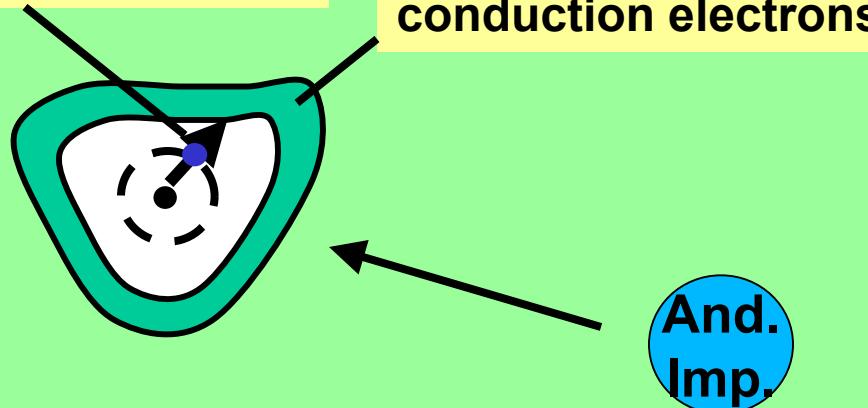


Mott-Hubbard metal-insulator transition

NEW VIEW from Dynamic Mean Field Theory

(Vollhardt, Metzner, Kotliar, Georges ≈ 1990)

local orbital
electron with
magnetic moment



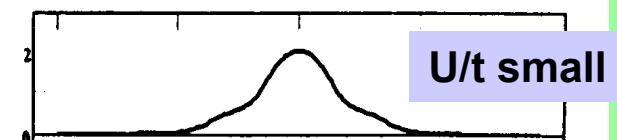
conduction electrons

And.
Imp.

Kin En t

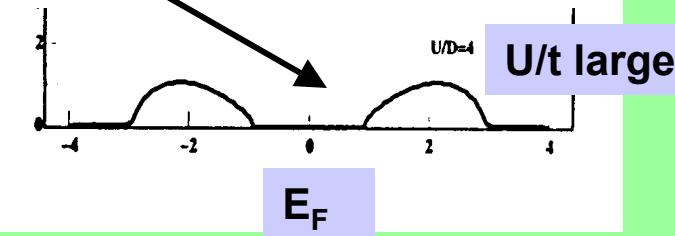


Hubbard model



U/t small

Gap in electron
addition/removal
spectrum due to U
gives insulator!



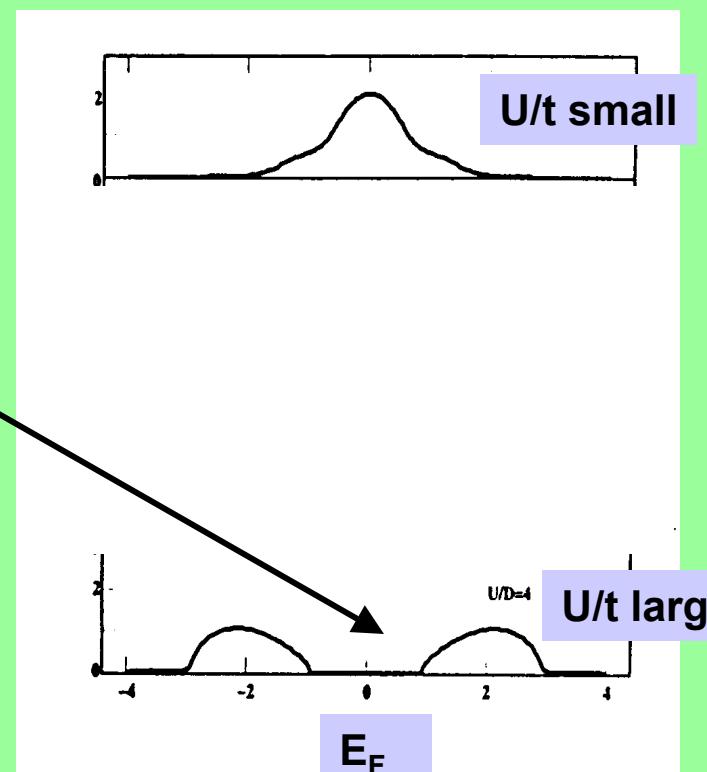
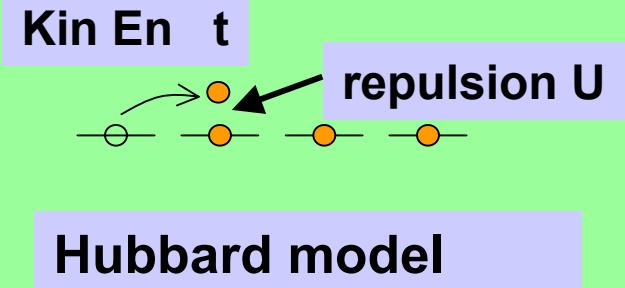
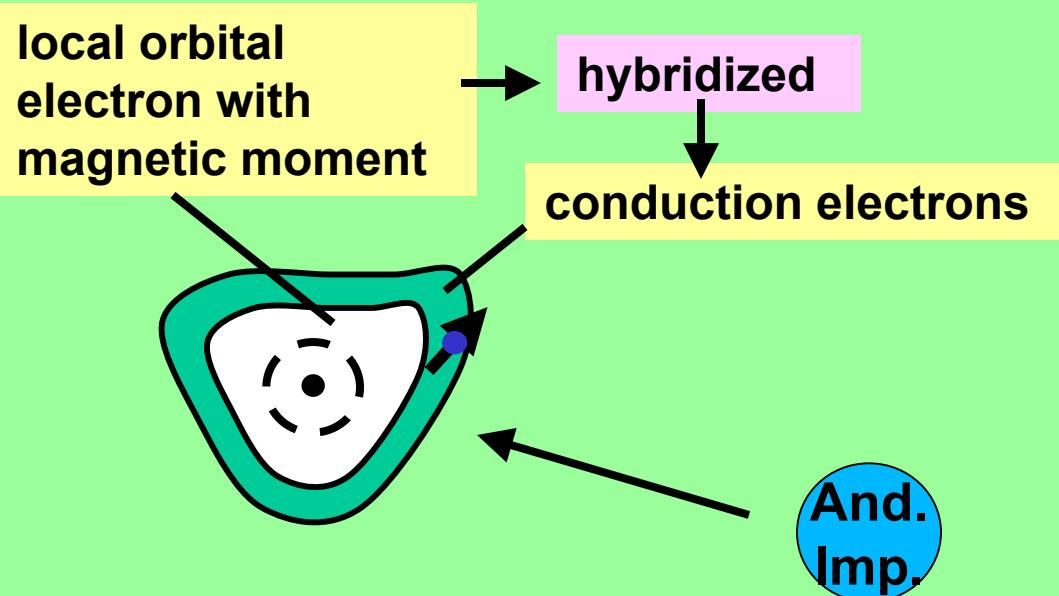
U/t large

E_F

Mott-Hubbard metal-insulator transition

NEW VIEW from Dynamic Mean Field Theory

(Vollhardt, Metzner, Kotliar, Georges ≈ 1990)

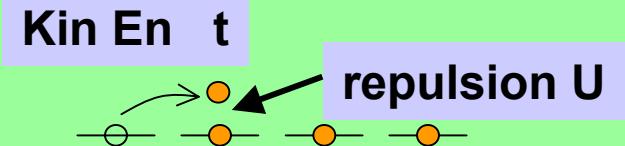
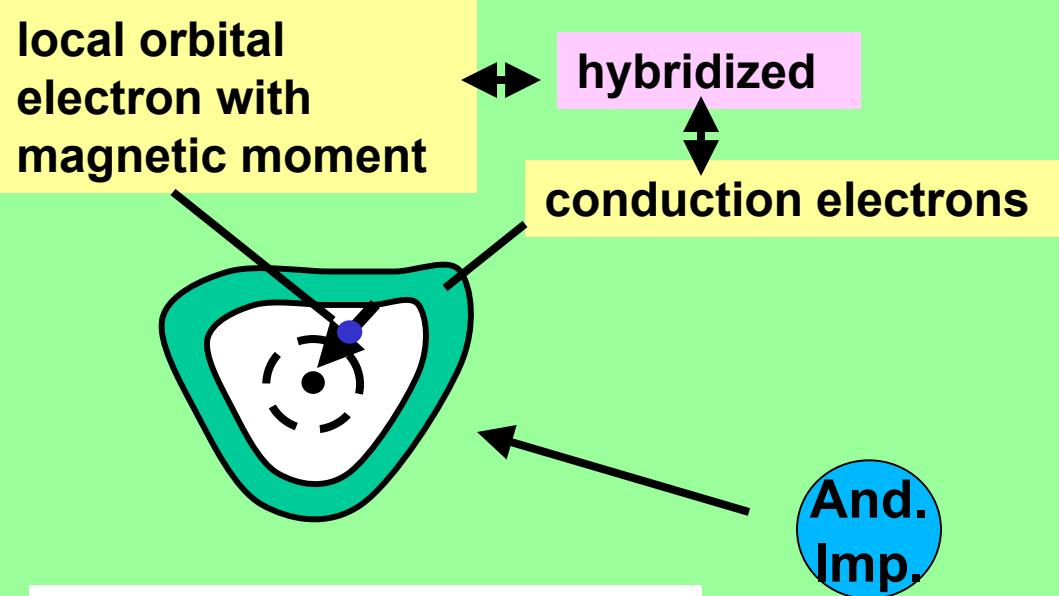


Gap in electron addition/removal spectrum due to U gives insulator!

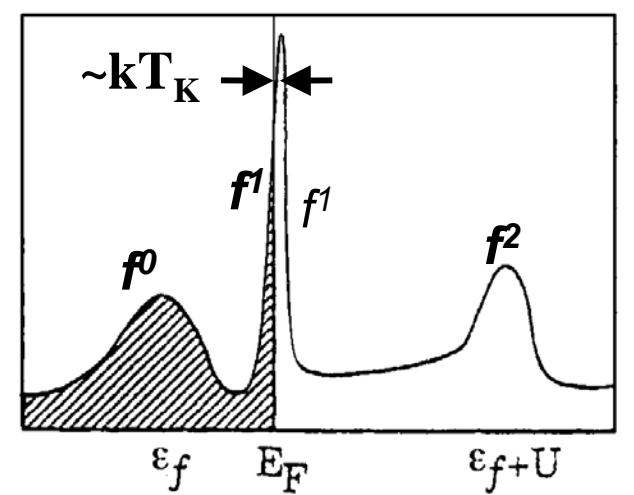
Mott-Hubbard metal-insulator transition

NEW VIEW from Dynamic Mean Field Theory

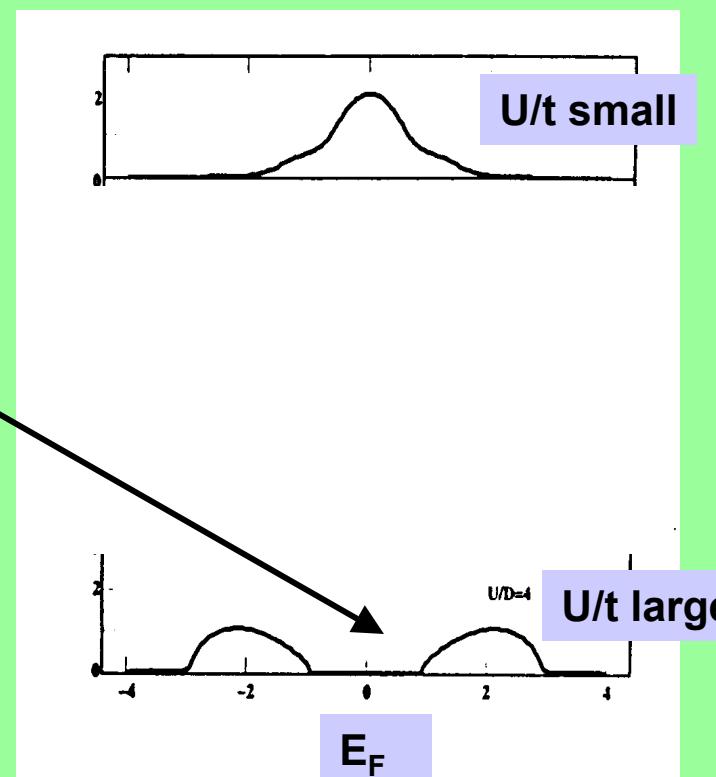
(Vollhardt, Metzner, Kotliar, Georges ≈ 1990)



Hubbard model



Gap in electron addition/removal spectrum due to U
gives insulator!



Kondo physics—moment loss &
Suhl-Abrikosov/Kondo resonance

Electron addition/removal spectrum

Quasi-particle (Kondo) peak at low energy

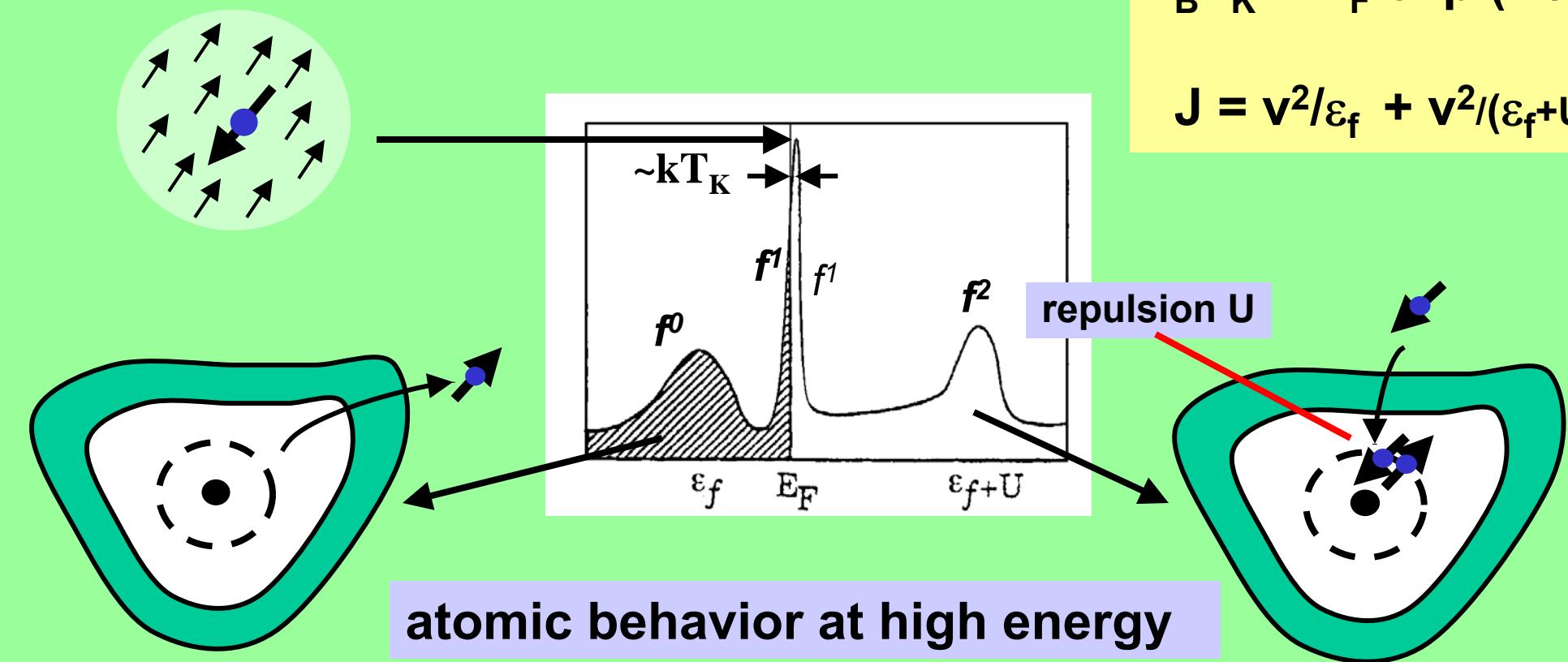
A Fermi liquid: -- QP peak implied by Friedel sum rule (Langreth 1966)

Emergent low energy scale: $k_B T_K$

$T < T_K$ magnetic moments quenched

$$k_B T_K = E_F \exp(-1/J)$$

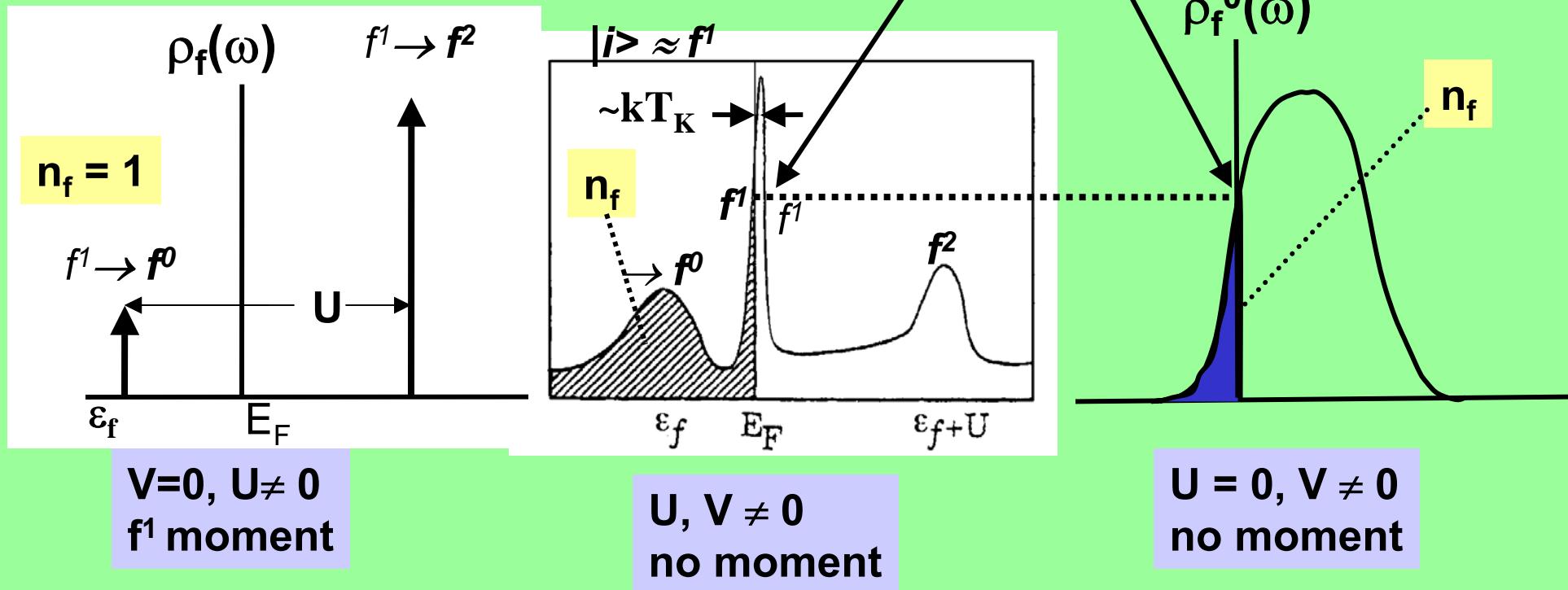
$$J = v^2/\epsilon_f + v^2/(\epsilon_f + U_{ff})$$



Quasi-particle of Anderson impurity model

Kondo resonance implied by
Friedel Sum Rule (Langreth) for fixed n_f

$$\rho_f(\omega = E_F) = \rho_f^0(\omega = E_F)$$



Kondo resonance in angle integrated Ce 4f spectra: early experiment and theory

Spectra from photoemission



and x-ray inverse photoemission (Xerox PARC) samples:

(Maple, UCSD)

Allen et al
PRB 1983

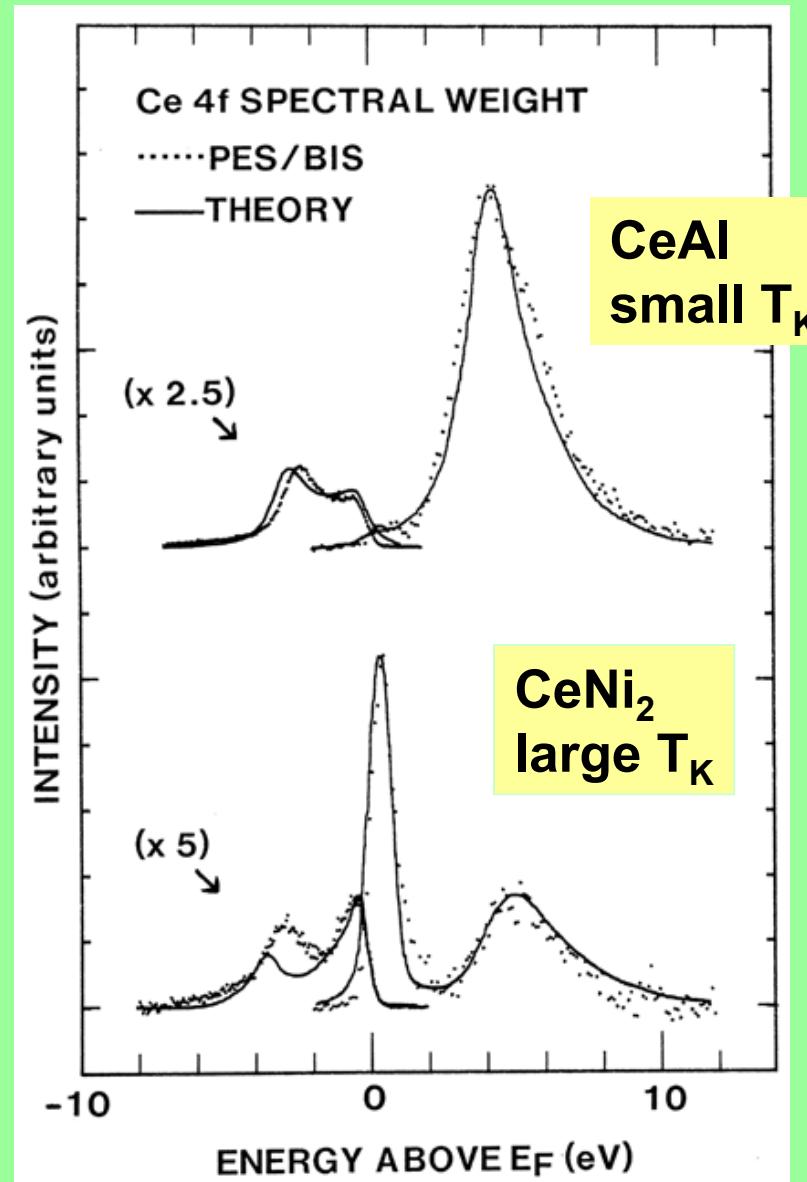
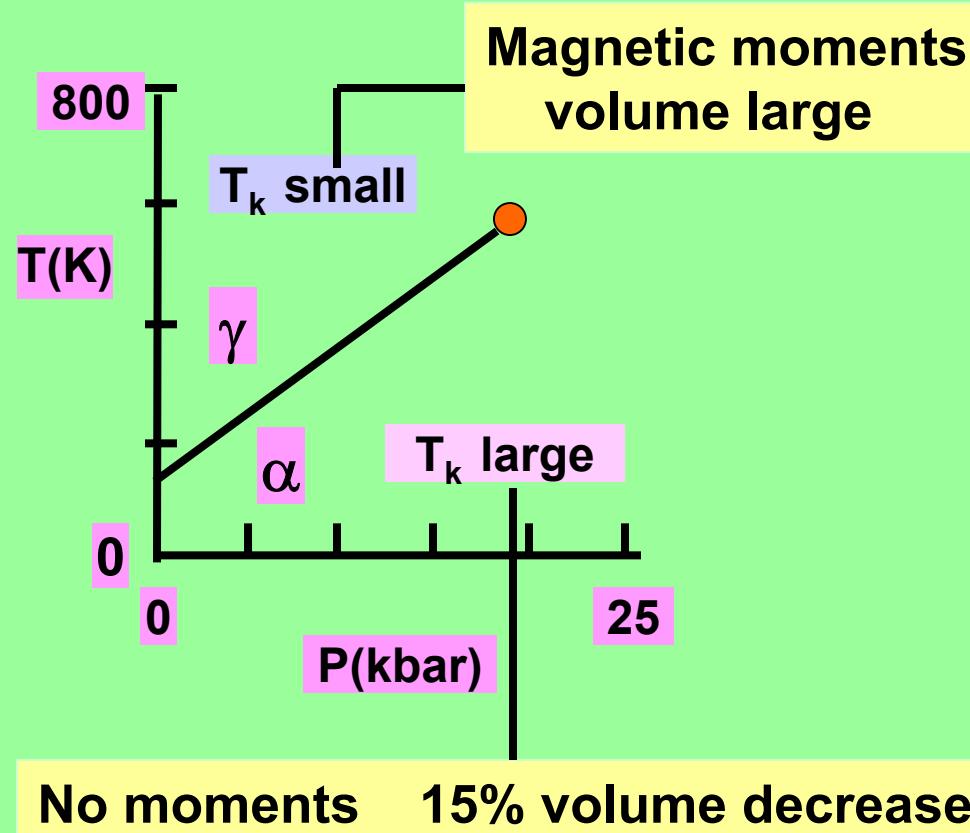


Fig. from
Allen et al
Adv. in Physics
1985

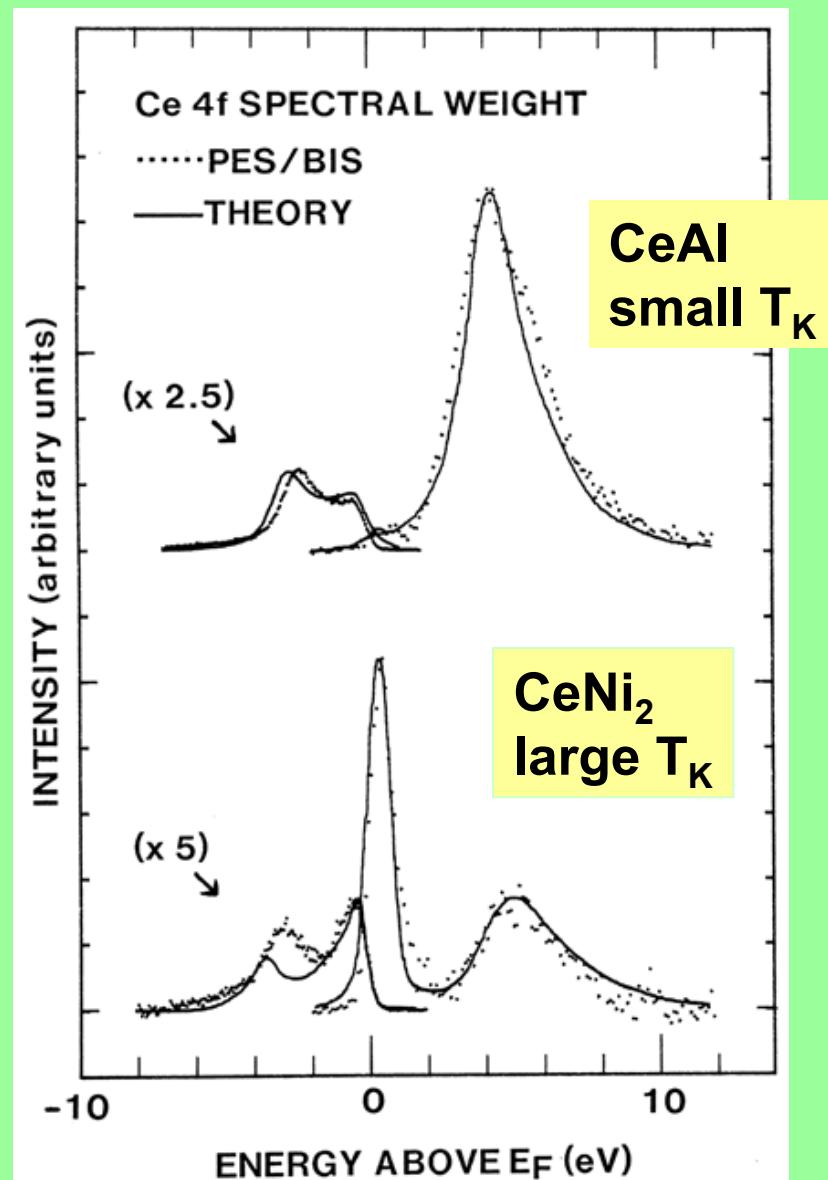
Spectral theory:
Gunnarsson
& Schönhammer
PRL 1983

Ce α - γ transition: similar spectral change ⇒ "Kondo Volume Collapse" (Allen & Martin 1982)

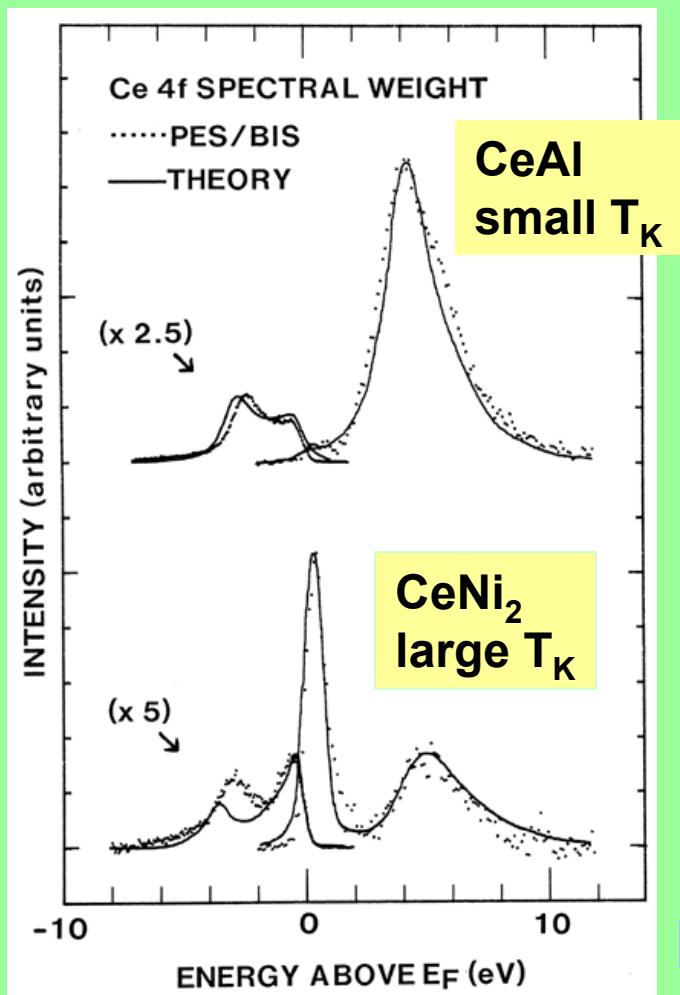
γ stabilized by spin entropy
 elastic energy decrease



α stabilized by large Kondo
 Kondo binding energy
 overcomes elastic energy increase

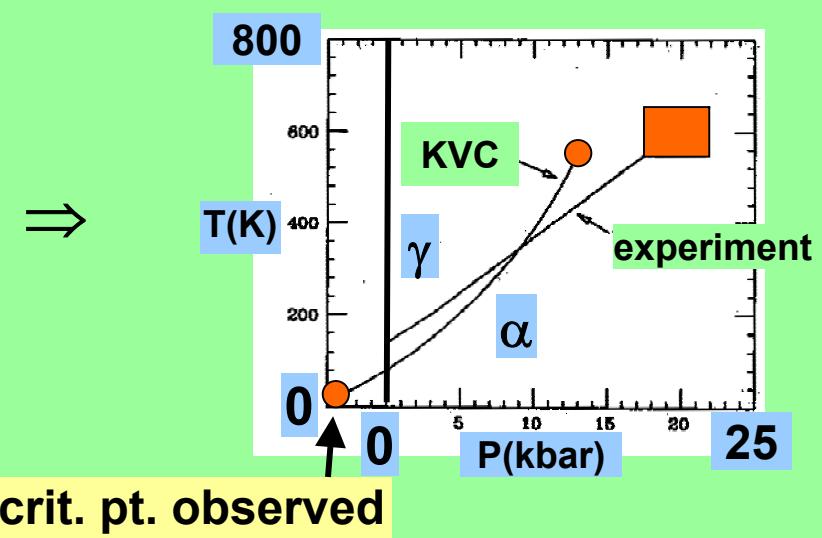
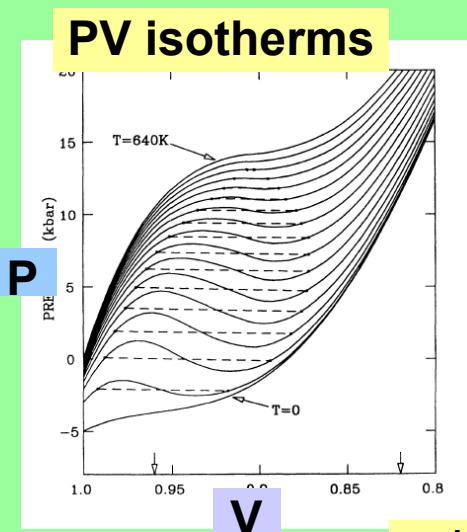


Kondo volume collapse and Ce α - γ transition using impurity Anderson model



Kondo Volume Collapse in Ce (Allen & Martin 1982)

- hybridization volume dependence from LDA--- elastic energy from experiment
---- ϵ_f and U and scaling of V from spectra
- volume dependent $F = (E - TS)$ from impurity model



“Dense impurity ansatz” for Ce compounds

Use of impurity model for concentrated cerium materials?

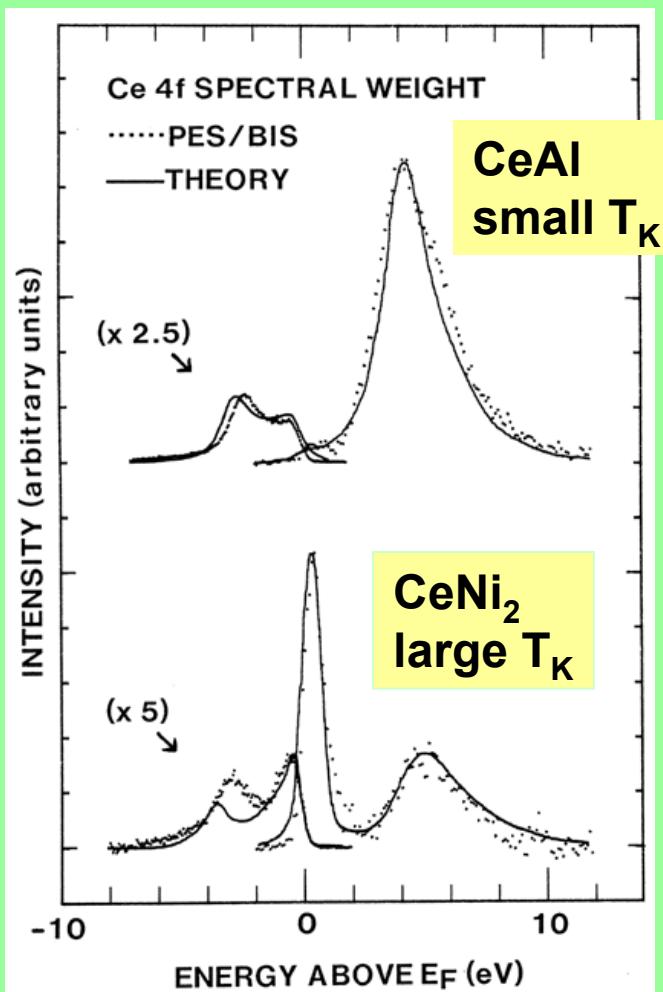
Impurity spectral function an ansatz
for local (k -summed) spectral function

$$\sum_k \rho(k, \omega) \equiv \rho_{\text{LOC}}(\omega) \approx \rho_{\text{IMP}}(\varepsilon)$$

Impurity model \Leftrightarrow local properties

angle integrated Ce f-spectrum

find small T_K f-spectrum \approx x-independent: e.g. $(La_{1-x}Ce_x)Al_2$



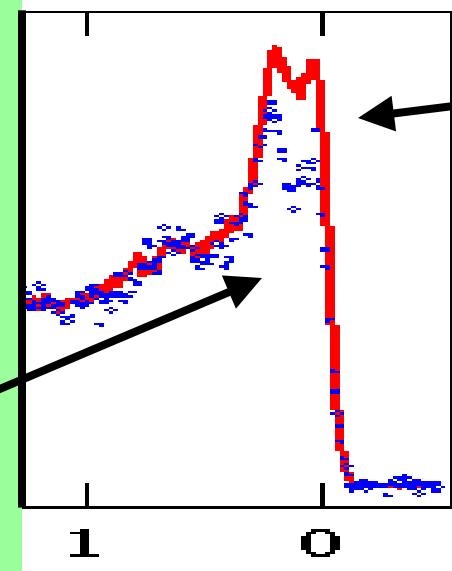
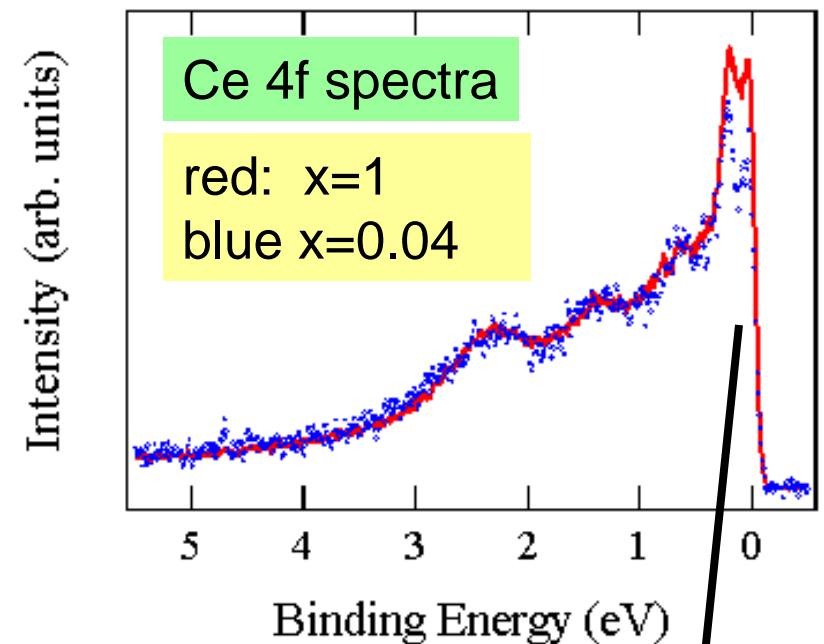
Adv. Phys. 1985
Theory: Gunnarsson & Schönhammer
Samples: Brian Maple

H.-D. Kim et al
Physica B, 2002

RESPES to get
diluted
f-spectrum



**Volume expansion
with dilution**
 $\Rightarrow T_K$ decreases
5K ($x=1$)
 \rightarrow 0.5K ($x=0.04$)
 \Rightarrow small change
near E_F



"Dense impurity ansatz" for Ce compounds

Use of impurity model for concentrated cerium materials?

Impurity spectral function an ansatz
for local (k-summed) spectral function

$$\sum_k \rho(k, \omega) \equiv \rho_{\text{LOC}}(\omega) \approx \rho_{\text{IMP}}(\varepsilon)$$

Impurity model \Leftrightarrow local properties

For lattice: (Müller-Hartmann, Z. Phys. B 76, 211 (1989))
if self energy k-independent

$$\rho_{\text{LOC}}(E_F) \equiv \rho_{\text{LOC}, 0}(E_F)$$

i.e. same as exact impurity model sum rule

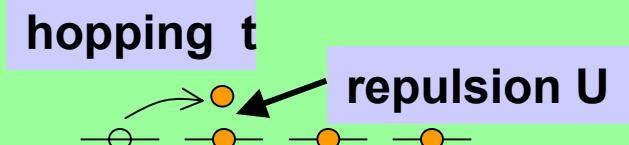
Possibility for "impurity model" with $\rho_{\text{LOC}}(\omega) \equiv \rho_{\text{IMP}}(\varepsilon)$???

Mott-Hubbard metal-insulator transition

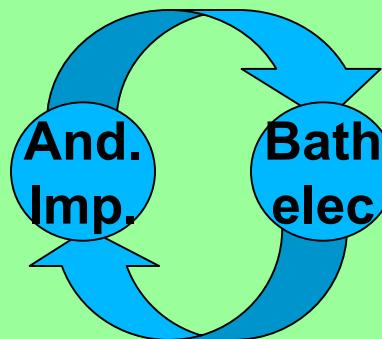
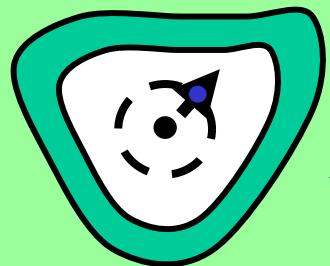
new view from Dynamic Mean Field Theory

(Vollhardt, Metzner, Kotliar, Georges ≈ 1990)

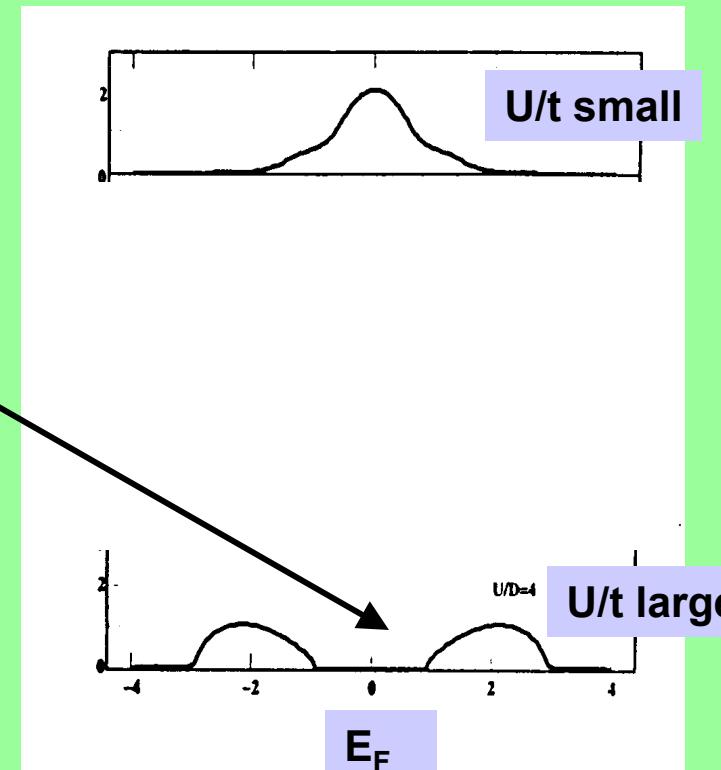
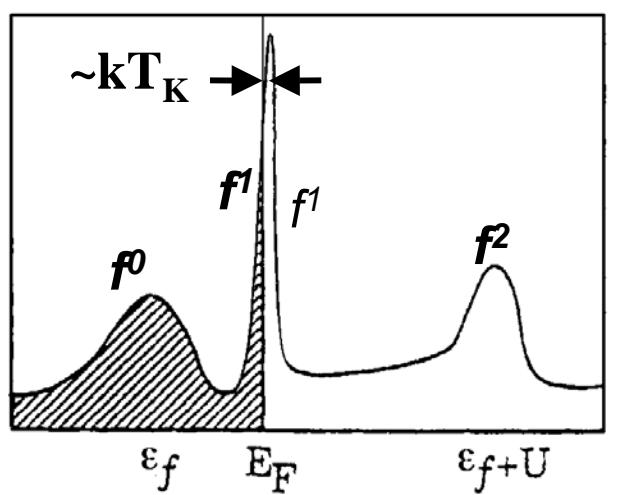
DMFT: \Rightarrow **a self-consistent**
Anderson impurity model (exact
in ∞ dimensions -- finds $\Sigma(k,\omega) = \Sigma(\omega)$)



Hubbard model



Gap in electron addition/removal spectrum due to U
gives insulator!



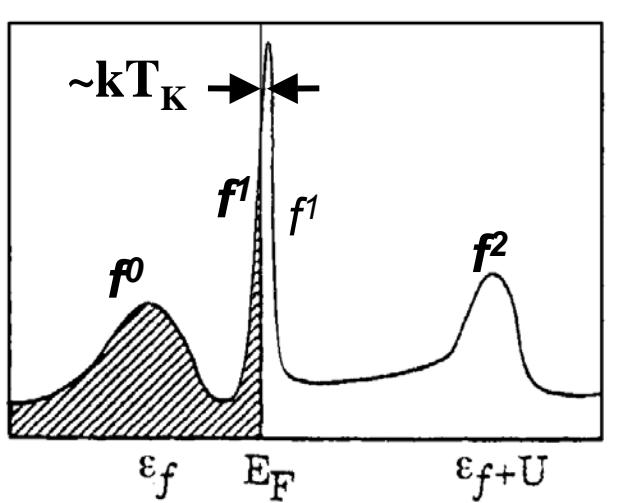
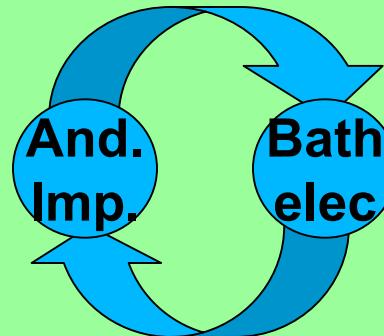
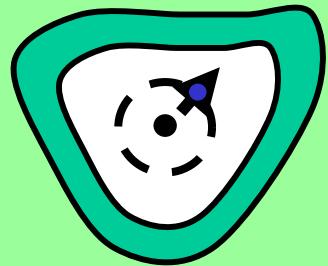
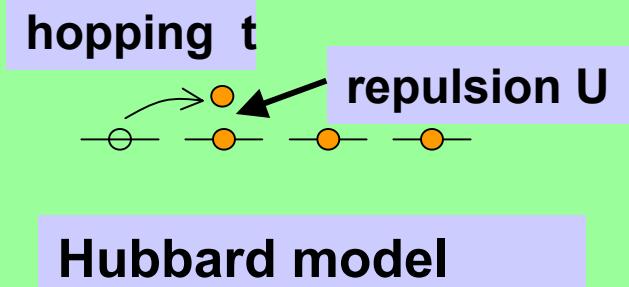
Kondo physics—moment loss &
Suhl-Abrikosov/Kondo resonance

Mott-Hubbard metal-insulator transition

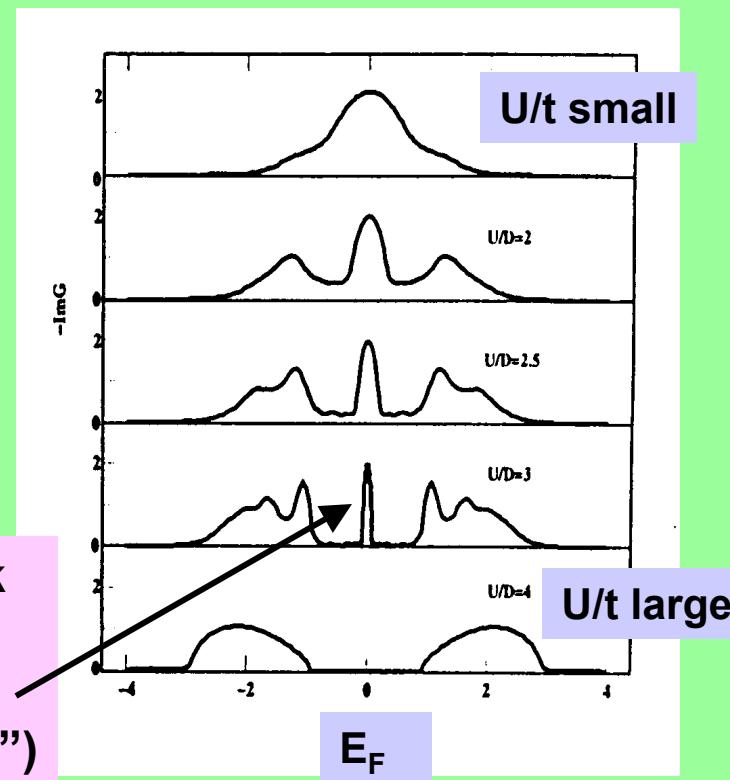
new view from Dynamic Mean Field Theory

(Vollhardt, Metzner, Kotliar, Georges ≈ 1990)

DMFT: \Rightarrow **a self-consistent**
Anderson impurity model (exact
in ∞ dimensions -- finds $\Sigma(k,\omega) = \Sigma(\omega)$)



quasi-particle peak
growing in gap
as U/t decreases
("bootstrap Kondo")

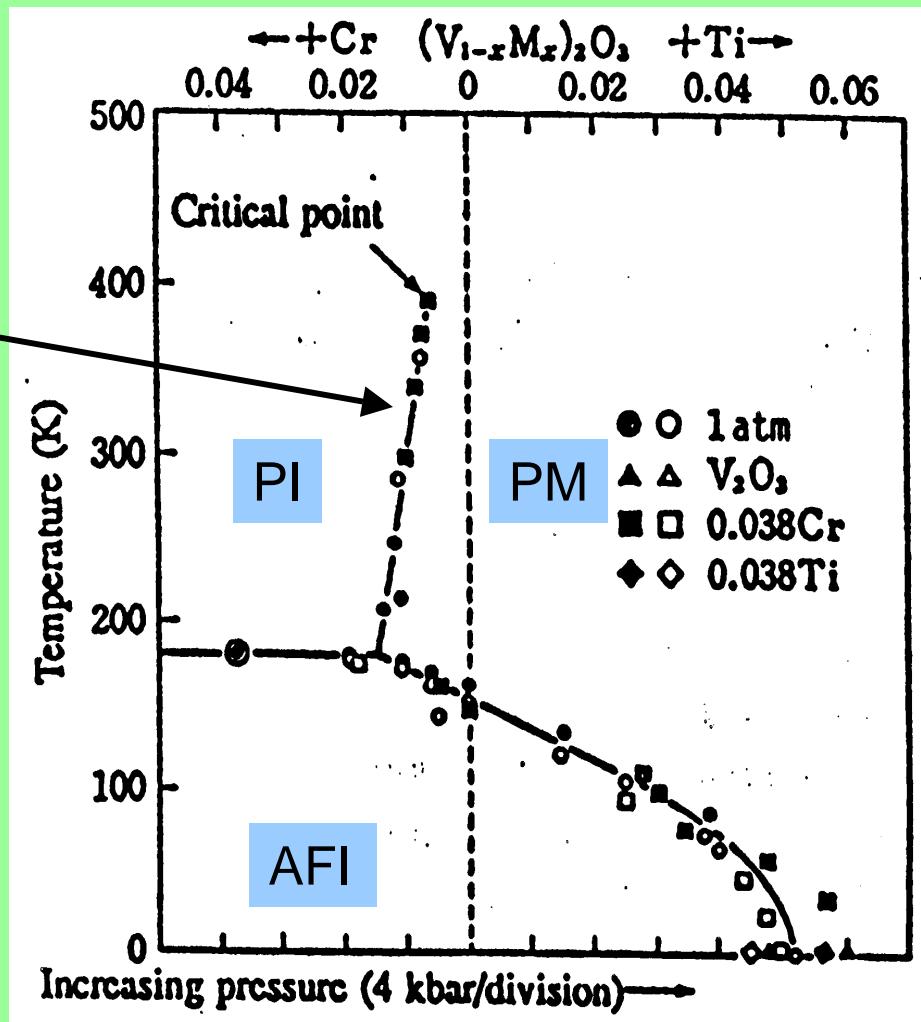


Kondo physics—moment loss &
Suhl-Abrikosov/Kondo resonance

Paradigm material: $(V_{1-x}M_x)_2O_3$ (M=Cr, Ti)

McWhan, Rice et al.
PRL '69, PRB '73

$PI \Leftrightarrow PM$
interpreted
as Mott transition of
1-band
Hubbard model



2e⁻/ V³⁺ ion
3 orbitals/ion
4 ions/cell

more
complex
than
1-band
Hubbard

Importance of realism: Ezhov et al, PRL '99, Park et al, PRB '00

⇒ Motivation for LDA + DMFT calculations (Held et al, PRL '01)

Angle integrated bulk sensitive spectra for Mott transition in $(V_{1-x}Cr_x)_2O_3$

Experiment: SPring-8 BL 25SU (S. Suga)

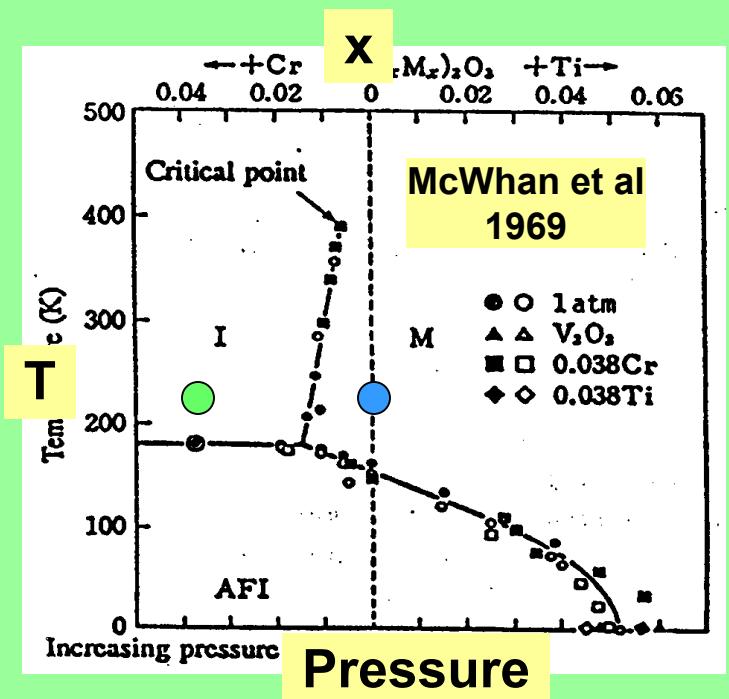
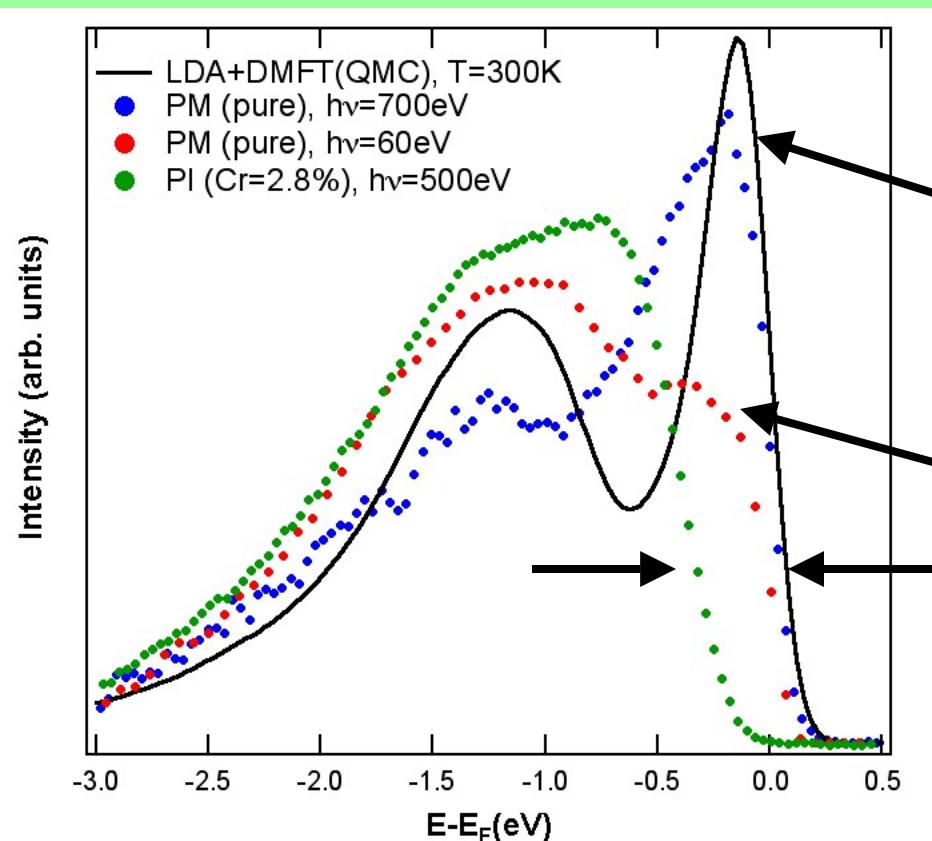
- $h\nu = 500\text{-}700 \text{ eV}$ total $\Delta E \approx 90 \text{ meV}$

- Cleaved single crystals from P. Metcalf, Purdue



Mo et al, PRL (2003)

Vollhardt and Kotliar, Physics Today (2004)



"Kondo peak"
theory
and
experiment
in M phase

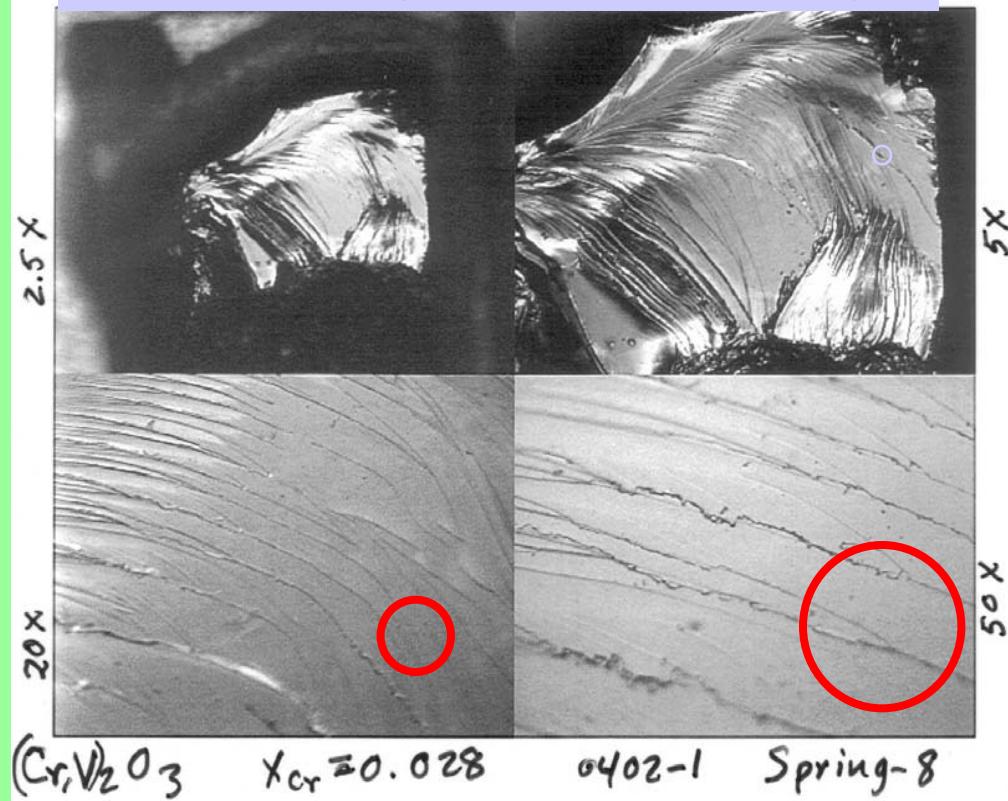
Previous work, 30 years
NO M phase peak

I phase
GAP

Surface layer more
correlated than bulk

Small photon spot also essential for large E_F peak !

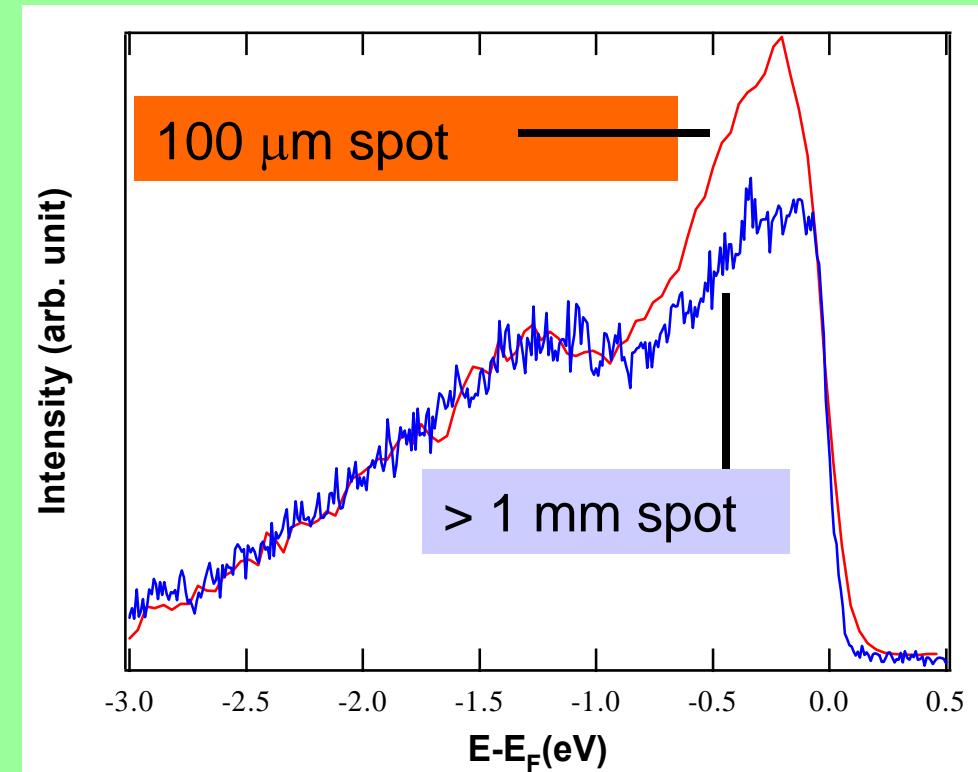
Optical micrograph—J.D. Denlinger



○ = 100 μm spot size

With small spot can select probing point to avoid steps and edges as much as possible

Steps, edges: even lower coordination than smooth surface

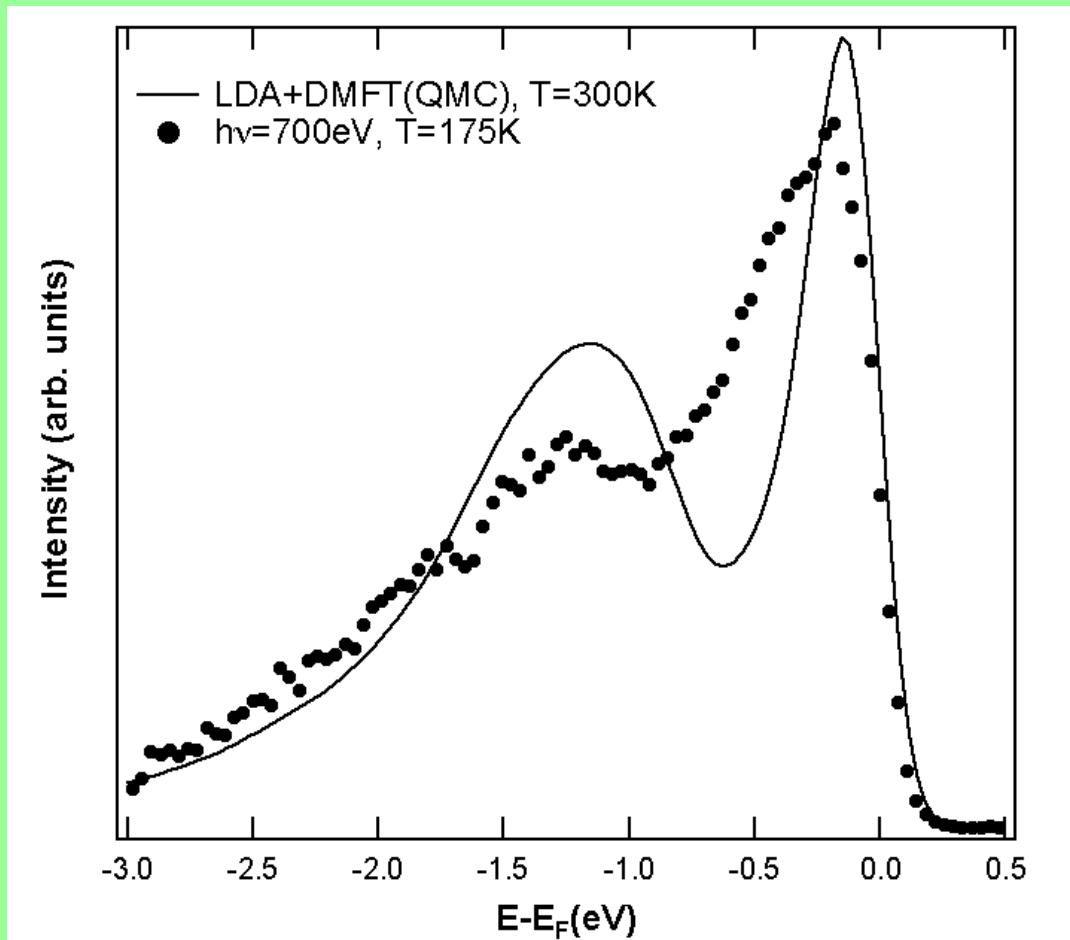


E_F peak much reduced with larger spot

Difference for 300 eV to 500 eV range even larger

Compare V_2O_3 PM phase spectrum to LDA + DMFT (t-orbitals, $U=5.0$ eV, 300K)

S.-K. Mo et al, PRL 90, 186403 (2003)

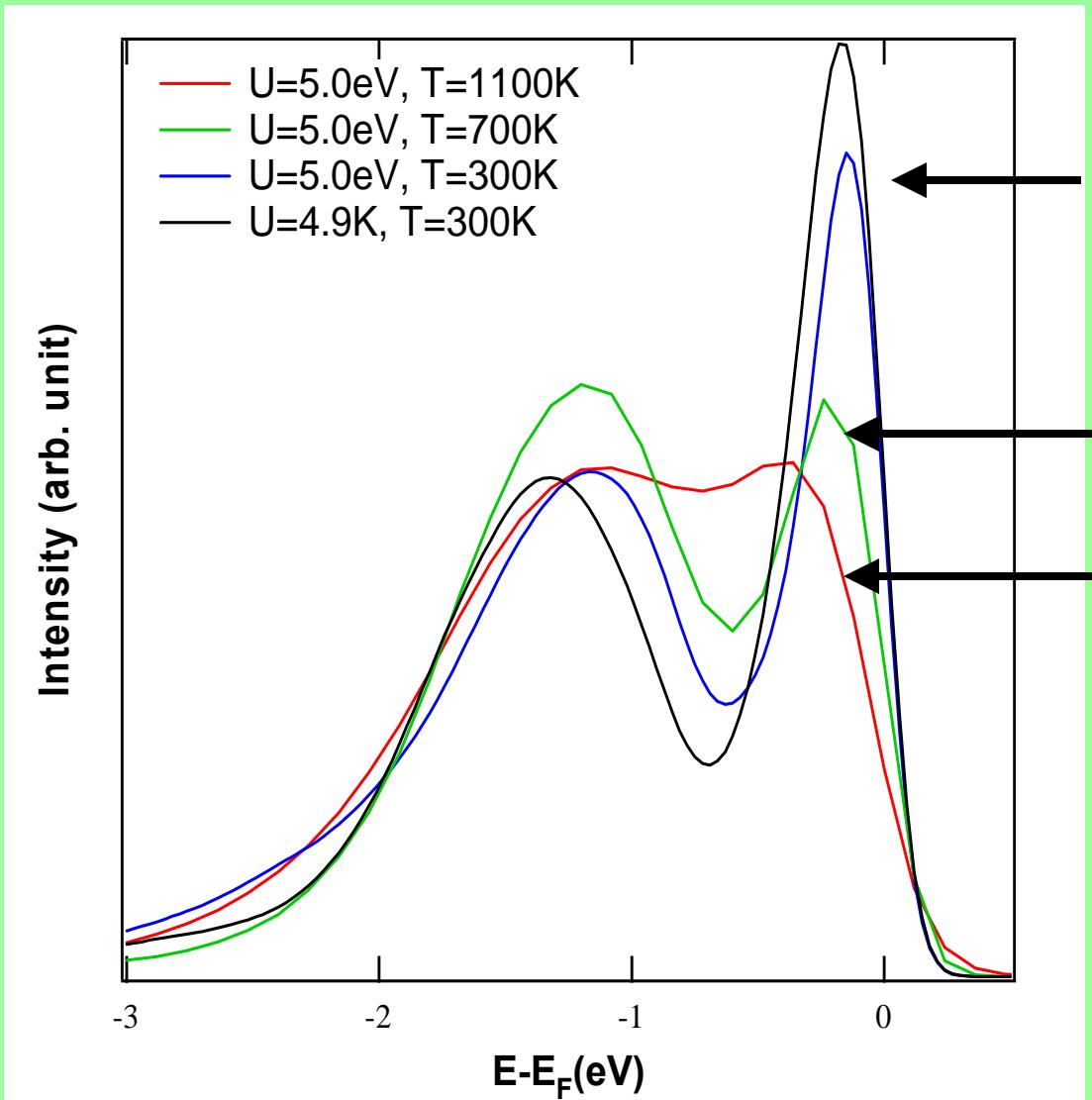


Qualitative agreement on presence of prominent E_F peak in spectrum

But experimental peak width larger than theory width, roughly by factor of 2

And experimental peak weight larger than theory weight

DMFT predicts high T broadening of metal phase E_F peak



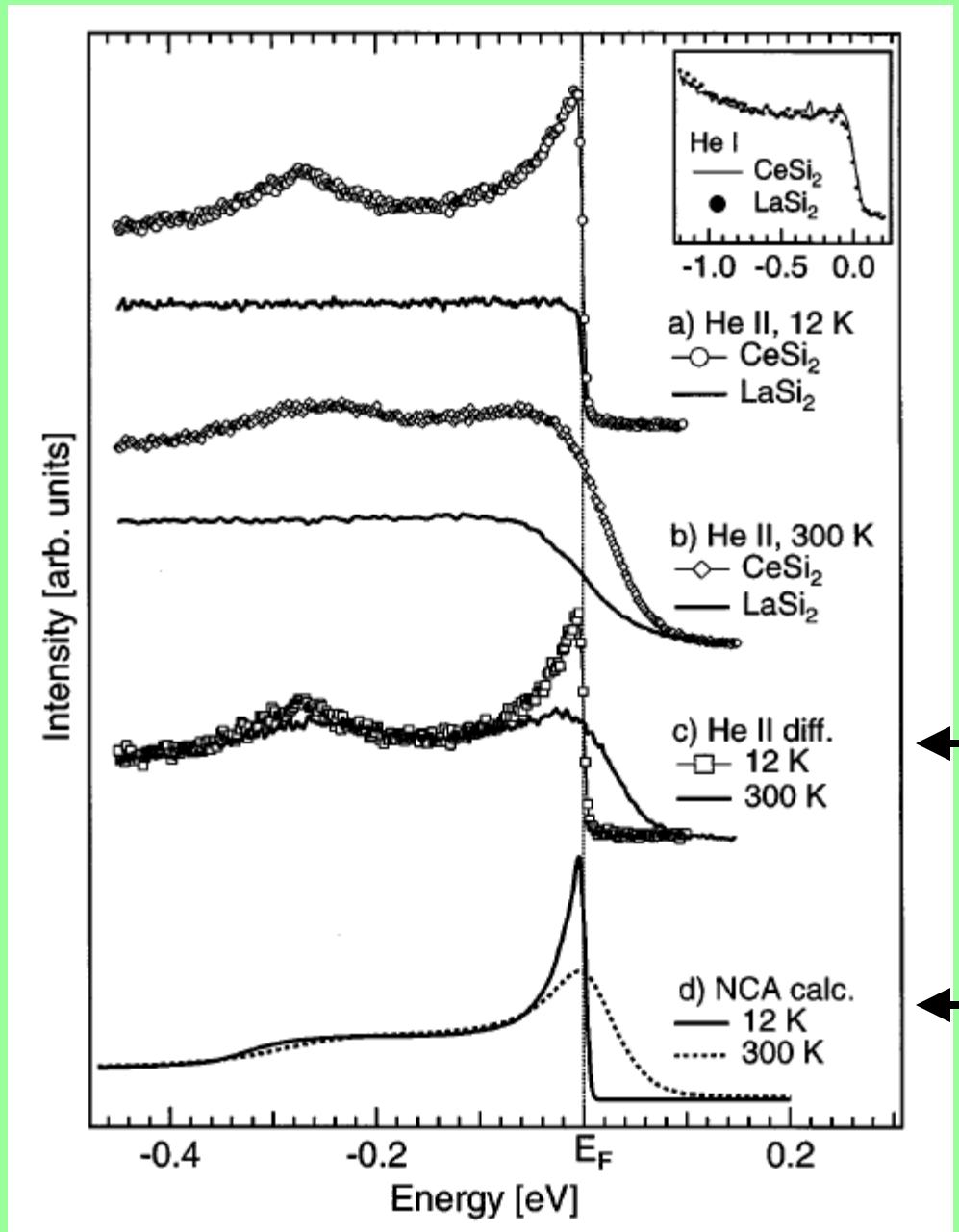
T=300 K
(two similar U values)

T = 700 K

T = 1100 K

quasi-particle peak
→ incoherent

Kondo resonance broadening in CeSi_2

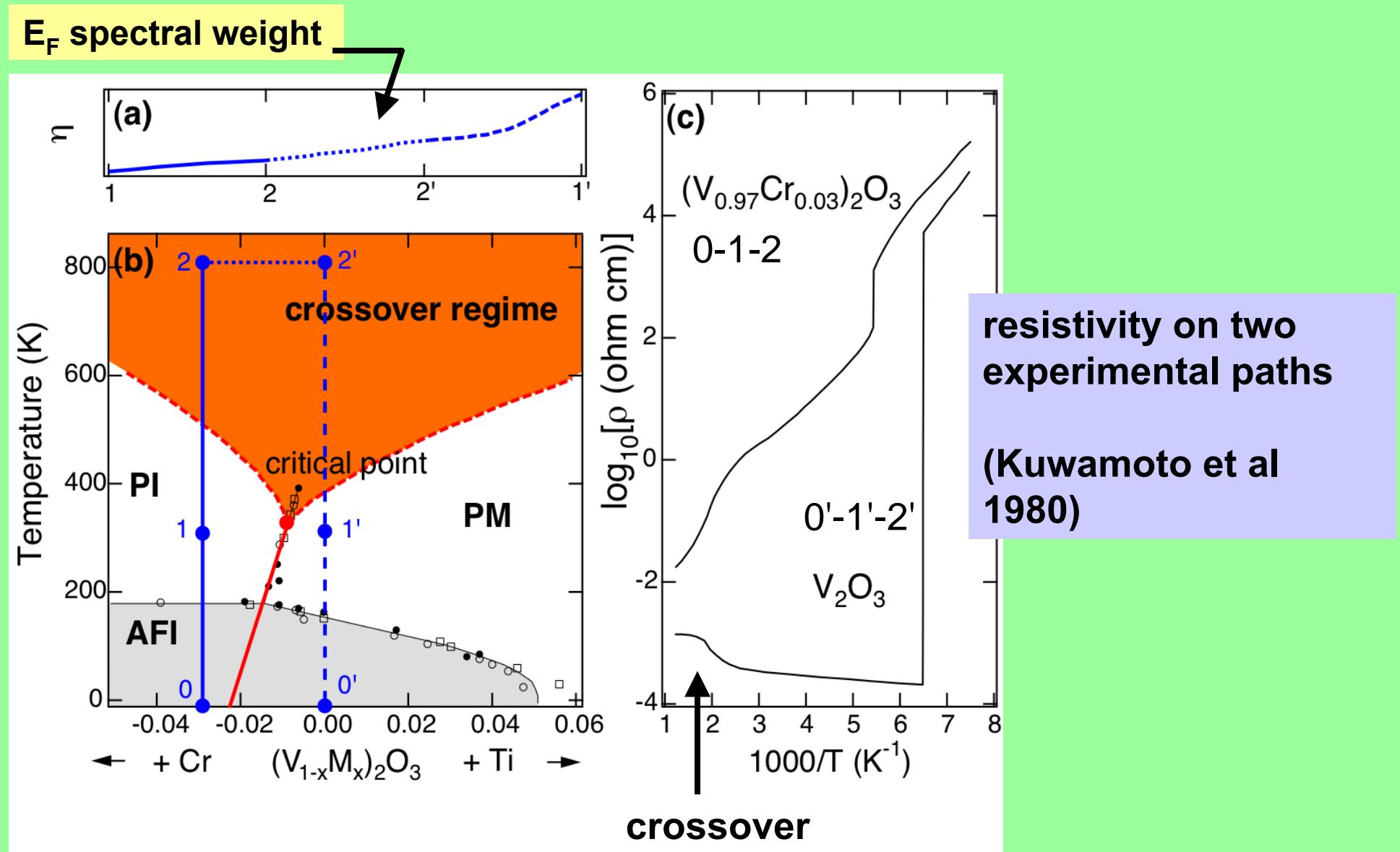


Garnier et al
PRL 81, 1349 (1998)

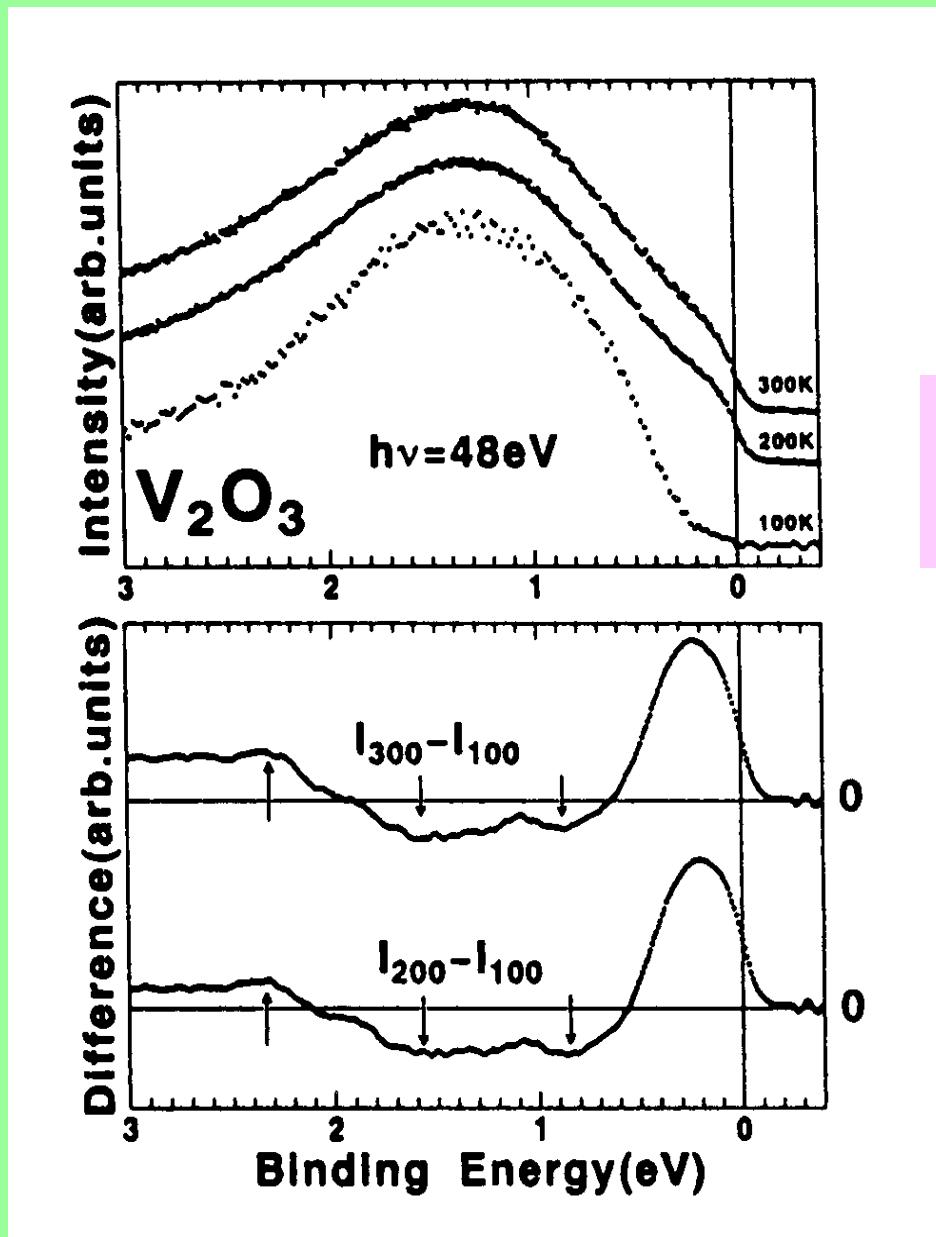
low T & high T spectra

low T & high T
impurity model theory

High T DMFT Landau theory (Kotliar) phase diagram with cross-over regime (red)



Unsuccessful early search for broadening in low $h\nu$ photoemission for PM phase of V_2O_3 (no E_F peak to study!)



Two temperatures in the PM phase

One low temperature in the AFI phase

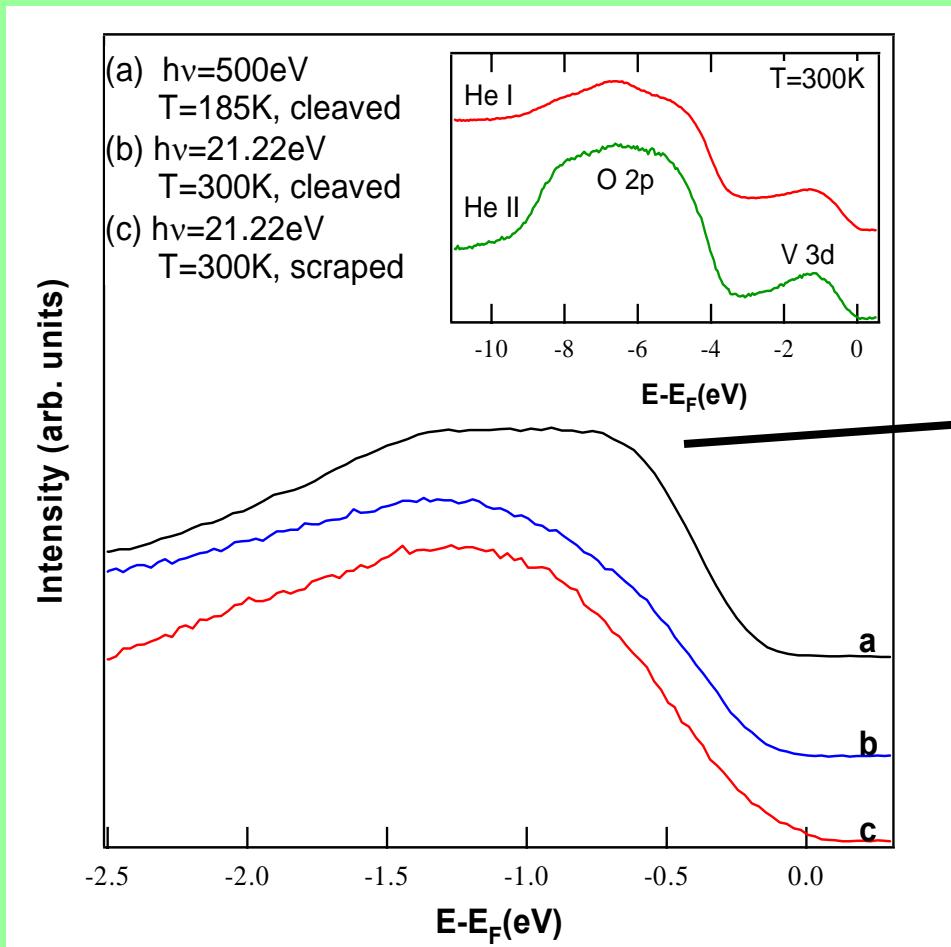
S. Shin et al.
J. Phys. Soc. Jpn.
64, 1230 (1995)

New Approach at low $h\nu$: high temperature PI phase experiment to see correlation gap filling

Home lab, helium lamp $x=2.8\%$ PI phase at 300K

Surface layer more correlated.

So spectra valid to study insulating phase gap filling



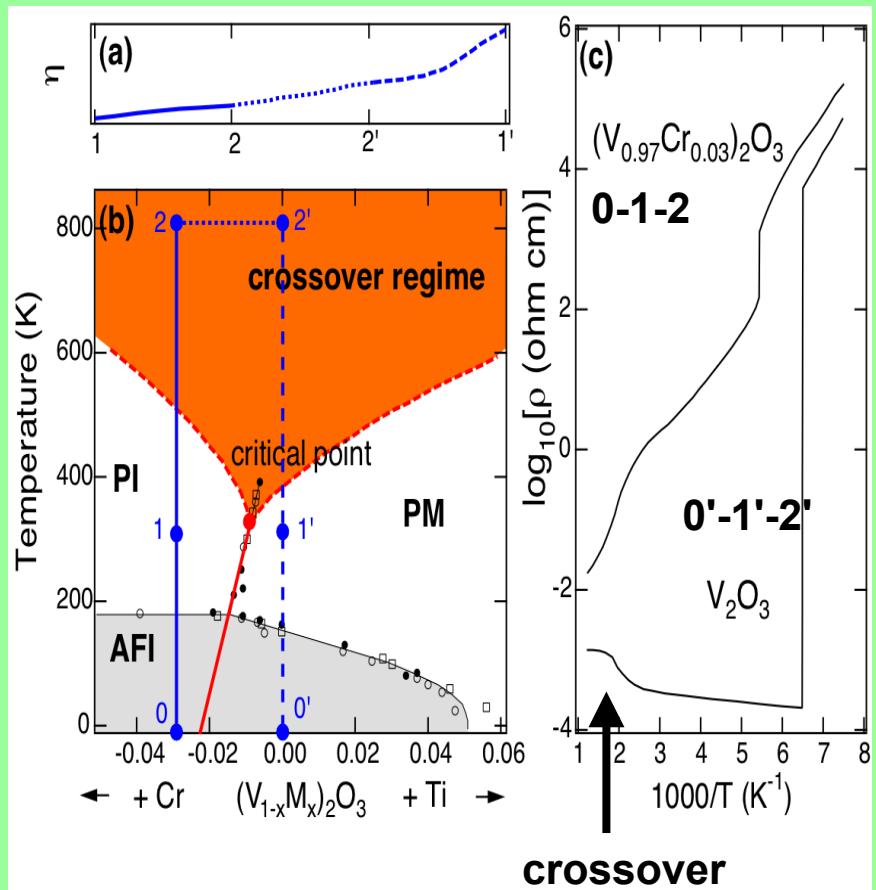
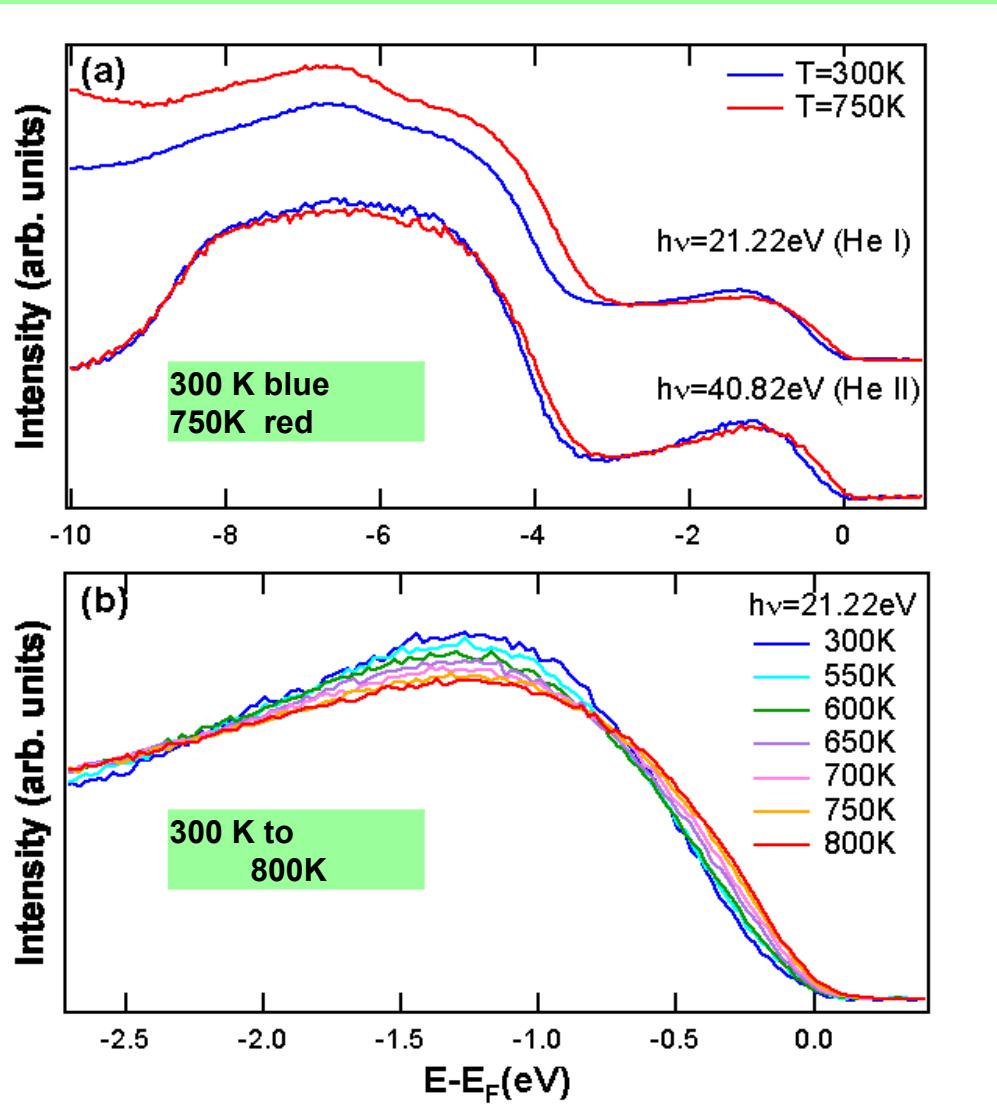
Clean by scraping for extended time and multiple measurements

Must calibrate effect of scraping

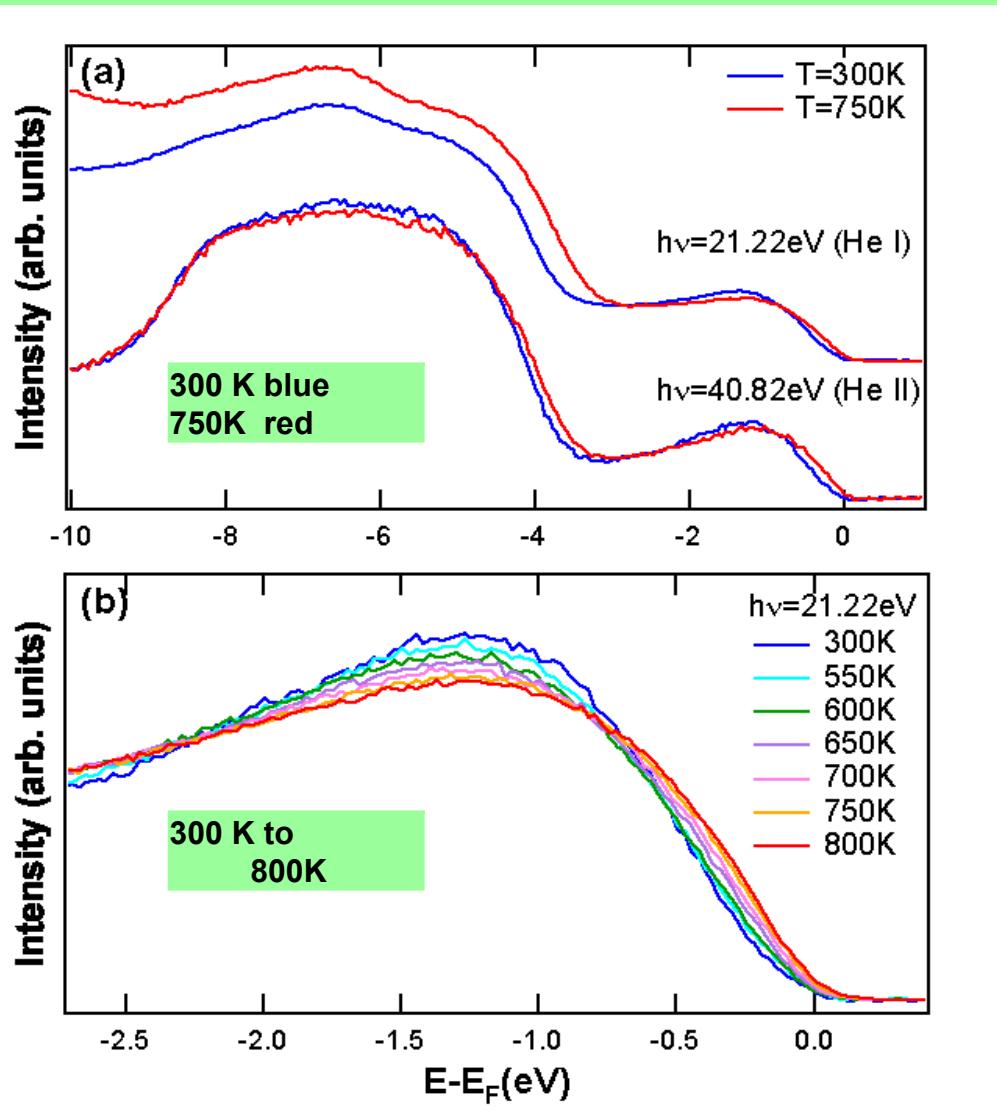
Low binding energy shoulder

- reduced at low photon energy
- more rounded with scraped surface, but still visible so scraped surface OK to study.

High temperature correlation gap filling in $(V_{0.972}Cr_{0.028})_2O_3$ PI phase: spectra to 800K

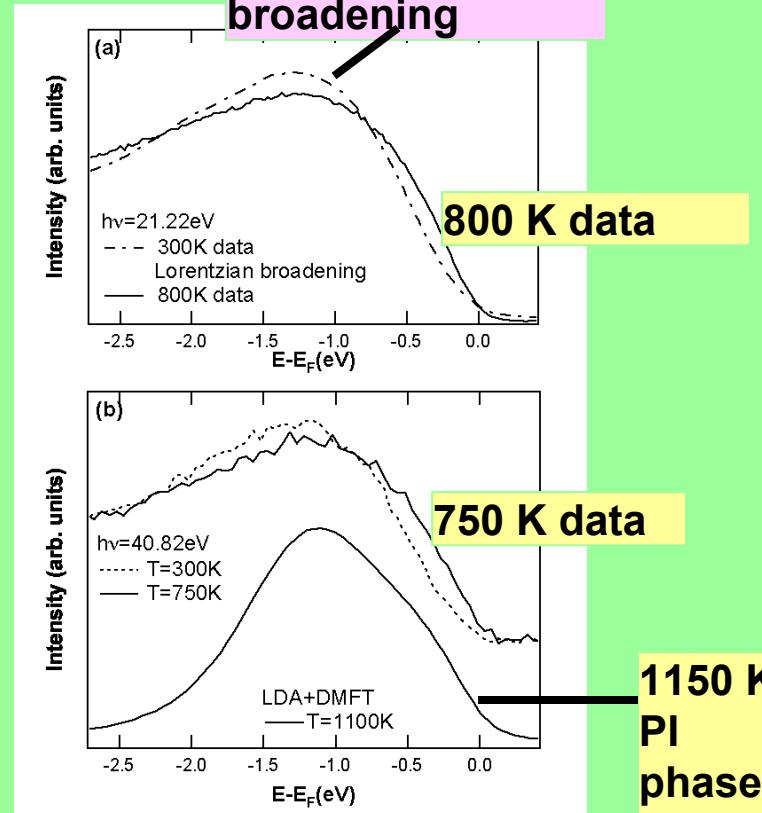


High temperature correlation gap filling in $(V_{0.972}Cr_{0.028})_2O_3$ PI phase: spectra to 800K



negative curvature
near E_F , theory and
experiment
due to gap filling

300K data with
1150 K Lorentizian
broadening



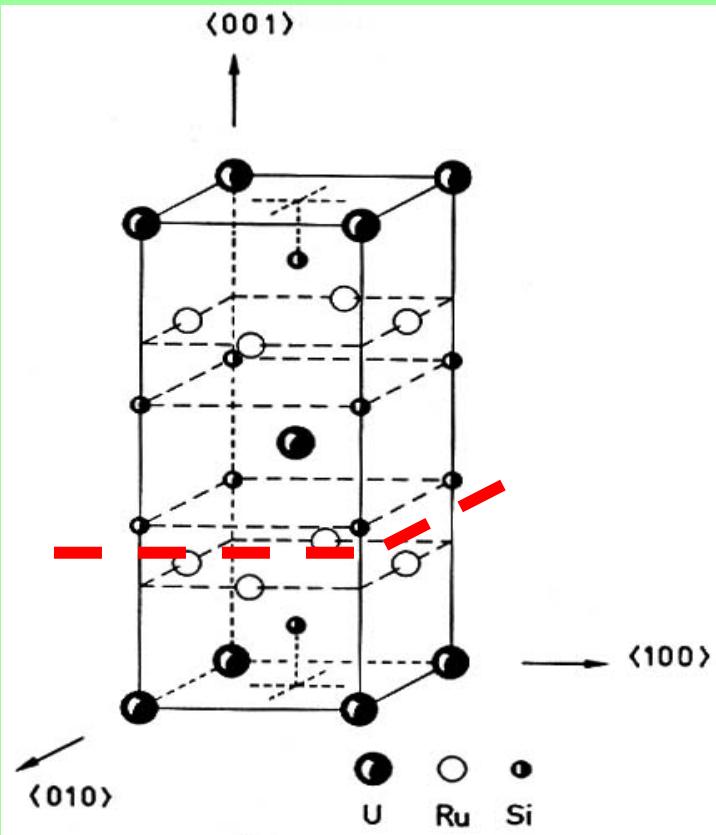
Summary for V₂O₃

- Metal-insulator transition in V₂O₃
- See DMFT “Kondo peak” in PM phase 3d PES spectrum
- Need high $h\nu$ and small photon spot to get bulk 3d
Surface more correlated---peak hardly seen
- Peak width and weight larger than in theory

- High T gap filling of PI phase
- Qualitatively like DMFT theory in cross-over regime
- Correlates well with high T resistivity

Kondo and Mott physics intertwined!

XRu₂Si₂ Overview



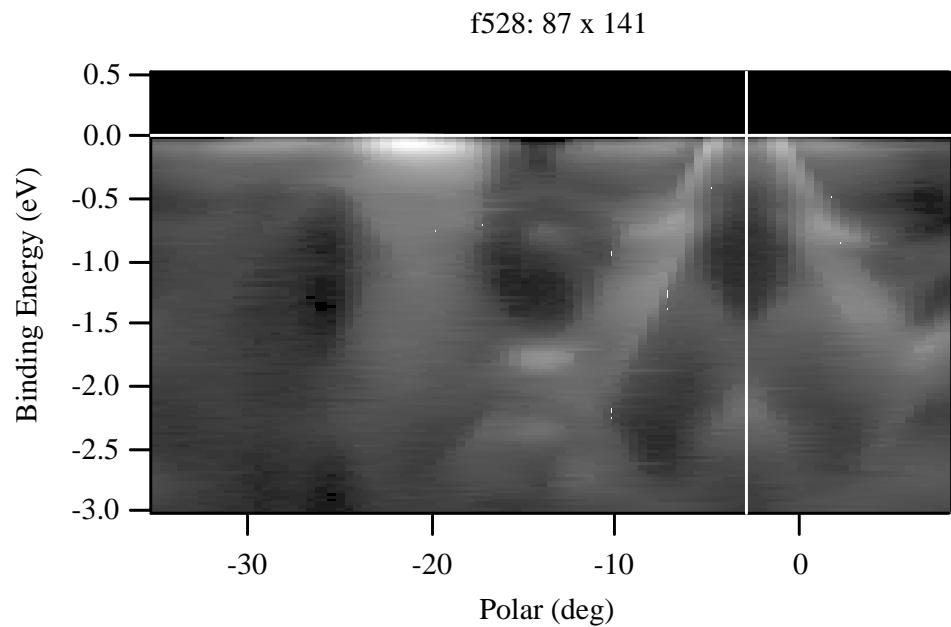
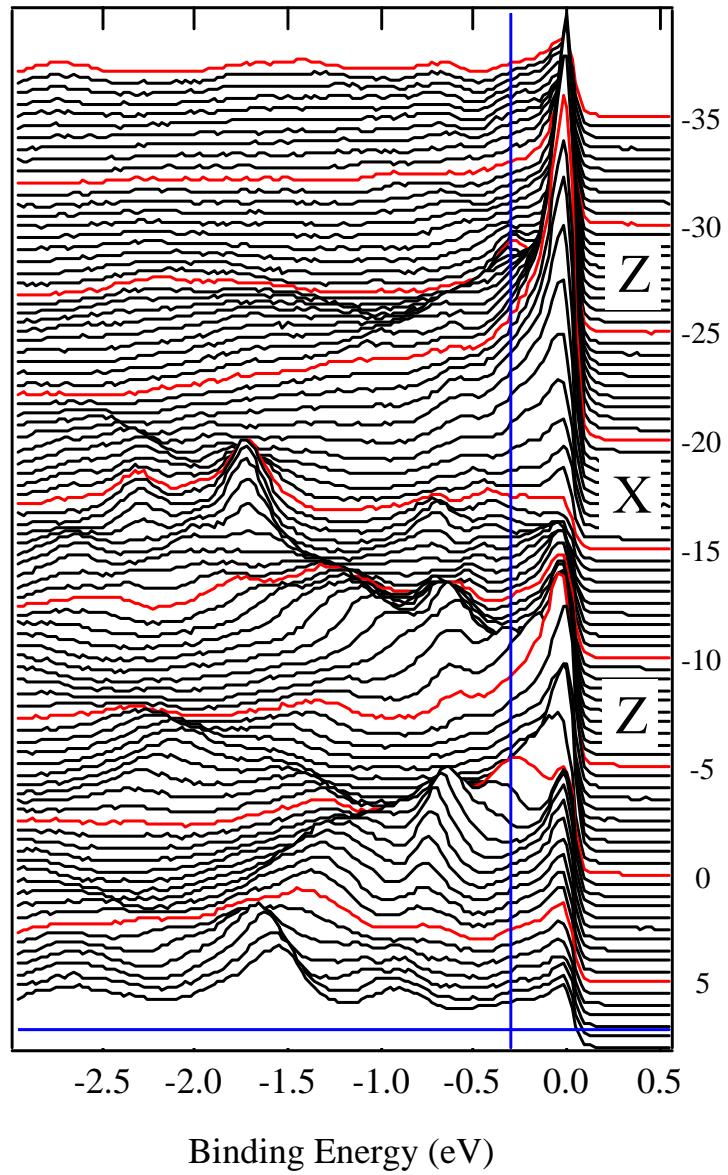
La	Ce	Pr	Nd
57	58	59	60
f0	~f1		
Ac	Th	Pa	U
89	90	91	92
	f0		~f2

Ce 4f results provide context for U 5f studies

	Phase	γ (mJ/mol K ²)	a (Å)	c (Å)
LaRu ₂ Si ₂			4.215	9.930
CeRu ₂ Si ₂	heavy ferm.	350	4.192	9.780
ThRu ₂ Si ₂			4.193	9.746
URu ₂ Si ₂	PM AF SC <1.2K)	(>17.5K) (>1.2K) <1.2K)	180 65	4.129 9.575

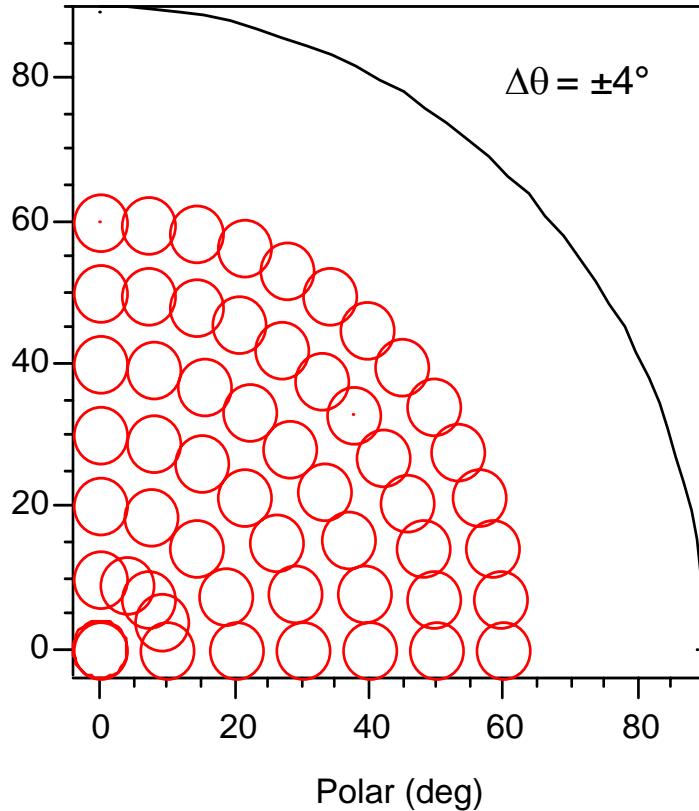
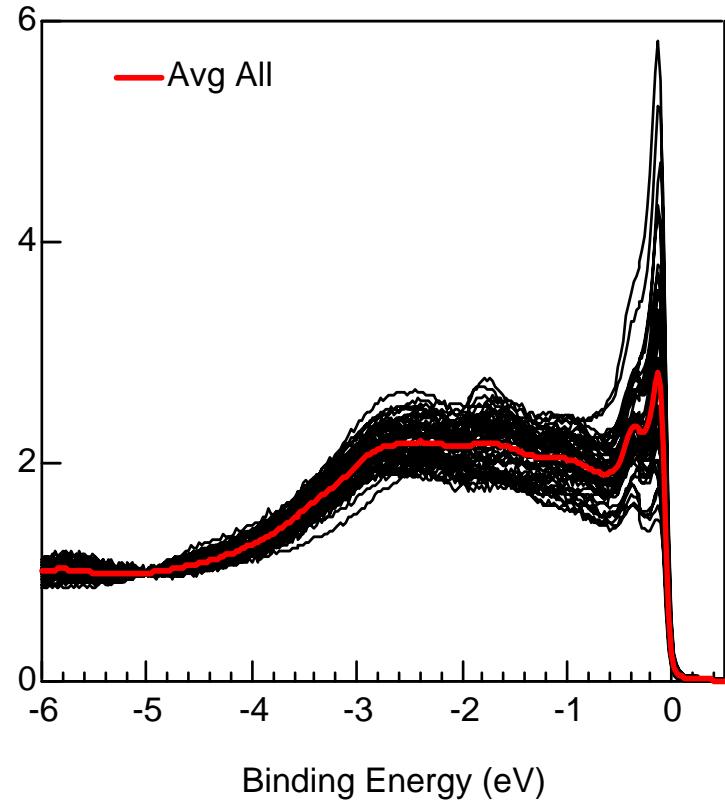
AF moment very small, can't account for large entropy of URu₂Si₂ transition at 17.5K
 \Rightarrow “hidden order” in low T phase

CeRu₂Si₂ ARPES on resonance ($h\nu=122$ eV)

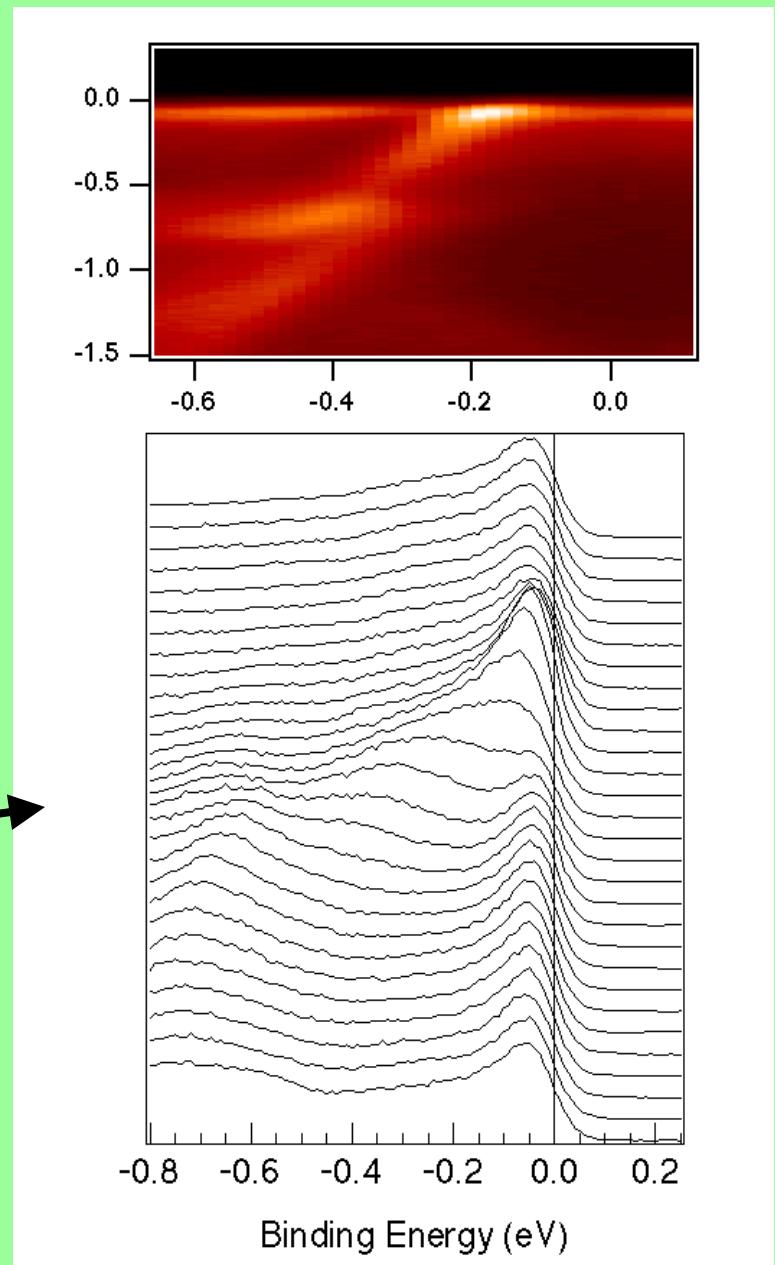
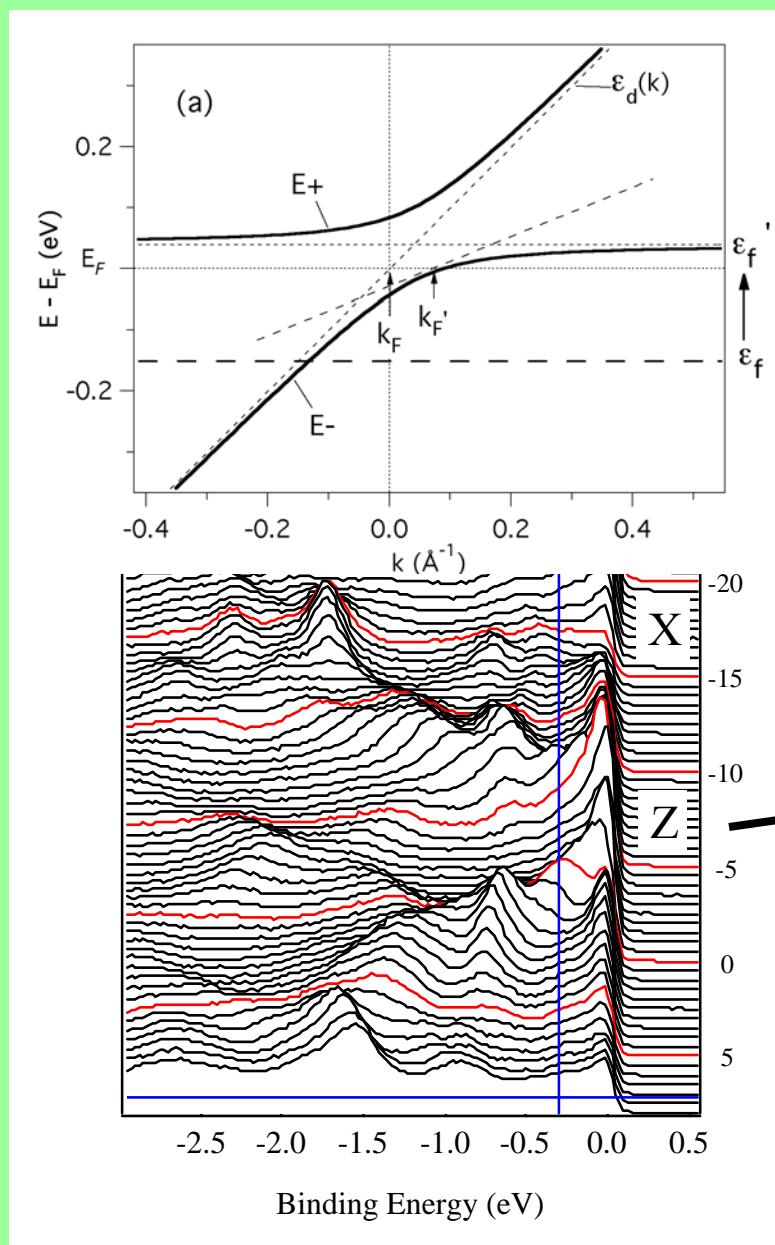


CeRu₂Si₂ ARPES angle sums to impurity model Kondo resonance

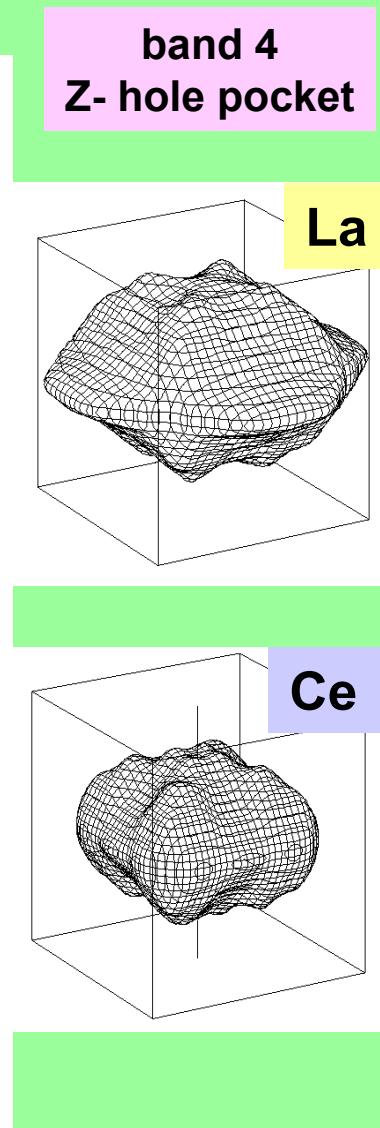
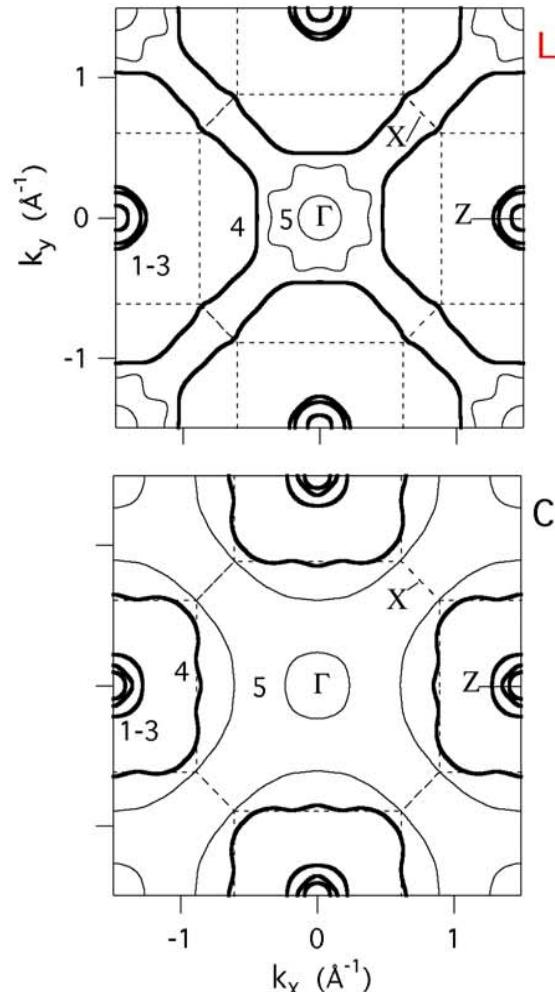
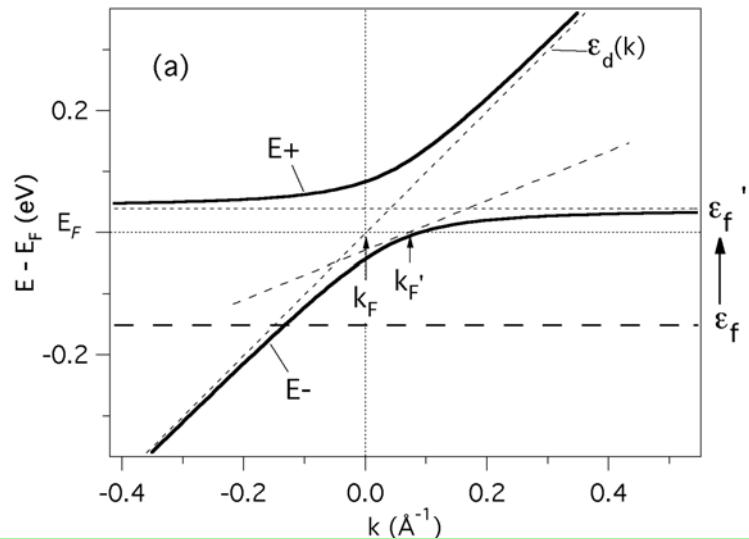
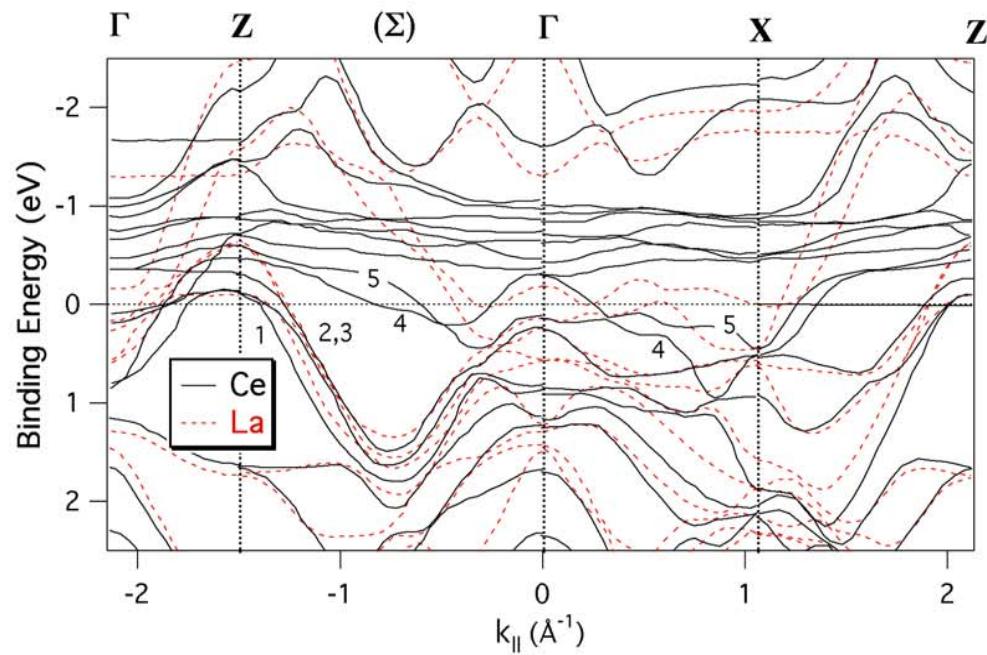
angle-integrated 4d RESPES from ARPES
53 angles, normalize at 5 eV, average



CeRu₂Si₂ ARPES near Z-point like 2-band renormalized Anderson lattice model



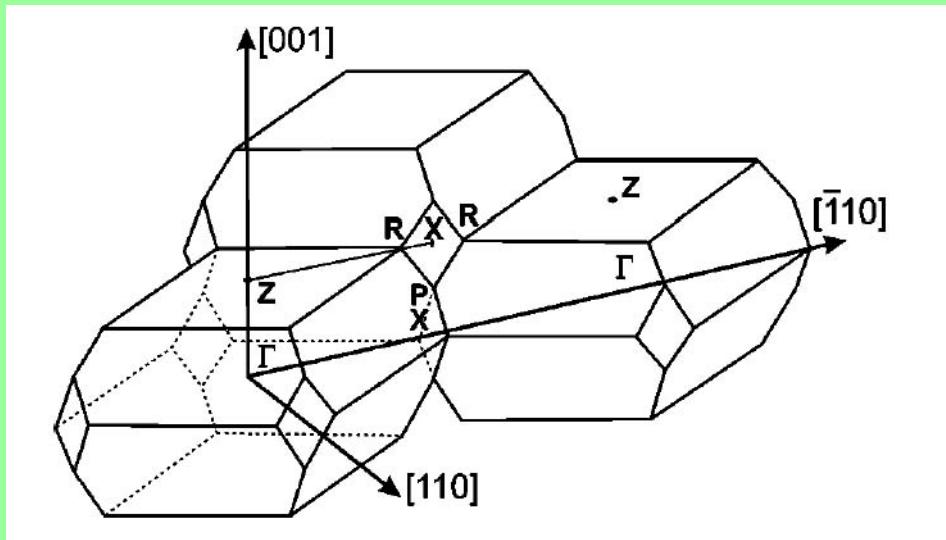
LDA for LaRu₂Si₂ and CeRu₂Si₂ compared



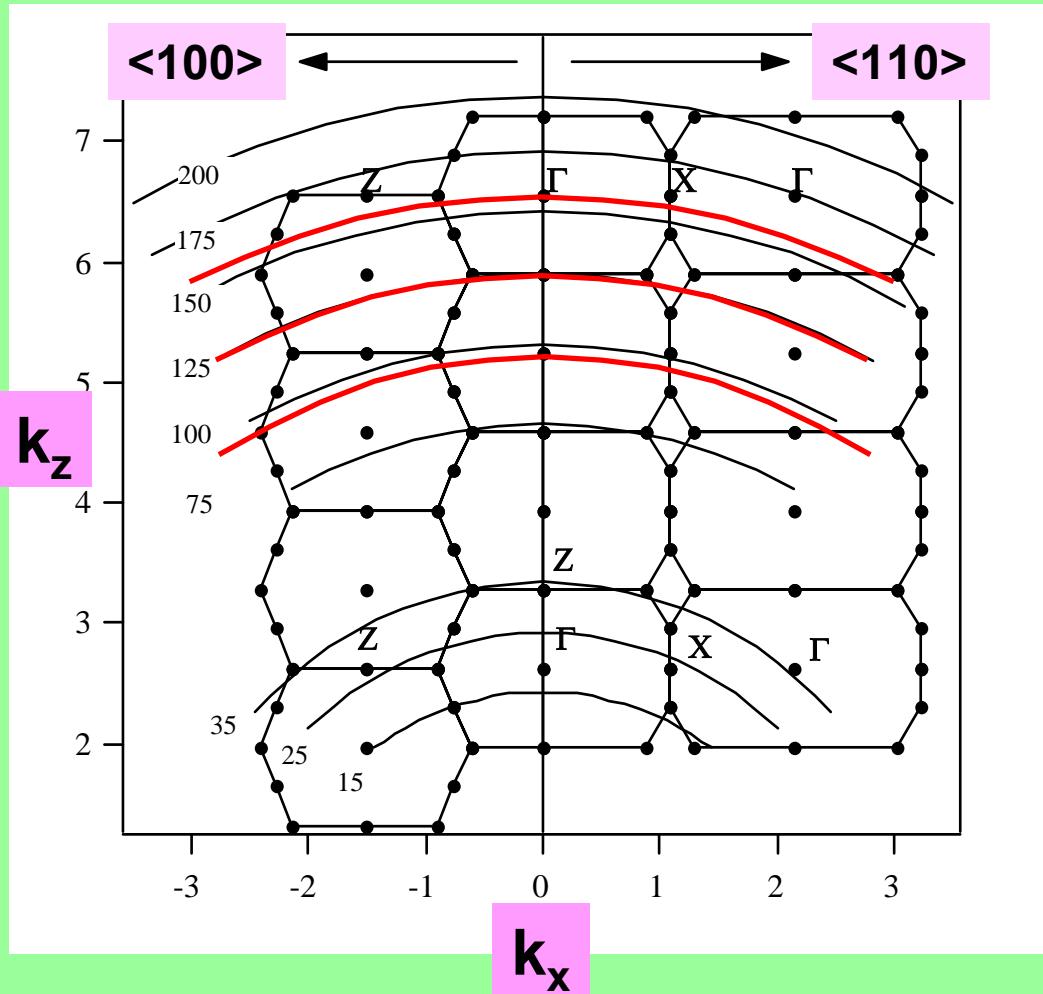
For Ce LDA and Anderson lattice similar
(except for energy scale)---only 1 f-electron

XRu₂Si₂—3d crystal k-space arcs for varying photon energy

Brillouin Zones

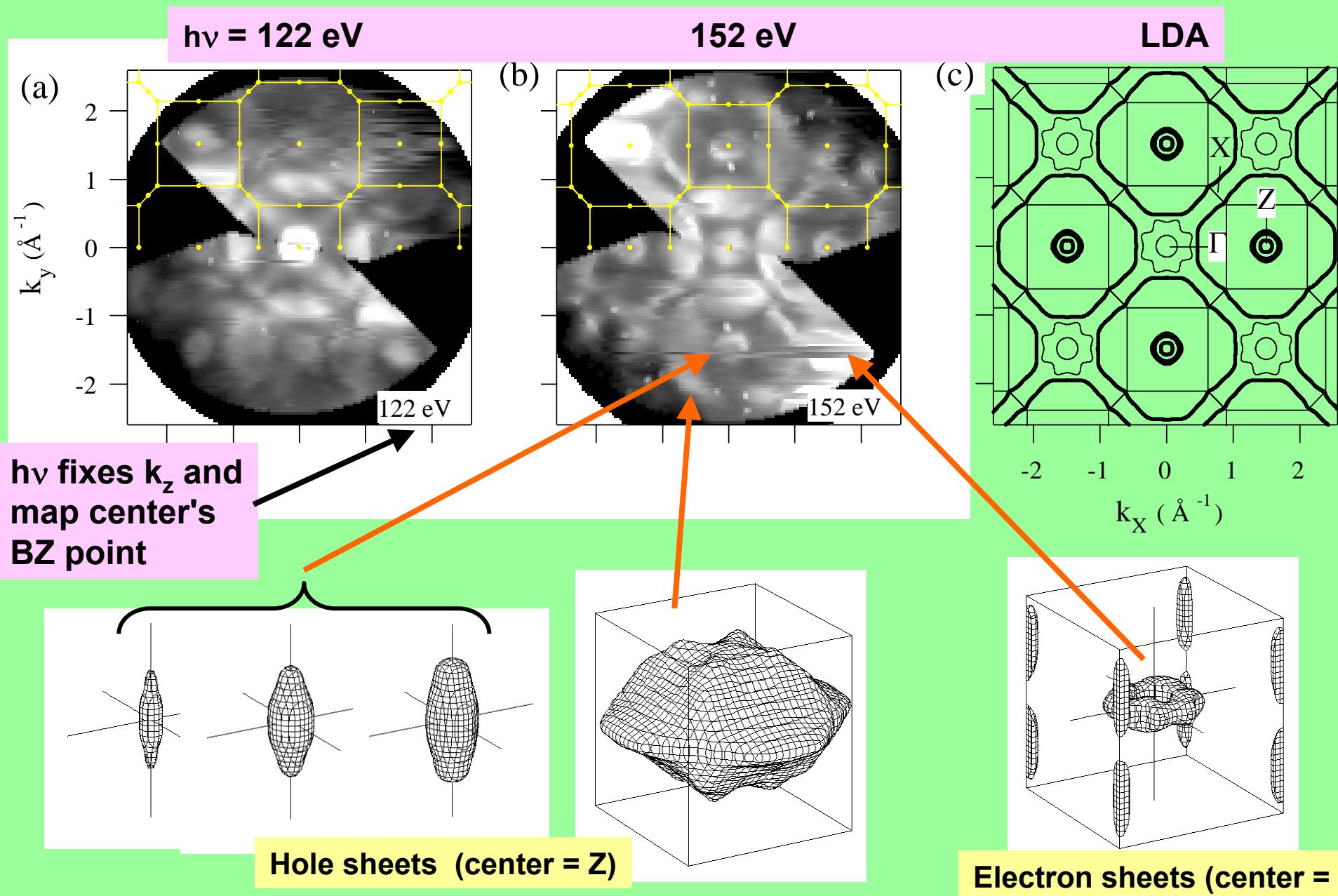


ARPES arcs**



**ARPES arcs slightly changed
in newer work (Denlinger talk)

LaRu_2Si_2 Fermi surface from ARPES J.D. Denlinger (data from ALS)



Fermi volume change at Kondo temperature: the f-electron in CeRu_2Si_2

Luttinger counting theorem \Rightarrow

f-electrons counted in Fermi volume
IF magnetic moments quenched

(as in Kondo effect)

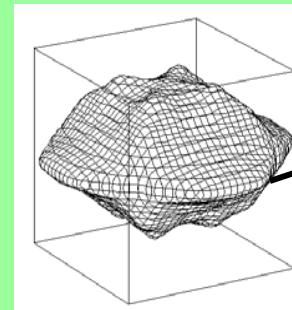
Conjecture (Fulde & Zwicknagl, 1988)

f-electrons excluded from FS above
Kondo temperature T_K

Difficult to test with low-T dHvA.

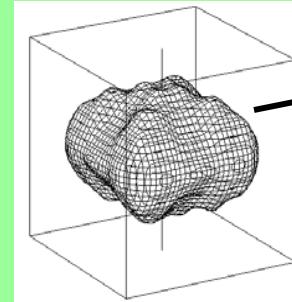
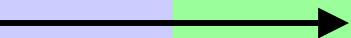
paradigm (dHvA) (Tautz et al, 1995)

- large Z-point hole FS
 $\text{f}^0 \text{ LaRu}_2\text{Si}_2$



LDA
“band 4” hole
Fermi surface
no f-electron

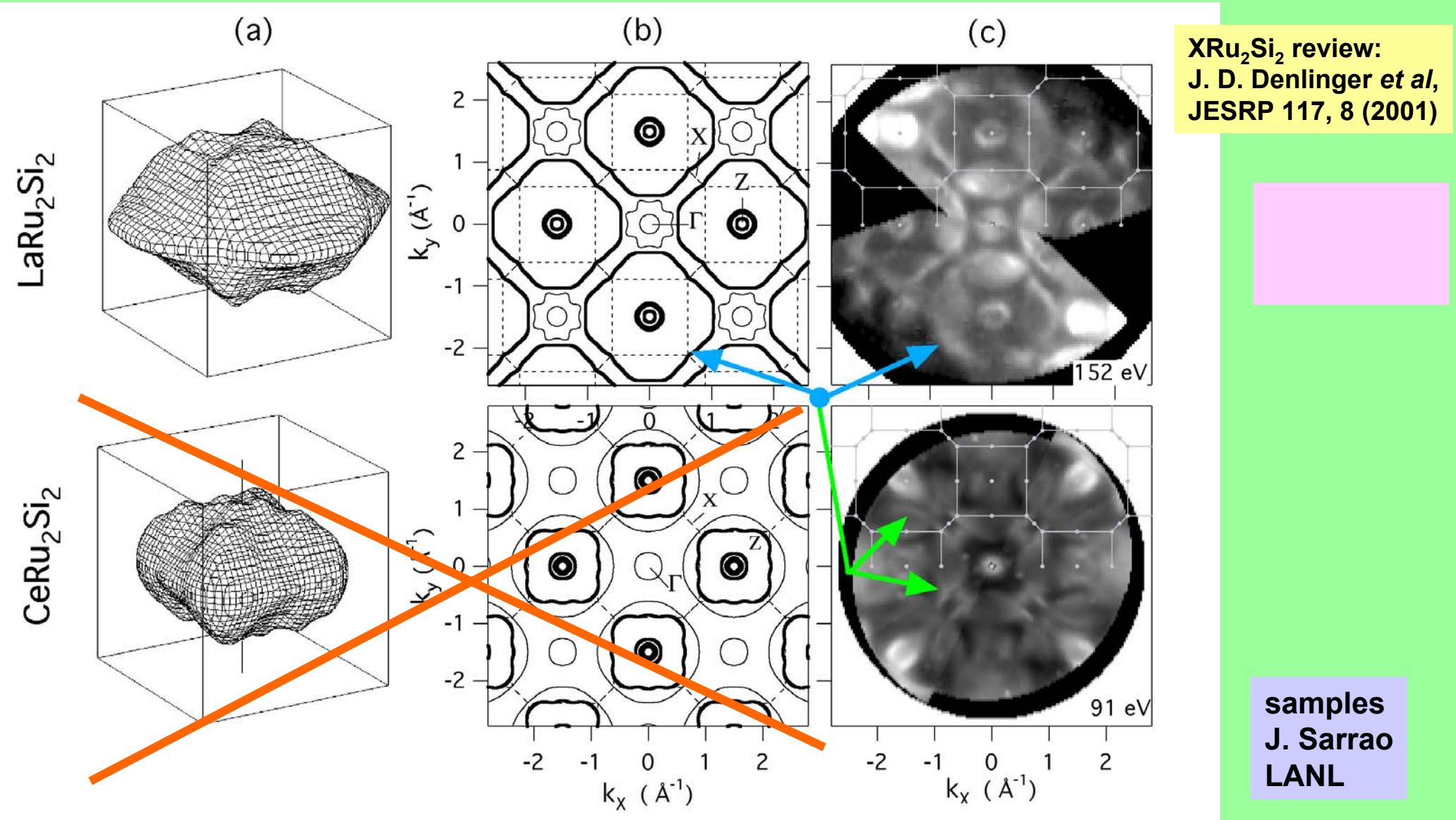
- reduced “pillow” hole FS
counts $\approx \frac{1}{2}$ Ce f-electron
in Kondo CeRu_2Si_2
--at temperature below T_K



$\approx \frac{1}{2}$ extra f-electron
here

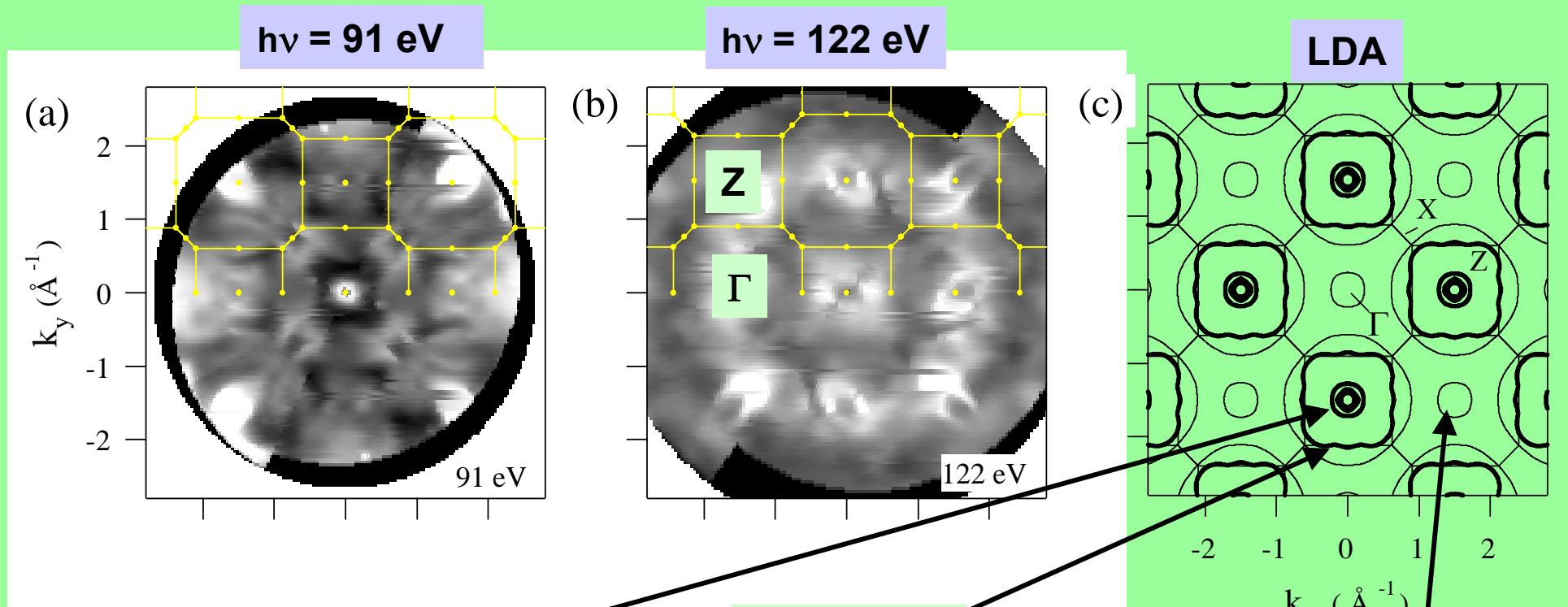
($\approx \frac{1}{2}$ f-electron in other
multiply-connected
complex FS piece)

**Same large hole FS for LaRu₂Si₂ and CeRu₂Si₂ for
T≈ 120K > 6T_K ⇒ f-electrons excluded from FS!**

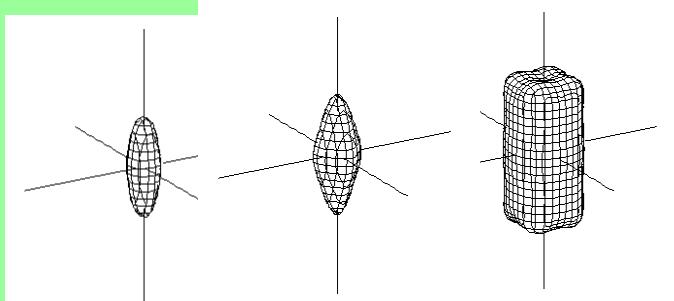


Same conclusion from 2d angular correlation of positron annihilation studies--
(Monge et al, PRB, 2002) but didn't actually measure the "pillow"

Fermi surface at high T — 4f weight at low mass Γ , Z points for CeRu_2Si_2

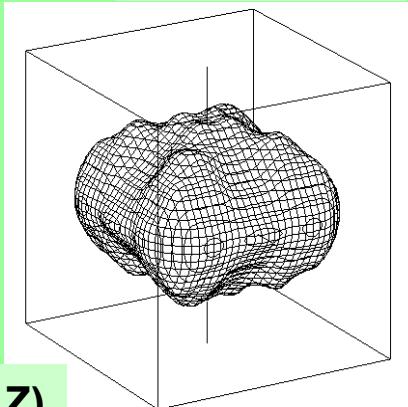


dHvA: $m/m_e = 4, 2.5, 1.6,$



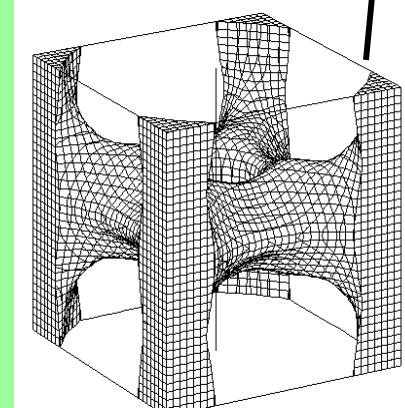
Hole sheets (center = Z)

$m/m_e = 120$

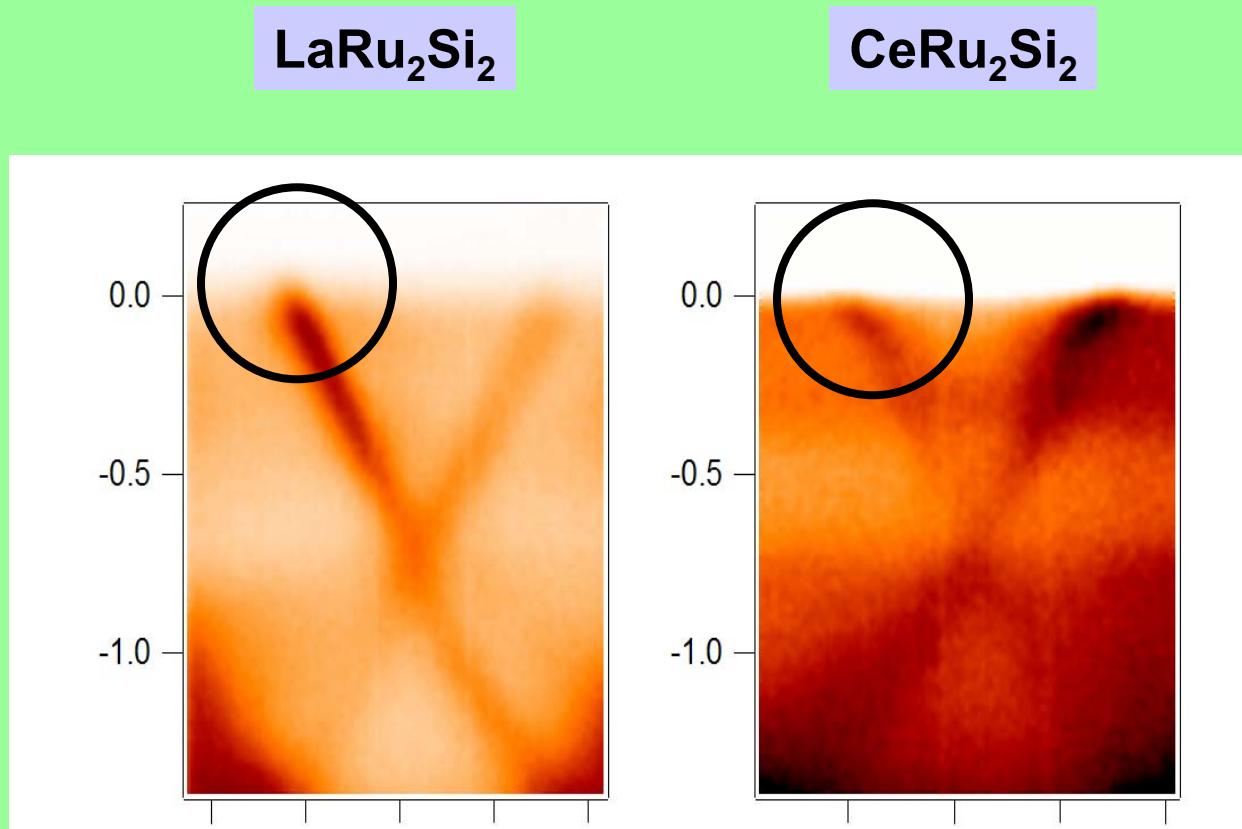


Electron sheets (center = Γ)

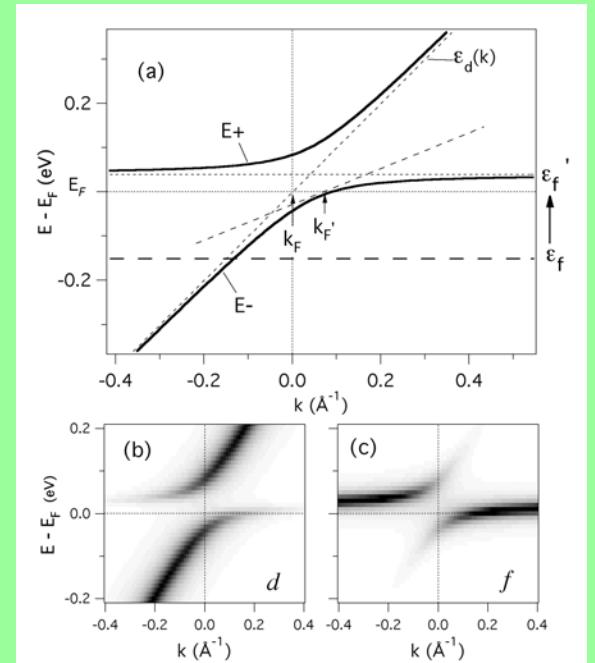
$m/m_e = 13,20$



Butremnant of f-d mixing in high T CeRu_2Si_2

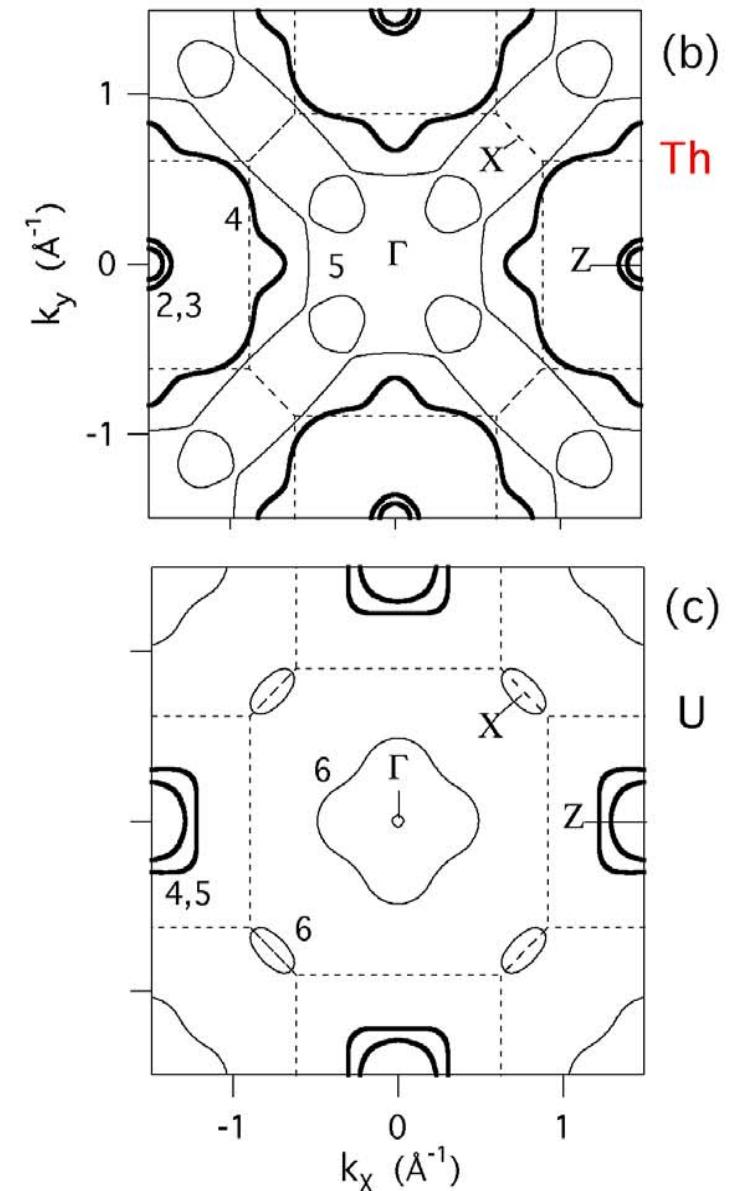
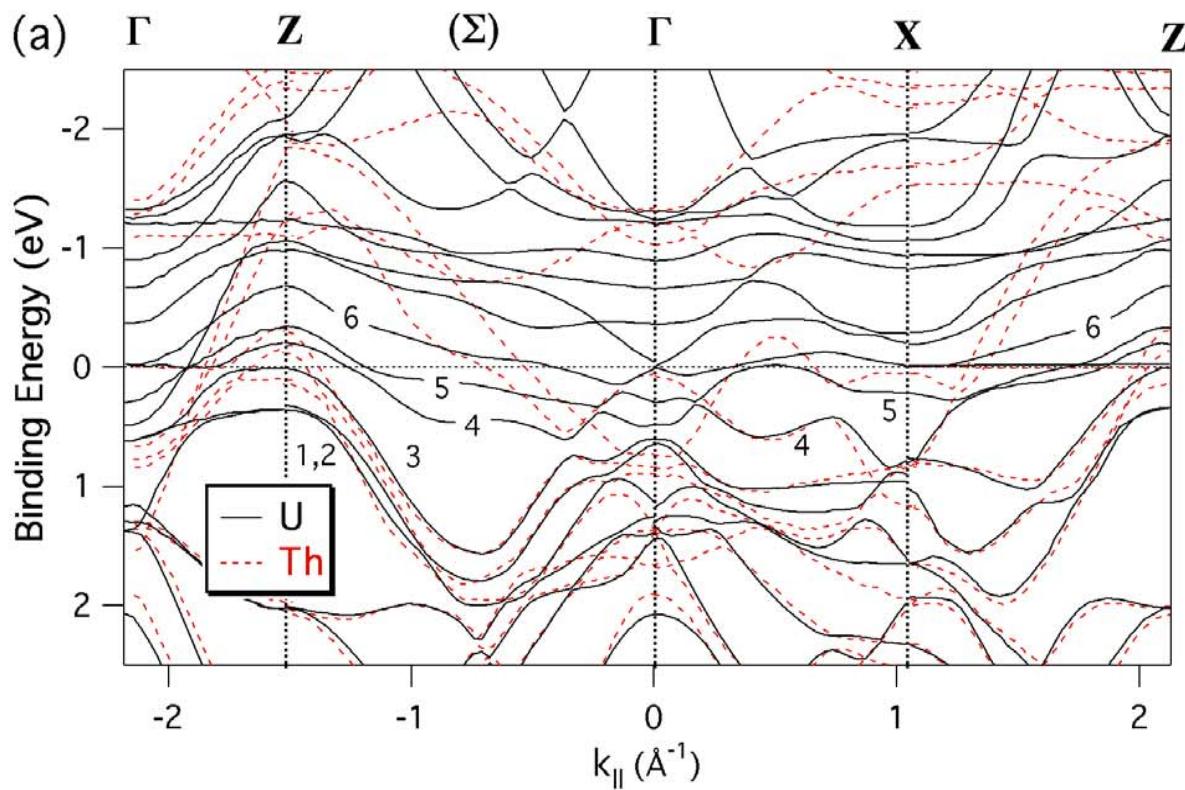


curvature near E_F
for CeRu_2Si_2 (f^1) but not LaRu_2Si_2



f-d mixing in
Anderson
Lattice model

LDA ThRu₂Si₂ vs URu₂Si₂

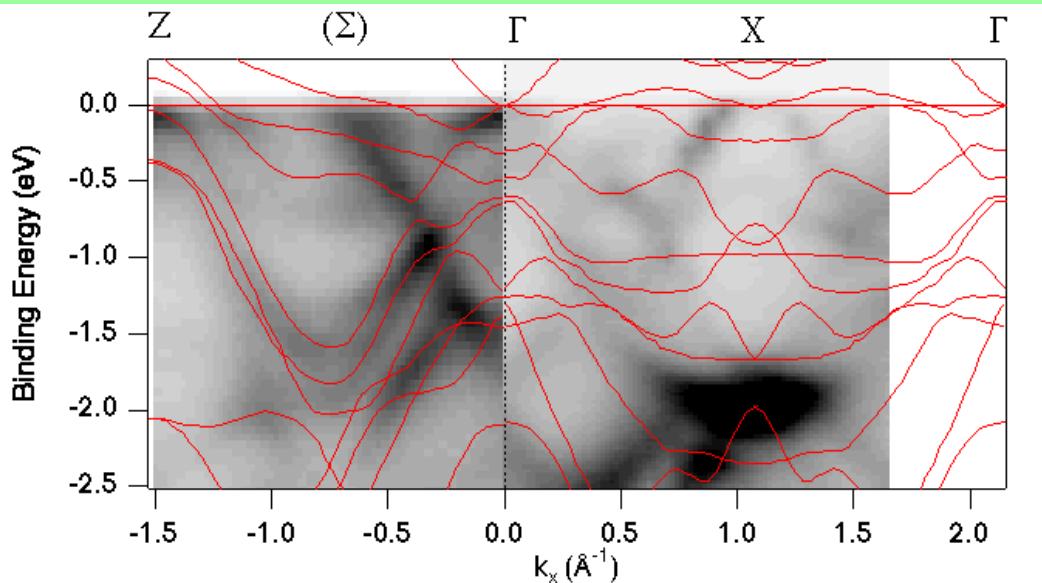


for uranium LDA NOT like Anderson lattice
too many (2.5 to 3) f-electrons

Resonant ARPES of URu₂Si₂

(samples from M. B. Maple, J. Serrao)

Comparison to LDA



LDA with 5f's bad especially near E_F

---better agreement with LDA
calculated for f⁰ compound!

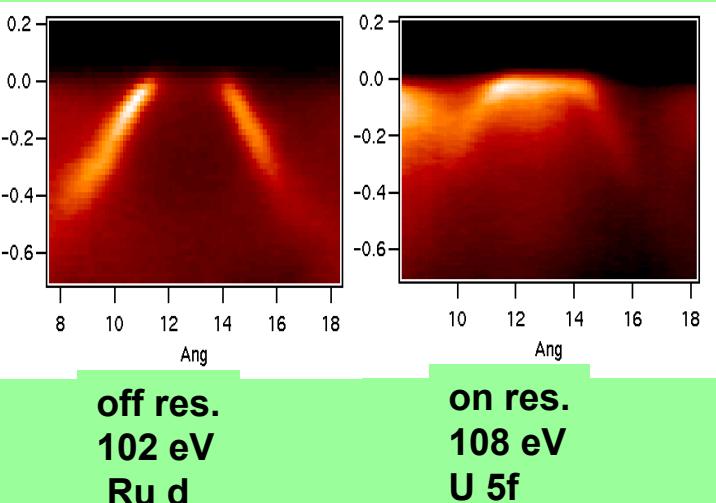
New idea for U 5f's: {f² core + 1}

(Zwicknagl, Fulde)

Idea applied to δ-Pu and PuCoGa₅:

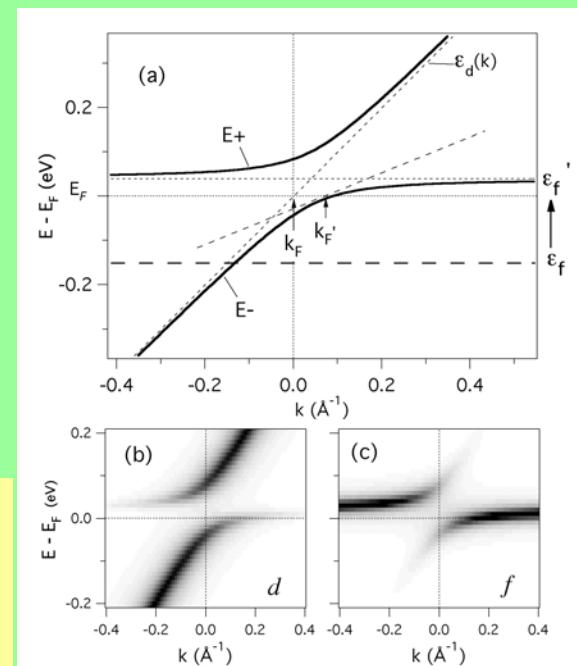
{f⁴ core + 1}

(Wills et al, Joyce et al)



off res.
102 eV
Ru d

on res.
108 eV
U 5f

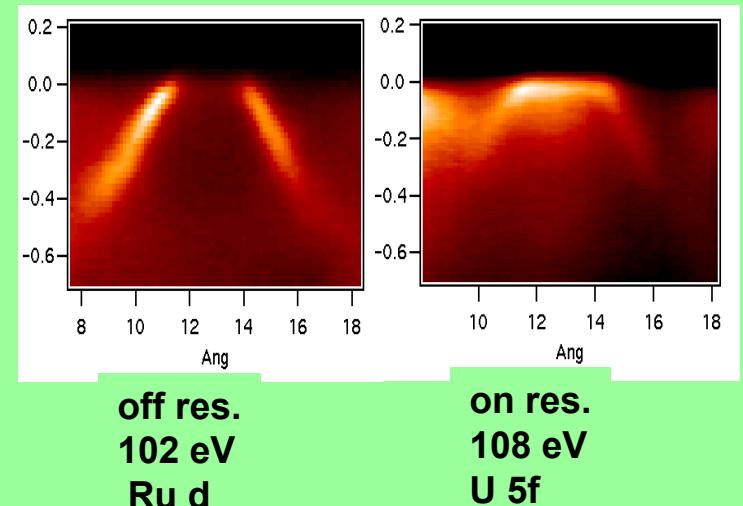
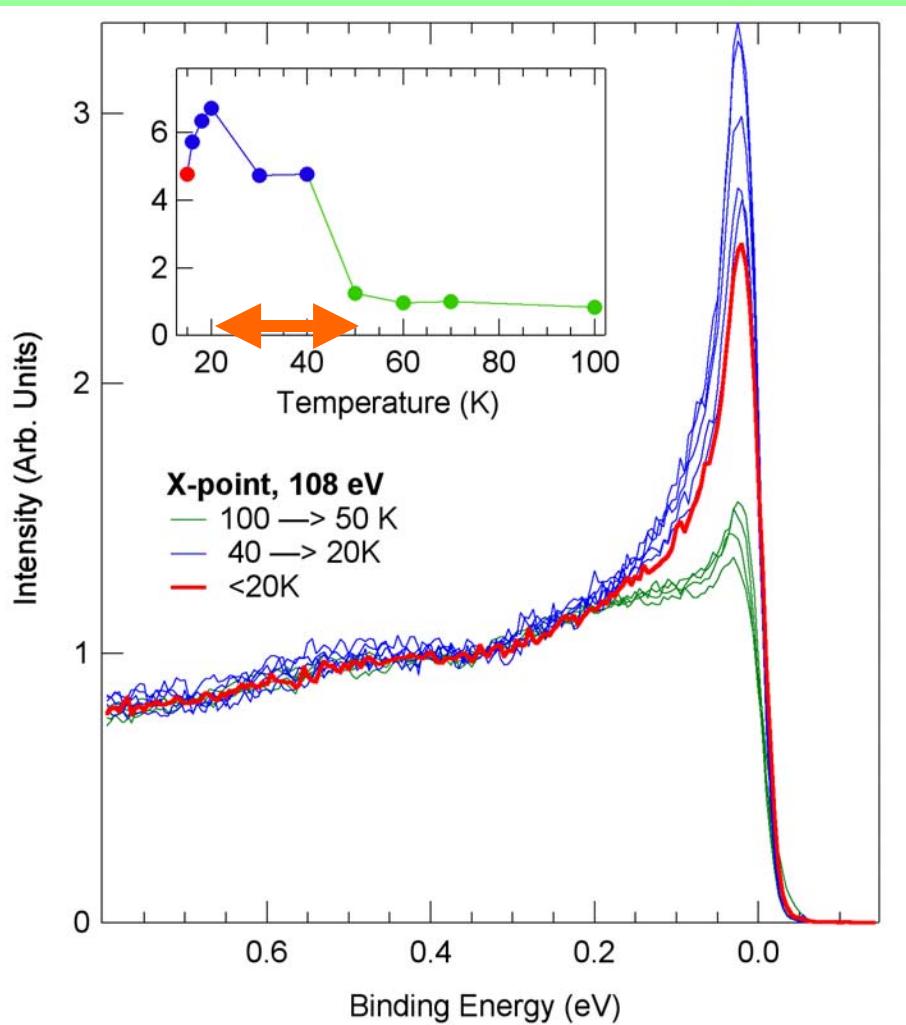


f-weight confined
to d-band hole
pocket

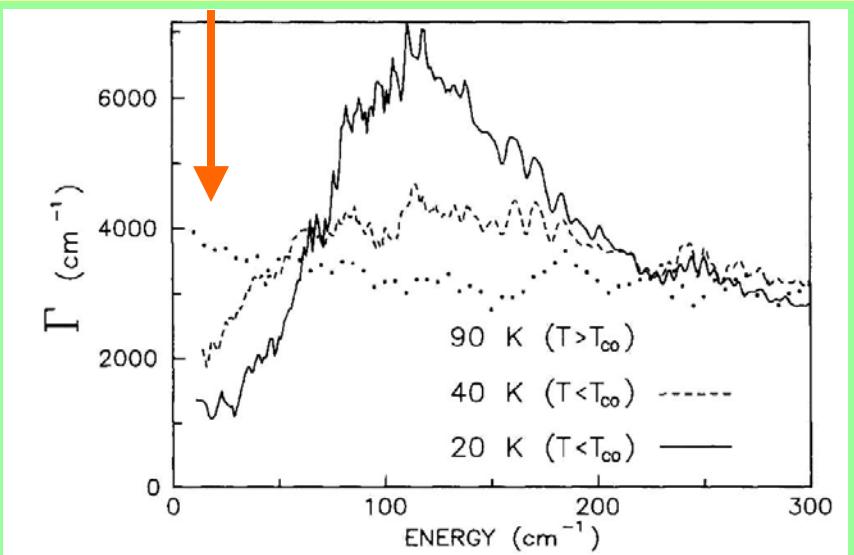
like in renormalized
Anderson lattice
model

URu₂Si₂ X-point f-weight T-dependence

X-point, 108 eV, T = 100 → 15K

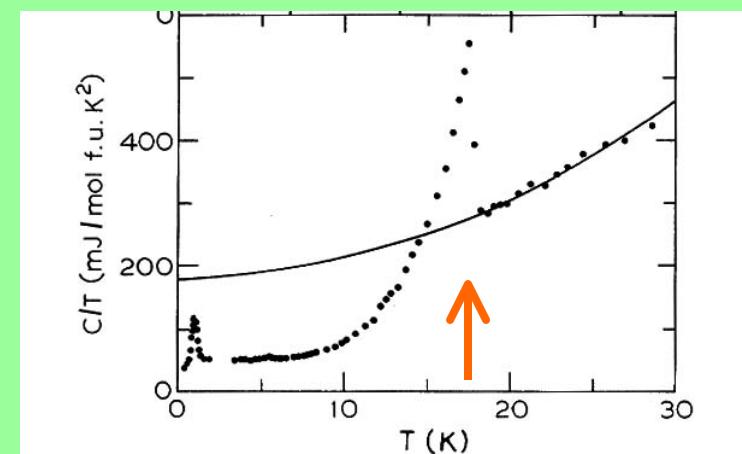
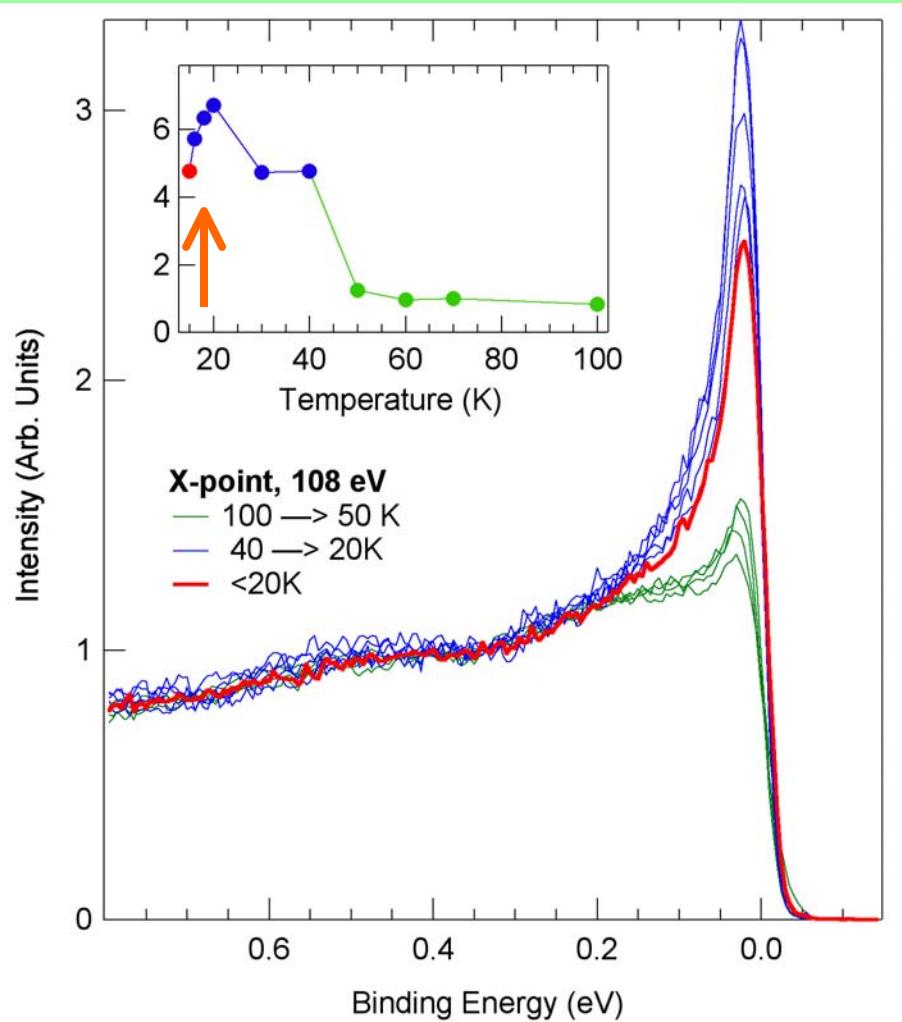


Optical relaxation time shows coherence developing $\leq 40\text{K}$ (Bonn et al PRL '88)



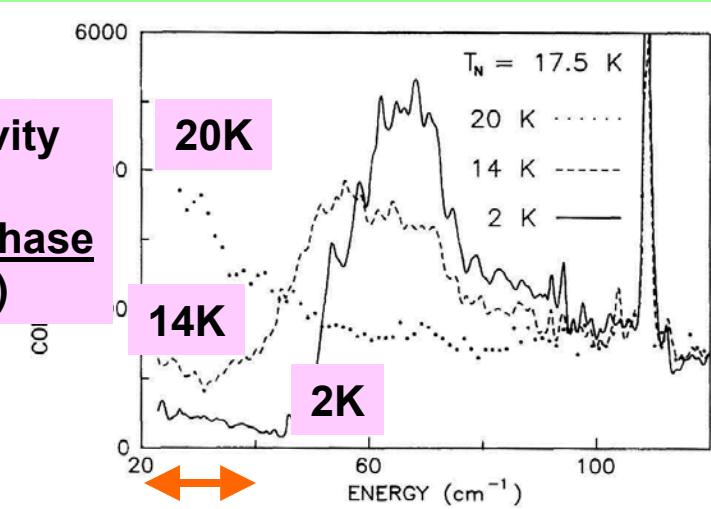
URu_2Si_2 f-weight T-dependence

X-point, 108 eV, $T = 100 \rightarrow 15\text{K}$



Specific heat implies gap opening at 17K
“hidden order” transition (Maple et al '86)

Optical conductivity
shows gap
in “hidden order” phase
(Bonn et al '88)



UGe₂ Phase Diagram and models

PM \rightarrow FM₁ transition at 53K

FM₁ \rightarrow FM₂ at 30K

Superconductivity in FM phase

SC T_{sc} highest at P_x

Coupled CDW-SDW fluctuation model

— S. Watanabe & K. Miyake, *Physica B* 312-313, 115 (2002).

- Phase boundary T_x(P) is related to coupled CDW and SDW formation
- FM Superconductivity

Assumes Fermi Surface Nesting

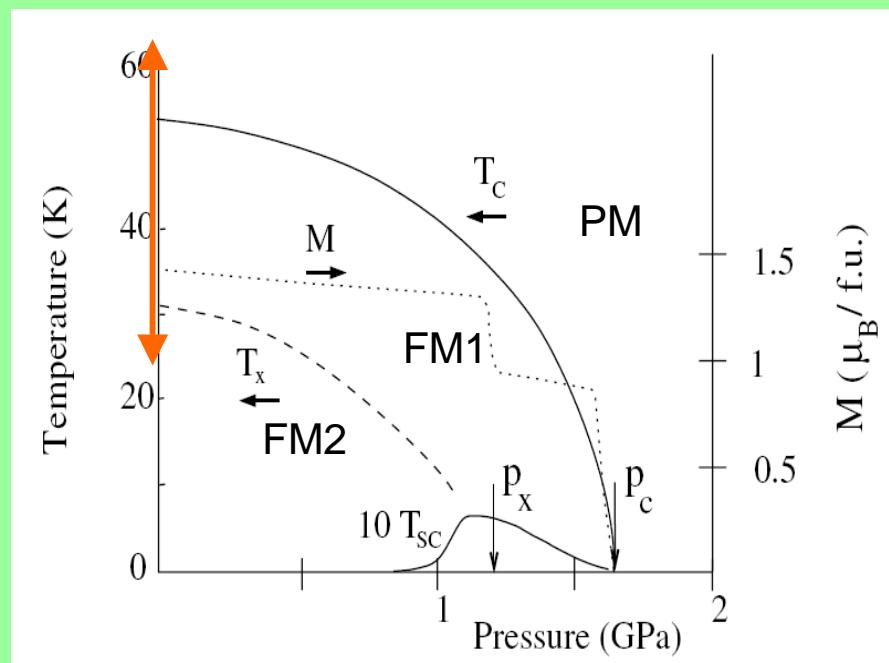
FS topology driven Model

— Sandeman et al., *PRL* 90, 160075 (2003)

- Mean field Stoner treatment
- Quasi 1-D 2-Peak DOS model

Assumes Fermi Surface Nesting

ARPES



Sandeman et al., *PRL* 90, 160075 (2003)

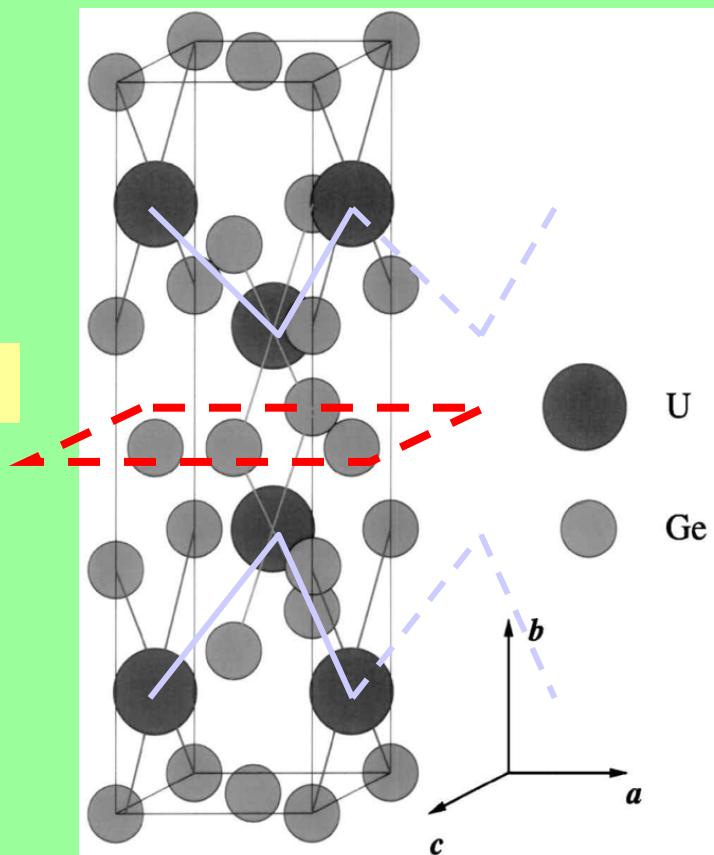
Moderately heavy fermion

$$\gamma = C(T)/T = 35 \text{ mJ/mol K}^2$$

Nature of the 2nd FM phase transition
and how they are related to the
development of SC are still not clear

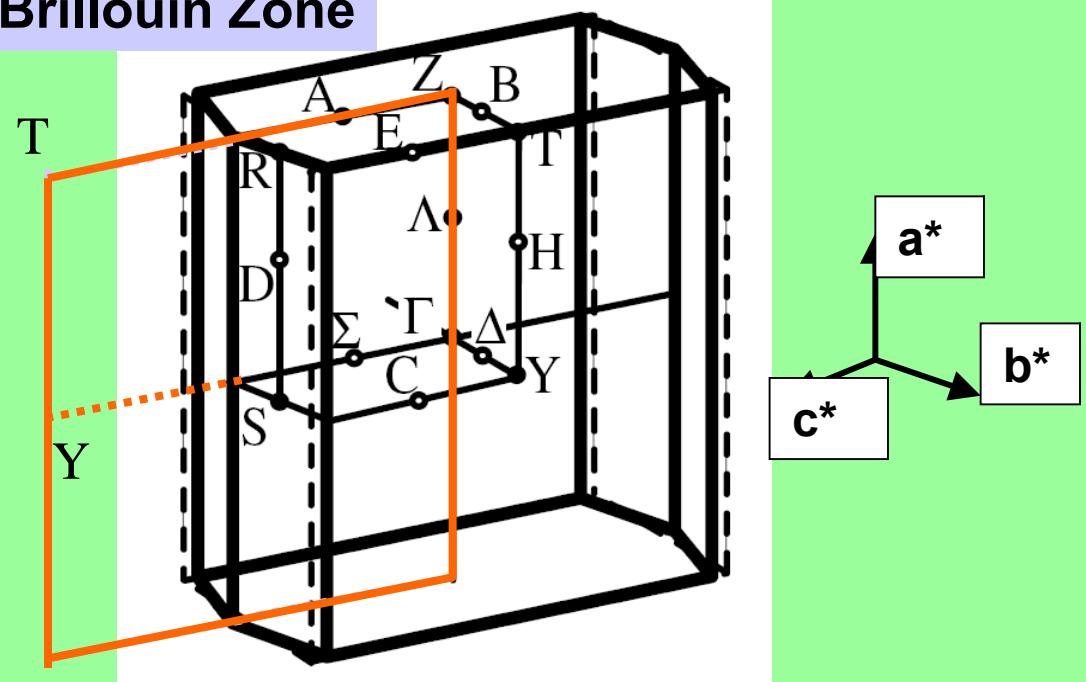
UGe₂ crystal structure and Brillouin zone

Crystal Structure



cleave

Brillouin Zone



Orthorhombic (Cmmm)
— base-centered ($b > a$)

$a = 4.009 \text{ \AA}$ -- Magnetic Easy axis

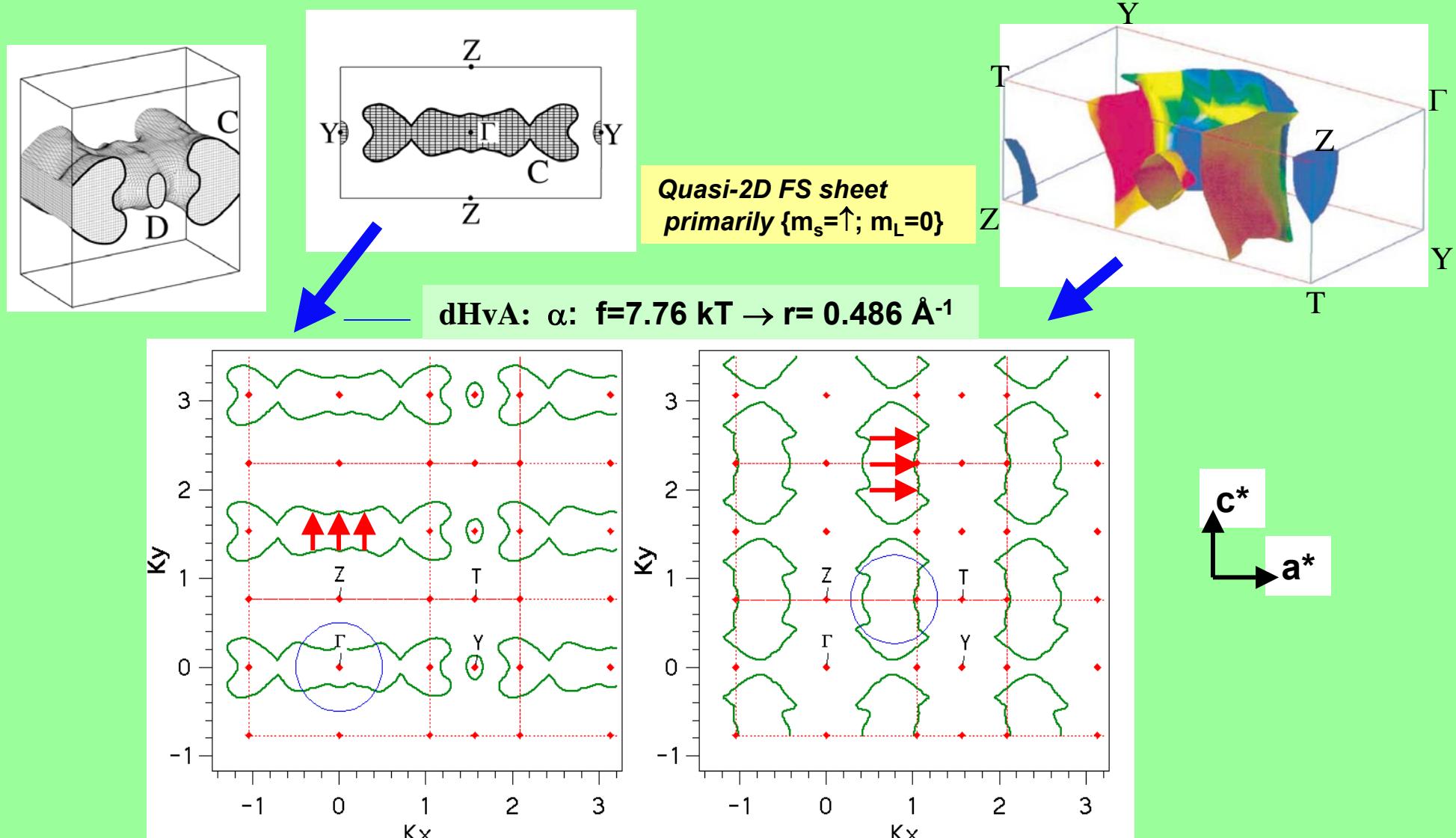
$b = 15.089 \text{ \AA}$

$c = 4.095 \text{ \AA}$

(Oikiwa, et al JPSJ 65, 3229 (1996))

Czochralski grown single crystal
— cleaved in-vacuum at $T < 100\text{K}$
— cleaving surface normal to b

UGe₂ Fermi Surface --- LDA vs. LDA+U



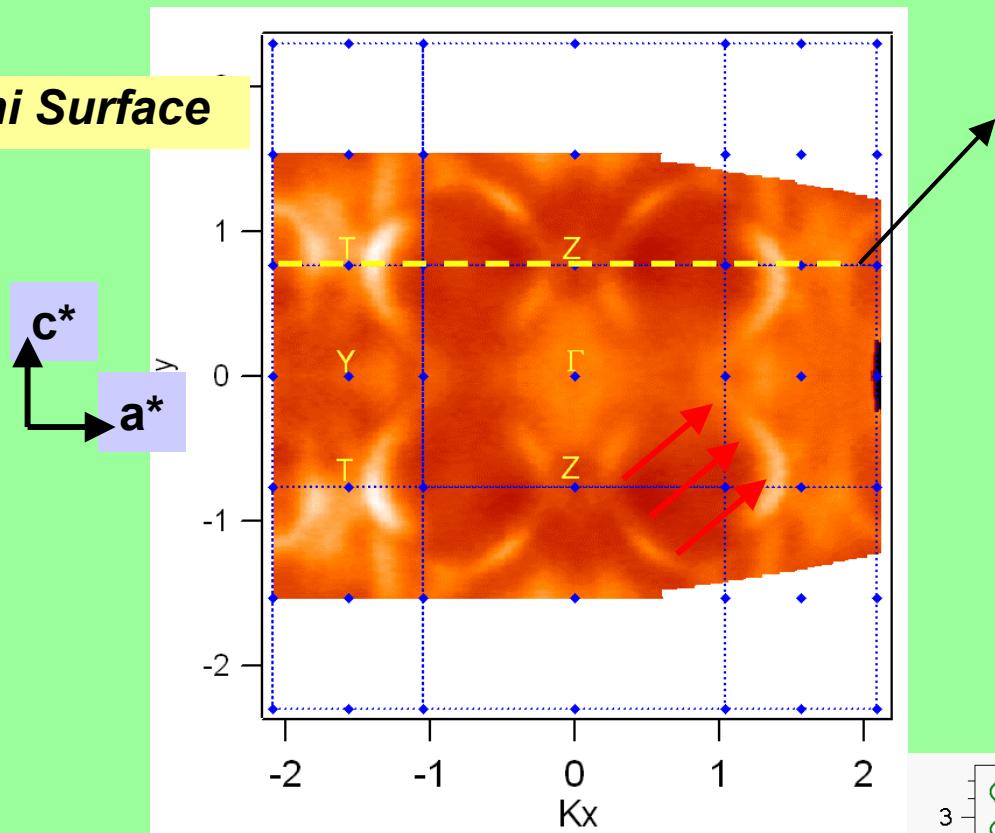
PM-LDA: R. Settai, et al., J. Phys.: Condens. Matter 14, L29 (2002)

LDA+U: A. B. Shick & W. Pickett, Phys. Rev. Lett. 86, 300 (2001).

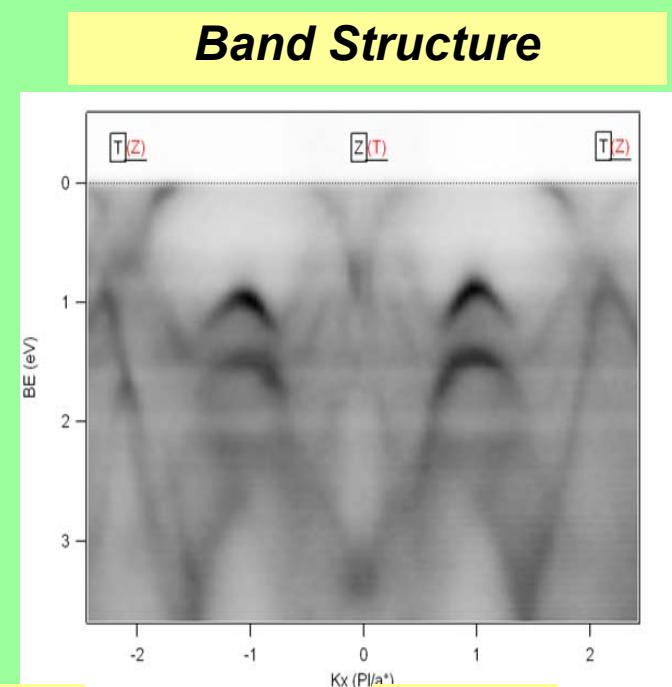
Experimental Fermi Surface and Band Structure

$h\nu = 92 \text{ eV}$ and $T = 30\text{K}$

Fermi Surface

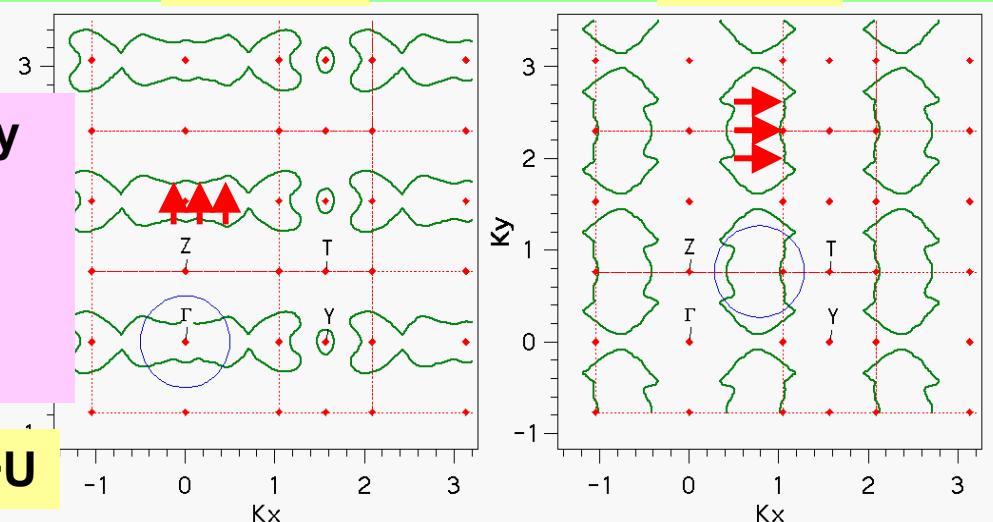


Band Structure



PM-LDA

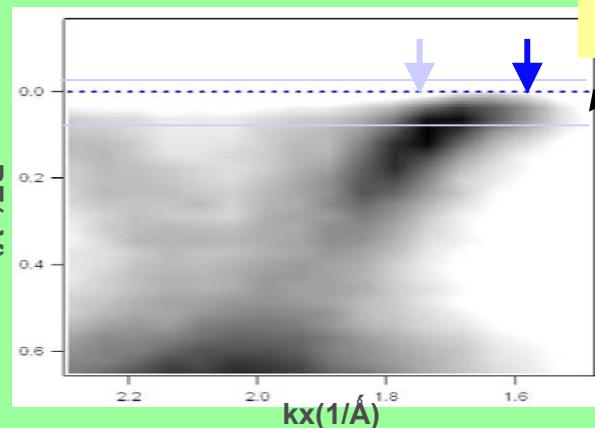
LDA+U



- Large FS observed in multiple BZs, defined by non-f band dispersion
- Diamond shape FS simpler than calculations
- FS more connected in one direction than the other
- Diagonal FS nesting, different from LDA/LDA+U

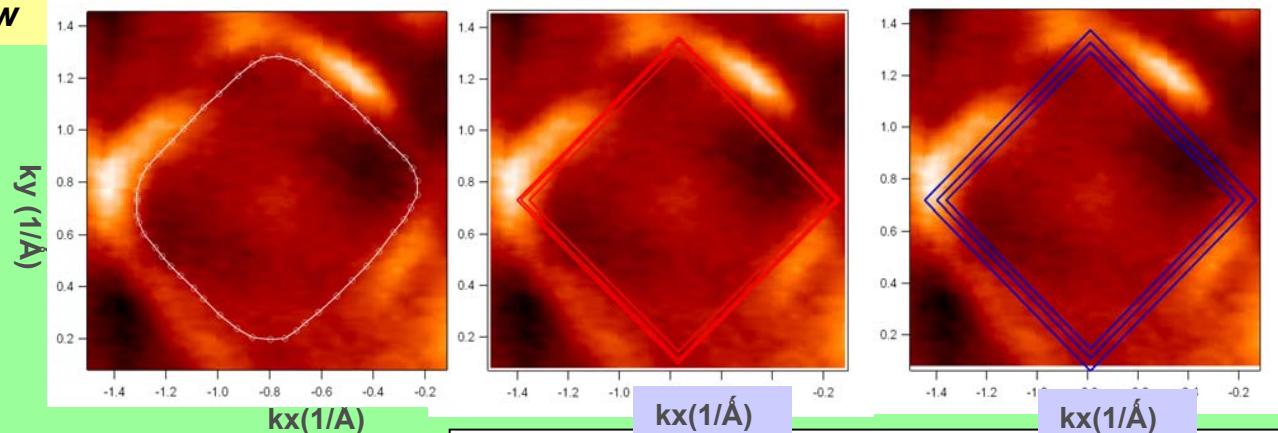
Fermi Surface and Band Structure Details

BS details



Integration
window

FS details, $h\nu = 92\text{eV}, T = 30\text{K}$



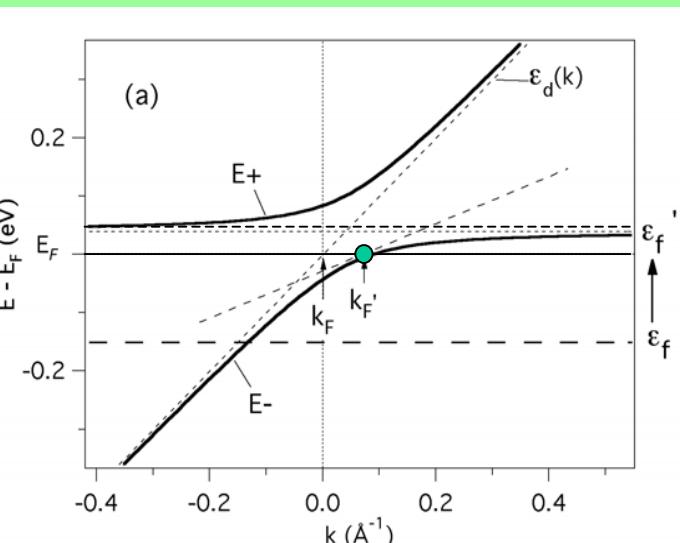
— dHvA PM
— dHvA FM

R. Settai, et al., J. Phys.:
Condens. Matter 14, L29 (2002)

- Band curvature: f-p/f-d hybridization in the Anderson Lattice Model

- Broadened FS feature due to integration

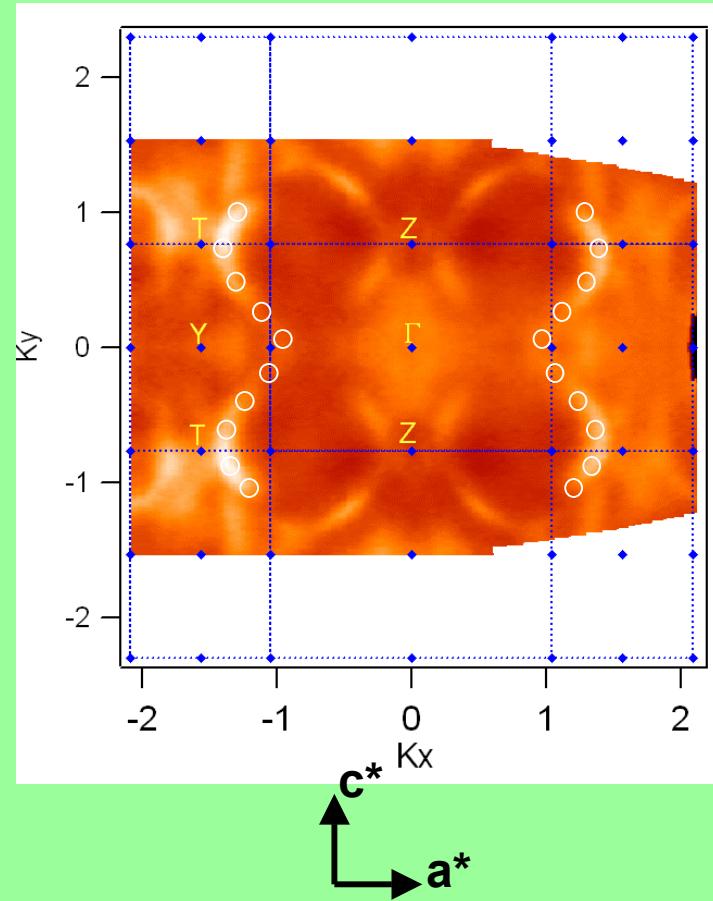
- FS size agrees with dHvA



Anderson lattice Model

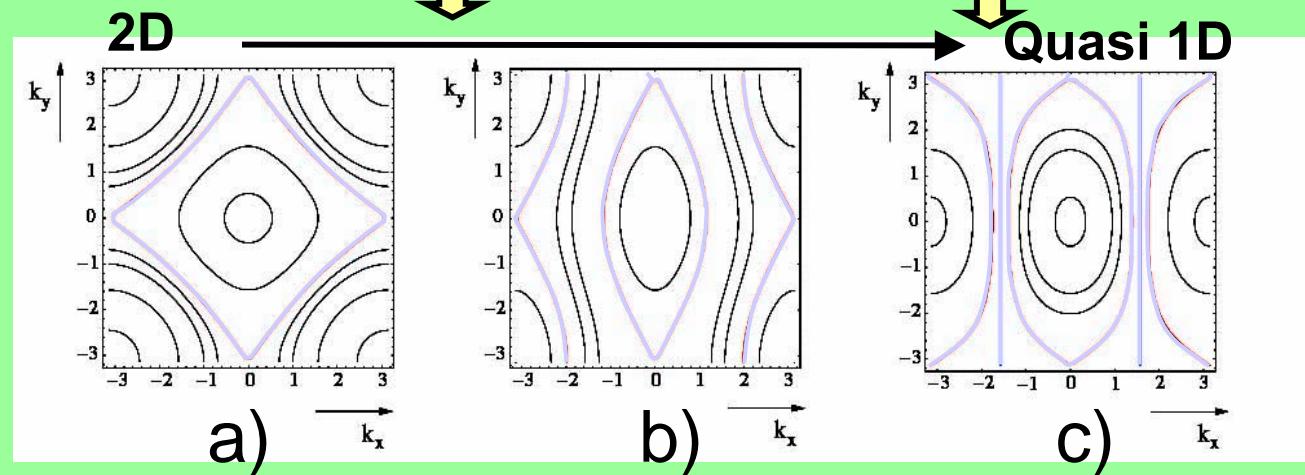
FS topology – compare to quasi 1-D model

Subtle connectivity in one direction (c^*), but not the other
→ quasi 1-D signature?



Our FS topology

FM-SC and both phase transitions reproduced

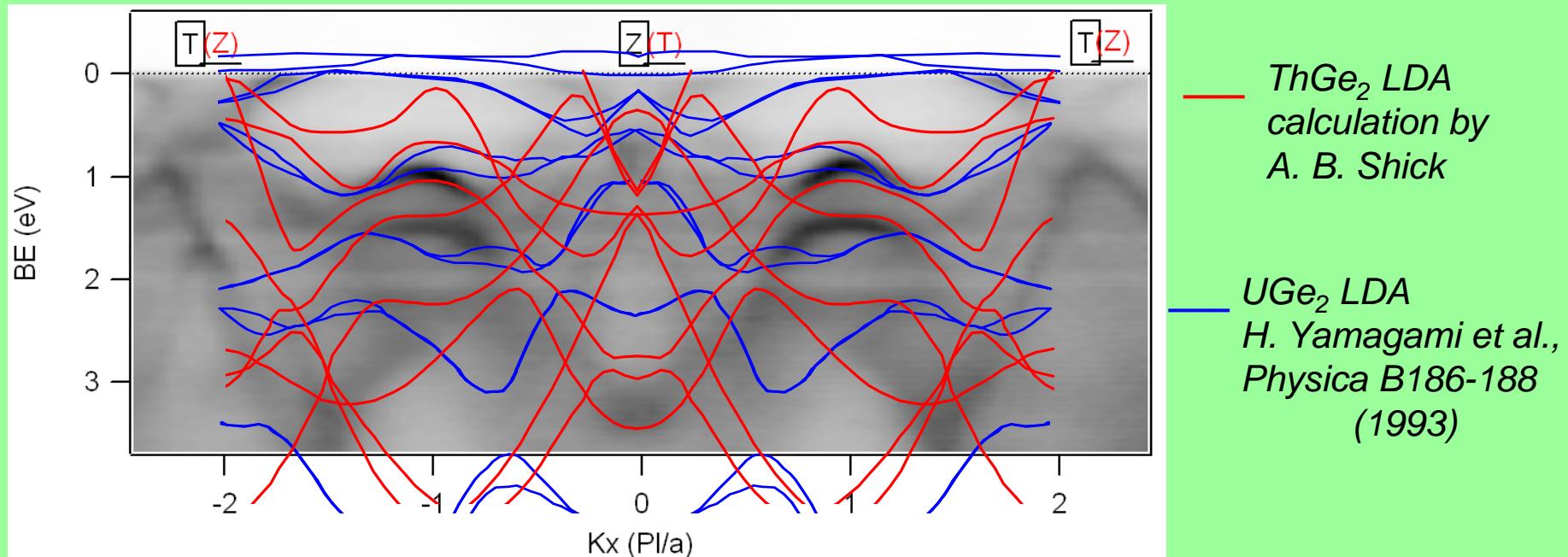


K. G. Sandeman, et al.
cond-mat/0210552 (2002)

- FS topology driven Model
 - Mean field Stoner treatment
 - Quasi 1-D 2-Peak DOS model
 - Lead to SC in FM and the 2nd FM phase transition

ARPES spectra: compare with LDA

Photon energy 92 eV T=300K



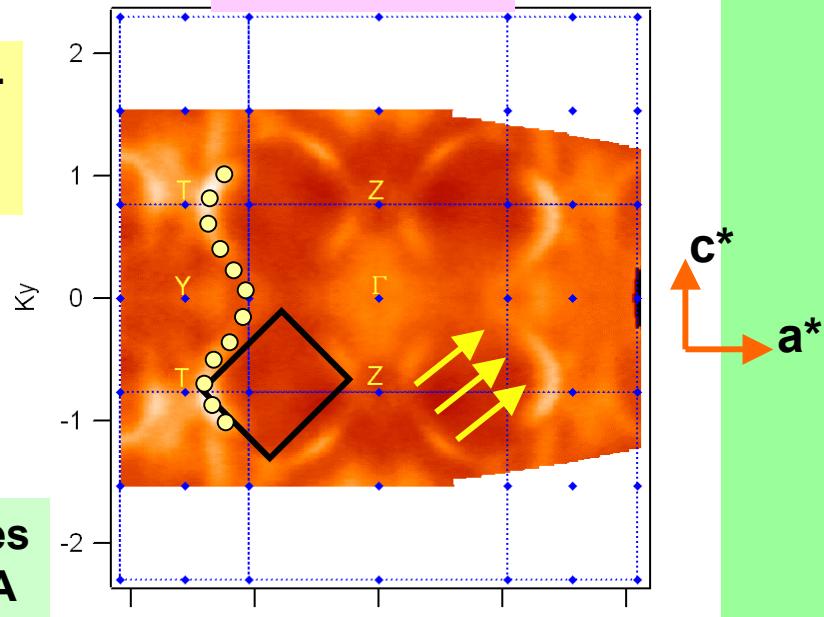
better agreement with f^0 bands
(will try f^2 core plus 1)

Samples:
A. D. Huxley
J. Flouquet

Fermi Surface – Experiment vs. Calculation--Summary

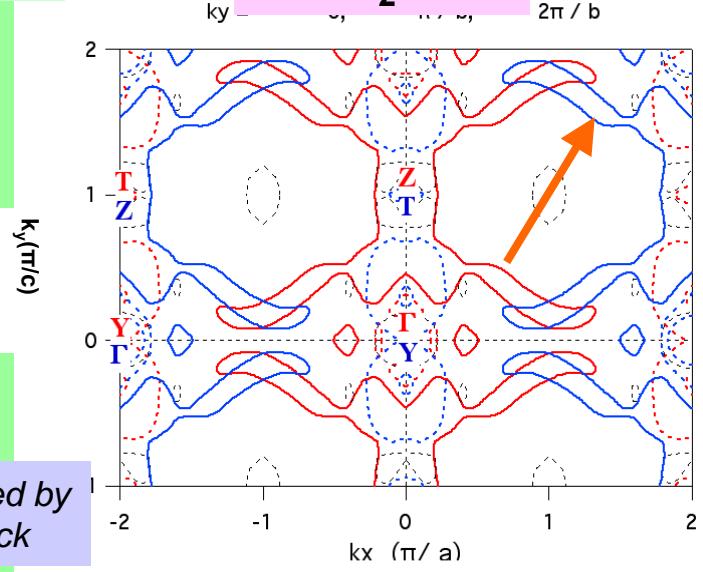
Quasi-
1d
hint

Experiment



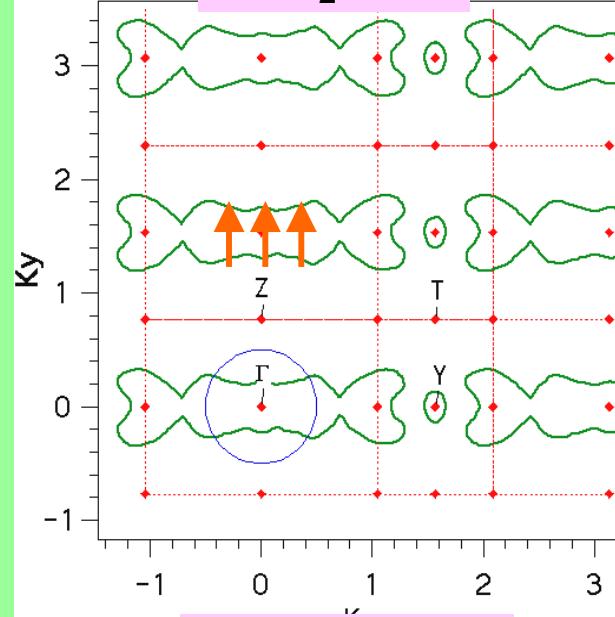
matches
a dHvA
orbit
area

ThGe_2 LDA



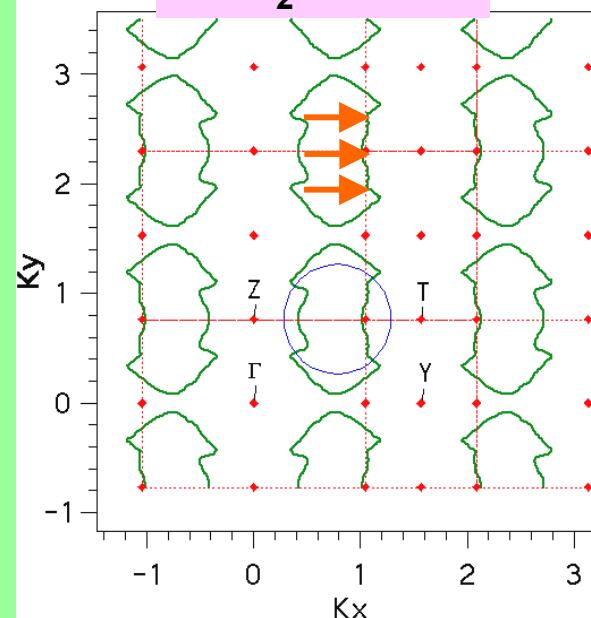
Calculated by
A. B. Shick

UGe_2 LDA



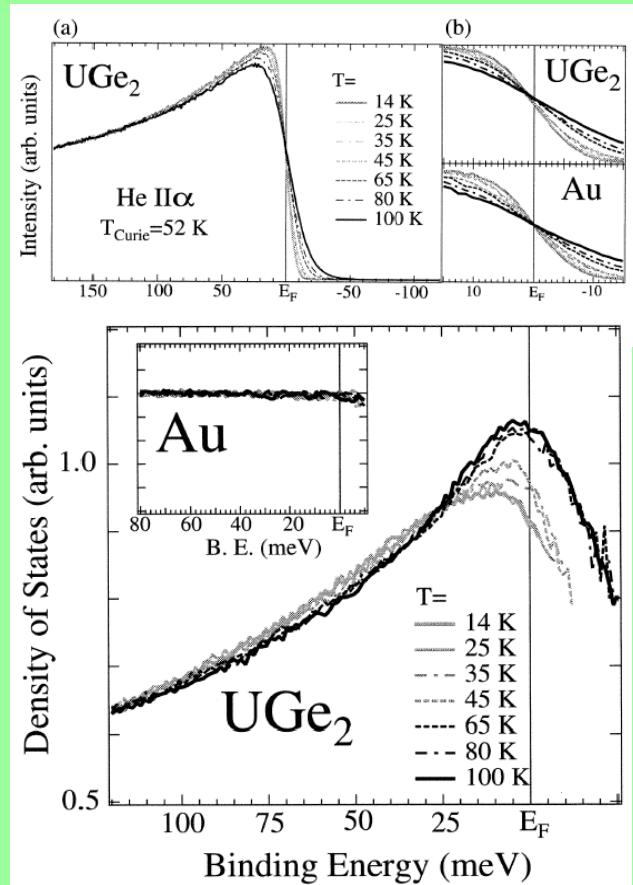
R. Settai, et al.,
J. Phys.: Cond. Matt. **14**,
L29 (2002)

UGe_2 LDA+U

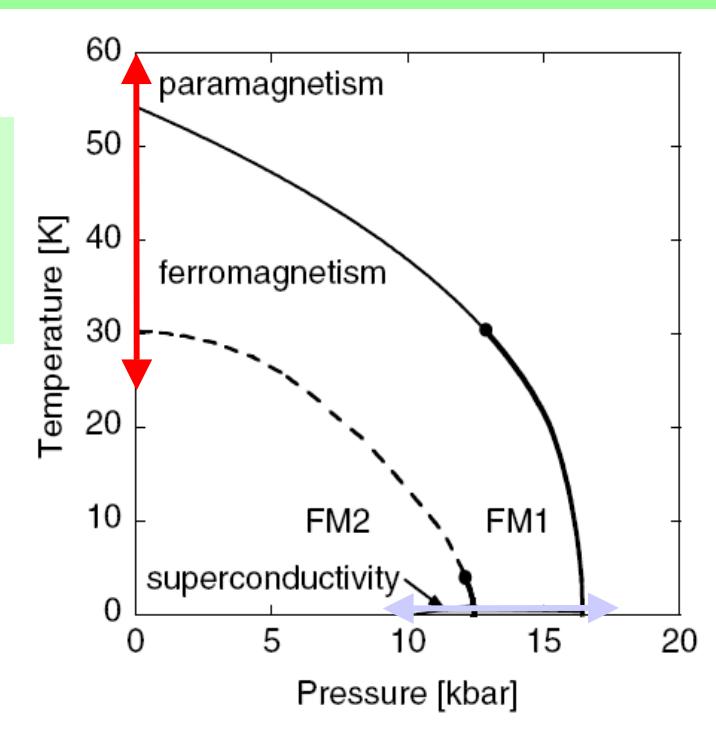


A. B. Shick & W. Pickett,
Phys. Rev. Lett. **86**, 300
(2001).

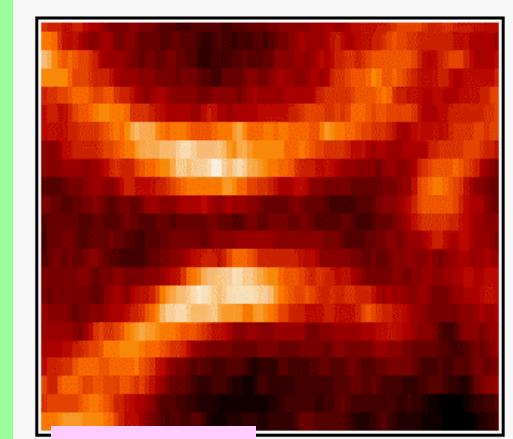
FM \leftrightarrow PM Transition



ARPES



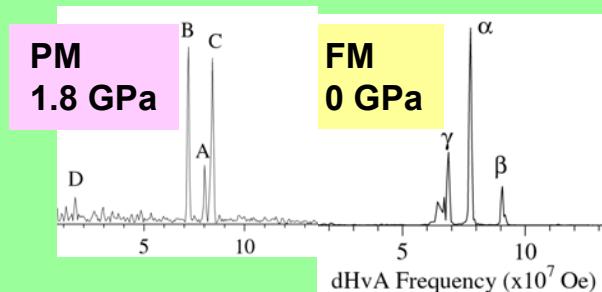
T=70K



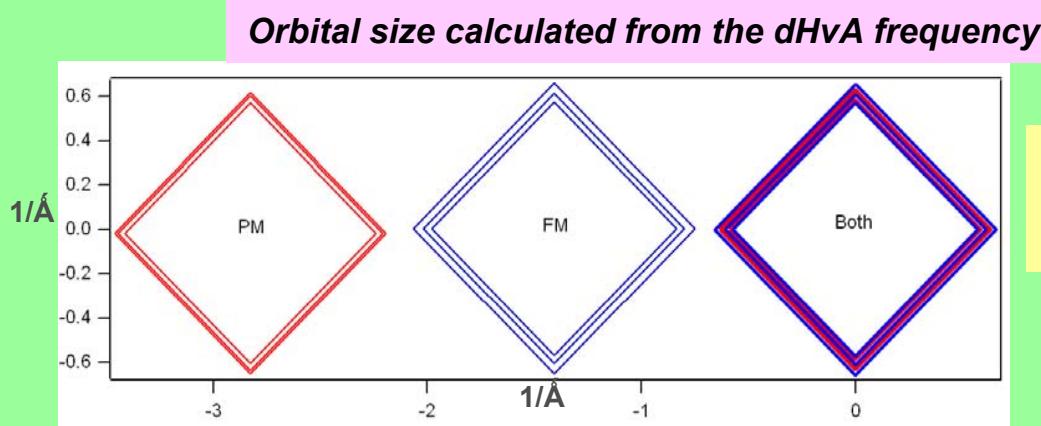
T=20K

Takahiro, et al. JPSJ 71, Suppl. 261 (2002)

FM-PM transition dHvA measured FS size change small



R. Settai, et al., J. Phys.:
Condens. Matter 14, L29 (2002)



$$A = 0.0955 * f [kT] \\ = [\text{\AA}^{-2}], \\ r = \sqrt{A/\pi} [\text{\AA}^{-1}]$$

Summary

- Anderson impurity ansatz in Ce systems
good for angle integrated spectra
- Kondo effects and Luttinger in CeRu_2Si_2 high and low T
need theory for k-dependence e.g. issue of f-weight
- LDA much like Anderson lattice for cerium—only f^1
- Uranium compounds: e.g. URu_2Si_2 , UGe_2
LDA f-bands bad, distort non-f bands and FS
too many f-electrons
LDA for f^0 gives better description of non-f bands
idea of core $f^2 + 1$
- Anderson lattice f-weight confined to hole pockets
- T-dependent f-weight in URu_2Si_2
- UGe_2
FS consistent with LDA, little change in FM transition
diagonal nesting, not like LDA or LDA + U
not enough low d character for 1d model