



Quasiparticle vanishing driven by geometrical frustration

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Outline

➡ Introduction: Hole dynamics in antiferromagnets

How does the frustration affect the hole dynamics?

➡ Model and methods

➡ Hole spectral functions: quasiparticle and string excitations

➡ Quasiparticle wave function

➡ Conclusions

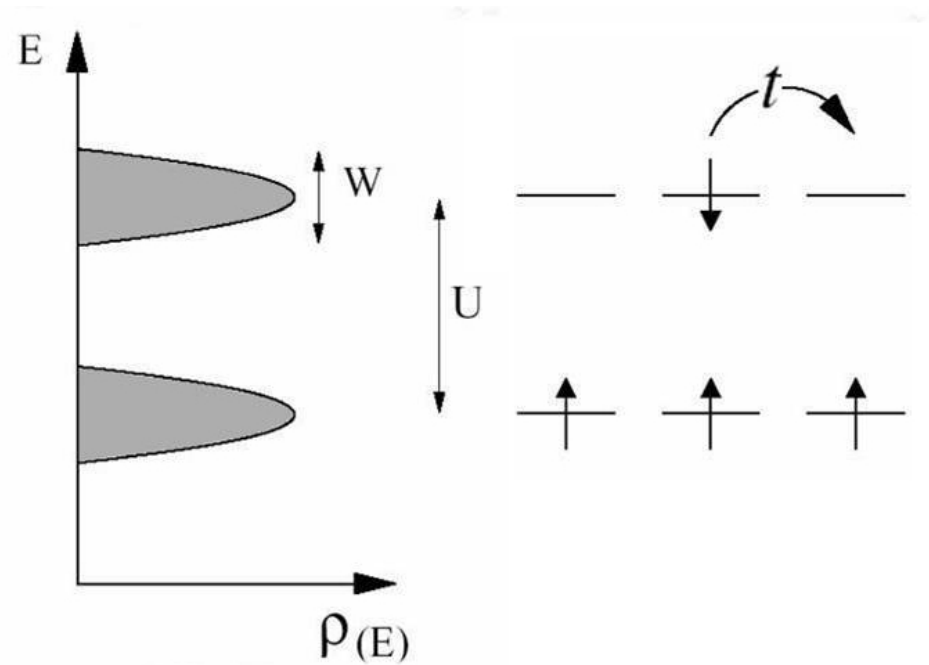
Mott insulators

Strong electronic correlation $W < U$



Mott insulating state

metal-transition oxides →
d orbitals $W \sim U \sim 2 \text{ eV}$



Hubbard model

$$H = \sum_{ij\sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

Low energy physics of a Mott insulator

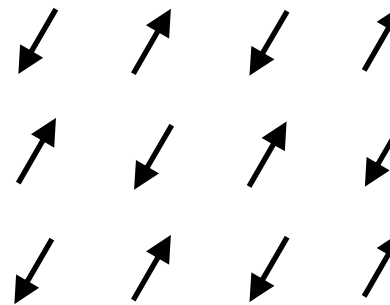
The low energy physics is dominated by spin fluctuations



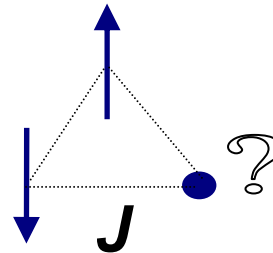
Heisenberg model
(localized spins)

$$H = \sum_{\langle ij \rangle} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j \quad J_{ij} = \frac{4t_{ij}^2}{U}$$

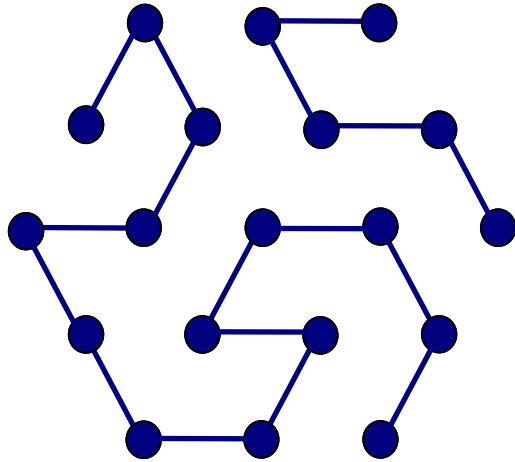
Square lattice \rightarrow Nèel order is the ground state, e.g. La_2CuO_4



Triangular lattice \rightarrow geometrical frustration might prevent magnetic long range order



Ground state of a triangular antiferromagnet

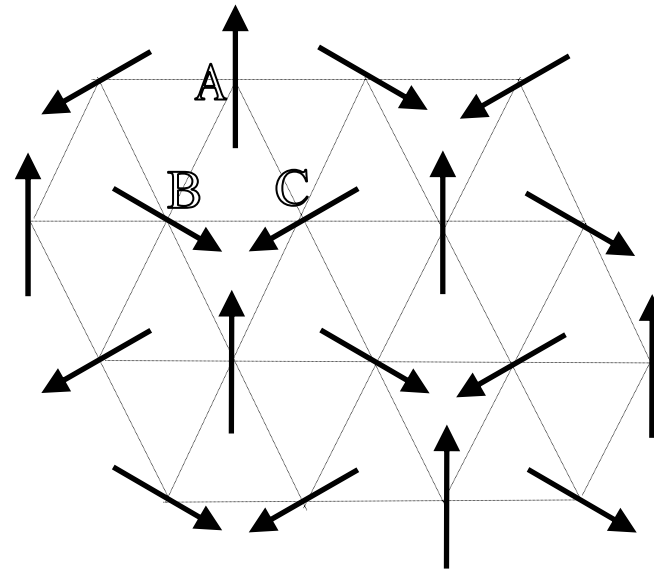


In 1973 P. W. Anderson proposed a **Resonant Valence Bond State (RVB)**

$$\text{---} = \frac{1}{2} [|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle]$$

...but the ground state is a “simple”
semiclassical **120° Néel order**

(Bernu et al, PRL '92,
Trumper et al, PRL '99)

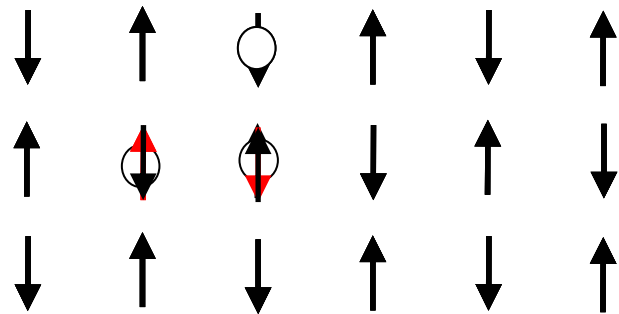


A single hole dynamics in an antiferromagnet

***t*-*J* model**
$$H = - \sum_{ij\sigma} t_{ij} \hat{c}_{i\sigma}^\dagger \hat{c}_{j\sigma} + \sum_{\langle ij \rangle} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

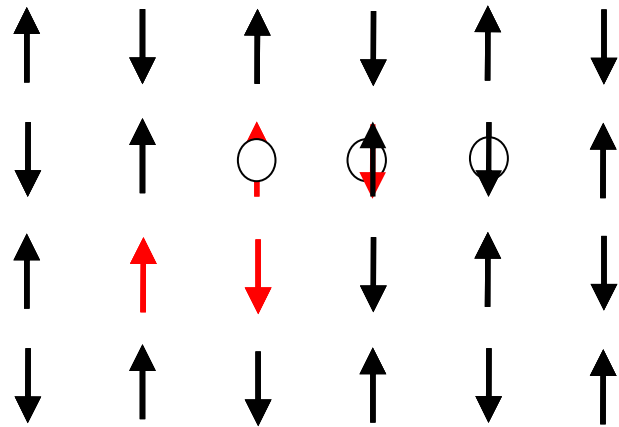


The hole can move only by disturbing the antiferromagnetic background



If $J \gg t$ then $\tau_{\text{exch}} \sim 1/J \ll \tau_{\text{hopp}} \sim 1/t$
 → the hole can propagate “easily”

Hole + surrounding cloud of spin flips = quasiparticle or spin polaron

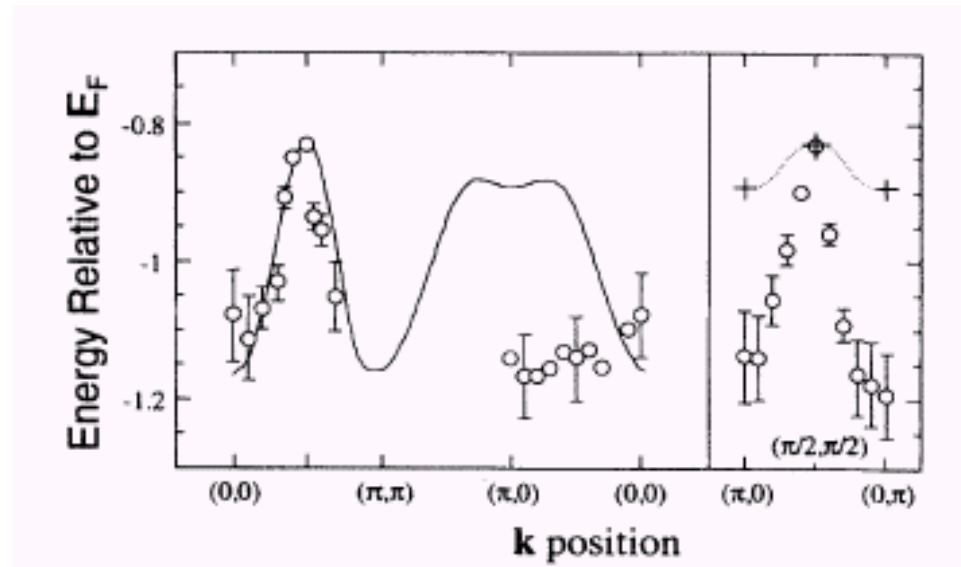


If $J \ll t$ then $\tau_{\text{exch}} \gg \tau_{\text{hopp}}$
 → the hole will leave behind a string of “wrong” spins, increasing its effective mass

In the square lattice antiferromagnet the spin polaron is always well defined (Martinez & Horsch PRB '91, Dagotto RMP '94).

ARPES seems to confirm this picture, e.g. $\text{Sr}_2\text{CuO}_2\text{Cl}_2$

(Wells et al, PRL '95)



How does the frustration affect the hole dynamics?

Let's look what happens when a hole is doped in an antiferromagnet on a triangular lattice

Model and method

We use the t - J model in local spin quantization axis, assuming a 120° Néel order

Representations: hole \rightarrow spinless fermion

spin fluctuations \rightarrow Holstein-Primakov bosons

$$\hat{c}_{i\uparrow} = h_i^\dagger \quad \hat{c}_{i\downarrow} = h_i S_i^-$$

$$S_i^x \sim \frac{1}{2}(a_i^\dagger + a_i) \quad S_i^y \sim \frac{i}{2}(a_i^\dagger - a_i) \quad S_i^z = \frac{1}{2} - a_i^\dagger a_i$$

Effective Hamiltonian

$$H = \sum_{\mathbf{k}} \epsilon_{\mathbf{k}} h_{\mathbf{k}}^\dagger h_{\mathbf{k}} + \sum_{\mathbf{q}} \omega_{\mathbf{q}} \alpha_{\mathbf{q}}^\dagger \alpha_{\mathbf{q}} - t \sqrt{\frac{3}{N_s}} \sum_{\mathbf{k}, \mathbf{q}} \left[M_{\mathbf{kq}} h_{\mathbf{k}}^\dagger h_{\mathbf{k}-\mathbf{q}} \alpha_{\mathbf{q}} + h.c. \right]$$

Free hopping
(due to non-collinearity)

Free magnon energy

hole-magnon interaction

Model and method (contd.)

$$\epsilon_{\mathbf{k}} = -3t\gamma_{\mathbf{k}} \quad \gamma_{\mathbf{k}} = \frac{1}{3} \sum_{\mathbf{e}} \cos(\mathbf{k} \cdot \mathbf{e})$$



half of the tight-binding energy dispersion in the triangular lattice

$$\omega_{\mathbf{q}} = \frac{3}{2} J \sqrt{(1 - \gamma_{\mathbf{q}})(1 + 2\gamma_{\mathbf{q}})}$$



spin wave dispersion

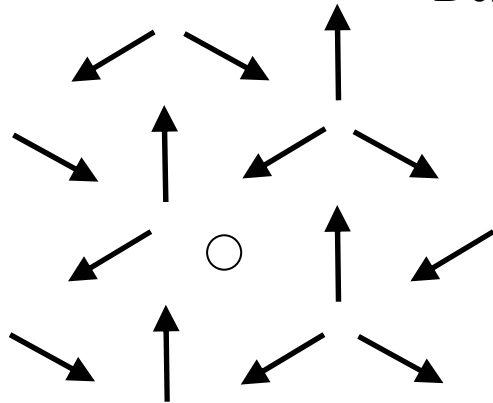
$$M_{\mathbf{kq}} = i(\beta_{\mathbf{k}} v_{-\mathbf{q}} - \beta_{\mathbf{k-q}} u_{\mathbf{q}}) \quad \beta_{\mathbf{k}} = \sum_{\mathbf{e}} \sin(\mathbf{k} \cdot \mathbf{e})$$



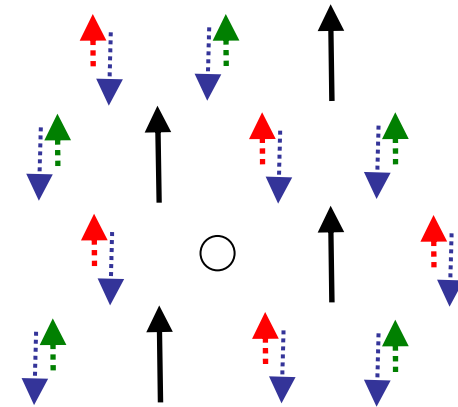
hole-magnon vertex interaction

u and v are the usual Bogoliubov coefficients

Descomposing the spins in an up-down basis



$$\begin{aligned} \swarrow &= \downarrow + \uparrow \\ \nwarrow &= \uparrow + \downarrow \end{aligned}$$



Two mechanisms for hole motion

**Magnon-assisted hopping
(hole-magnon interaction)**



**spin-polaron origin in
non-frustrated
antiferromagnets**

**Free hopping: no absorption or
emission of magnons (due to the
non-collinearity)**

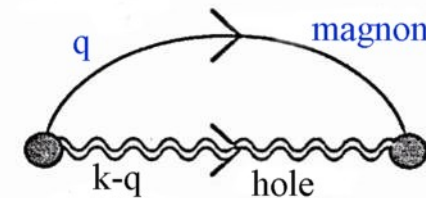
Self-consistent Born approximation (SCBA)

We calculate the hole **spectral function**

$$A_{\mathbf{k}}(\omega) = -\frac{1}{\pi} \text{Im} G_{\mathbf{k}}^h(\omega)$$

$$G_{\mathbf{k}}^h(\omega) = \langle AF | h_{\mathbf{k}} \frac{1}{(\omega + i\eta^+ - H)} h_{\mathbf{k}}^\dagger | AF \rangle$$

solving the self-consistent equation for the self-energy



$$\Sigma_{\mathbf{k}}(\omega) = \frac{3t^2}{N_s} \sum_{\mathbf{q}} \frac{|M_{\mathbf{k}\mathbf{q}}|^2}{\omega - \omega_{\mathbf{q}} - \epsilon_{\mathbf{k}-\mathbf{q}} - \Sigma_{\mathbf{k}-\mathbf{q}}(\omega - \omega_{\mathbf{q}})}$$

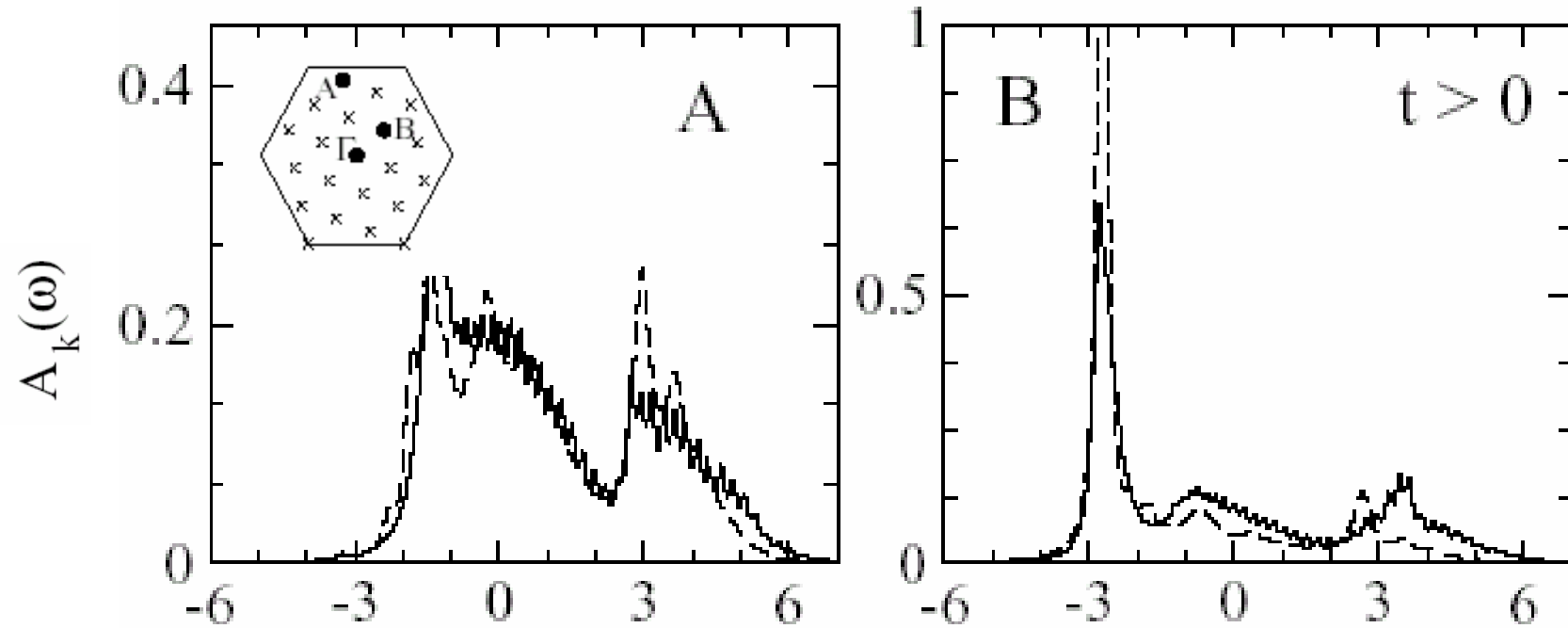
Quasiparticle weight

(How much of the hole survives)

$$z_{\mathbf{k}} = \left(1 - \frac{\partial \Sigma_{\mathbf{k}}(\omega)}{\partial \omega} \right)^{-1} \Big|_{E_{\mathbf{k}} = \Sigma_{\mathbf{k}}(E_{\mathbf{k}})}$$

Comparison SCBA vs exact results

N = 21 sites

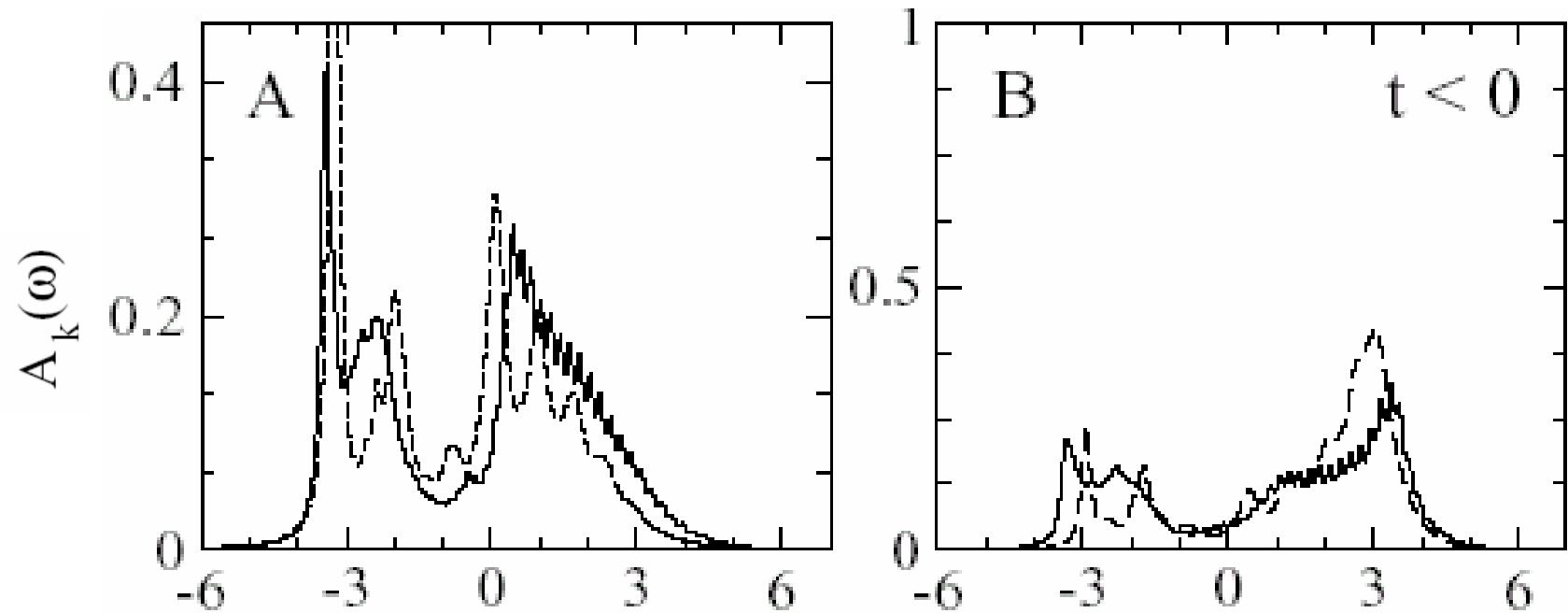


- ▶ Positive t
- ▶ $J/t=0.4 \rightarrow$ strong coupling regime

————— Lanczos
- - - - - SCBA

SCBA vs exact results

N = 21 sites



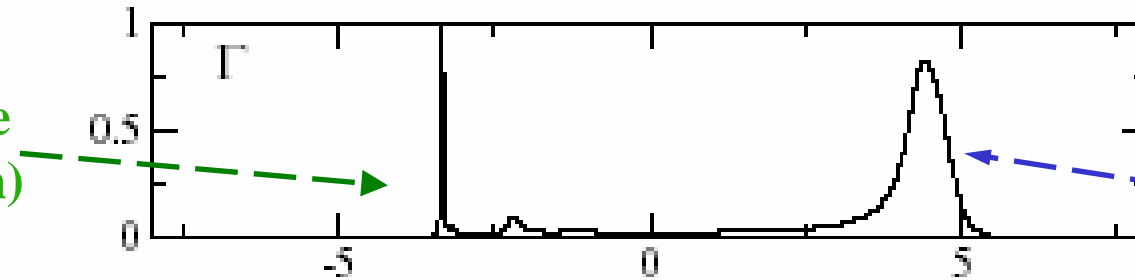
► Negative t

► $J/|t|=0.4$

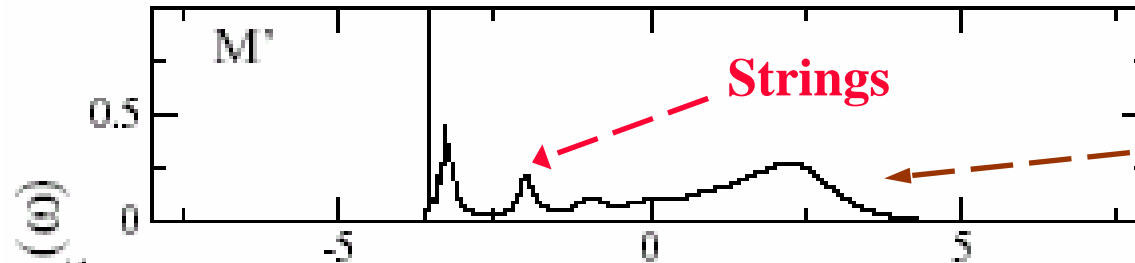
————— Lanczos
- - - - - SCBA

Hole spectral functions: negative t

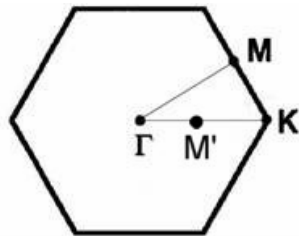
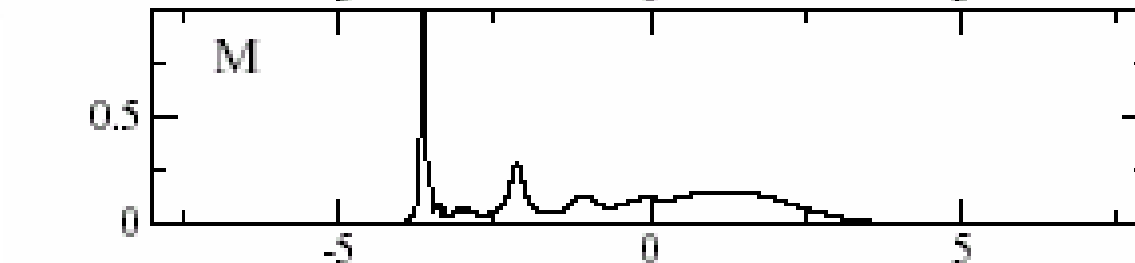
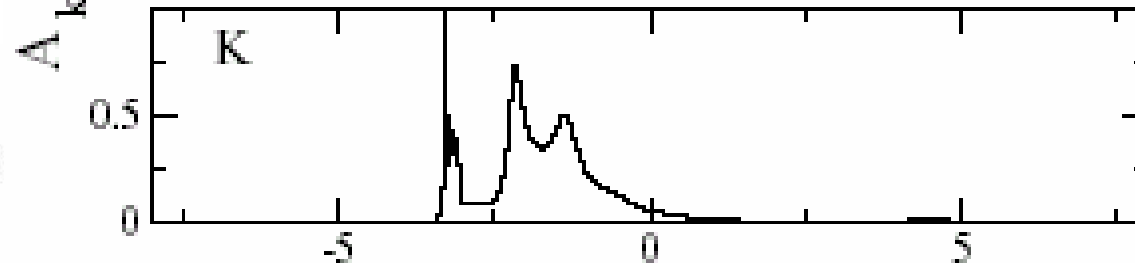
Quasiparticle
(spin polaron)



Free hopping



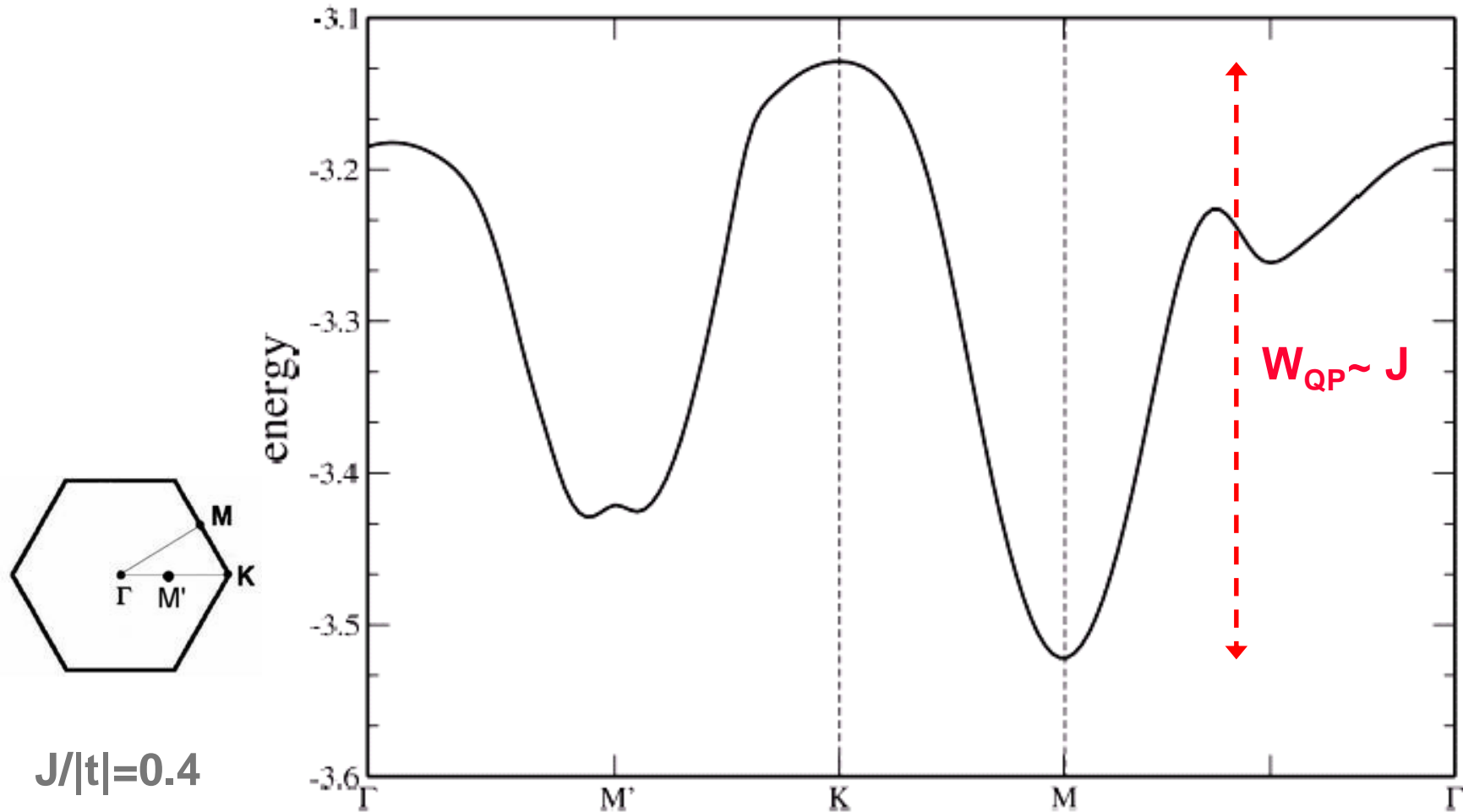
Incoherent
background



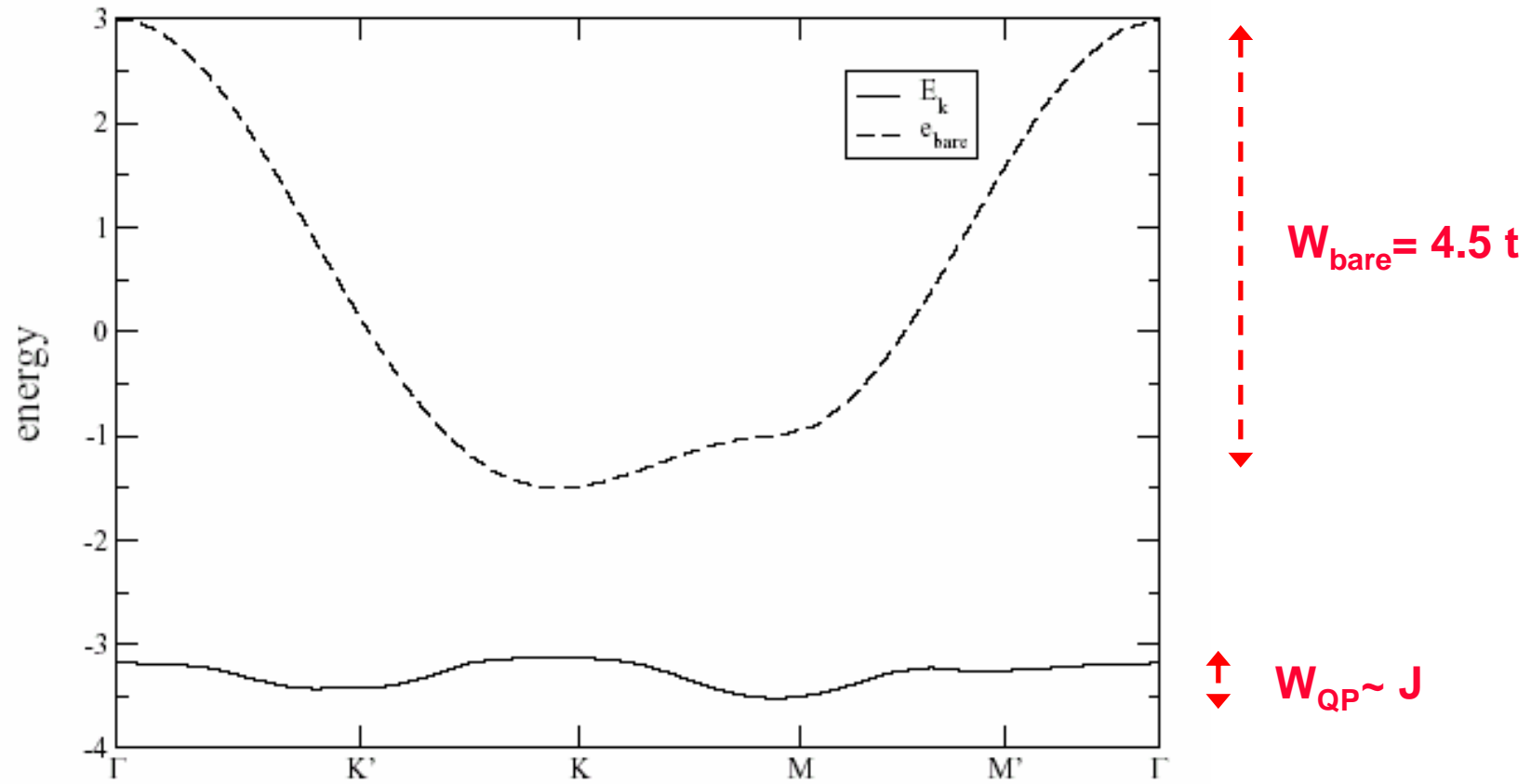
$J/|t|=0.4$

$\omega/|t|$

Quasiparticle energy dispersion: negative t

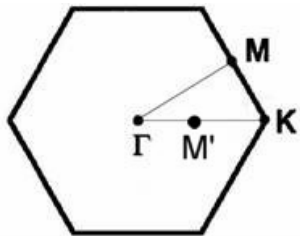


Quasiparticle energy dispersion

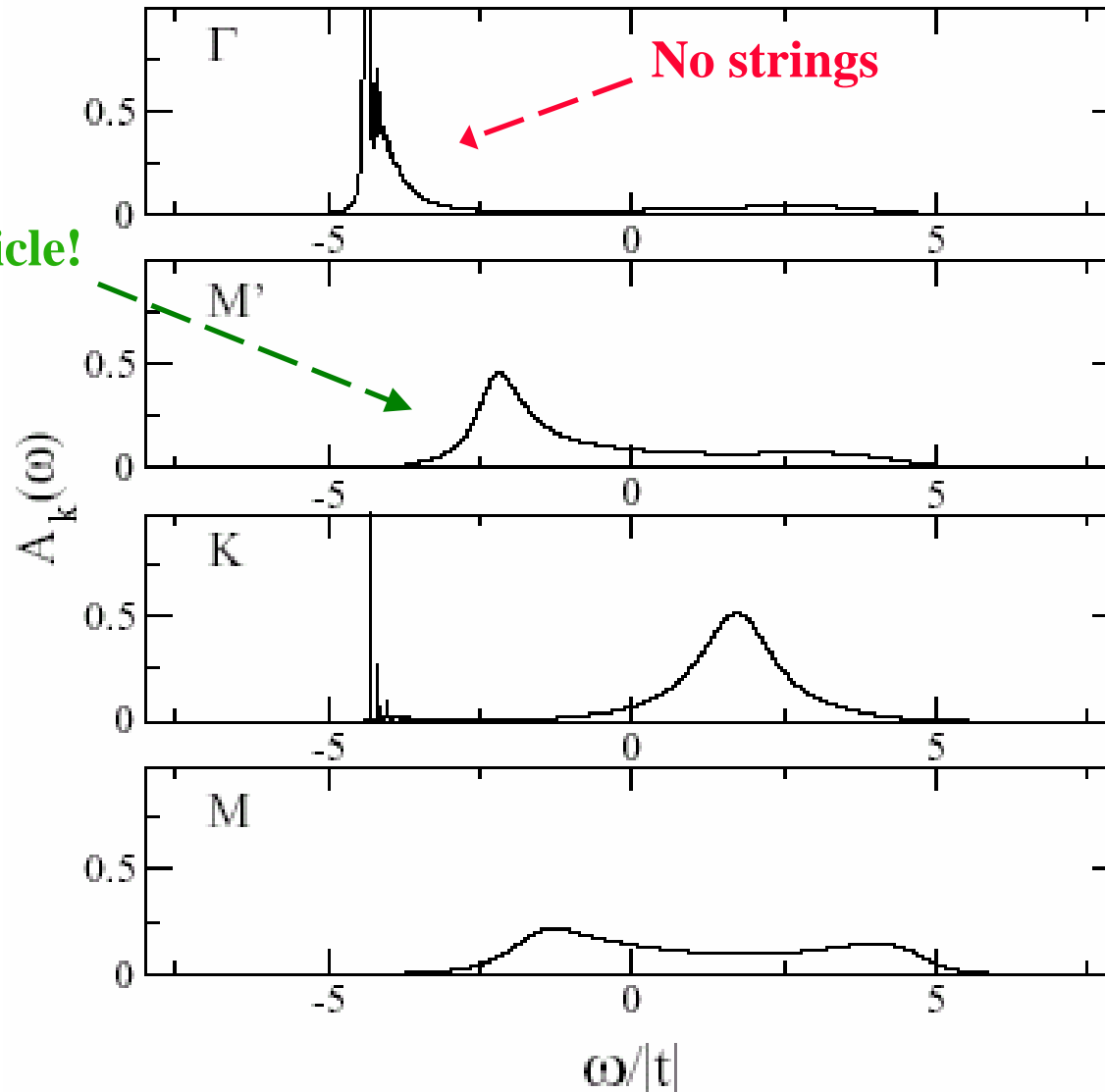


Hole spectral functions: positive t

No quasiparticle!

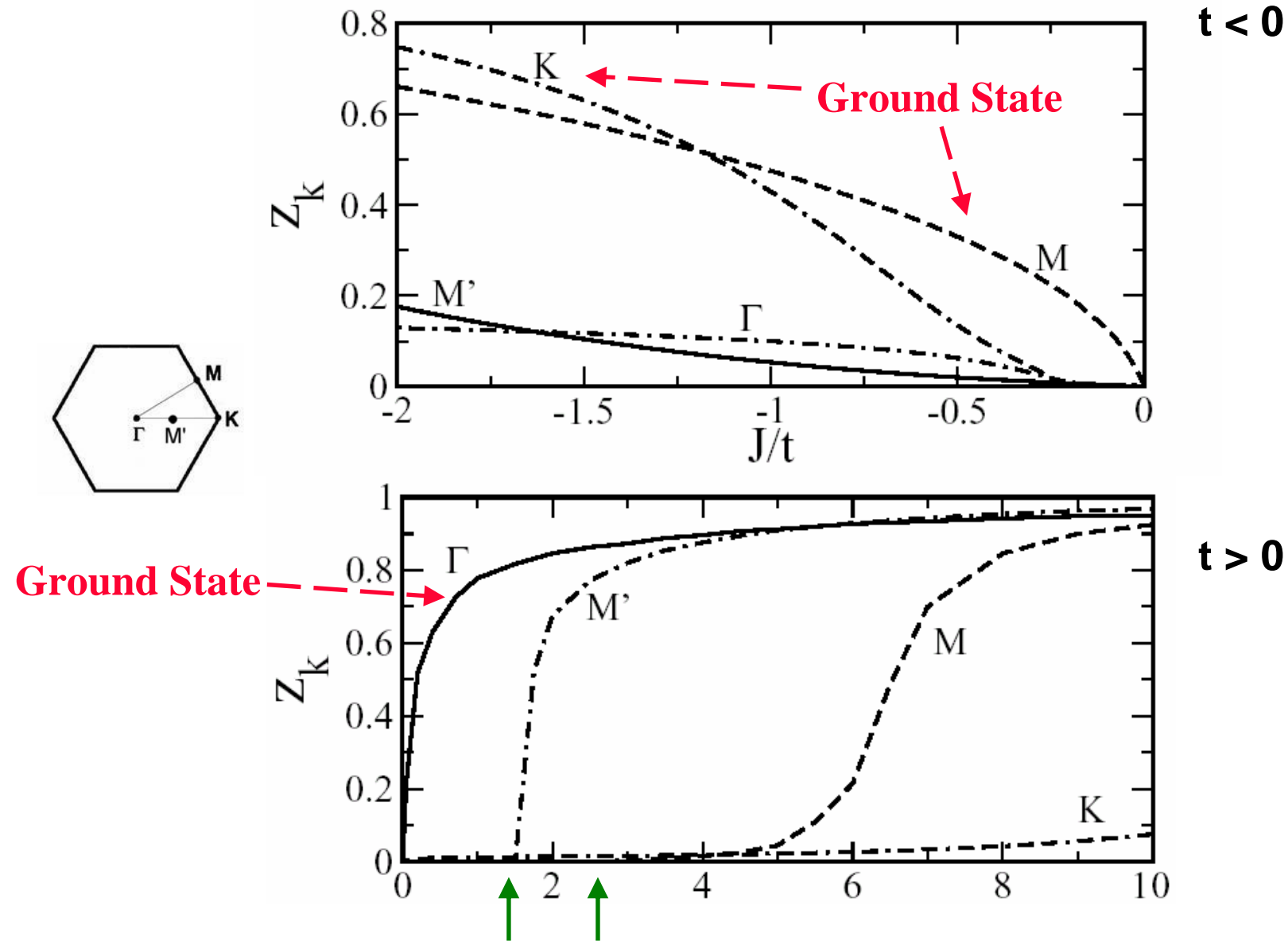


$J/t=0.4$

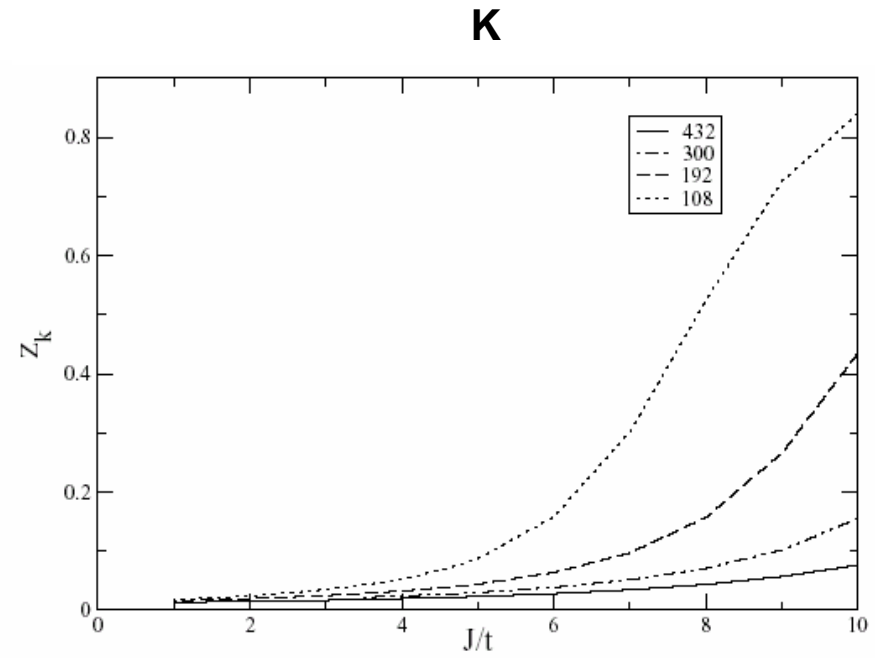
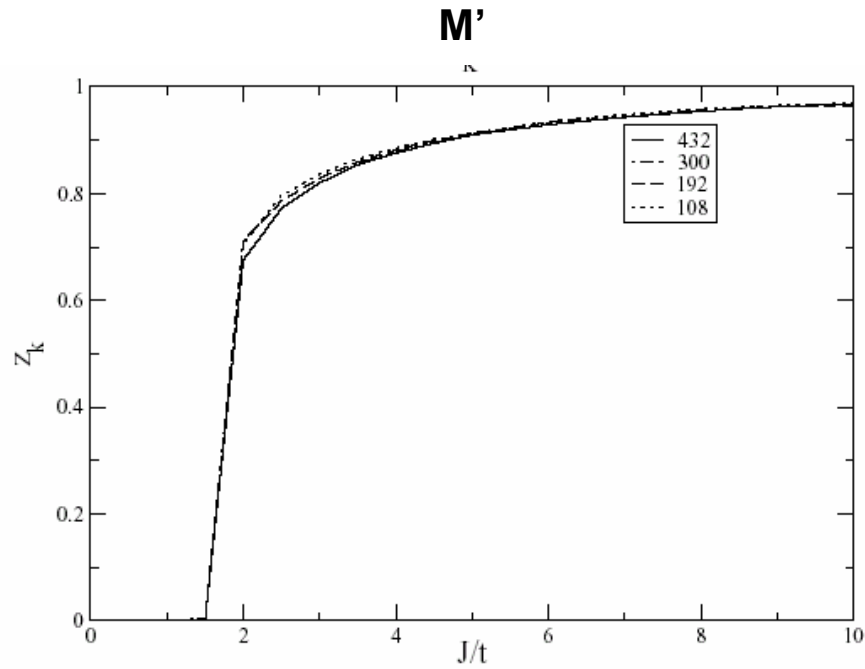


Sign reversal of t is not trivial!

Quasiparticle weight vs J/t



Quasiparticle weight: finite size effects

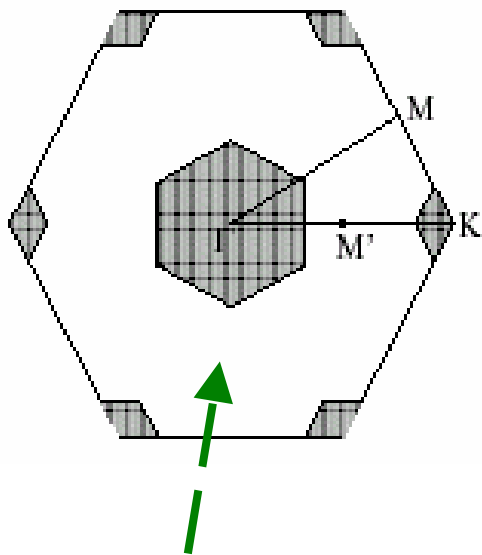


For positive t and in the weak coupling regime there are very strong finite size effects for momenta around the magnetic wave vector K

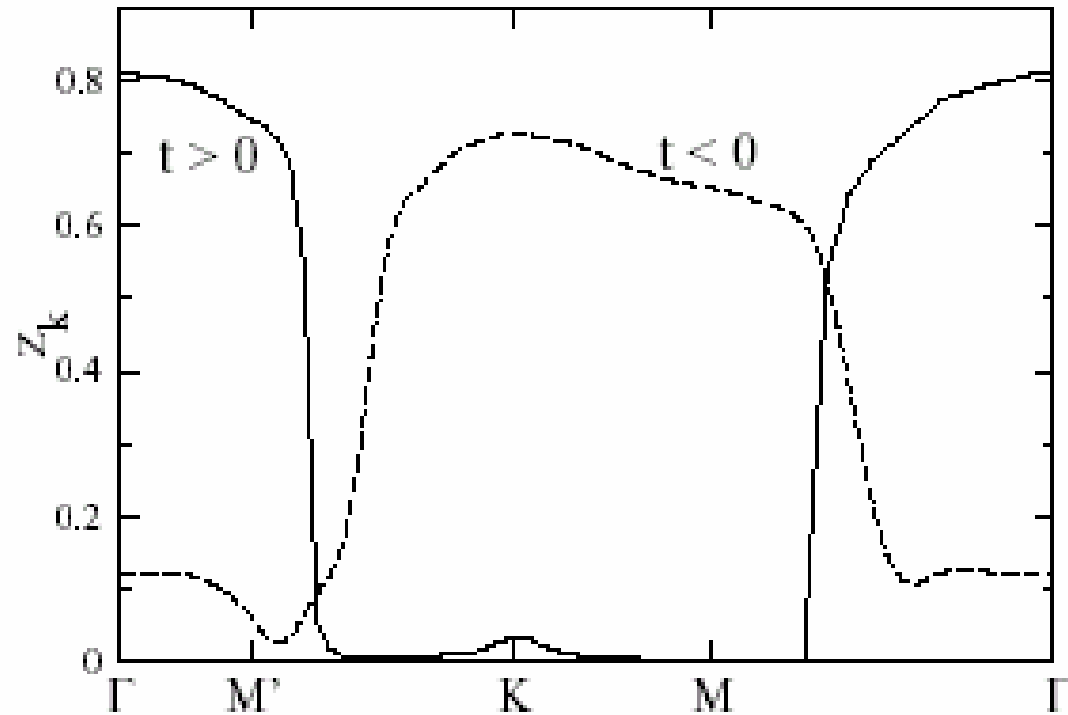
Momentum dependence of the quasiparticle weight

$$J/|t| = 2.0$$

$$J/t = 0.4$$

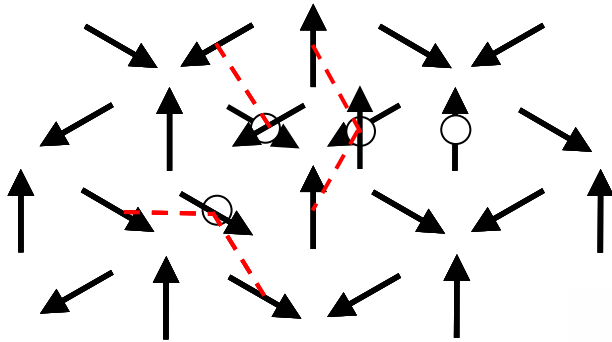


no quasiparticle



Goldstone modes

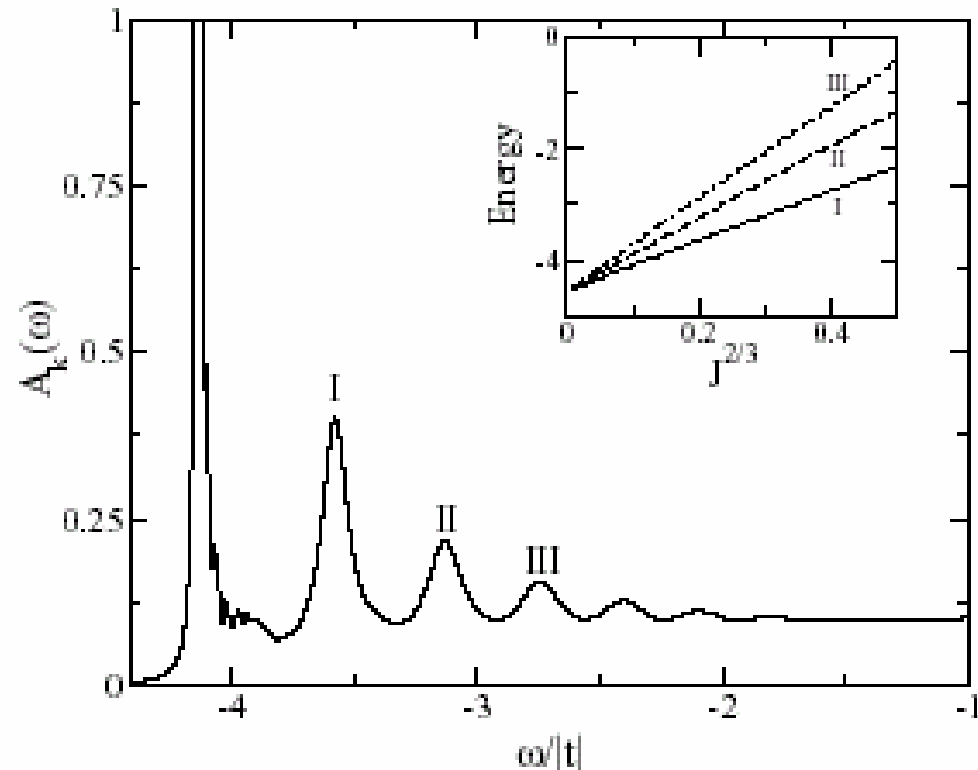
Strings excitations: Only for negative t !



For $J < |t|$ there will be a lot of “wrong” strings, leading to long lived resonances

$$E_{\text{string}} \sim (J/t)^{2/3}$$

Like a particle bounded by a linear potential



Quasiparticle energy scaling with J/t

For an antiferromagnetic spin polaron $E_{qp} \sim (J/t)^{2/3}$

For a ferromagnetic spin polaron (“ferron”) $E_{qp} \sim (J/t)^{1/2}$

In the thermodynamic limit we have found

➤ $t < 0 \rightarrow E_{qp} \sim (J/t)^{0.64} \rightarrow$ enhanced local AF environment around the hole

➤ $t > 0 \rightarrow E_{qp} \sim (J/t)^{0.54} \rightarrow$ enhanced ferromagnetic environment

...while for small cluster sizes ($N < 21$) we have found the opposite behaviour, as in Koretsune & Ogata, PRL'02.

Quasiparticle wavefunction

$$|\Psi_{\mathbf{k}}\rangle = a_{\mathbf{k}}^{(0)} h_{\mathbf{k}}^{\dagger} |AF\rangle + \frac{1}{\sqrt{N}} \sum_{\mathbf{q}_1} a_{\mathbf{k},\mathbf{q}_1}^{(1)} h_{\mathbf{k}-\mathbf{q}_1}^{\dagger} \alpha_{\mathbf{q}_1}^{\dagger} |AF\rangle + \frac{1}{N} \sum_{\mathbf{q}_1, \mathbf{q}_2} a_{\mathbf{k},\mathbf{q}_1, \mathbf{q}_2}^{(2)} h_{\mathbf{k}-\mathbf{q}_1-\mathbf{q}_2}^{\dagger} \alpha_{\mathbf{q}_2}^{\dagger} \alpha_{\mathbf{q}_1}^{\dagger} |AF\rangle + \dots$$

\uparrow
bare hole
 \uparrow
one magnon
 \uparrow
multi-magnon

We solve the Schrodinger equation for the spin polaron in the retraceable paths approximation [Ramsak & Horsch PRB'93, Reiter PRB'94]

$$H|\Psi_{\mathbf{k}}\rangle = E_{\mathbf{k}}|\Psi_{\mathbf{k}}\rangle$$

Normalization condition $\langle \Psi_{\mathbf{k}} | \Psi_{\mathbf{k}} \rangle = \sum_n A_{\mathbf{k}}^{(n)} = 1$

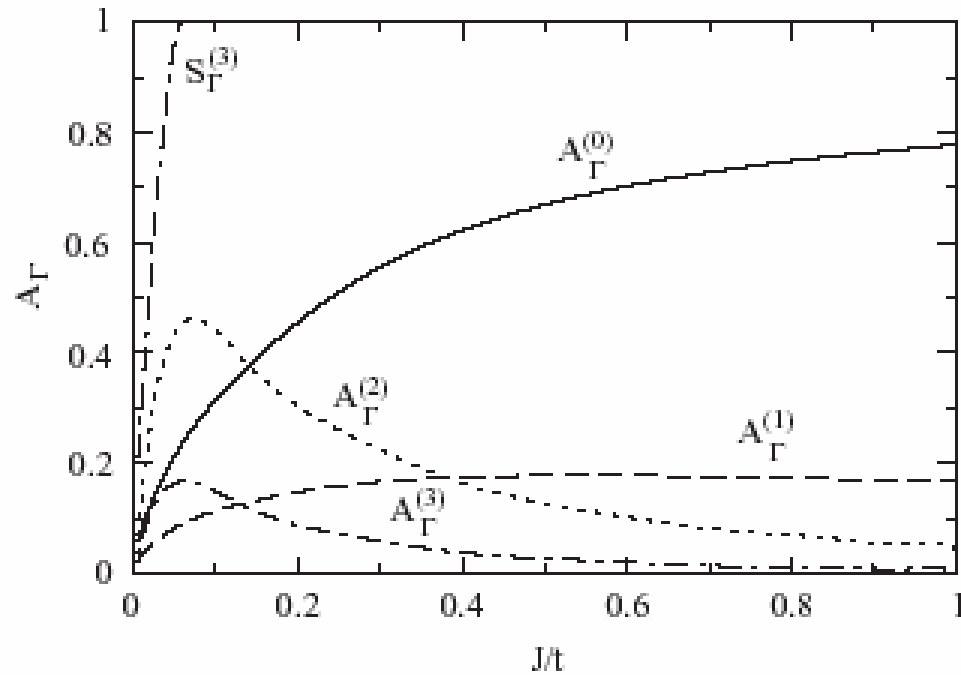
\uparrow
weight of the n -magnon contribution

In particular $\rightarrow A_{\mathbf{k}}^{(0)} = \langle \Psi_{\mathbf{k}} | h_{\mathbf{k}}^{\dagger} | AF \rangle \equiv z_{\mathbf{k}}$

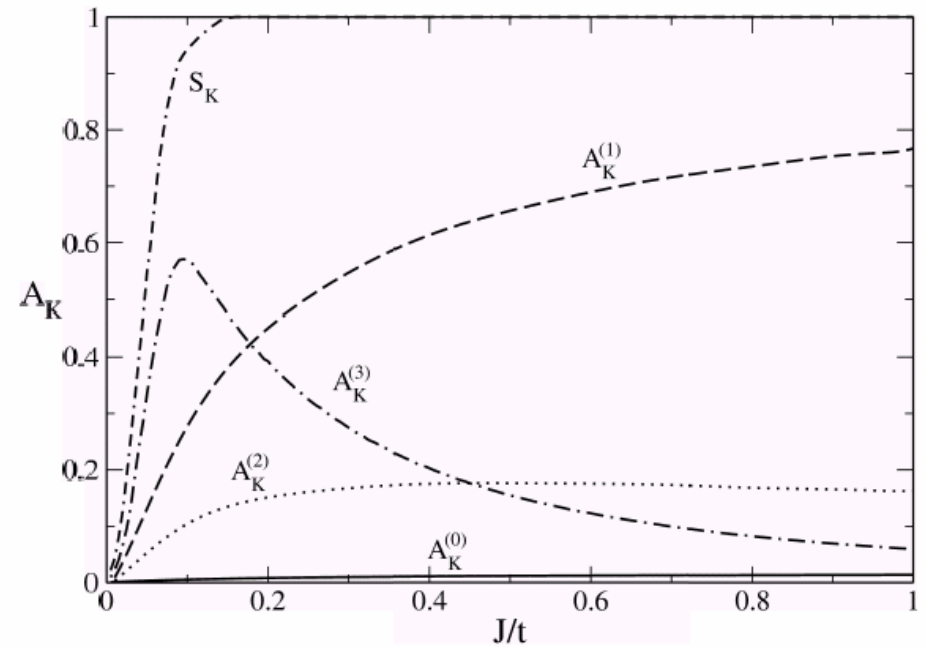
How many magnons?

Positive t

Three magnons are enough!

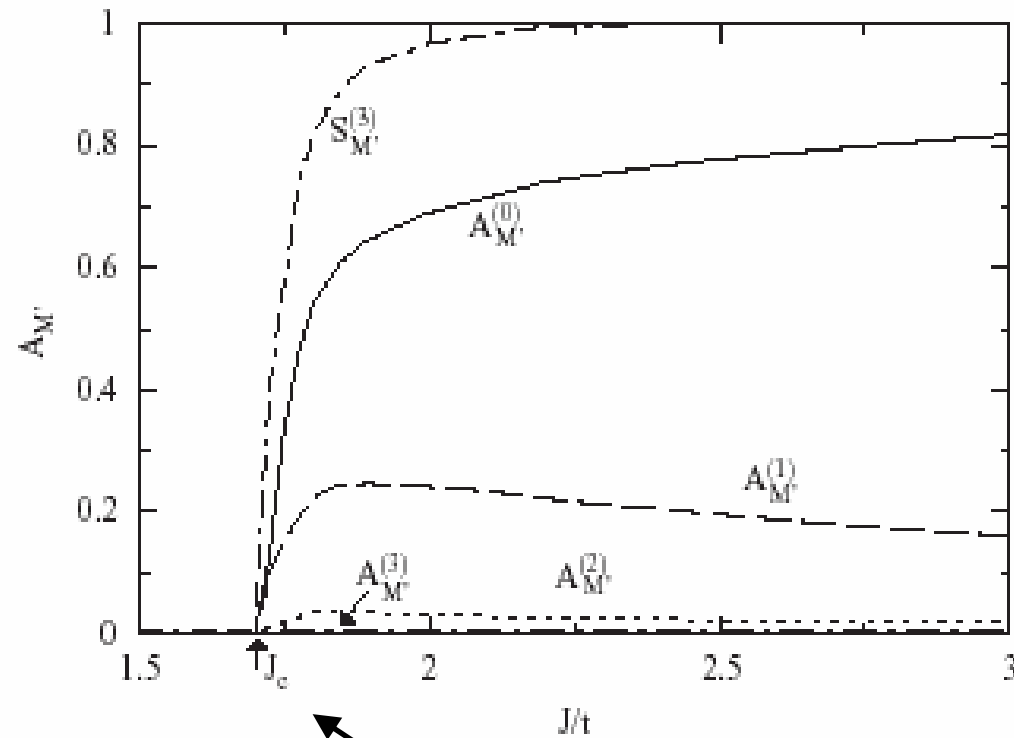


One magnon even for $J \gg t$



$$S_k^{(n)} = \sum_{m=0}^n A_k^{(m)}$$

How many magnons?



Magnon proliferation even for a relative large J/t !

Conclusions

► The magnetic frustration induces qualitative changes in the hole dynamics:

$t < 0 \rightarrow$ well defined quasiparticle and string excitations

$t > 0 \rightarrow$ no quasiparticle, no strings, magnon proliferation

► We give firm evidence that non-conventional excitations can be found in *non-collinear* spin-crystal phases like the one present in the triangular antiferromagnet. **There is no need of spin liquid phases!**

► Experiments? There is a plenty of strongly correlated materials with triangular topology: organic salts (BEDT-TTF)-X, cobaltates, silicon surfaces, etc, etc. Our findings could be of relevance for these compounds.