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# DENSITY FUNCTIONAL APPROACH TO THE ELECTRONIC STRUCTURE OF DOPED CUPRATES

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### 1. INTRODUCTION

Temperature vs. doping phase diagram of doped cuprates:



At T = 0:

sequence: AF insulator  $\longrightarrow x \approx 0.05 \longrightarrow$  spin glass  $\longrightarrow x \approx 0.16 \longrightarrow$  Fermi liquid

Questions:

How well can a Hubbard U on copper sites describe the sequence of ground states?

How does U depend on doping?

How do the magnetic interactions behave?

### 2. THE MODEL SYSTEM

 $Ca_{1-x}K_xCuO_2$  as the simplest model structure:



## 3. THE COMPUTATIONAL SCHEME

LSDA+U - CPA approach using our FPLO code

total energy calculations of constrained spin structures

CPA Bloch spectral densities (band structure) understanding the Kohn-Sham potential as an approximation to the electron-electron self-energy

Spin structures:

AFM: antiferromagnetic structure with alternating copper spins in all directions

FM: ferromagnetic order of copper spins

DLM: disordered local moments on copper sites, treated in CPA

NSP: non-magnetic state (equal occupation of spin up and down Cu states)

Oxygen spin polarization:

AFM: for symmetry reasons no polarization

FM: always ferrimagnetic polarization obtained

DLM: single-site CPA treatment does not allow for polarization

NSP: no polarization as constraint

### 4. **RESULTS**

4.1 Total Energy Differences (per 2 Cu atoms):



For x = 0, the energy difference between the AFM and the FM states well corresponds to the experimental nearest neighbor Cu-Cu exchange constant: it yields  $J \approx -100$  meV.

#### 4.2 Site Occupation:



In the spin polarized cases, the doped holes nearly exclusively go to the oxygen sites.



The anti-alignment of the oxygen spins with the copper spins speaks of a very strong AFM Cu-O exchange constant  $J_x$  (by far larger than J) which provides an effective FM Cu-Cu exchange proportional to x.

#### 4.3 Bloch Spectral Functions for x = 0:



CaCuO<sub>2</sub> AMF, U=8 eV J=0 eV









#### 4.3 Bloch Spectral Functions for x = 0.2:



 $CaCuO_2 AMF$ , U=8 eV J=0 eV







 $CaCuO_2 AMF$ , U=8 eV J=0 eV

DLM c=0.2, E<sub>tot</sub>=-4930.72850661



 $CaCuO_2 AMF$ , U=8 eV J=0 eV

AFM c=0.2, E<sub>tot</sub>=-4930.72611510



 $CaCuO_2 AMF$ , U=8 eV J=0 eV

NM c=0.2, E<sub>tot</sub>=-4930.65165805



Total Energy Differences (per 2 Cu atoms):



ARPES band structure of optimally doped  $Bi_2SrCa_2Cu_2O_{7+\delta}$ :



 $CaCuO_2 AMF$ , U=0 eV J=0 eV

NM c=0.2, E<sub>tot</sub>=-4930.63562753





## 5. CONCLUSIONS

- The AFM ground state of undoped cuprates and its magnetic nearest neighbor Cu-Cu spin coupling with an exchange constant  $J \approx -100$  meV are well described by the LSDA+U approach of density functional theory with U = 8 eV and J = 0 which keeps the exchange energy in the LSDA functional.
- The Bloch spectral function well resembles ARPES results for  $Sr_2CuO_2Cl_2$  in this case.
- Doped additional holes go predominantly to oxygen sites and develop a strong antiparallel coupling of their spin to the Cu spin with a Cu-O exchange coupling constant  $J_x$  much larger than J in magnitude.
- At a hole doping concentration of  $x \approx 0.07$ , the transition into a spin glass ground state is obtained, mainly caused by a strong effective FM Cu-Cu exchange coupling introduced by the O-holes.

- For U = 8 eV, a transition into a FM ground state is obtained at a hole concentration  $x \approx 0.11$ . The treatment of a superconducting ground state is beyond the applied density functional approach.
- For U = 8 eV and x = 0.2, a FM ground state is obtained, which together with its Bloch spectral function is in stark contradiction with experimental findings.
- For U = 0 and x = 0.2, the non spin polarized ground state is obtained with a Bloch spectral function in close resemblance of the ARPES results for Bi<sub>2</sub>SrCa<sub>2</sub>Cu<sub>2</sub>O<sub>7+ $\delta$ </sub>.
- In this case, the states at the Fermi level are very weakly scattered by the disorder potential in the spacer layer.

- Rather a switching behavior of U from about 8 eV to zero at a localization-delocalization transition of the nominal Cu holes between x = 0.1 and x = 0.2 is indicated instead of a gradual decrease of U.
- $\bullet$  Unfortunately, total energies for different  $U\mbox{-}values$  seem not to be comparable.

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