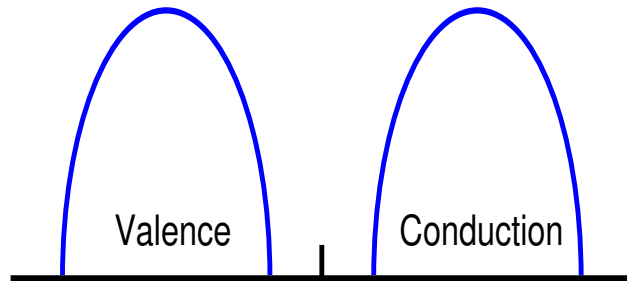


Hybrid Mott Band Metal Insulator Transitions

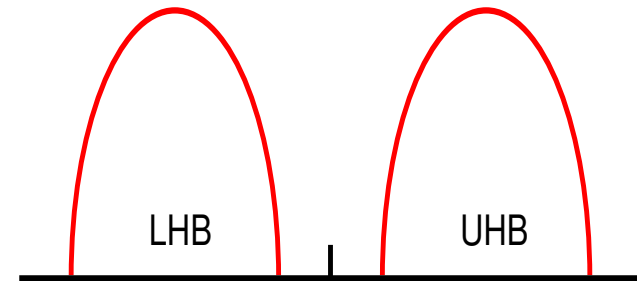
Ansgar Liebsch

**Institute for Solid State Physics
Research Center Jülich**

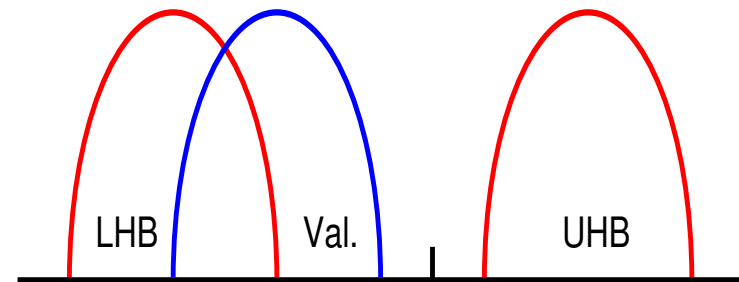
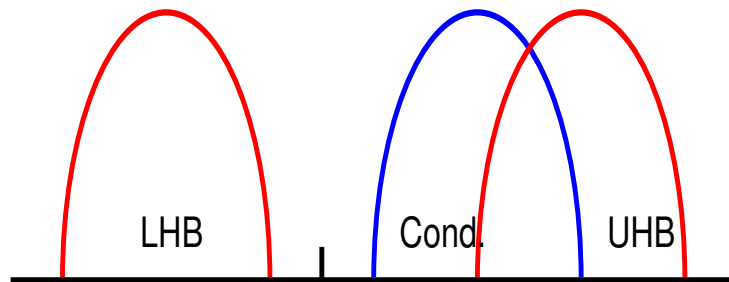
Band vs Mott Insulator → ‘Hybrid Insulators’



Band Insulator



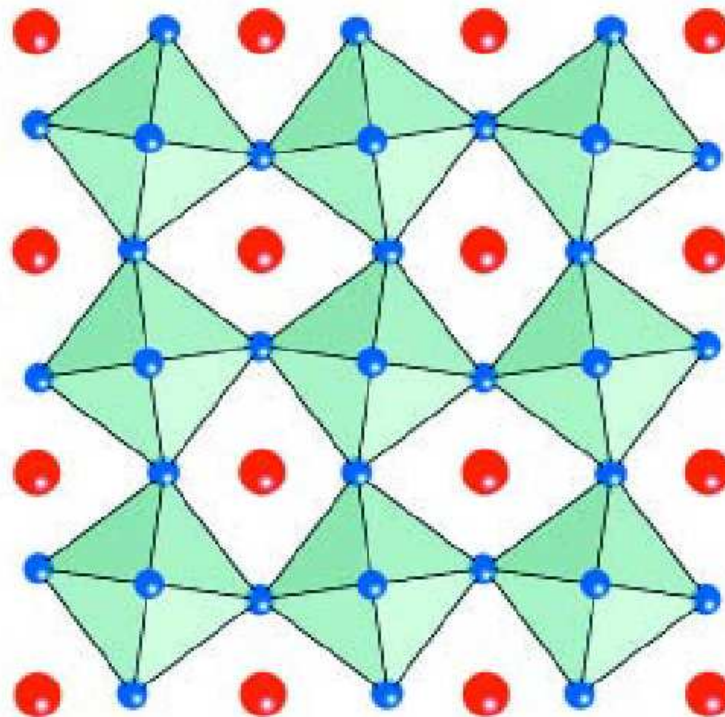
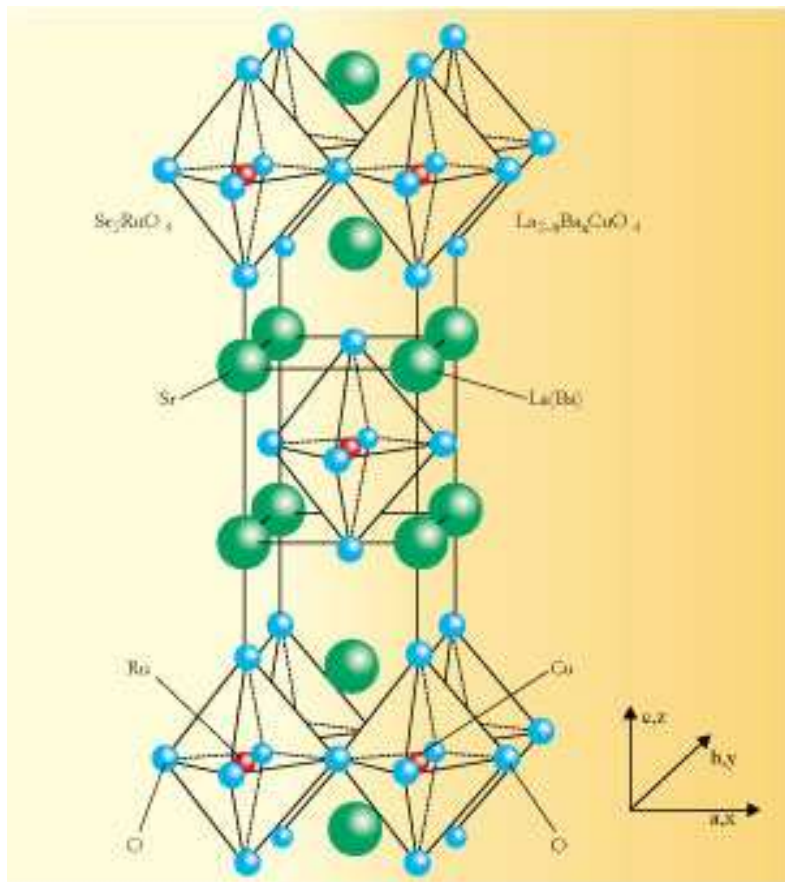
Mott Insulator



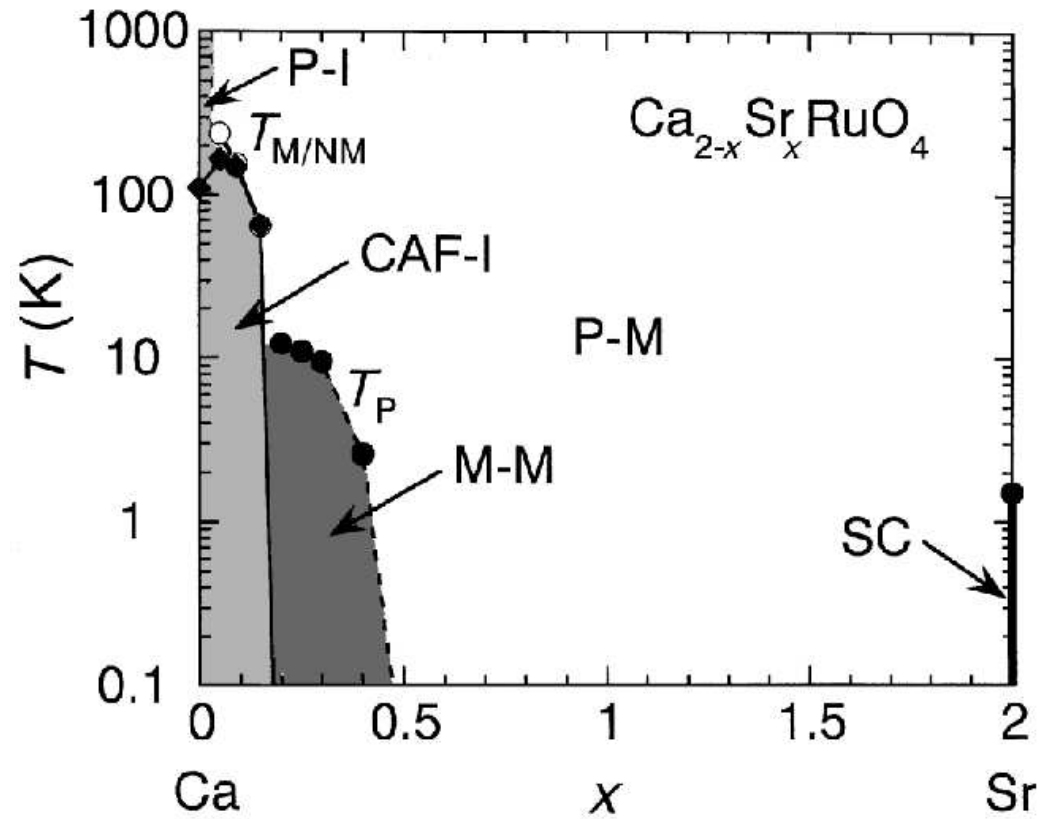
Overview

- Mott transition in multi-orbital materials:
 - Coulomb driven inter-orbital charge transfer
 - role of crystal field splitting
 - suppression of orbital fluctuations
 - subband filling / emptying → MIT
- Dynamical mean field theory:
 - exact diagonalization for multiband materials
- $\text{Ca}_{2-x}\text{Sr}_x\text{RuO}_4$ $4d^4$ orbital selective Mott transition ?
- V_2O_3 $3d^2$ Hund vs. Ising exchange ?
- LaTiO_3 / SrTiO_3 $3d^1$ MIT in heterostructures ?
 $3d^{1-x}$ doping driven Mott transition ?
- Na_xCoO_2 $3d^{5+x}$ topology of Fermi surface ?

Transition metal oxides:

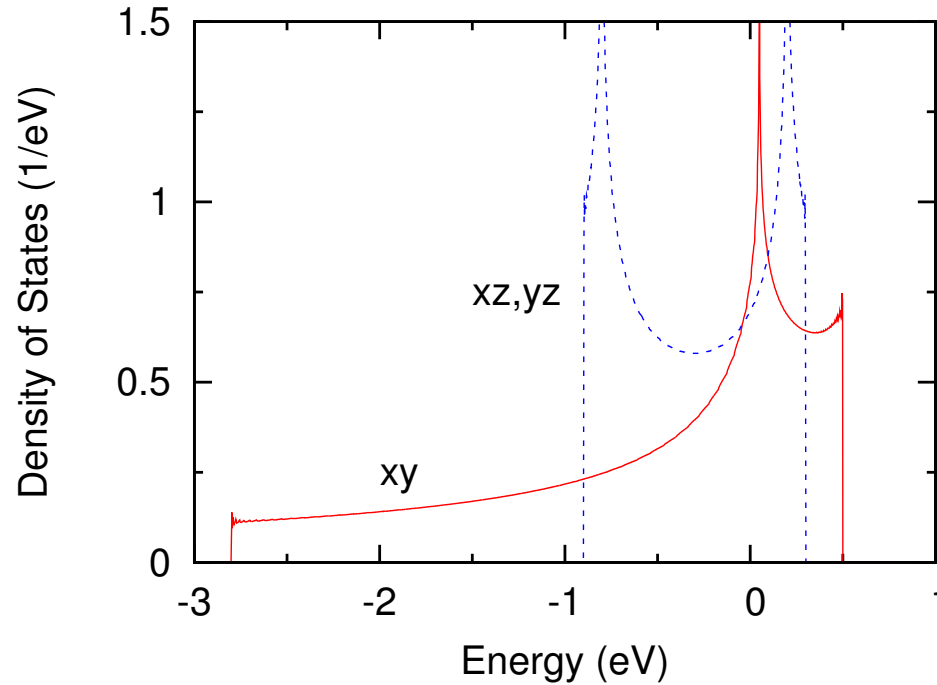


$\text{Ca}_{2-x}\text{Sr}_x\text{RuO}_4$: phase diagram



Maeno (PRL 2000)

$\text{Ca}_{2-x}\text{Sr}_x\text{RuO}_4$:



- coexisting narrow and wide bands: U/W_i ??
- orbital selective Mott transitions ? (Anisimov et al)
- crystal field splitting among t_{2g} bands ! (Fang et al)
- Sr \rightarrow Ca: octahedral distortions

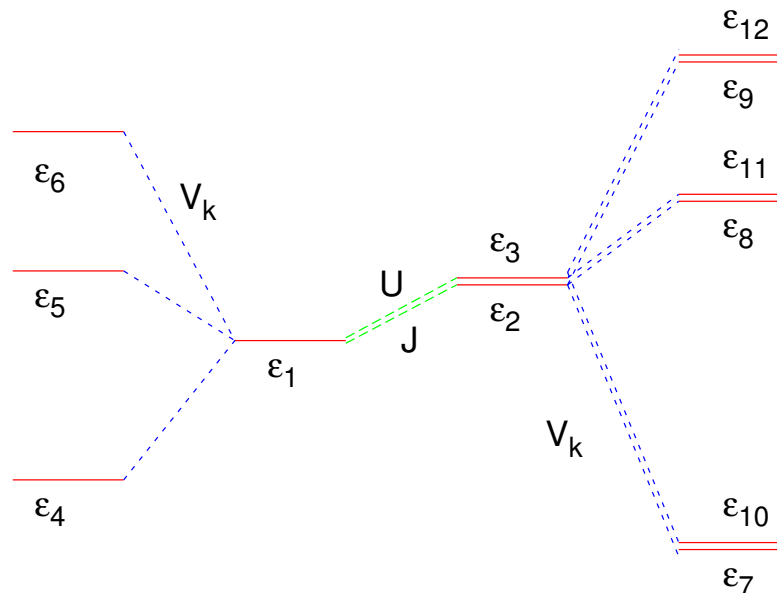
Dynamical mean field theory

$$G(i\omega_n) = \sum_k \left(i\omega_n + \mu - H(k) - \Sigma(i\omega_n) \right)_{ij}^{-1} \quad (t_{2g})$$

$$G_0 = (G^{-1} + \Sigma)^{-1}$$

exact diagonalization: solid \rightarrow cluster = impurity + bath

$$G_{0,i}(i\omega_n) \approx G_{0,i}^{cl}(i\omega_n) = \left(i\omega_n + \mu - \varepsilon_i - \sum_{k=4}^{n_s} \frac{|V_{ik}|^2}{i\omega_n - \varepsilon_k} \right)^{-1}$$



cluster Hamiltonian

$$H^{cl} = \sum_{i\sigma} (\varepsilon_i - \mu) n_{i\sigma} + \sum_{k\sigma} \varepsilon_k n_{k\sigma} + \sum_{ik\sigma} V_{ik} [c_{i\sigma}^+ c_{k\sigma} + \text{H.c.}] \\ + \sum_i U n_{i\uparrow} n_{i\downarrow} + \sum_{i < j, \sigma \leq \sigma'} (U' - J \delta_{\sigma\sigma'}) n_{i\sigma} n_{j\sigma'} - \sum_{i \neq j} J [c_{i\uparrow}^+ c_{i\downarrow} c_{j'\downarrow}^+ c_{j\uparrow} + c_{i\uparrow}^+ c_{i\downarrow}^+ c_{j\uparrow} c_{j\downarrow}]$$

cluster Green's function:

$$G_i^{cl}(i\omega_n) = \frac{1}{Z} \sum_{\nu\mu} \frac{|\langle \mu | c_{i\sigma}^+ | \nu \rangle|^2}{E_\nu - E_\mu - i\omega_n} [e^{-\beta E_\nu} + e^{-\beta E_\mu}] \\ = \frac{1}{Z} \sum_\nu e^{-\beta E_\nu} \left(\sum_\mu \frac{|\langle \mu | c_{i\sigma}^+ | \nu \rangle|^2}{(E_\nu - E_\mu) - i\omega_n} + \sum_\mu \frac{|\langle \mu | c_{i\sigma} | \nu \rangle|^2}{(E_\mu - E_\nu) - i\omega_n} \right)$$

assumption: cluster self-energy \approx solid self-energy:

$$\Sigma^{cl} = 1/G_0^{cl} - 1/G^{cl} \approx \Sigma$$

H^{cl} sparse: Arnoldi algorithm $n_s = 12$ $N = 853776$

level spacing < 1 meV \rightarrow finite size effects reduced

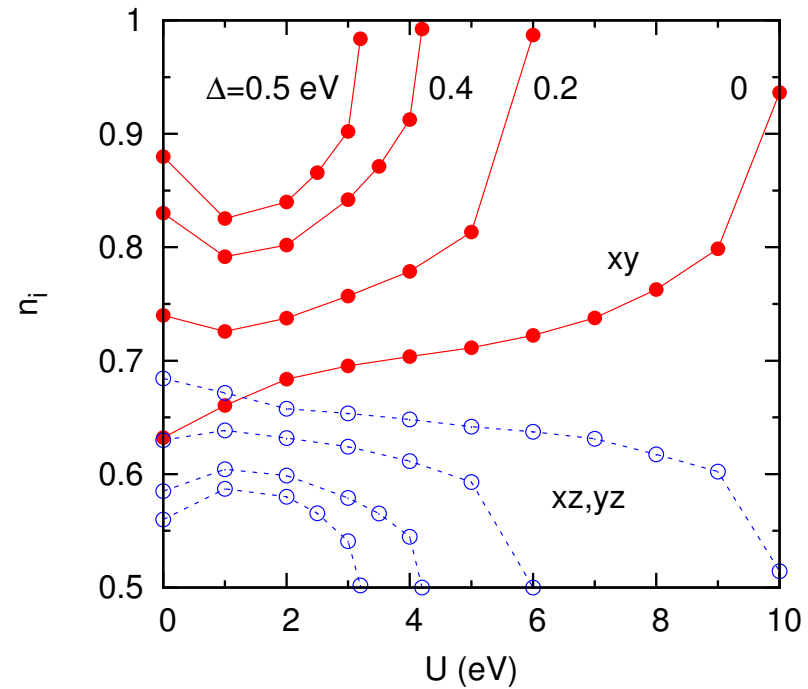
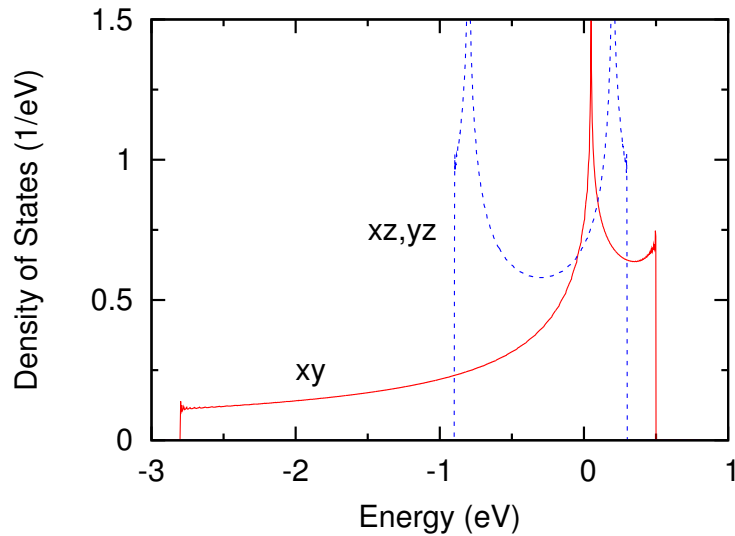
ED/DMFT for realistic t_{2g} materials, Hund exchange

complementary to QMC/DMFT

Perroni, Ishida + A.L. PRB (2007)

$\text{Ca}_{2-x}\text{Sr}_x\text{RuO}_4$ nature of Mott transition ?

Sr \rightarrow Ca : n_{xy} increases : crystal field Δ Fang et al (2004)



dyn. correl.: $n_{xy} \rightarrow 1$

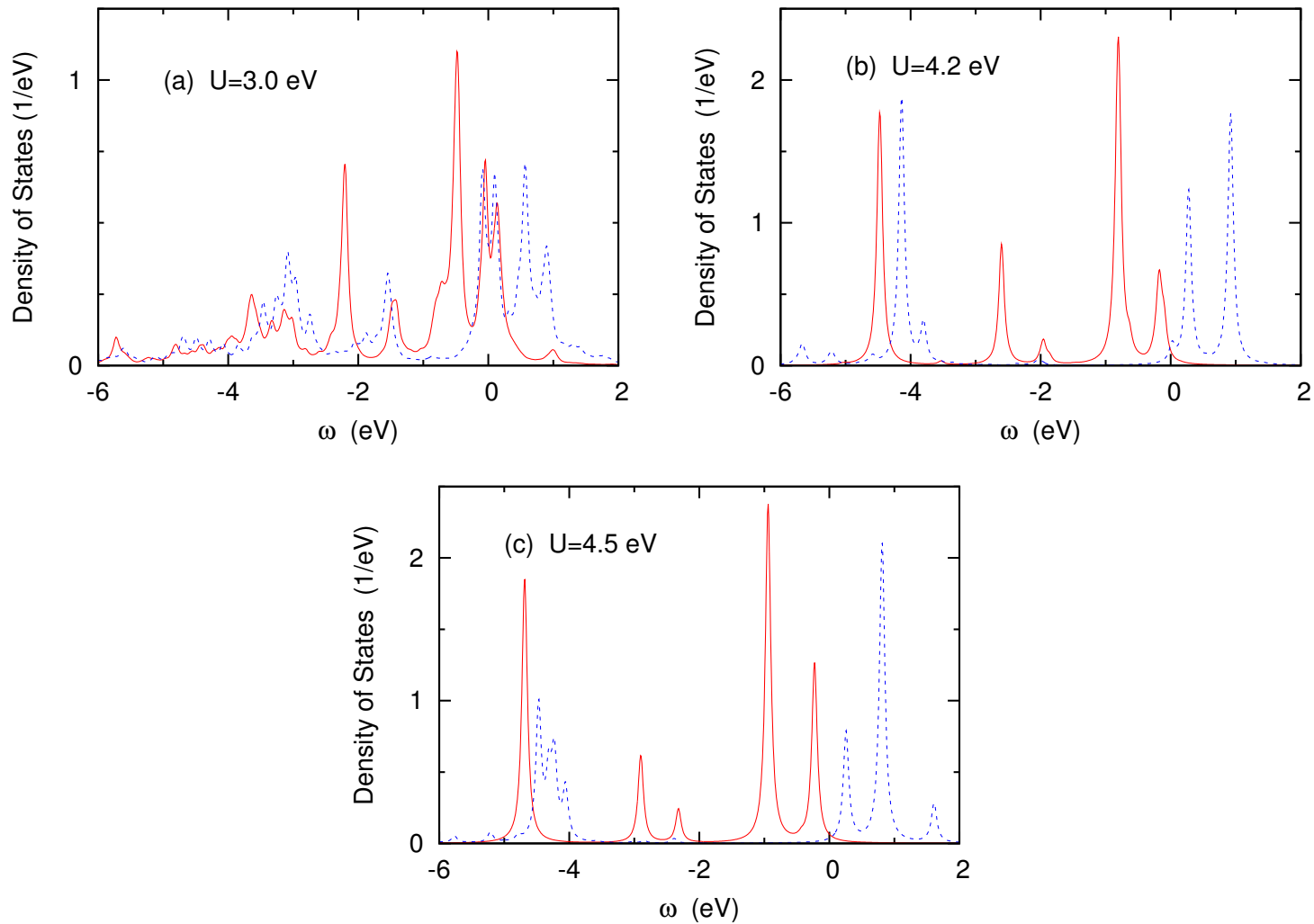
A.L.+ Ishida, cond-mat/0612539 PRL(2007)

suppression of orbital fluctuations:

MIT in half-filled xz,yz band \rightarrow no orbital selective MIT

future: role of octahedral distortions ? magnetic phases ?

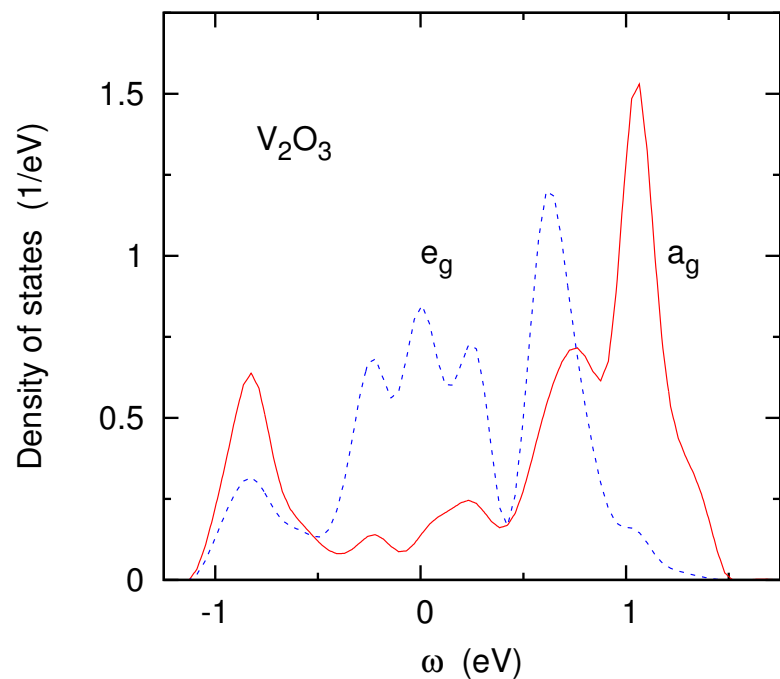
Ca_2RuO_4 cluster spectra $\Delta = 0.4 \text{ eV}$



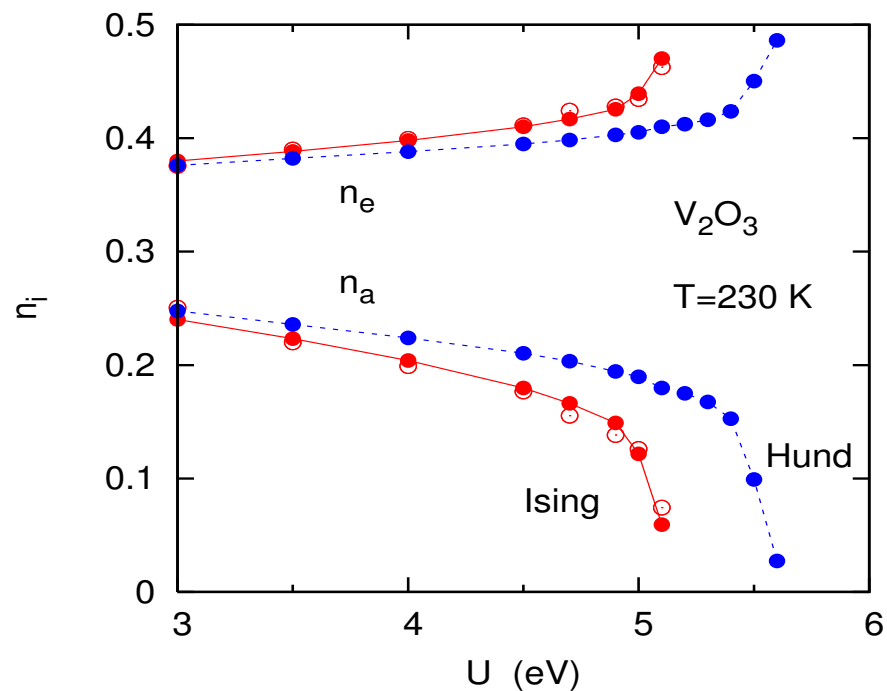
gap between filled xy and xz,yz upper Hubbard band

V_2O_3 $3d^2$

ED vs QMC



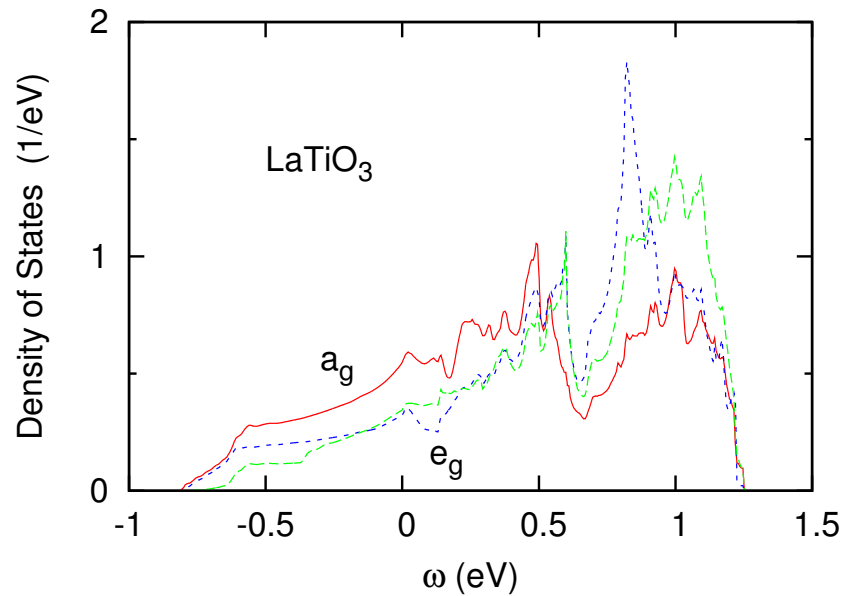
Keller et al, PRB (2004)



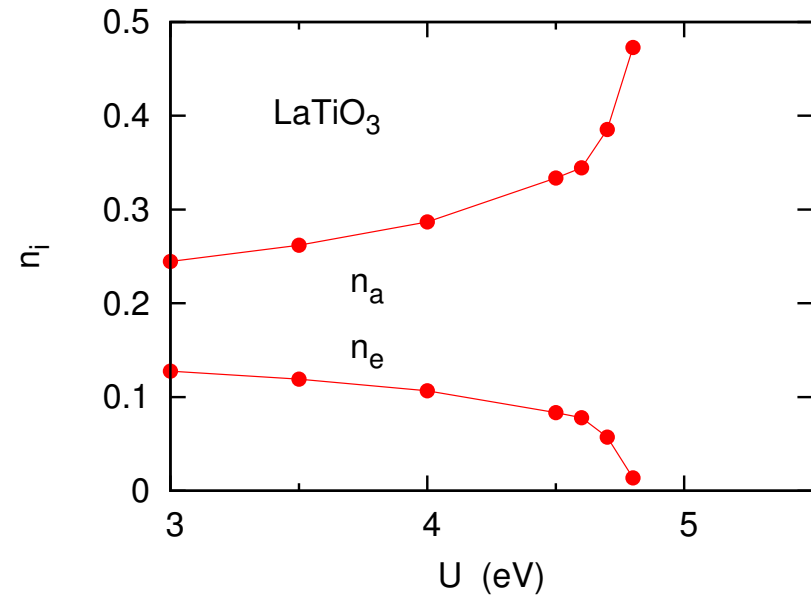
A.L. (2007)

dynamical correlations: $n_{a_g} \rightarrow 0$, MIT in half-filled e'_g
 suppression of orbital fluctuations

LaTiO₃ 3d¹



Pavarini et al, PRL (2004)



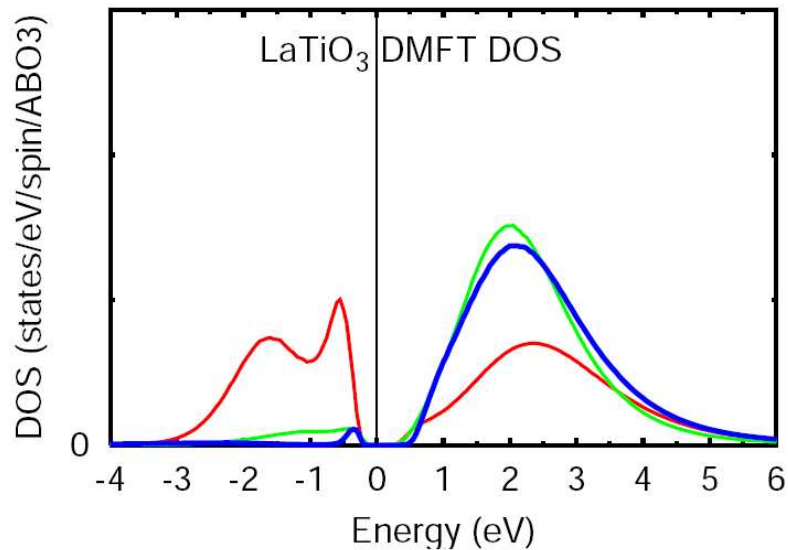
A.L. (2007)

dynamical correlations: $n_e \rightarrow 0$, MIT in half-filled a_g
suppression of orbital fluctuations

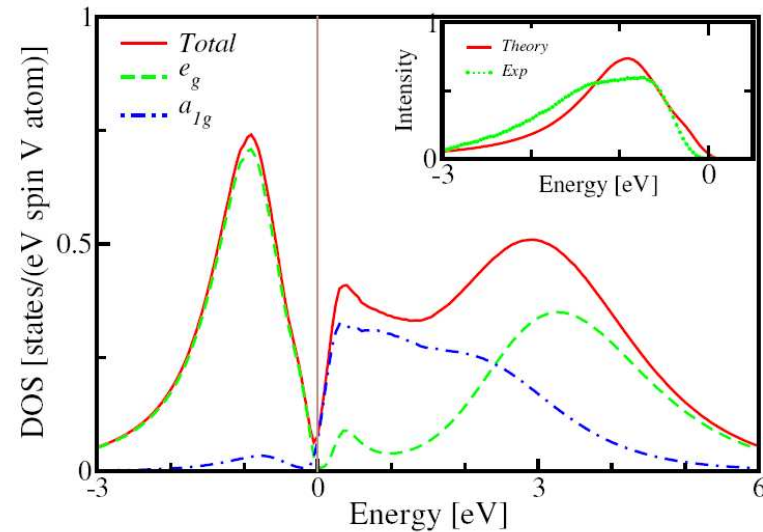
quasi-particle spectra:

LaTiO₃

V₂O₃



Pavarini et al (2006)



Poteryaev et al, cond-mat/0701263

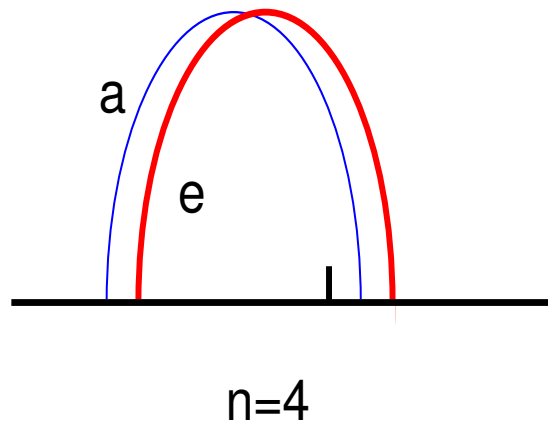
excitation gap:

LaTiO₃: LHB a_g → empty e_g bands

V₂O₃: LHB e_g → empty a_g band

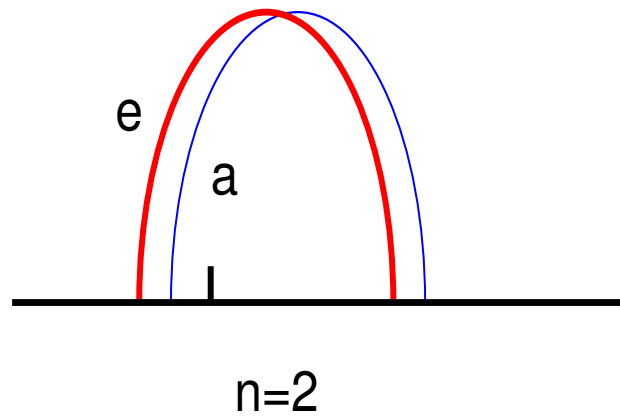
Ca₂RuO₄

$$n_{\sigma} \approx (0.8, 0.6, 0.6) \\ \rightarrow (1.0, 0.5, 0.5)$$



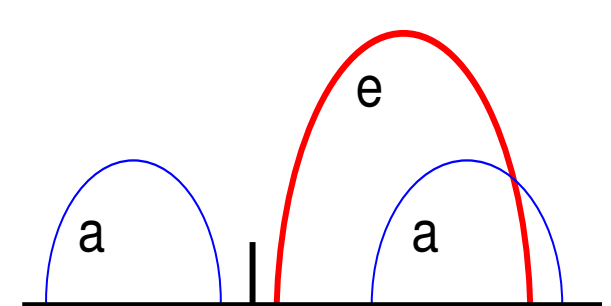
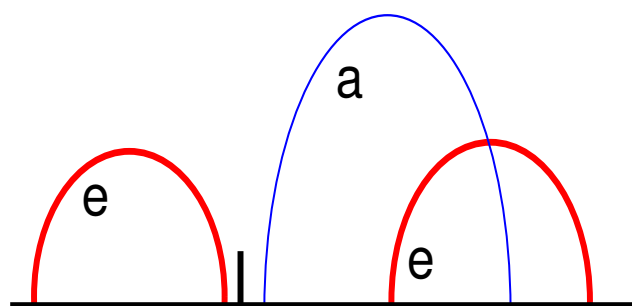
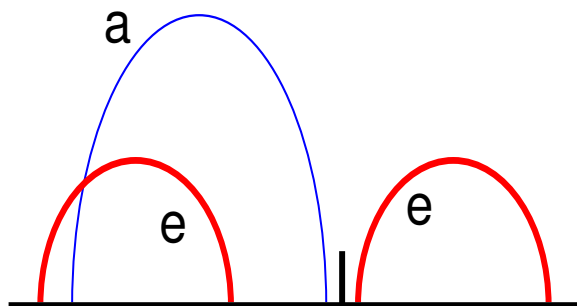
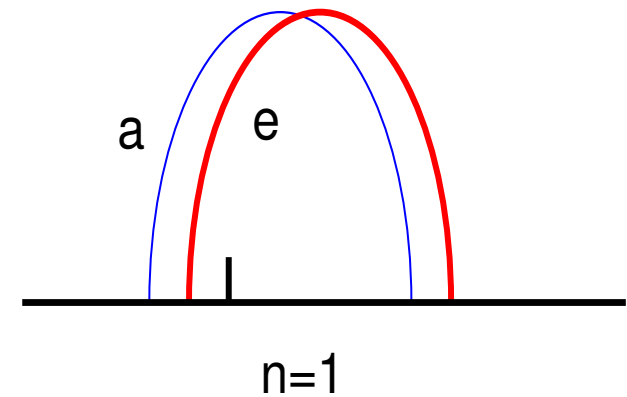
V₂O₃

$$n_{\sigma} \approx (0.2, 0.4, 0.4) \\ \rightarrow (0.0, 0.5, 0.5)$$

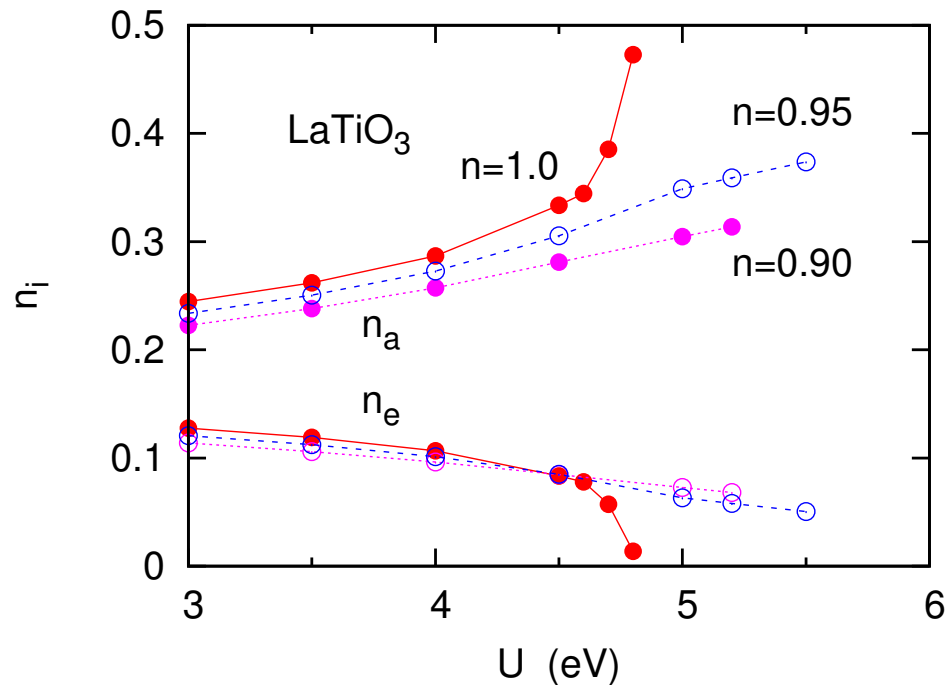


LaTiO₃

$$n_{\sigma} \approx (0.3, 0.1, 0.1) \\ \rightarrow (0.5, 0.0, 0.0)$$



$\text{La}_{1-x}\text{Sr}_x\text{TiO}_3$ $3d^{1-x}$ doping driven MIT



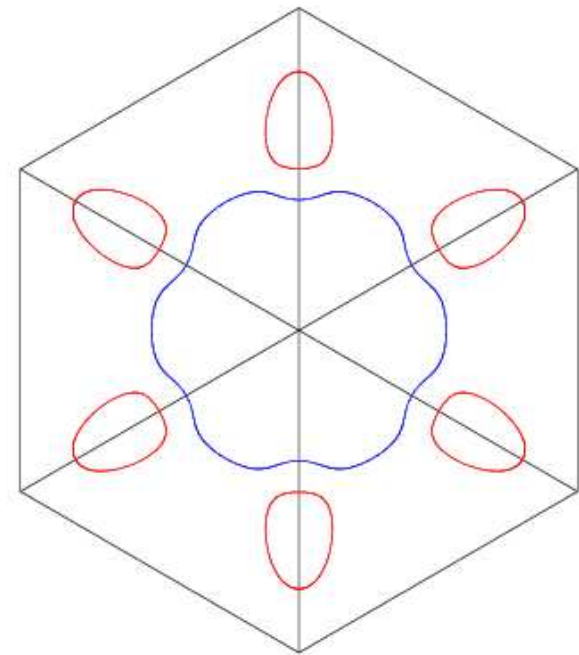
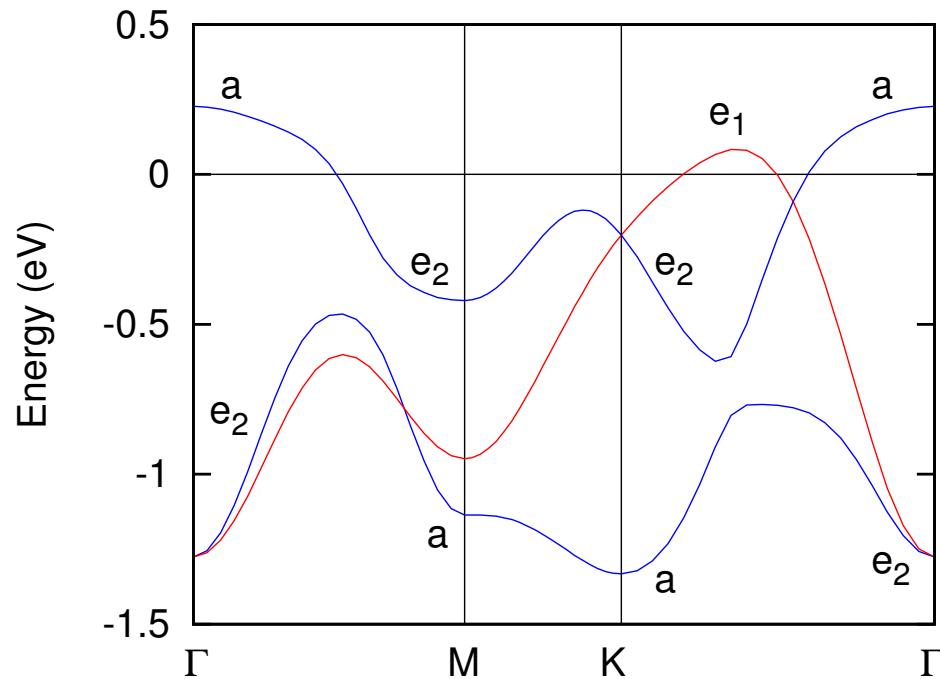
A.L. (2007)

$\text{LaTiO}_3 / \text{SrTiO}_3$ heterostructures: La / Sr interdiffusion:
 $3d^{0.95}$ inhibits $e_g \rightarrow a_g$ charge transfer: no MIT
 thin LaTiO_3 layers on SrTiO_3 :
 cubic symmetry shifts U_c upwards \rightarrow no MIT at U_{Ti}

$\text{Na}_{0.3}\text{CoO}_2$: topology of Fermi surface ?

t_{2g} bands 0.4 a_g holes 0.3 e'_g holes

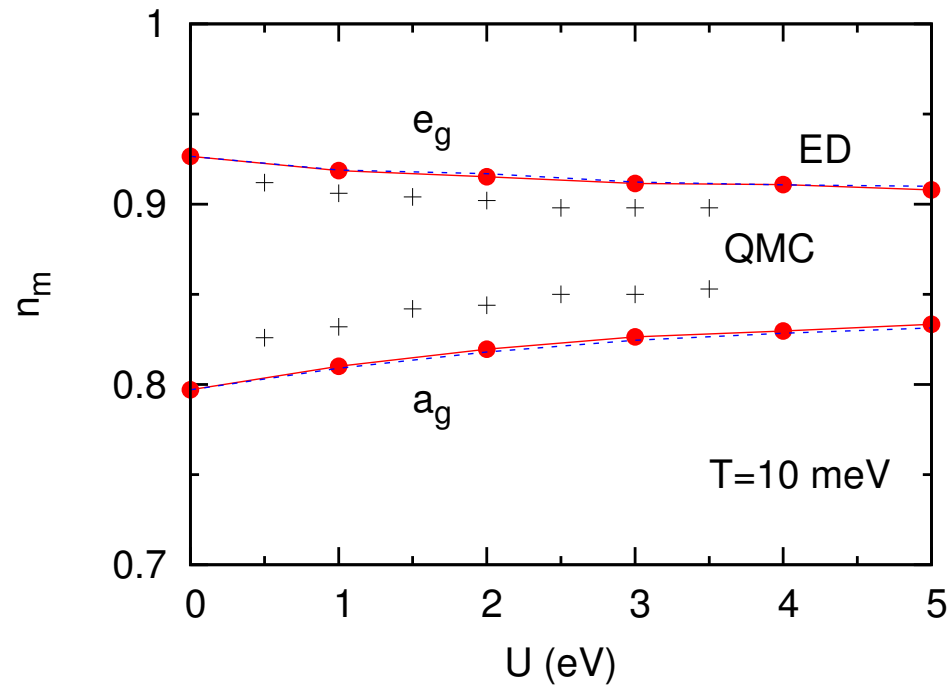
D.J. Singh, PRB (2000)



e_1 hole pockets not seen in ARPES ??

$\text{Na}_{0.3}\text{CoO}_2$ QMC vs ED / DMFT

Coulomb driven inter-orbital charge transfer for $J = U/4$

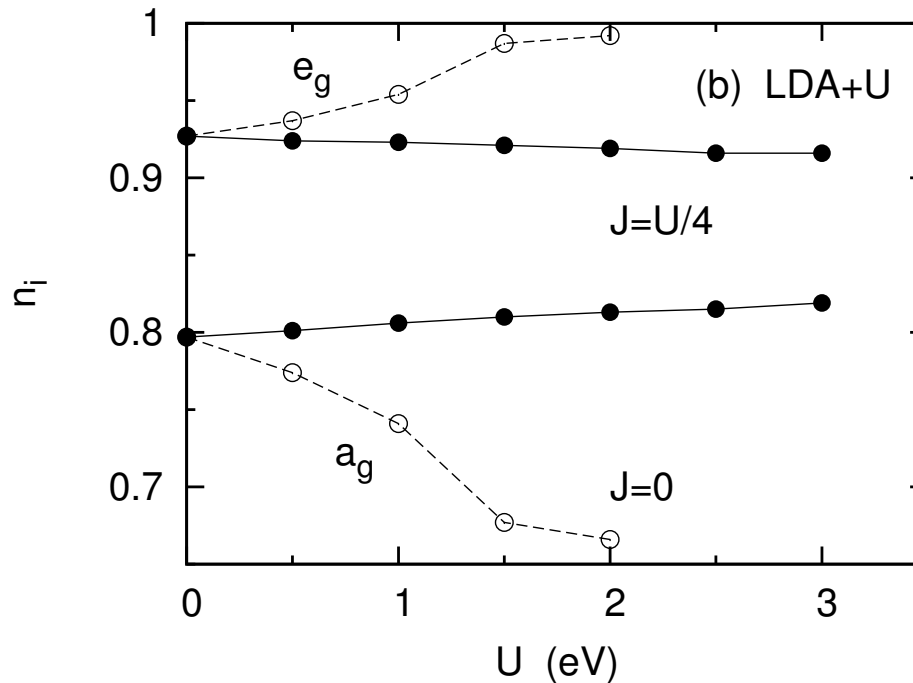


dynamical correlations: stabilization of e_g hole pockets

QMC: Ishida, Johannes + A.L. PRL (2005)

ED: Perroni, Ishida + A.L. PRB (2007)

$\text{Na}_{0.3}\text{CoO}_2$ LDA + U



Ishida, Johannes + A.L. PRL (2005)

$$\Delta\epsilon_a = \frac{2}{3}(n_e - n_a)(U - 5J)$$

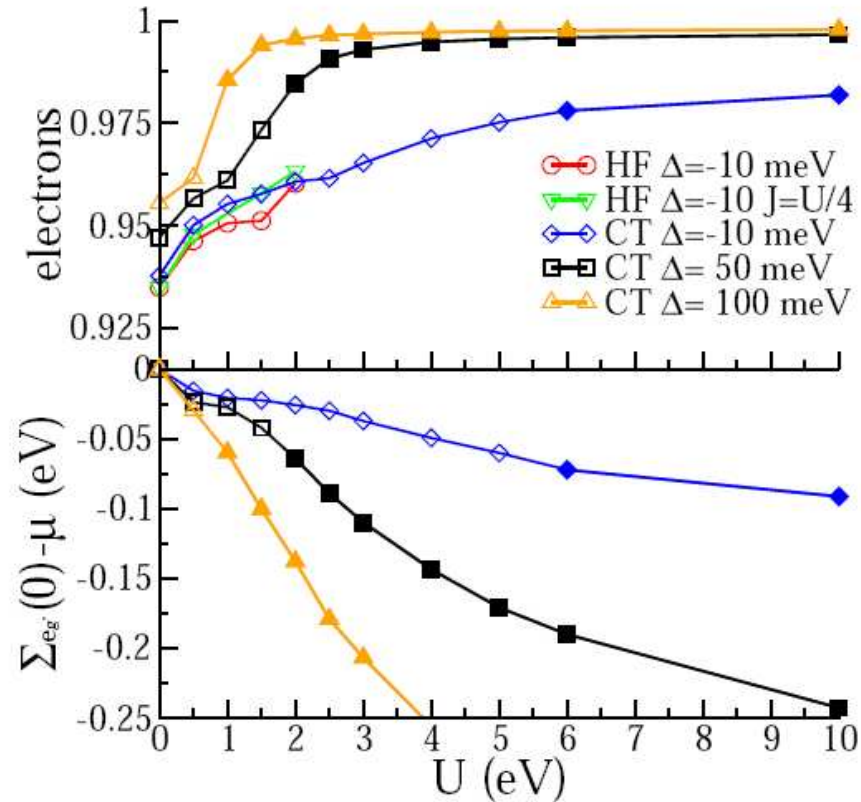
$$\Delta\epsilon_e = -\frac{1}{3}(n_e - n_a)(U - 5J) \rightarrow J=0.9 \text{ eV: } U_c=4.5 \text{ eV}$$

subtle balance:

J vs U, shape of DOS, dynamical vs static correlations

$\text{Na}_{0.3}\text{CoO}_2$ QMC + crystal field

$\Delta = \epsilon_a - \epsilon_e$: e_g bands shifted down $J=0$

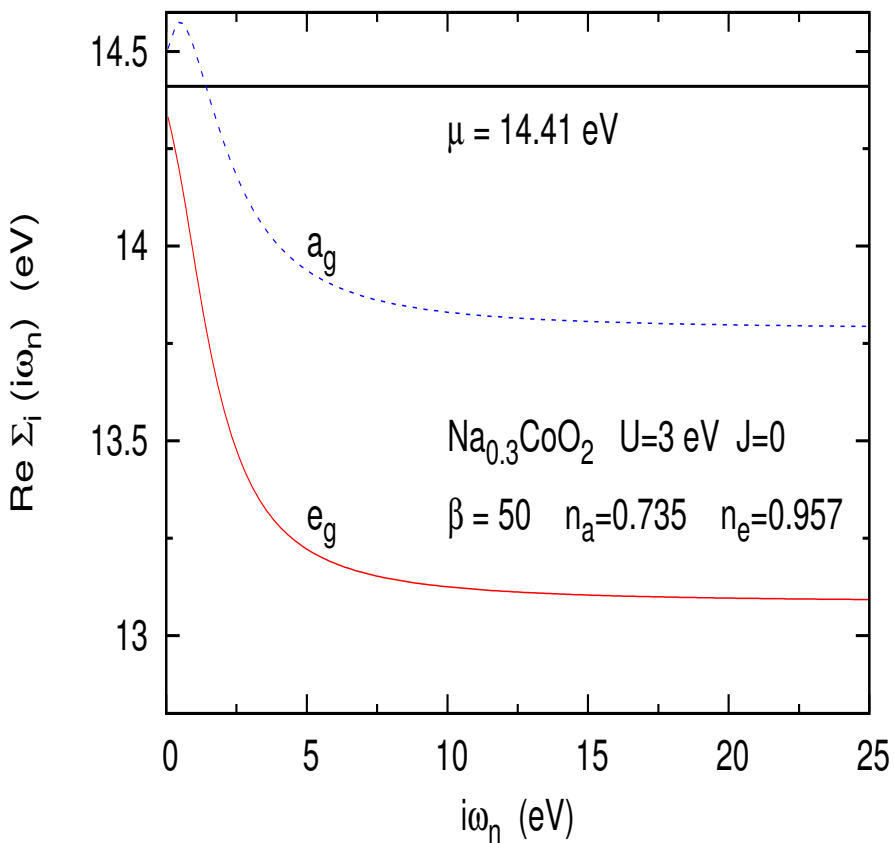


role of $H(\mathbf{k})$!

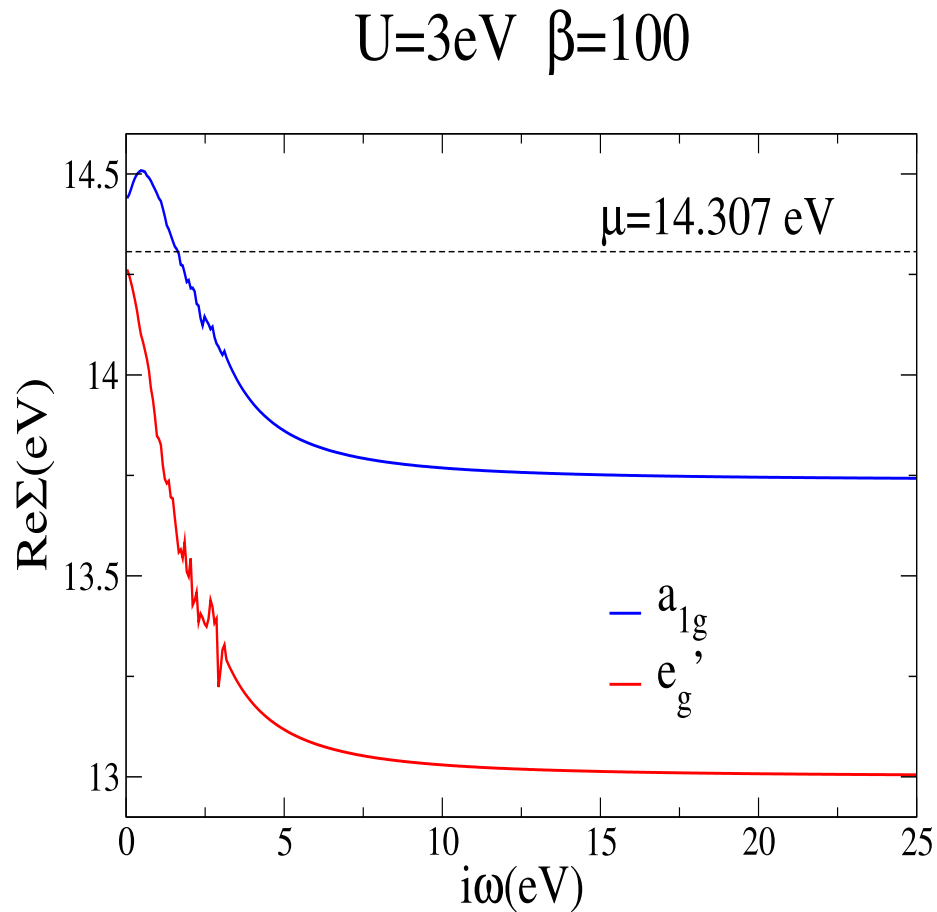
Marianetti, Haule, Kotliar, cond-mat/0612606

Na_{0.3}CoO₂

ED vs QMC same H(k)



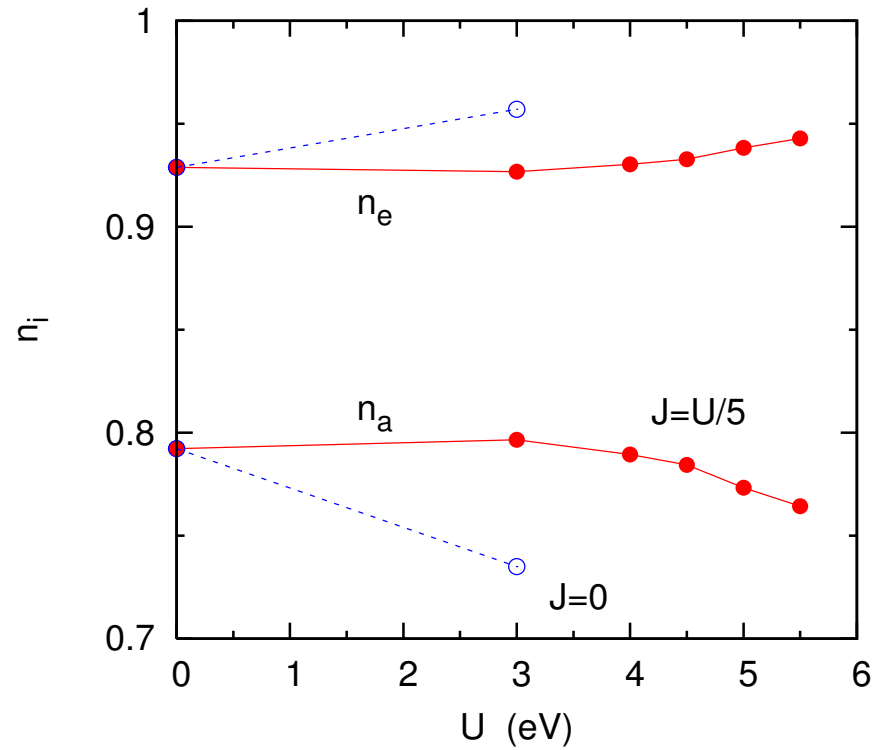
A.L. (2007)



Marianetti, Haule, Kotliar, cond-mat/0612606



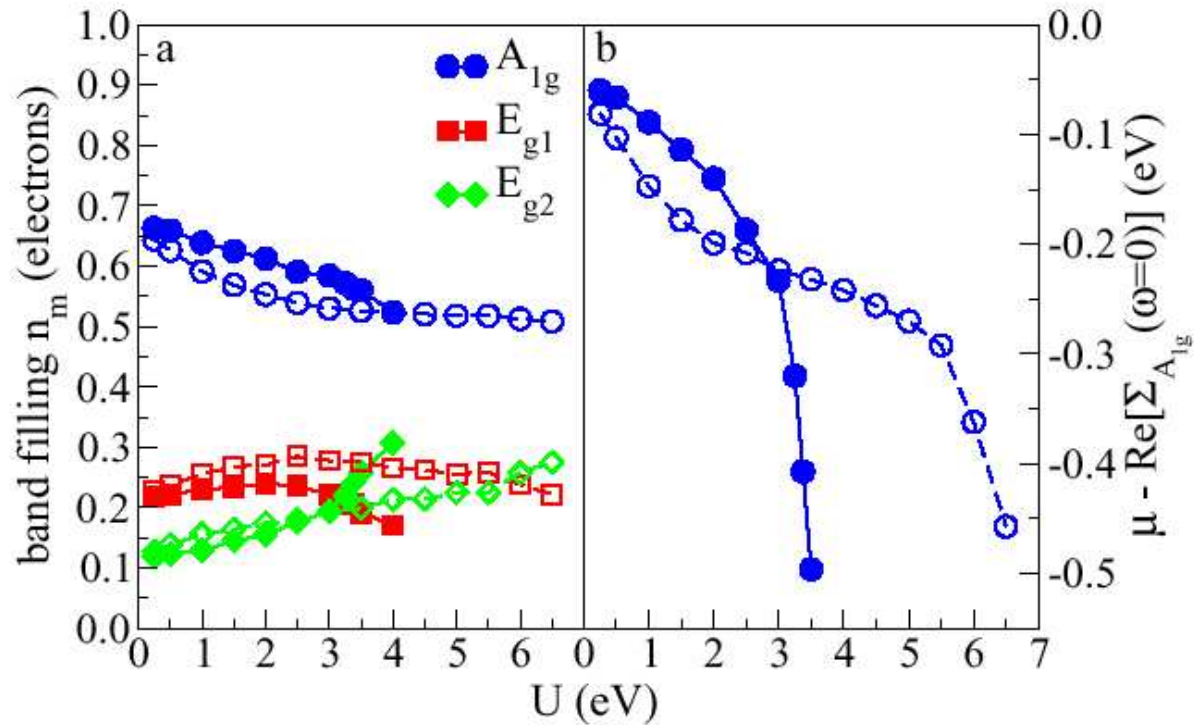
ED



H(k) Zhou et al, PRL (2005)

A.L. (2007)

BaVS₃

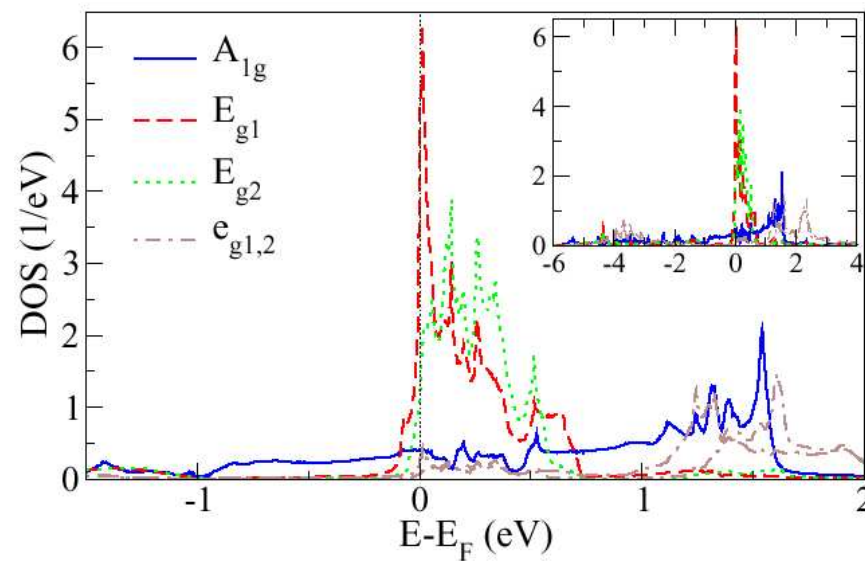
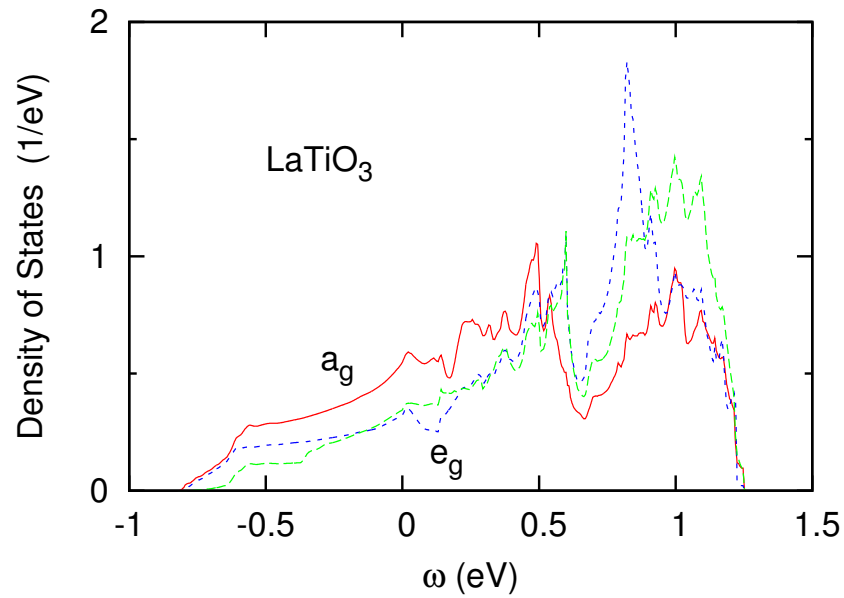


$$J = U/4 \text{ vs } J = U/7$$

Lechermann et al, PRL (2005)

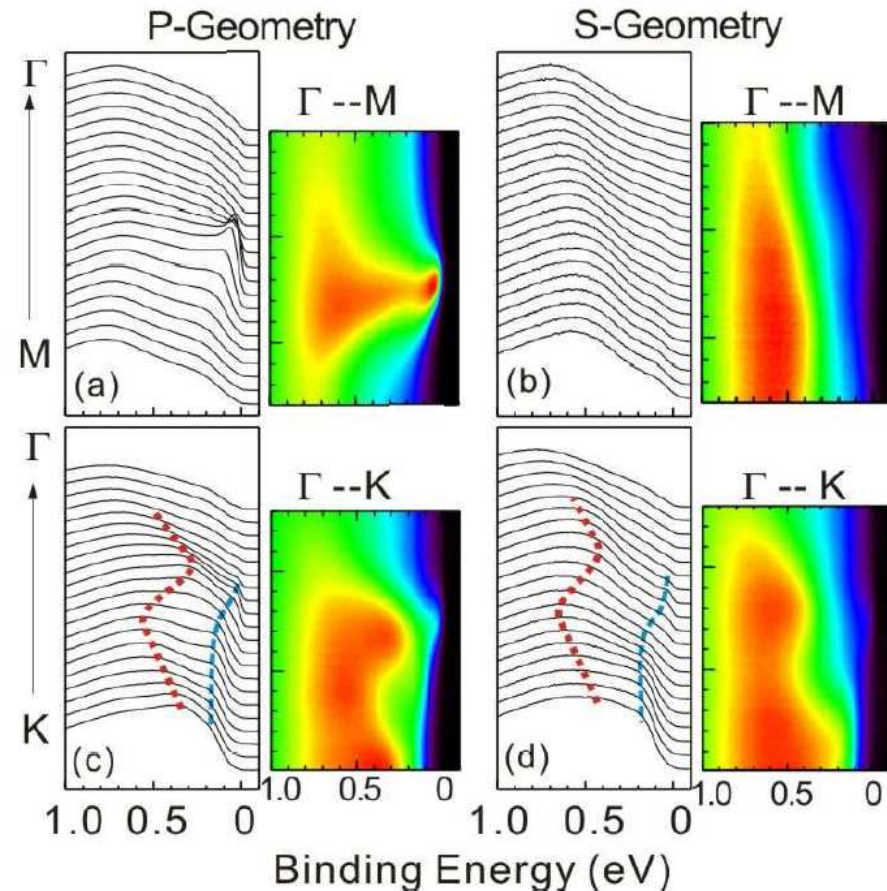
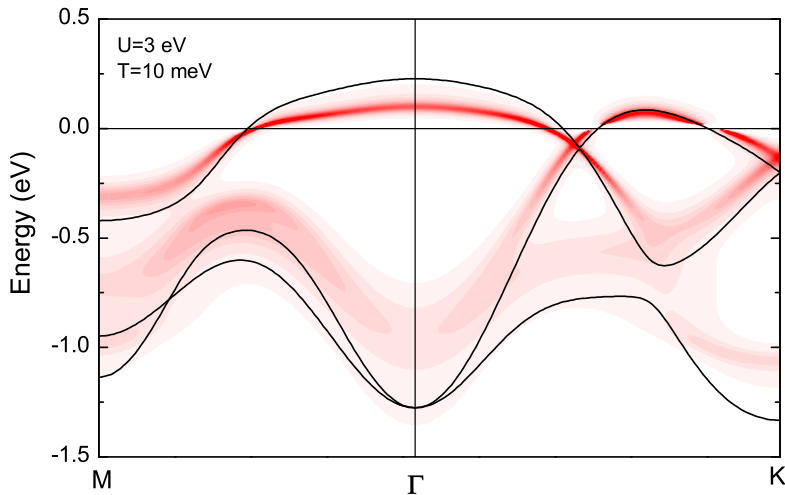
local Coulomb correlations can reduce / enhance orbital fluctuations !

LaTiO₃ vs BaVS₃: both 3d¹



opposite charge transfer: importance of density of states!

$\text{Na}_{0.3}\text{CoO}_2$ quasi-particle bands vs ARPES



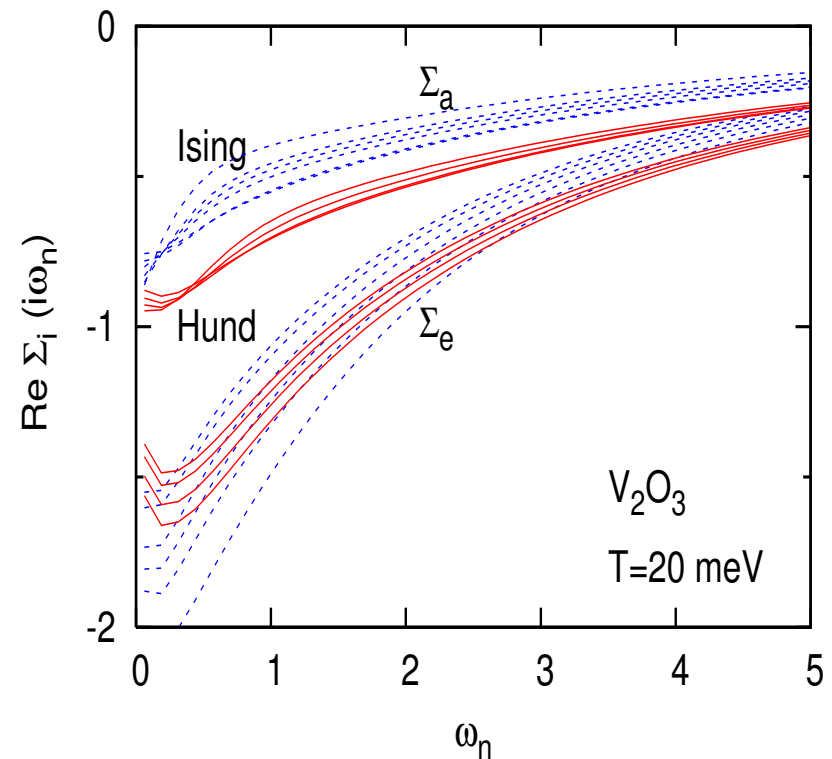
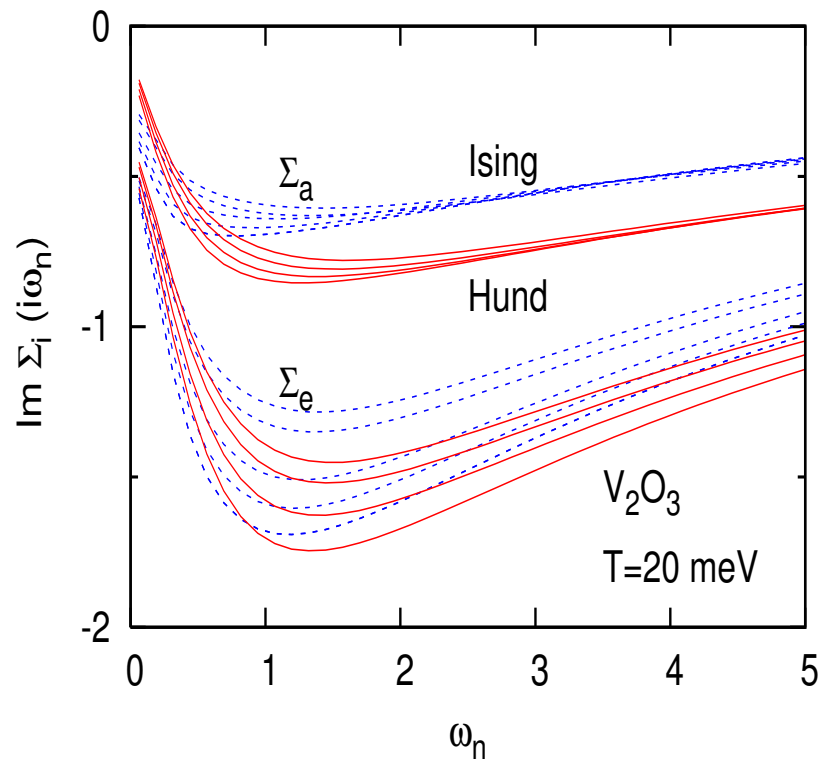
Perroni, Ishida + A.L. PRB (2007)

Qian et al PRL (2006)

$\sim 30\%$ band narrowing: $1.5 \rightarrow 1.0$ eV



ED: Hund vs Ising exchange



A.L. (2007)

Ising: nearly localized e_g :
modifies (i) a_g self-energy (ii) intra- e_g scattering
(see: two-band model !)