

# Short-range dynamical probabilistic prediction of extreme atmospheric events.

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ECODYC10. Dresden 25–29 January 2001

## American Heritage Dictionary

### ▶ ex · treme:

...

3. Extending far beyond the norm

4. Of the greatest severity, drastic

...



# AIMS

- ▶ What I mean by *extreme* ?
- ▶ Why is it *extreme*? Clues to prediction.
- ▶ Is it predictable? Why?
- ▶ How is extreme weather forecast nowadays?





# What I mean by extreme?

**Gare Montparnasse, 22 October 1895**

Different definitions:

- ▶ Maxima/minima
- ▶ Magnitude
- ▶ Rarity
- ▶ Severity

“Man can believe the impossible,  
but man can never believe the  
improbable.” - Oscar Wilde

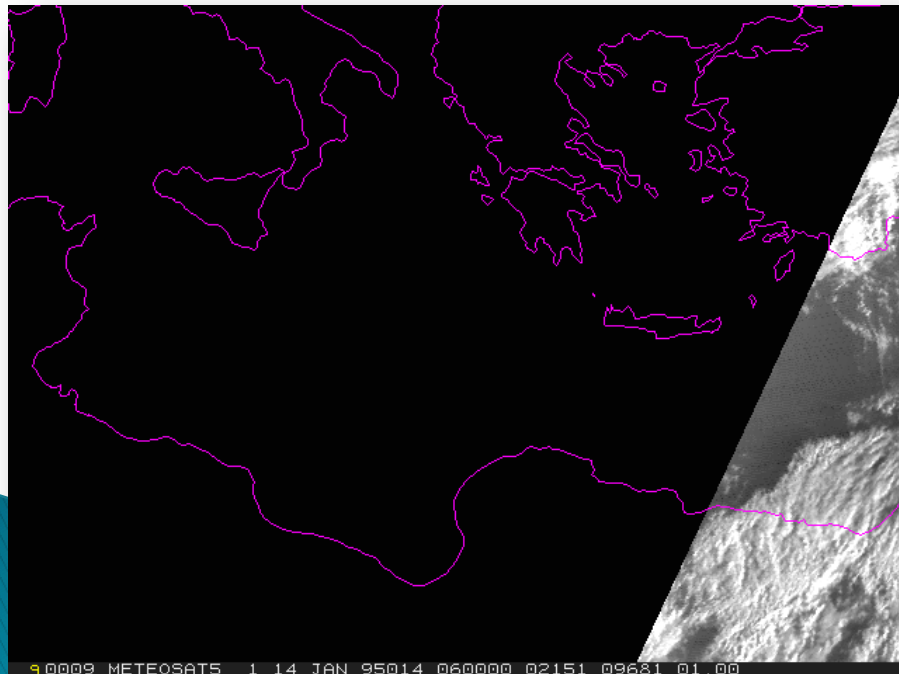


D. B Stephenson



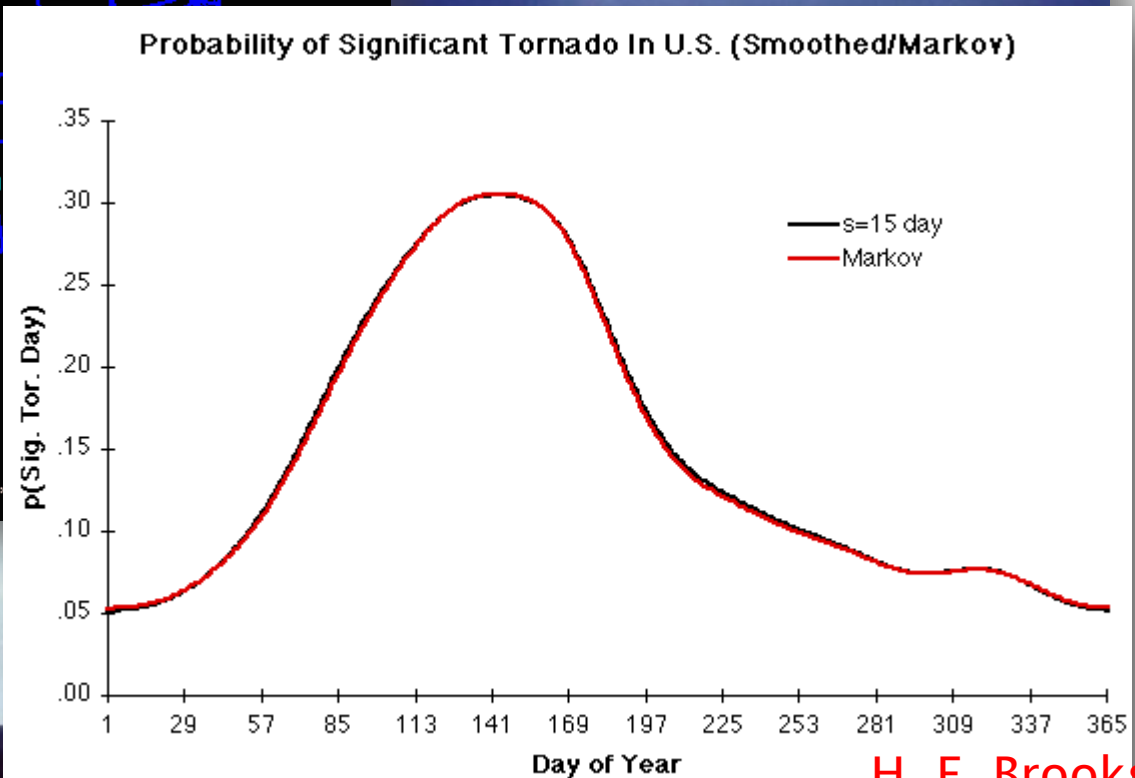
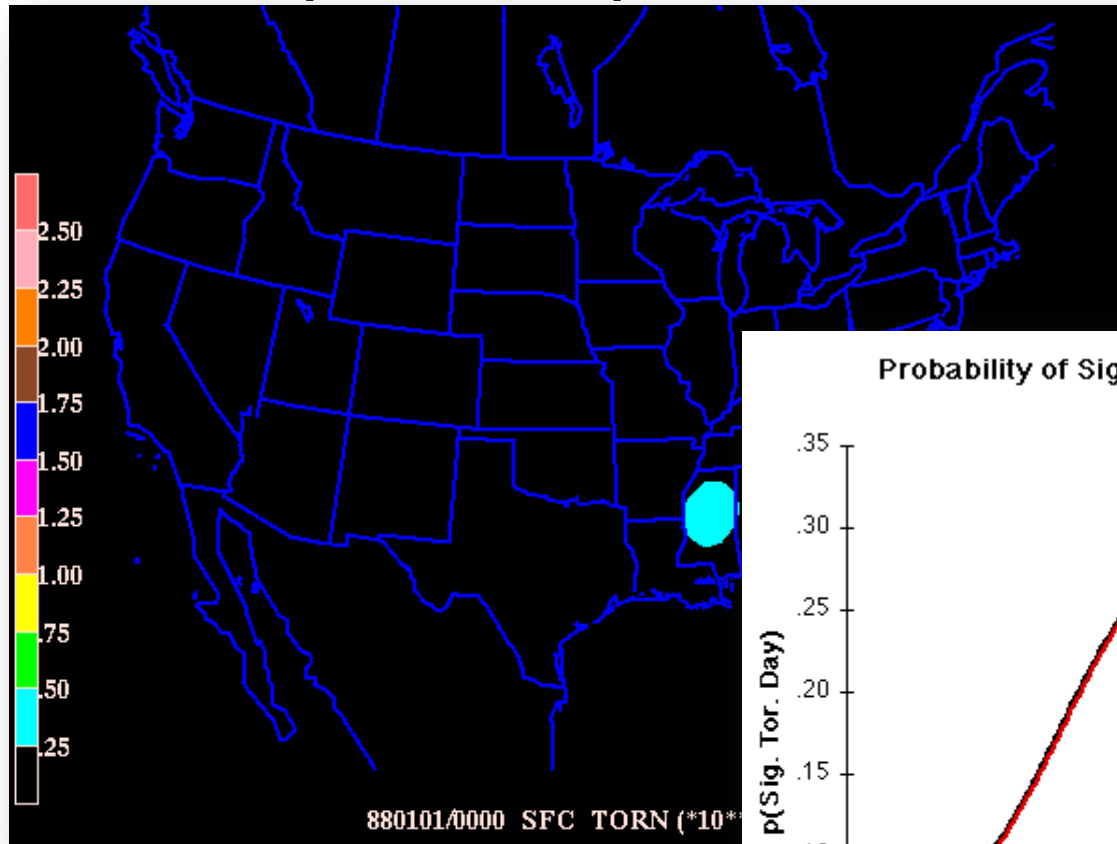
# What is extreme weather?

- ▶ Magnitude exceeding thresholds  
(*far beyond the norm*)



# What is extreme weather?

- ▶ Rarity (*far beyond normal frequency*)



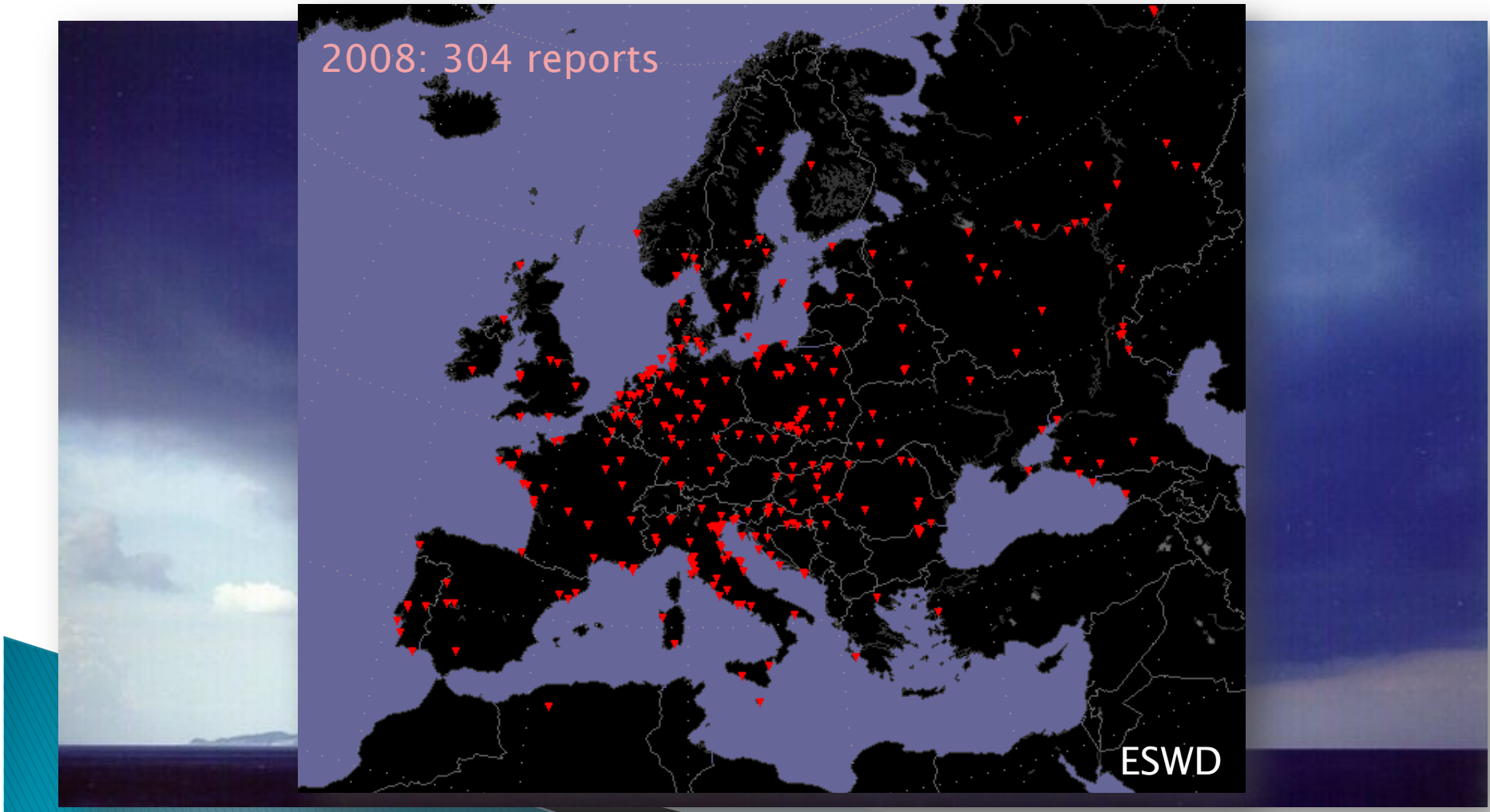
# What is extreme weather?

- ▶ Rarity (*far beyond normal frequency*)

*Tornadoes in Europe?*

2008: 304 reports

ESWD





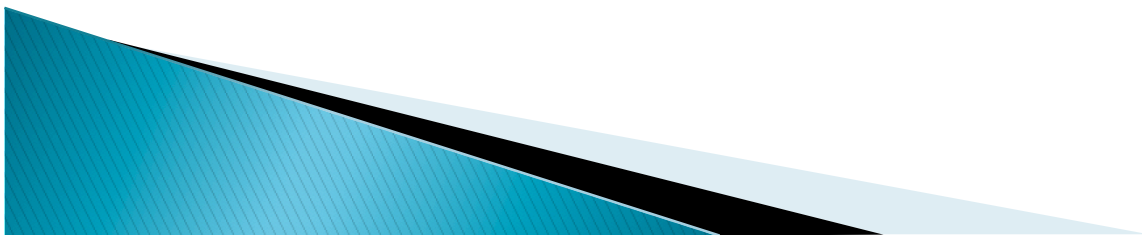
# What is extreme weather?

- ▶ Severity (*greatest severity, drastic*)

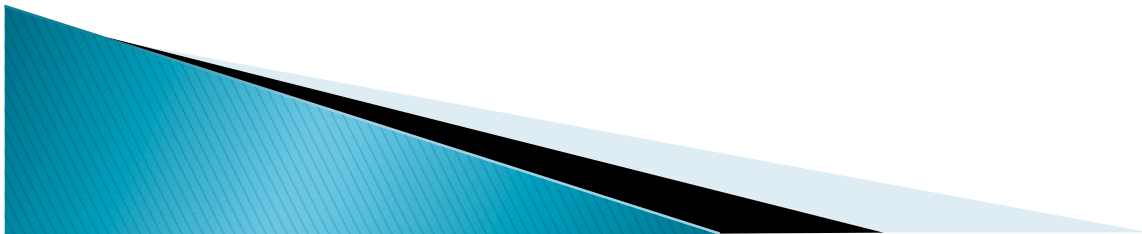


# What is extreme weather?

- ▶ I'll use the "*4. of the greatest severity, drastic*" definition of extreme:
  - SPC: **Tornadoes, Large Hail and Strong winds**
  - ESWD: SPCs + **Heavy Rain**



Why is it extreme?





# Why is it extreme (*severe, drastic*)?

Systems with high *energy density*:

- ▶ Tornadoes:  $10^4$  kWh in a very small volume [ $10^4$  m<sup>3</sup>]  
(Hurricanes:  $10^{10}$  kWh in  $10^{15}$  m<sup>3</sup>)
- ▶ Strong Wind:  $10^4$  J/m<sup>3</sup>
- ▶ Large hail:  $10^2$  J/m<sup>2</sup>
- ▶ *Heavy Rain*

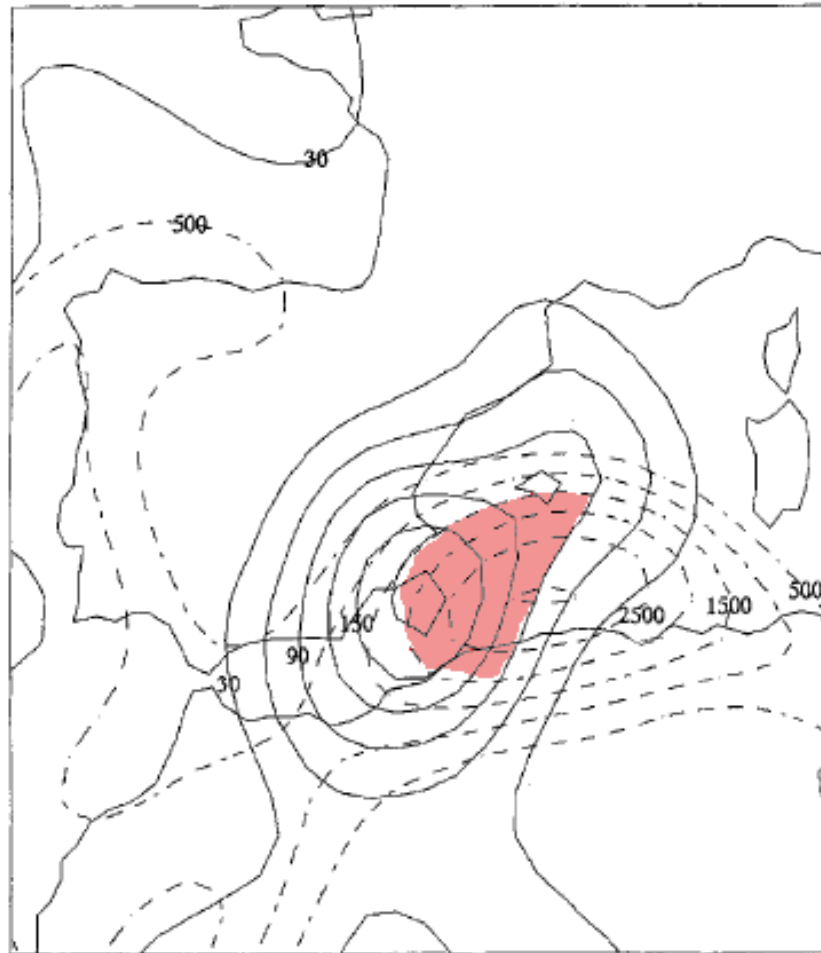


# Why is it rare (*far below frequent*)?

- ▶ Extreme events occur:

- ▶ Useful model

- Tornadoes: C
- Heavy rain: C
- Large Hail: C



convec

nces

ingredients

ear + Low LCL

ty + PW

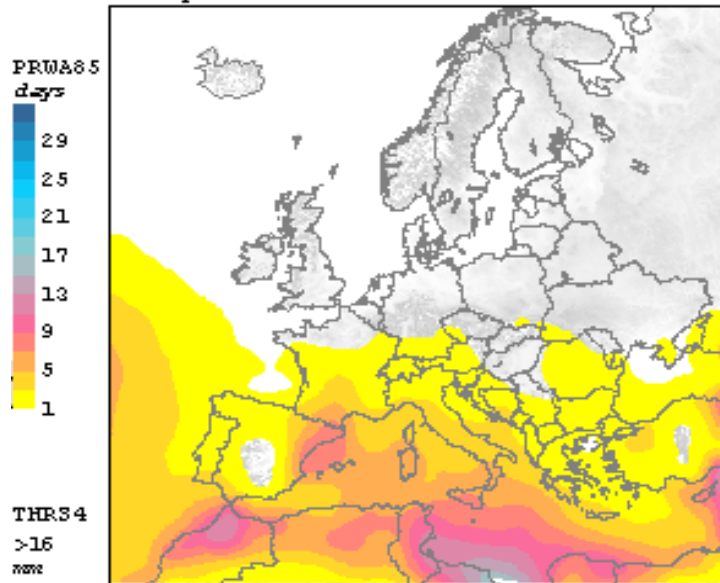
profile of T/H

Extreme weather is rare because overlap of all ingredients is rare

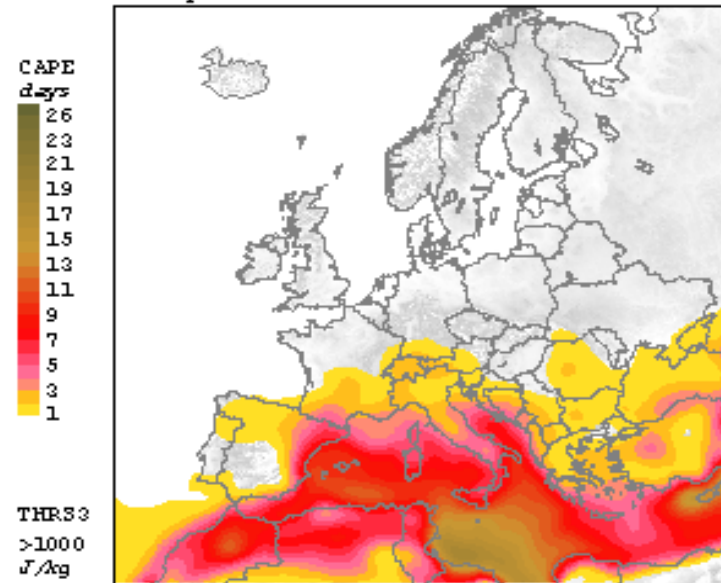
# Why is it rare (*far below frequent*)?

Extreme weather is rare because overlap of all ingredients is rare

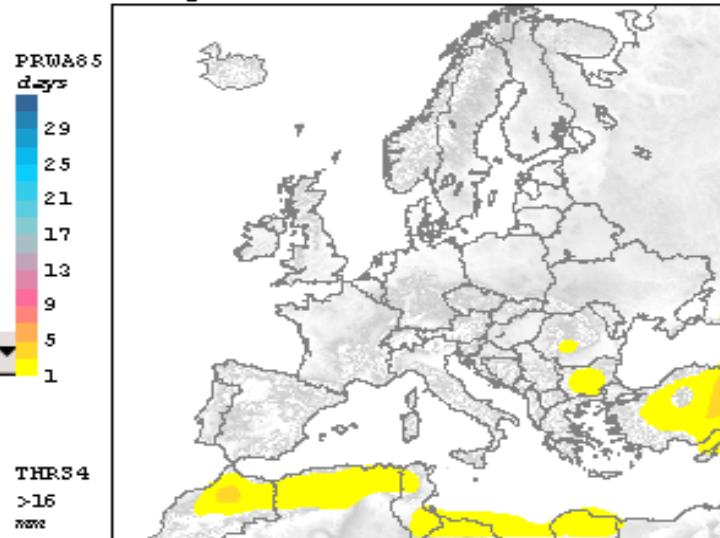
MONTH: Sep CLIMATOLOGY: 12 UTC 1971-2000



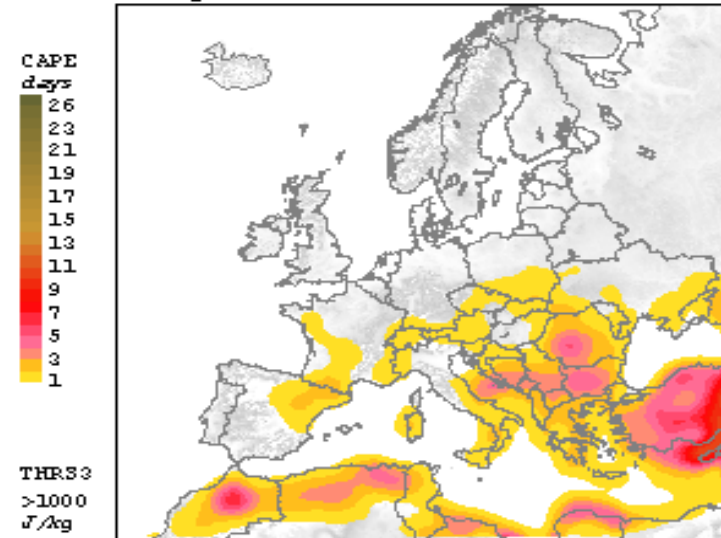
MONTH: Sep CLIMATOLOGY: 12 UTC 1971-2000



MONTH: May CLIMATOLOGY: 12 UTC 1971-2000



MONTH: May CLIMATOLOGY: 12 UTC 1971-2000

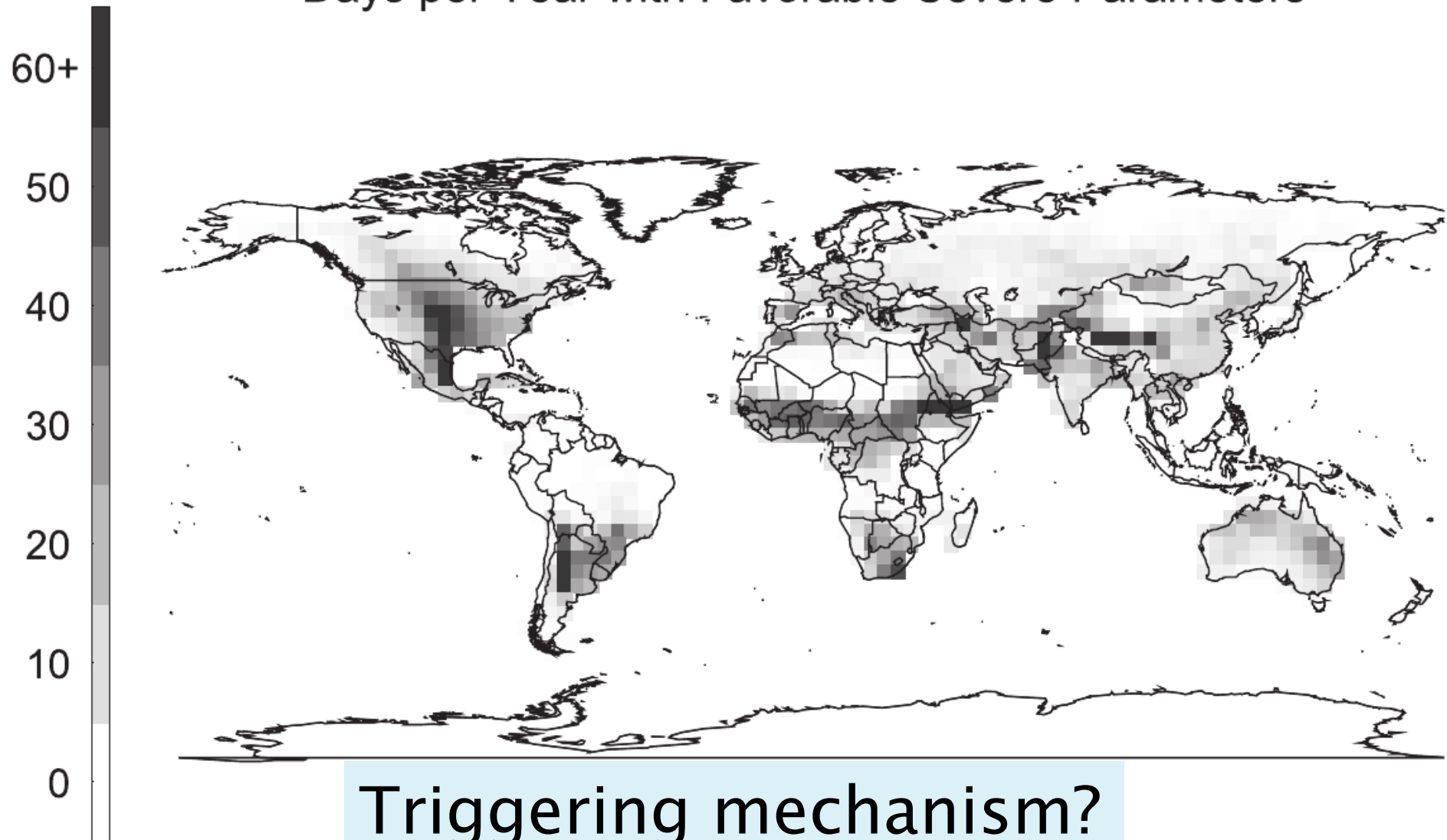




# Why is it rare (*far below frequent*)?

Extreme weather is rare because overlap of all ingredients is rare

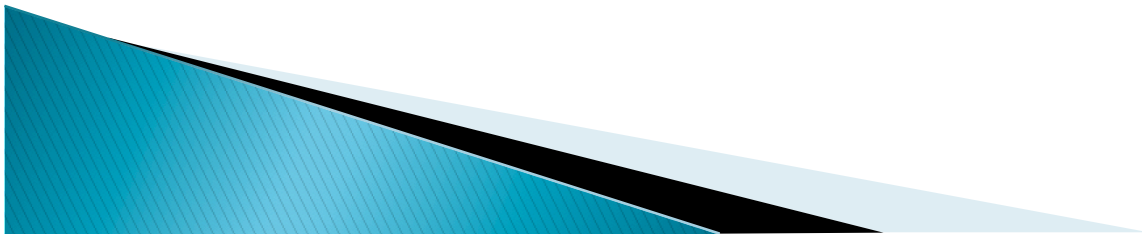
Days per Year with Favorable Severe Parameters



Triggering mechanism?

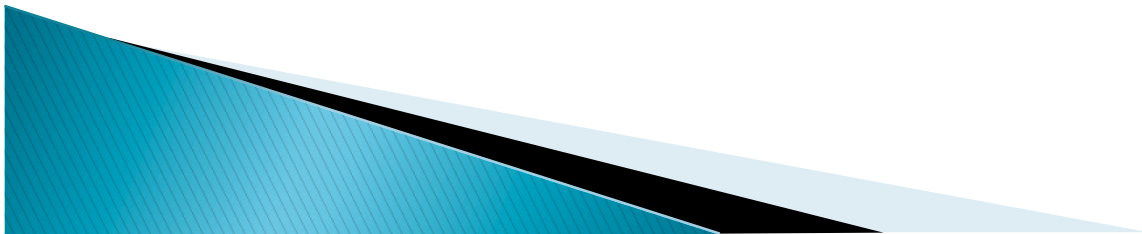
H. E. Brooks

Is it predictable?



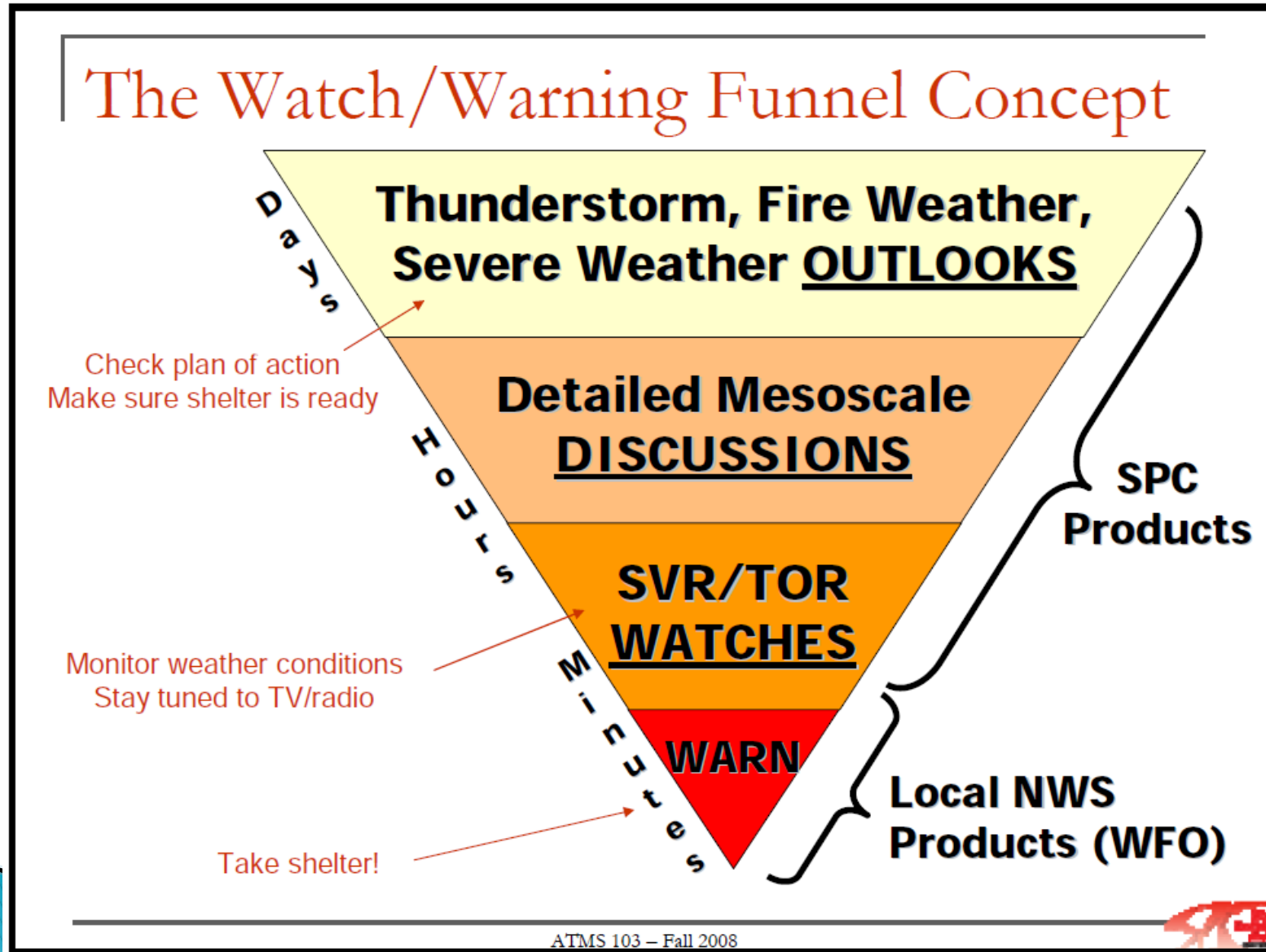
“Predictable?? Don’t even know how to define predictability in a useful way for severe weather!”

H. E. Brooks

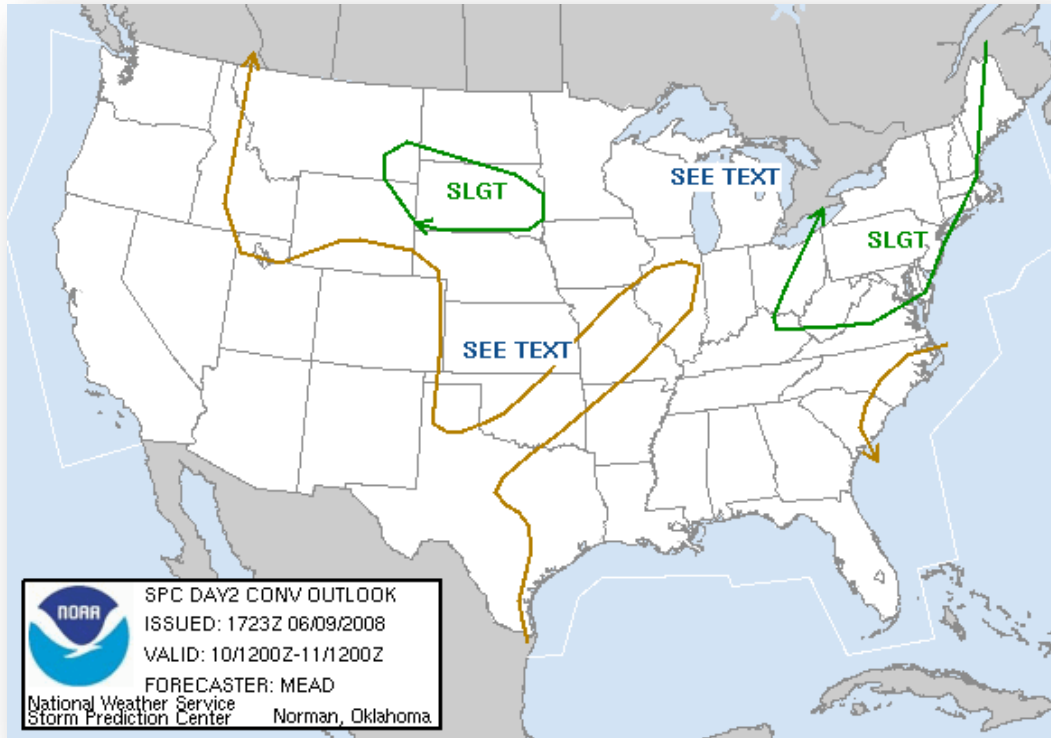




# Is it predictable?



# Is it predictable?

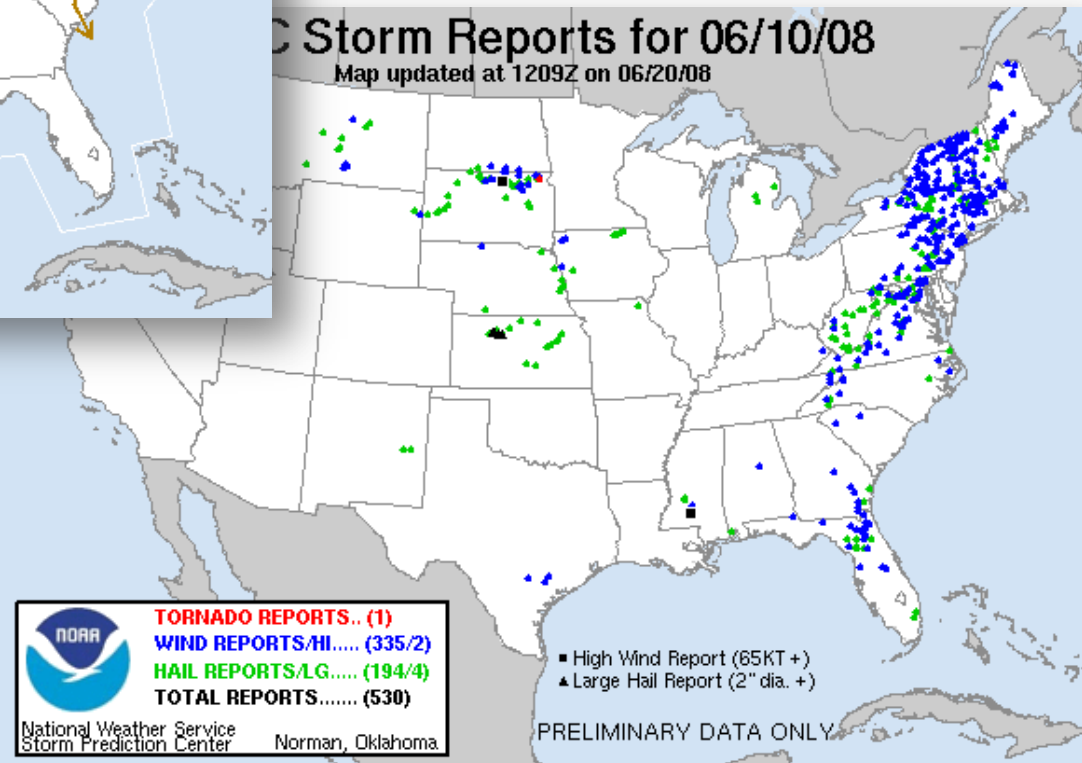


SPC 1 DAY FORECAST

## SEVERE REPORTS

### Severe Storm Reports for 06/10/08

Map updated at 1209Z on 06/20/08



# Is it predictable?

- ▶ Atmospheric convection (at least our models of it) is:

- highly non-linear
- chaotic (highly sensitive to environment)

- ▶ Crucial aspects for valuable forecasts:

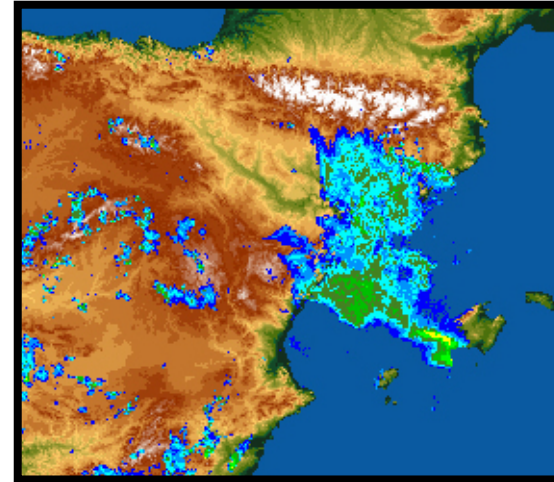
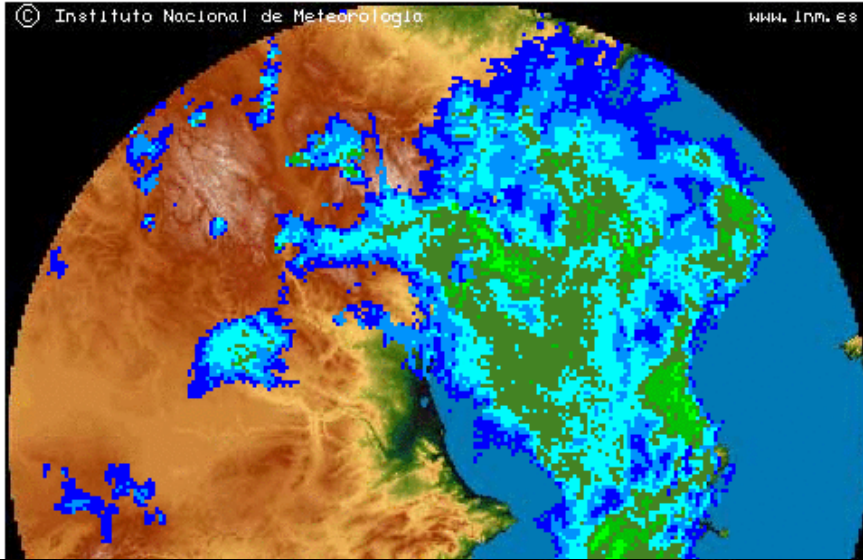
- **Initiation** (where and when)
- **Evolution** (where and when)
- **Type or organization** (how intense)
- **Intensity** (how intense)

... depend on small scale structures not observed by regular observing systems (e.g. Stensrud and Frisch 1994).



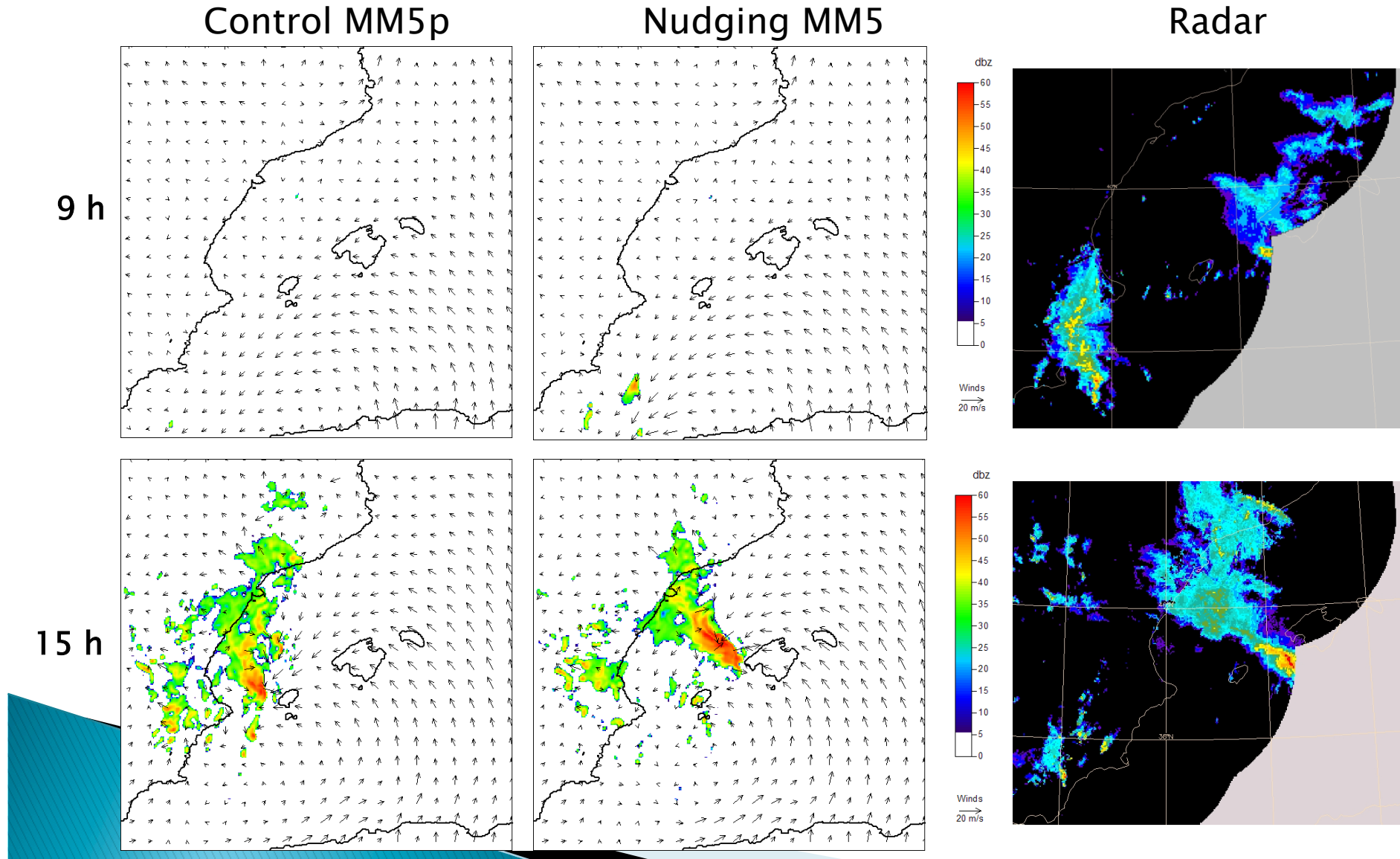


# Limited predictability: 4th October 2007



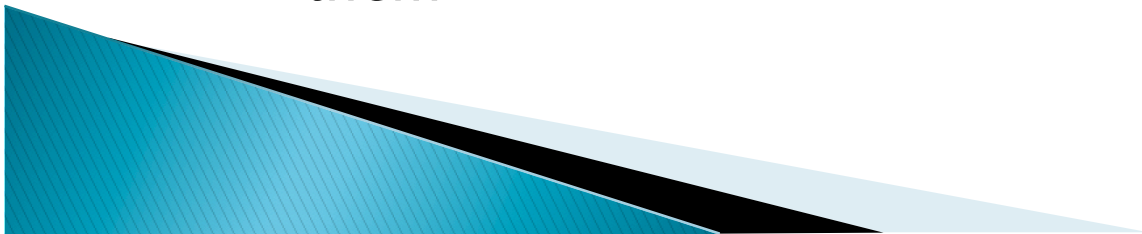


# Limited predictability: 4th October 2007



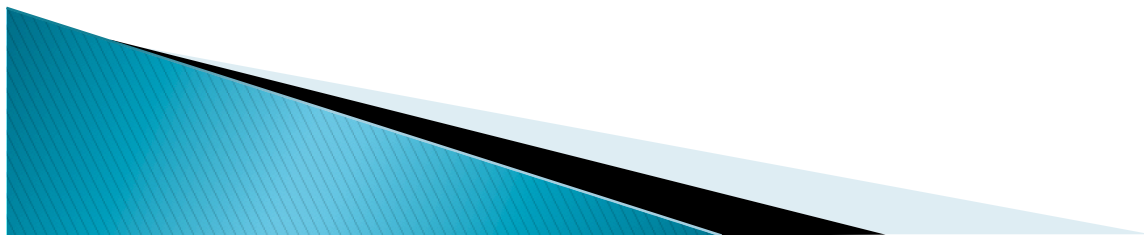
# Error growth

- ▶ Regarding error growth and scales (Lorenz 1993):
  1. Small errors in coarse structures double in  $\sim 2-3$  days. As errors become larger the growth rate subsides
  2. **Small errors in fine structure grow much faster, doubling in hours**
  3. Errors in fine structure produce errors in the coarse structure (!!!!)
  4. Averaged and accumulated quantities might be more predictable than the systems responsible for them.



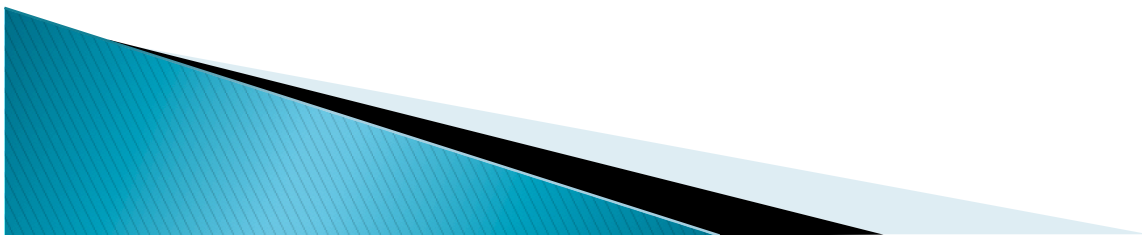
# Is it predictable?

- ▶ **NOAA/NWS target for tornado lead-time prediction:**
  - 2004: 13 minutes for 2012
  - 2008: 30 minutes for 2025
  - 2010: “Warn of Forecast” project



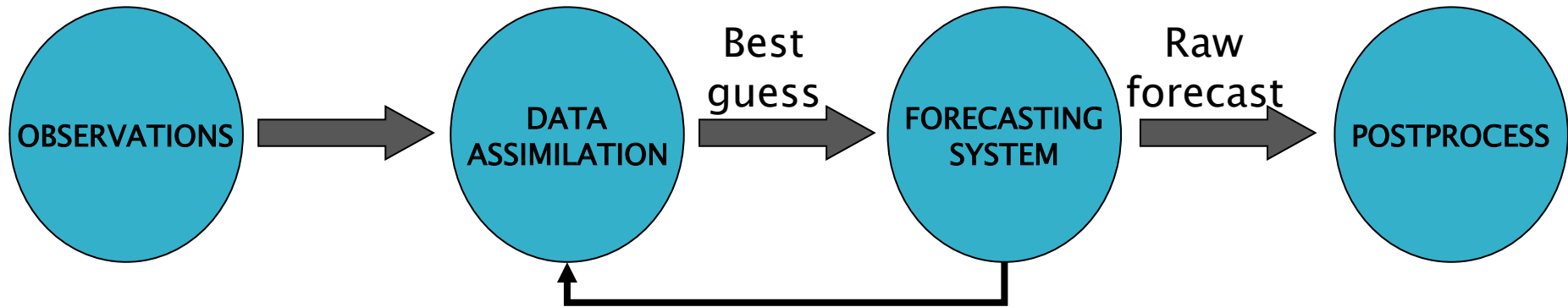
# How is it predicted?

- ▶ **Few minutes: Nowcasting + Emergency management protocols**
- ▶ **Hours and days: Numerical forecasts**

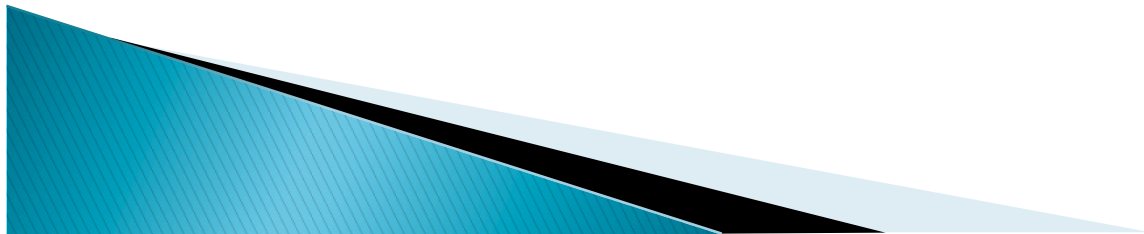
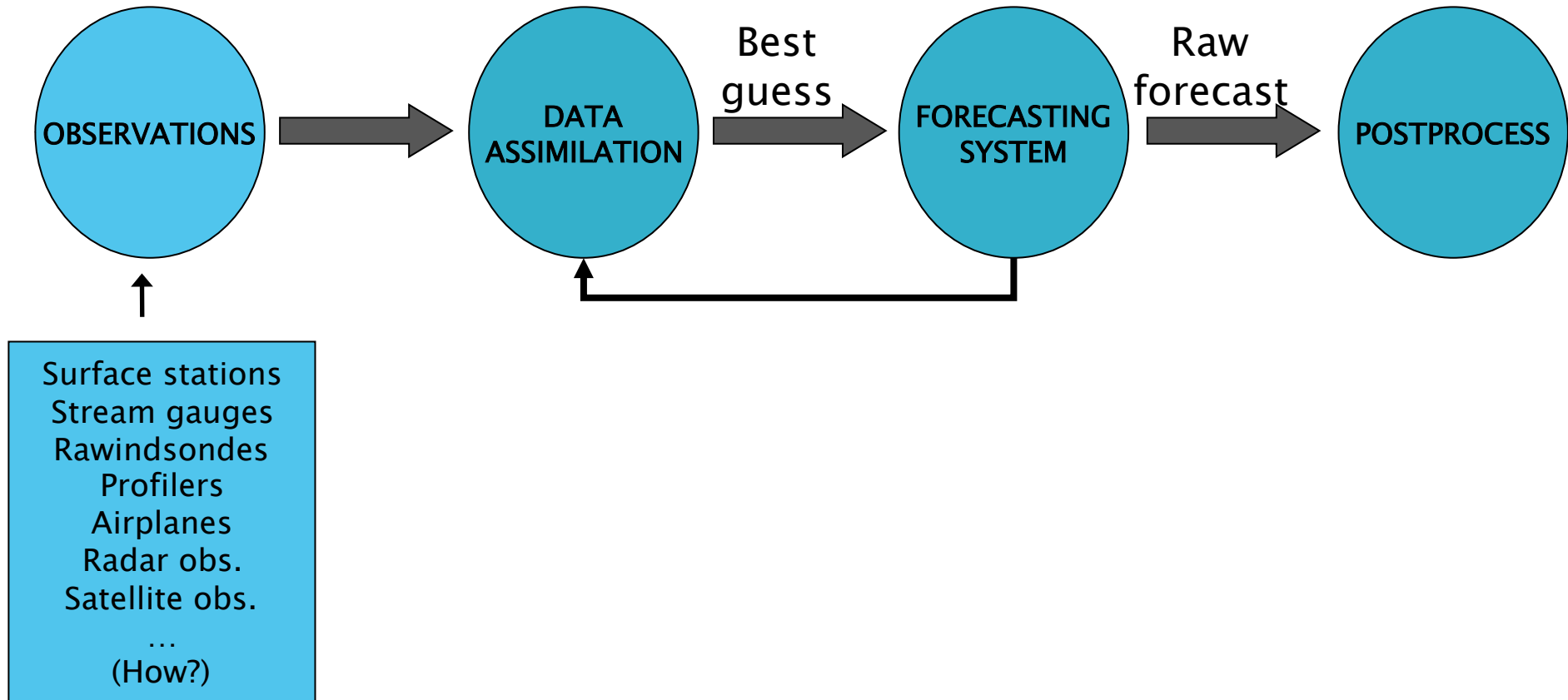




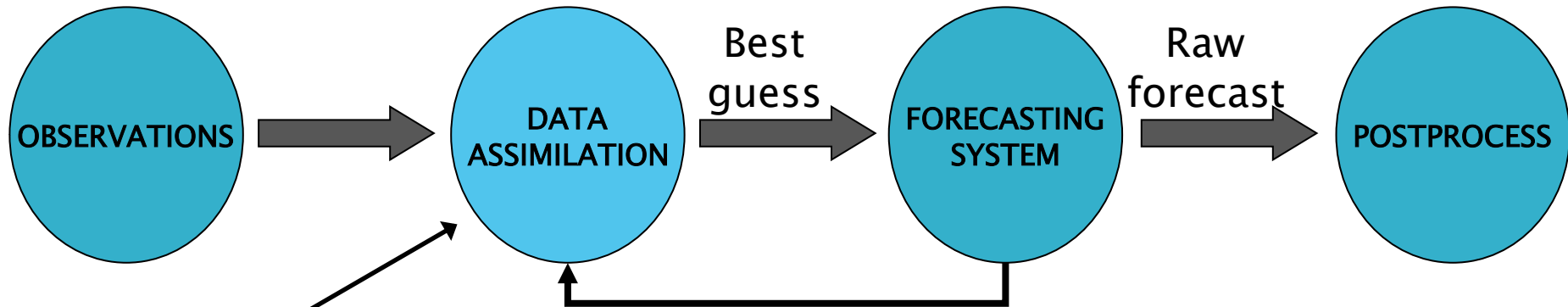
# Numerical forecast



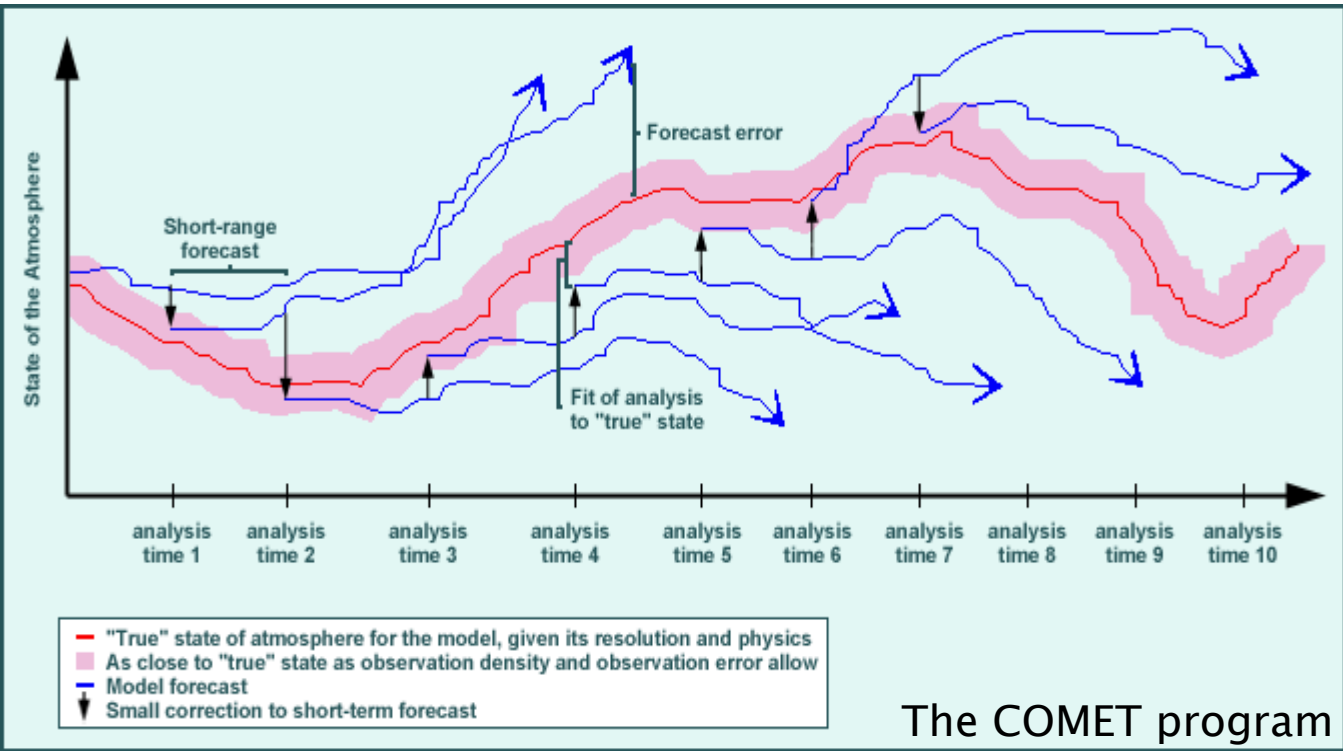
# Numerical forecast



# Numerical forecast

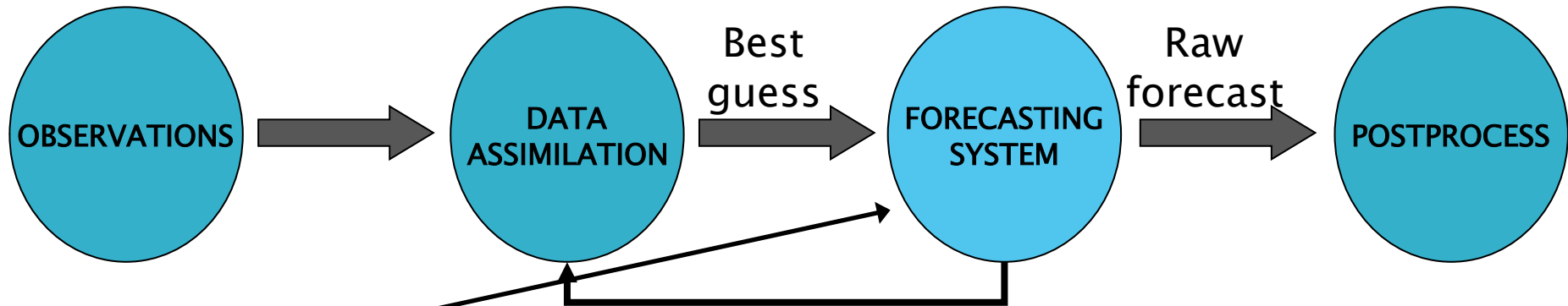


- OI
- Kalman Filters
- 3D-VAR
- 4D-VAR
- Bayesian Stats.
- Ensemble KF
- ...
- ALSO**
- Lagged Avg.
- Singular Vect
- Bred Vect
- Adj. methods
- ...



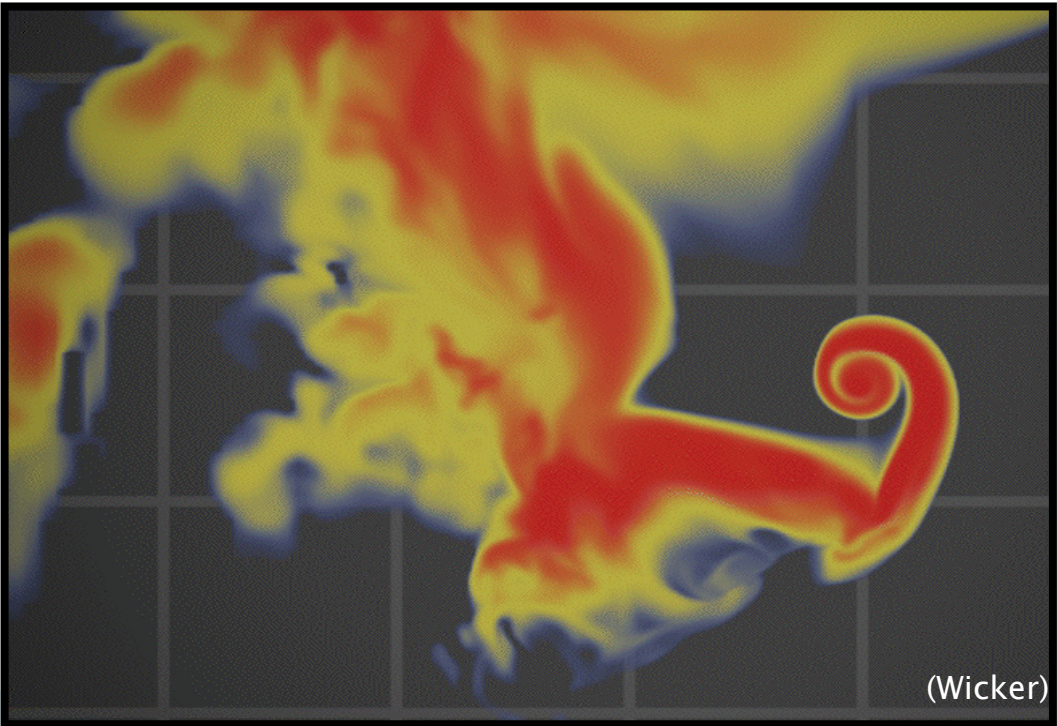
The COMET program

# Numerical forecast



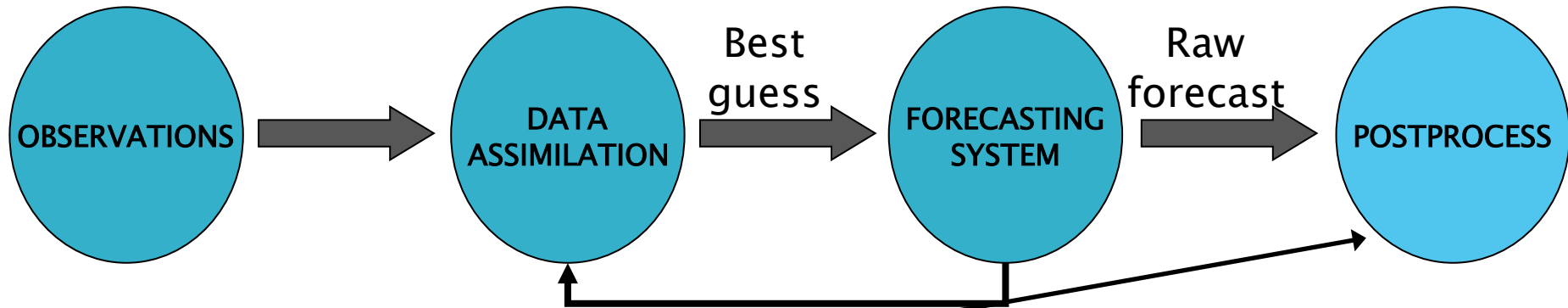
**SINGLE MODEL**  
IFS, GFS, ETA, UK,  
MM5, WRF,  
HIRLAM, ... (long)

**ENSEMBLE**  
Multi-physics  
Multi-model  
Stochastic Physics



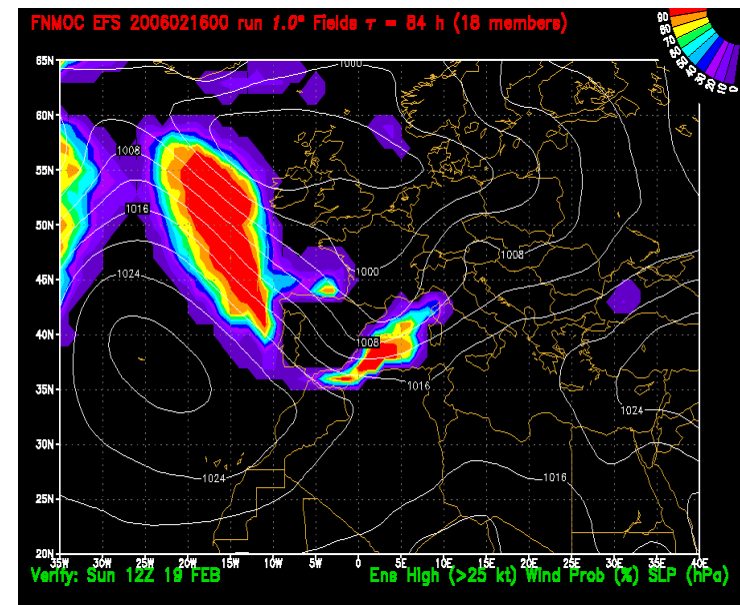
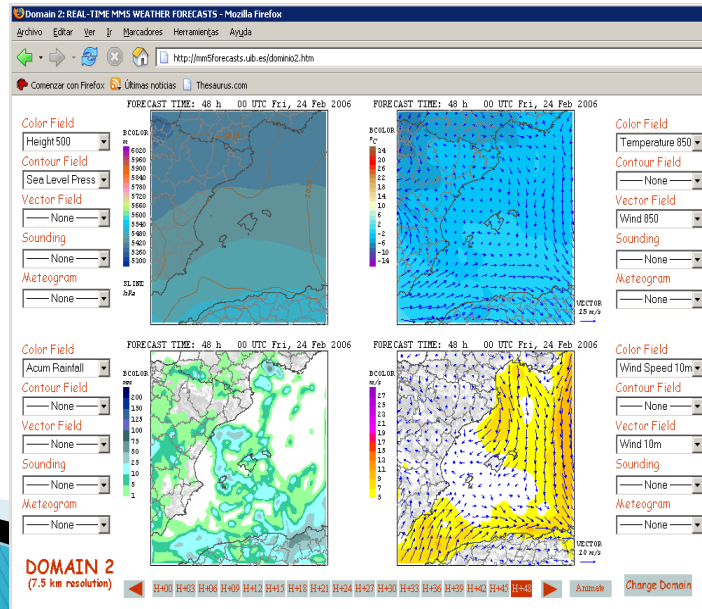


# Numerical forecast

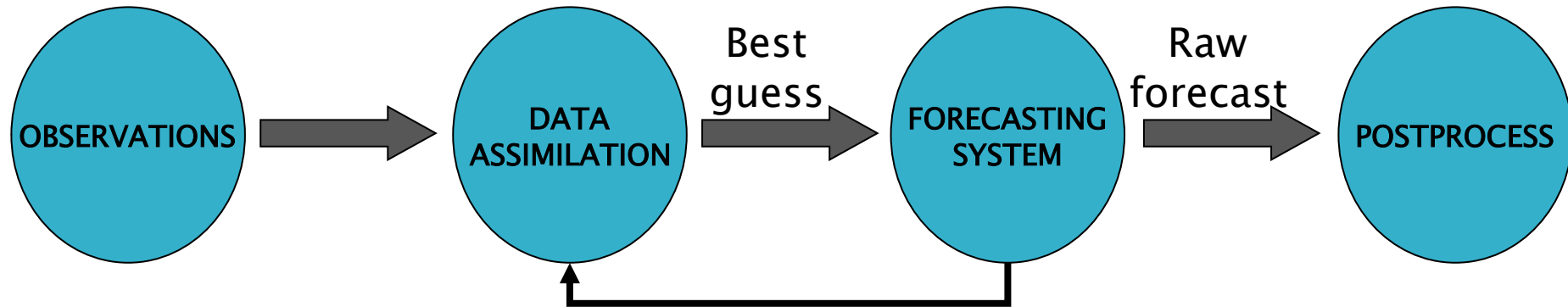


**CORRECTION**  
 MOS, Multilinear regression, BIAS removal, calibration, human filter

**END-USER DEMANDS**  
 Adapted forecasts, Probabilistic products



# Numerical forecast. Errors



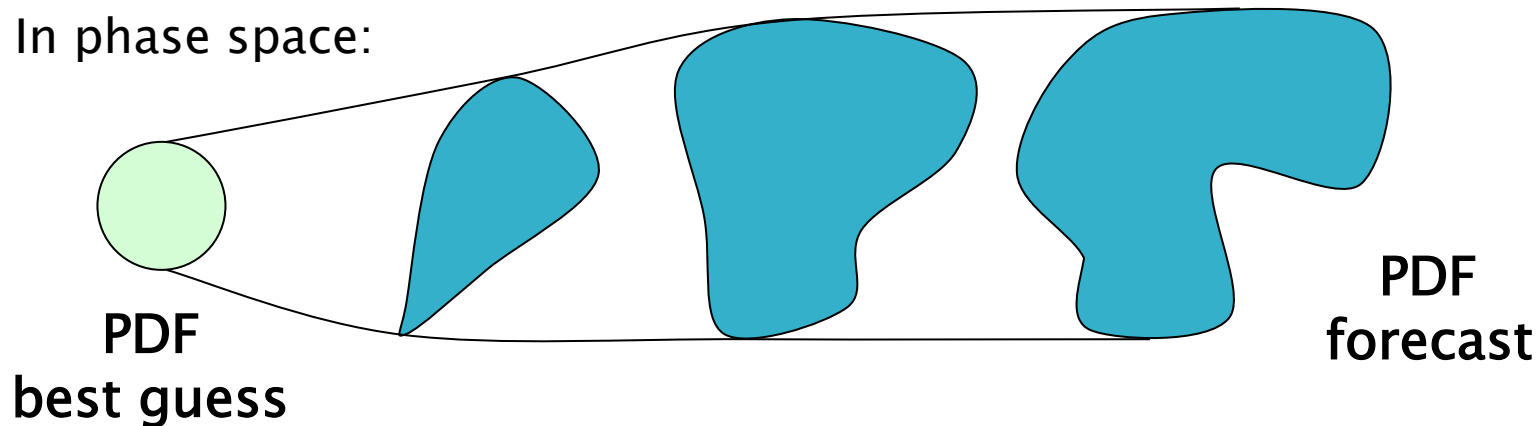
- ▶ Errors are present in each of the steps in the forecasting system, coping with (both reducing and accounting for) these errors is currently focus of active research
- ▶ “Forecasts cannot be used to their best advantage unless **forecast uncertainty is quantified** and expressed to users” (Winkler and Murphy, 1979)
- ▶ Smith (2002): **“to sell any forecast as unequivocal is to invite lawsuits”**

# Coping with errors

- ▶ The state of the atmosphere is described by a probability density function that we ought to evolve in time to get a forecast pdf:

$$\dot{\rho} = f(\rho)$$

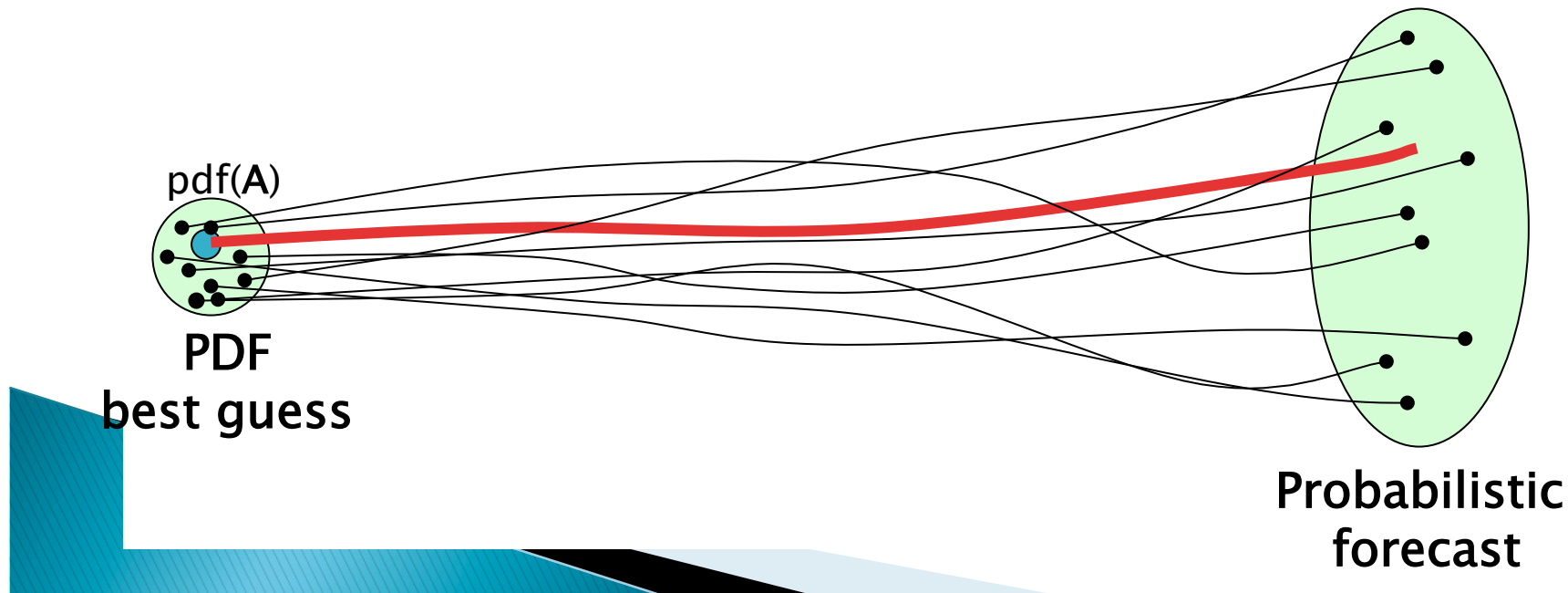
In phase space:



**HOW??**

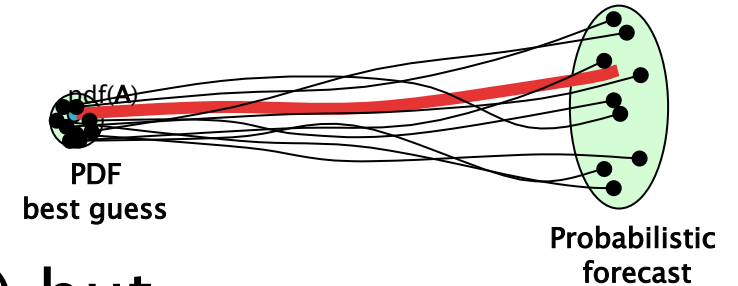
# Ensemble methods

- ▶ The Fokker–Plank equation cannot be solved yet and the current approximation is to explore the pdf of plausible atmospheric states taking an ensemble of samples and evolving each one independently





# Coping with errors



- ▶ The idea is clear (even clever) but...
- ▶ Hands on:
  - VERY expensive HR forecasts (limited members)
  - So, optimization of resources (business) is crucial

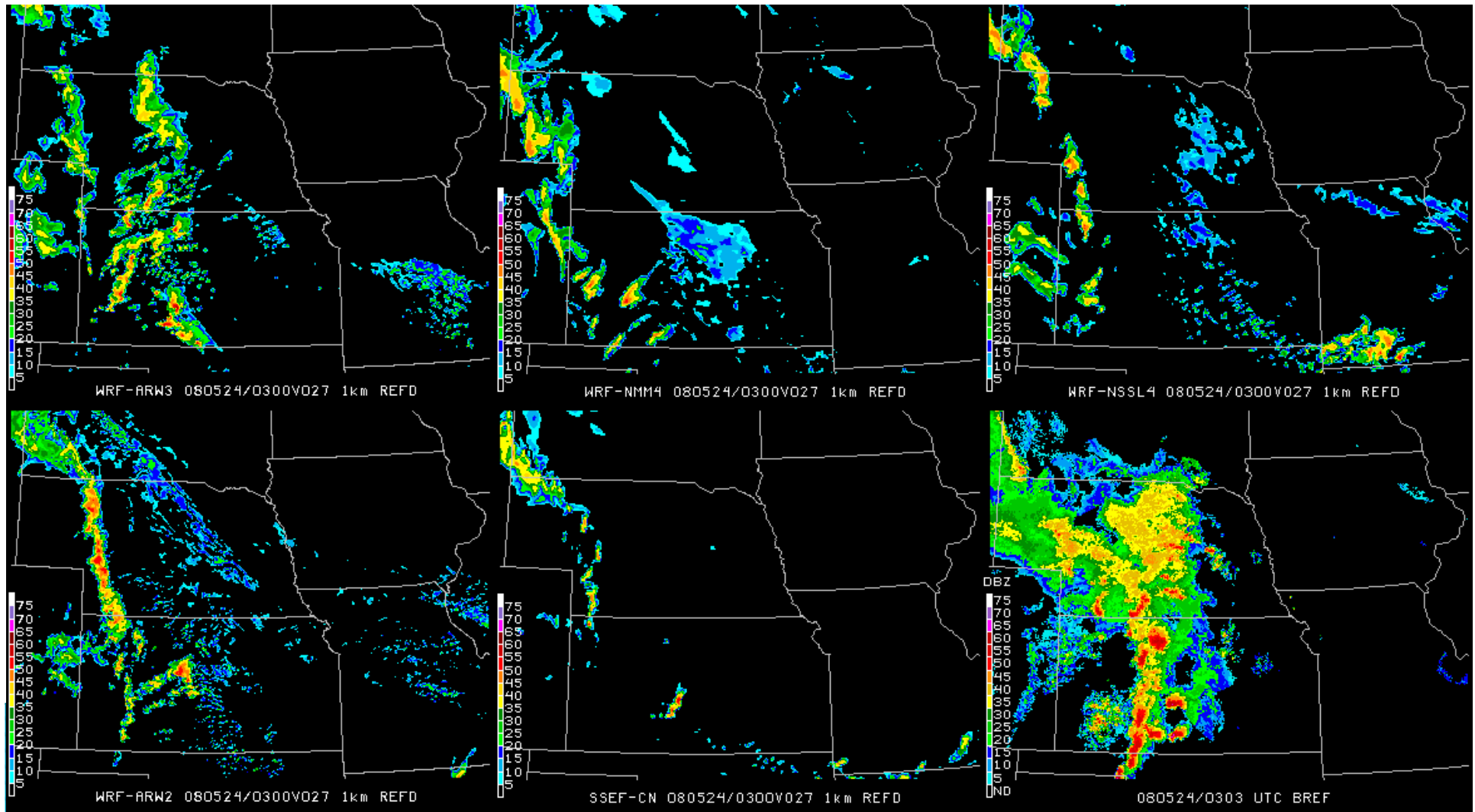
## How to sample the subspace of forecast uncertainties?

If we want to use ensembles of deterministic runs:

- Perturbing the observations
- Perturbing the IC
- Perturbing the model



# Example: experimental ensemble



Jack Kain. SPC/NSSL Spring Program 2008

# What's available? Ensemble methods

- ▶ Synoptic/large mesoscale:
  - **Montecarlo** (mid- 1900's).
  - **EnKF**: Multiple assimilation cycles with perturbed observations, modulated by previous ensemble performance statistics.
  - Most unstable nonlinear modes:
    - **Singular Vectors**: Tangent linear approximation (ECMWF)
    - **Bred vectors**: Future MU modes are estimated from past nonlinear MU modes (NCEP)



# What's available? Ensemble methods

Mesoscale ( $\sim 5\text{km}$  res):

Larger IC uncertainties: d.f.  $\uparrow$  # obs  $\downarrow$

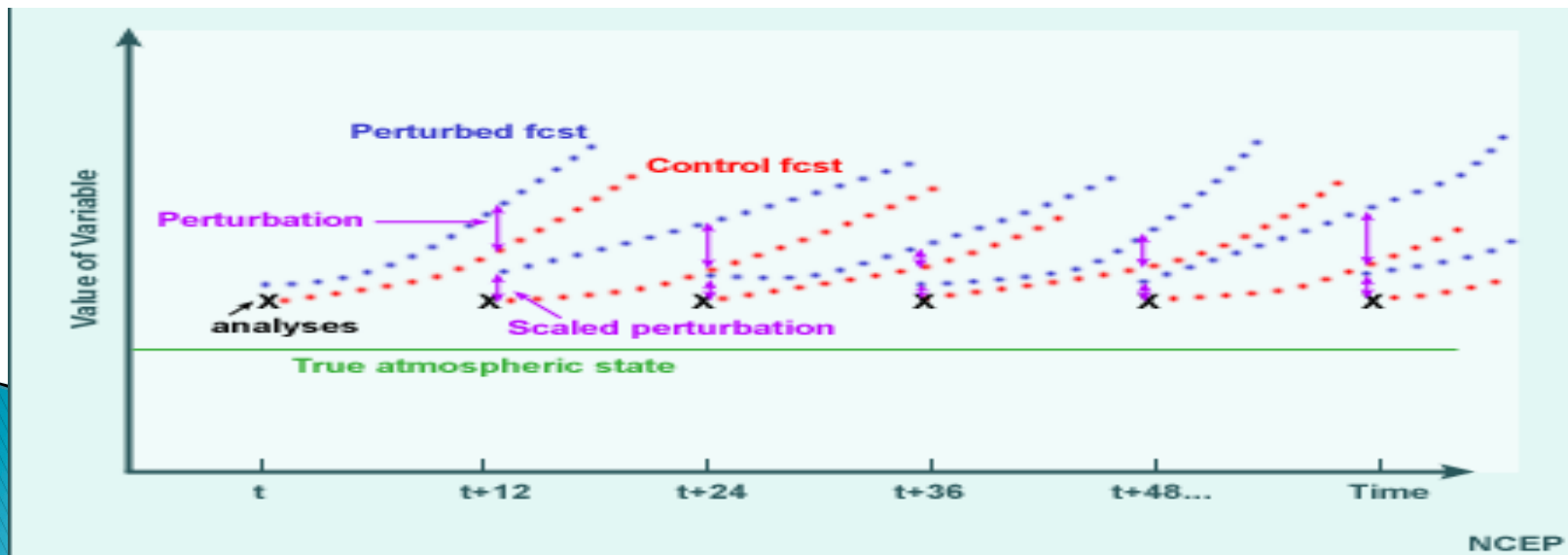
Shorter linear regime ( $\sim h$ )

Presence of BC (mitigating diversity)

Most unstable nonlinear modes:

~~Singular Vectors~~

Bred vectors (SREF): best nonlinear estimate of growing modes.





# The breeding method

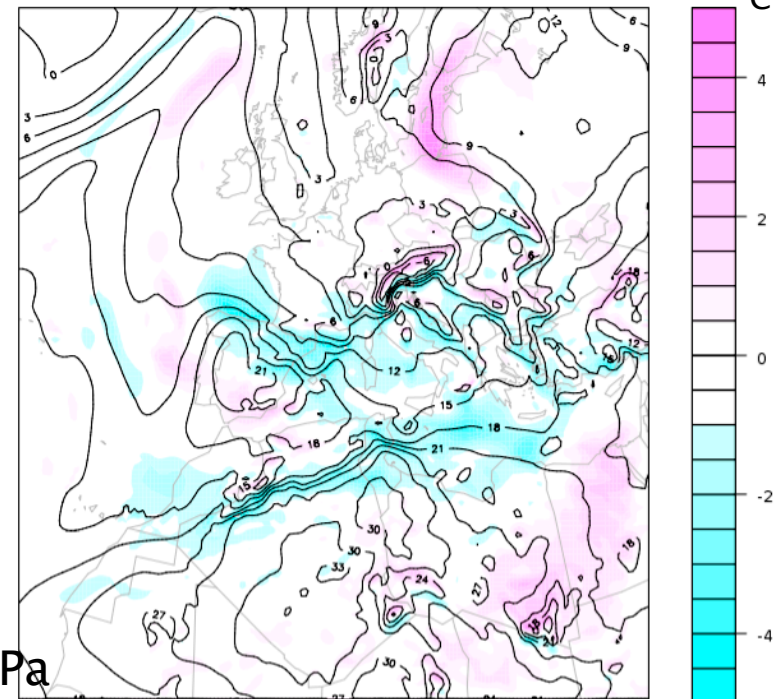
Bred vectors:

$$\vec{bv} = \frac{\vec{x}_p - \vec{x}_c}{\alpha} = \frac{\vec{\delta x}}{\alpha} \quad \text{with } \alpha ; \quad f(\vec{bv}) = \text{cnt.}$$

Example of a typical  
rescaling function (SREF):

$$f(\vec{bv}) = \sqrt{\frac{1}{N} \sum (T_p - T_c)^2} \quad (\text{fixed RMS})$$

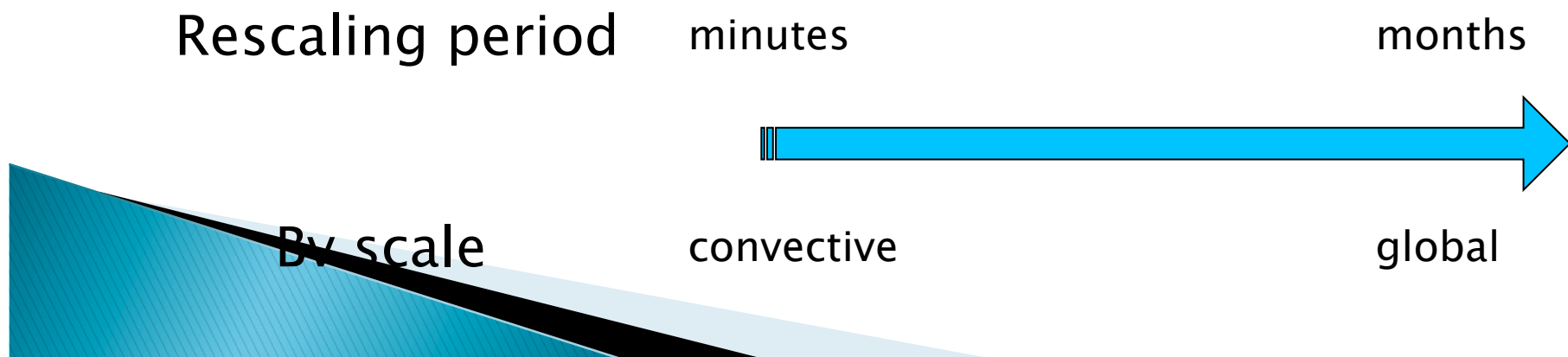
T Bred Vector @ lev = 17 for  
arithmetic2-pos 200109170000



RMS = 0.75 for T at ~850hPa

# The breeding method

- ▶ Bred vectors characteristics:
  - The spread of an ensemble depends on the growth rate of its members
  - The growth rate of IC perturbations depends on their scale and amplitude (besides location)
  - The scale of bv can only be controlled through the rescaling period (fixed by analysis times)



# The breeding method

- ▶ From theory of finite fluctuations on dynamical systems:

“The scale of bvs can also be controlled by using a different rescaling function:

$$f(\overline{\mathbf{bv}}) = \prod (\mathbf{T}_p - \mathbf{T}_c)^{1/N} \quad (\text{fixed geometric mean})$$

which is shown to apply for 1D toy models.”

The analysis characterize perturbations with:

$\ln(\rho)$ : Amplitude  
(Controlled)

$$\ln(\rho) = \overline{\ln(\overline{\delta\mathbf{x}})} = \ln \prod \delta\mathbf{x}^{1/N}$$

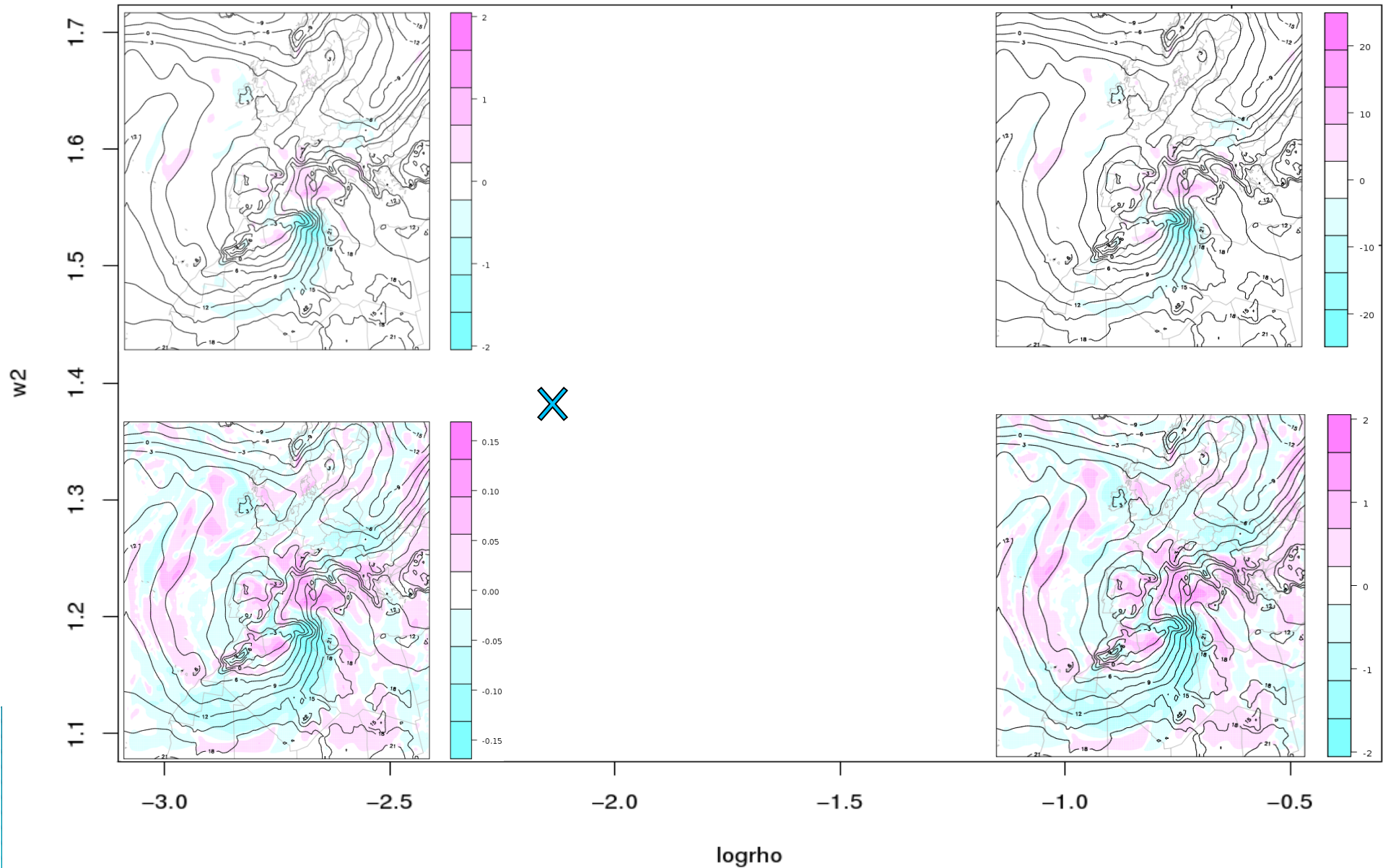
$\omega^2$ : Scale

$$\omega^2 = \overline{(\ln(\overline{\delta\mathbf{x}}) - \ln(\rho))^2} \quad (\text{Provided})$$



# The breeding method

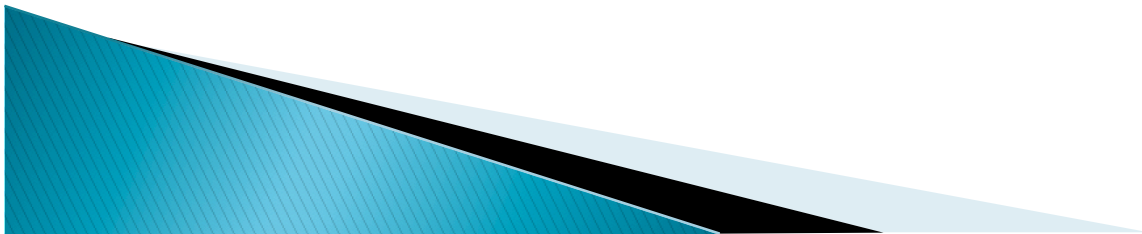
$\omega_2$  vs  $\ln(\rho)$  diagram:





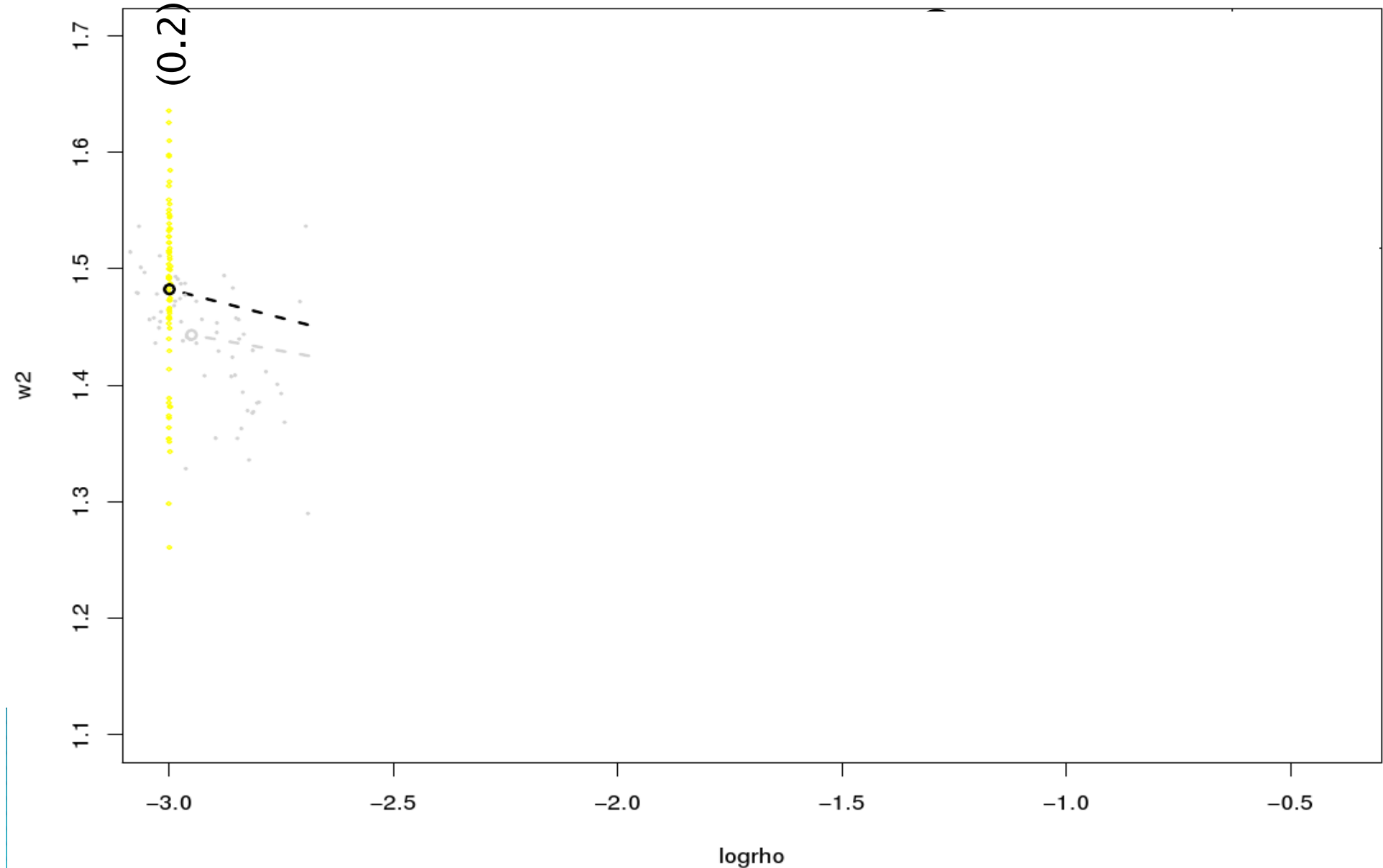
# The breeding method

Is the logarithmic rescaling any different from the RMS based for realistic weather models (MM5 or WRF)?



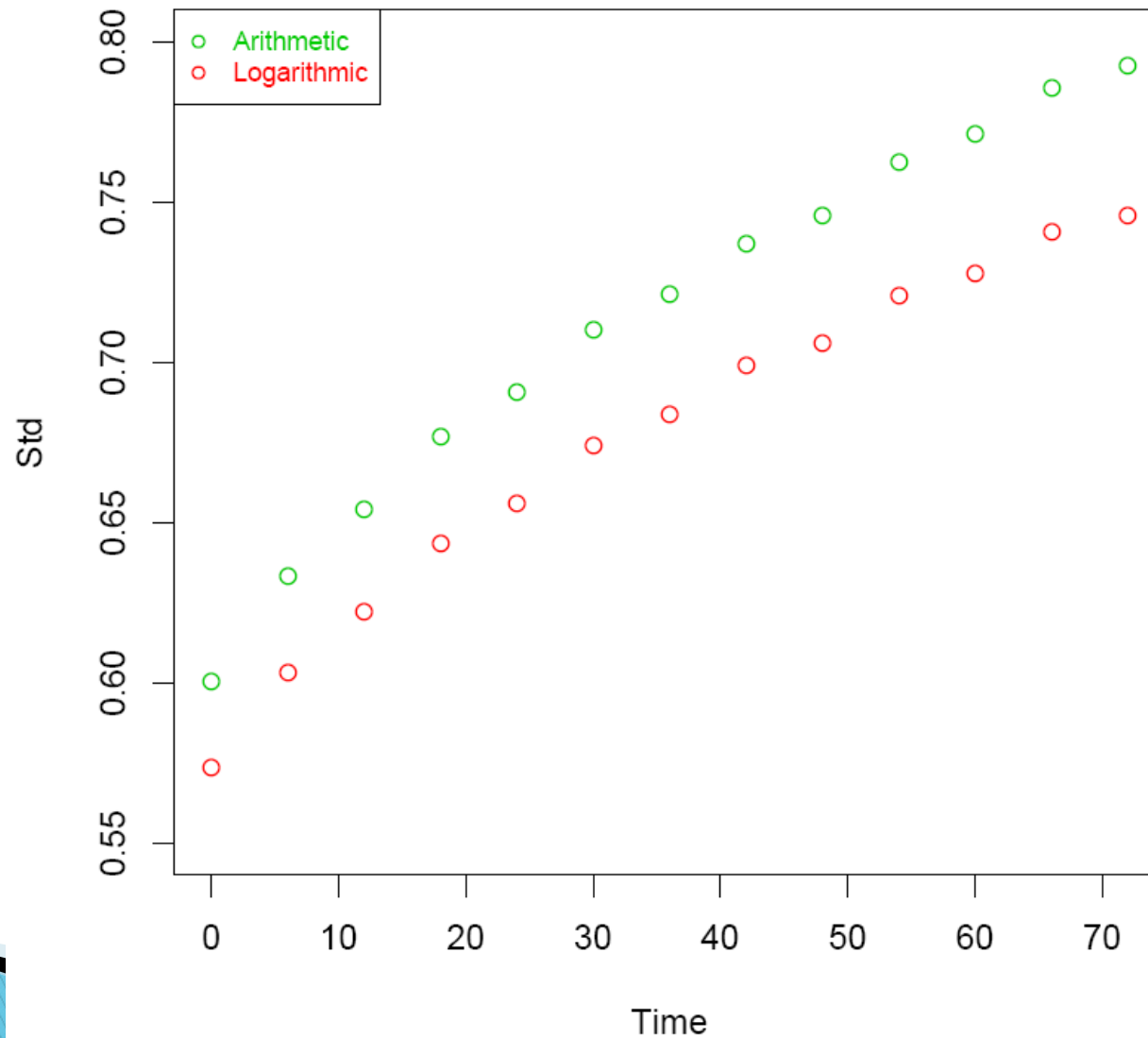
# The breeding method

Is logarithmic rescaling different than RMS based?



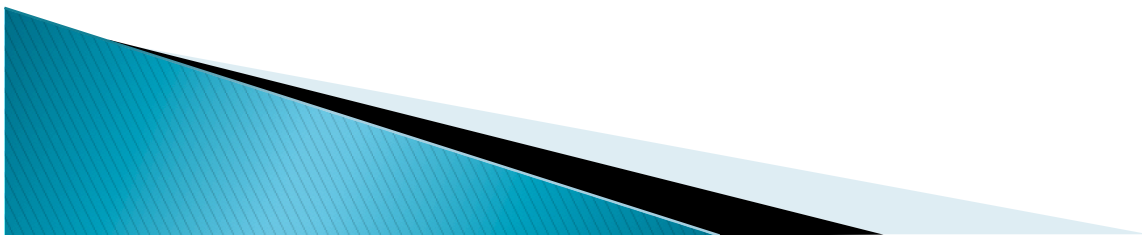
# The breeding method

Average spread for ensembles ARI & LOG



# New (proposed) generation method

**Is  $\omega^2$  (scale) really uncontrollable  
(given by the model dynamics only)?**





# New generation method

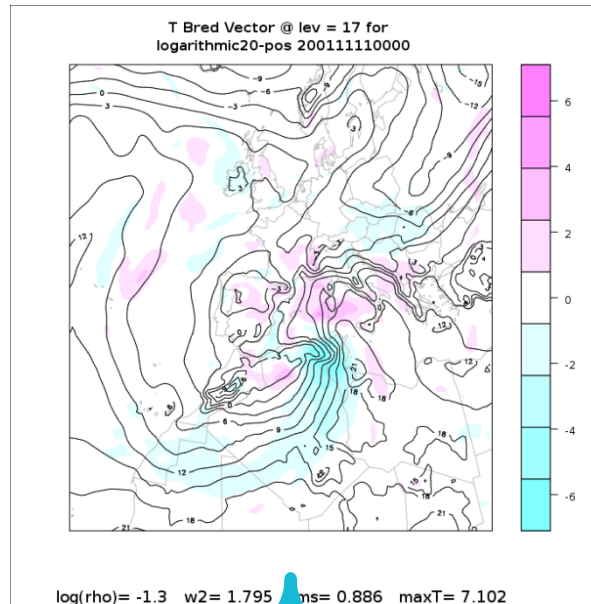
The scale of the perturbation can be modified with:

$$\overrightarrow{\text{sbv}}^* = \frac{\overrightarrow{(\delta x)^{1/\beta}}}{\alpha} \quad \text{with} \quad \beta = \frac{\omega}{\omega^*}$$

In fact:

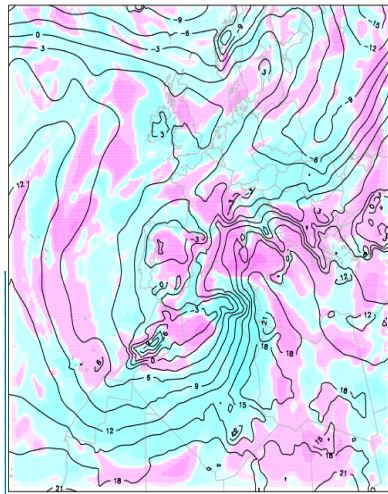
Any single perturbation  $\delta x$  (not only bvs) can be used to generate a new set of perturbations with prescribed amplitude **AND SCALE**.

# New generation method

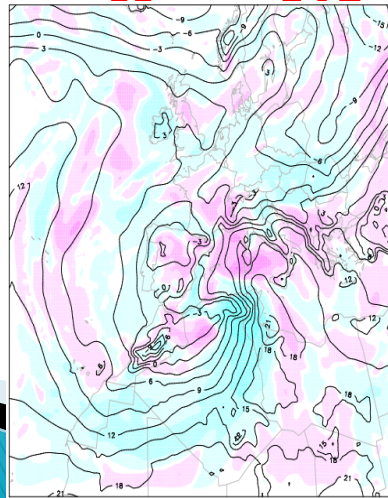


$$\ln(\rho) = -1.3$$
$$\omega^2 = 1.8$$

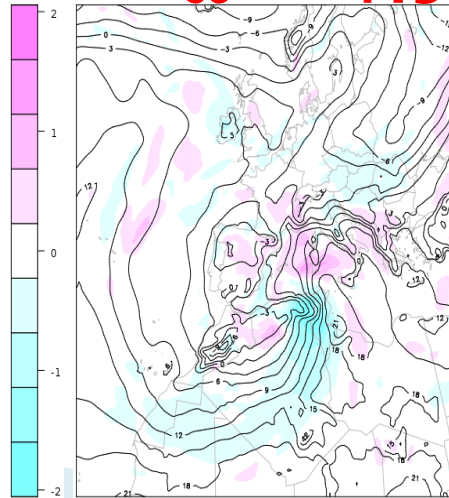
$$\ln(\rho) = -3.5$$
$$\omega^2 = 0.1$$



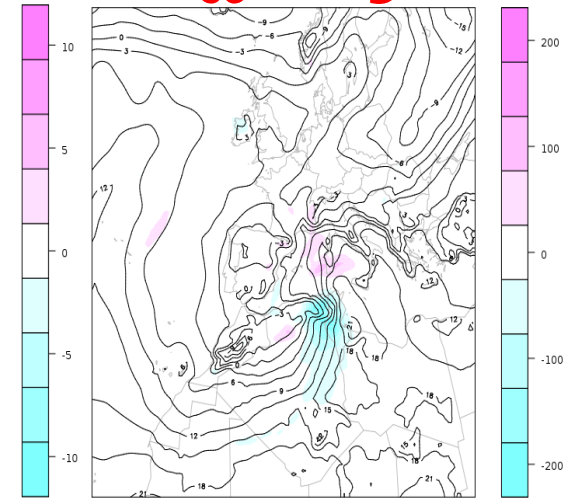
$$\ln(\rho) = -1$$
$$\omega^2 = 0.5$$



$$\ln(\rho) = -.5$$
$$\omega^2 = 1.5$$

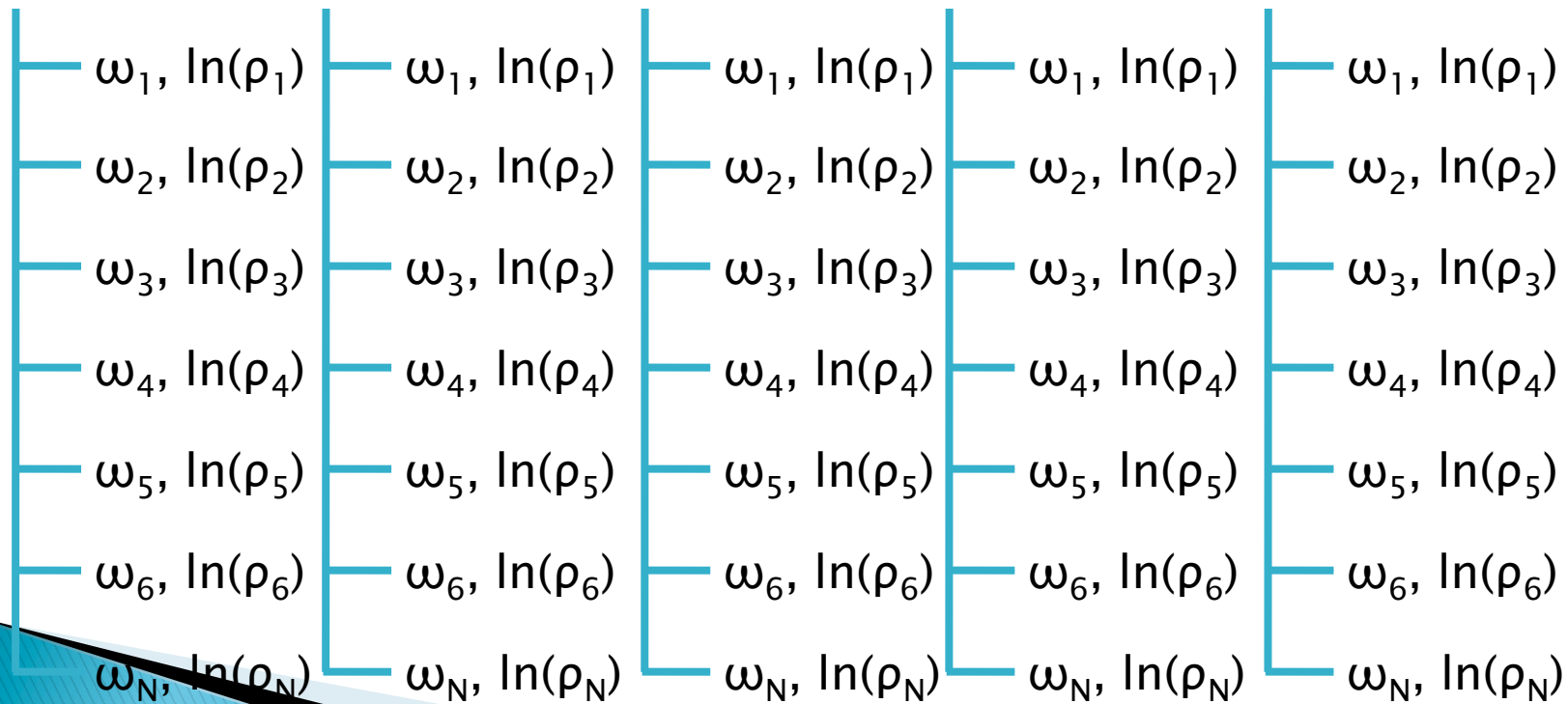
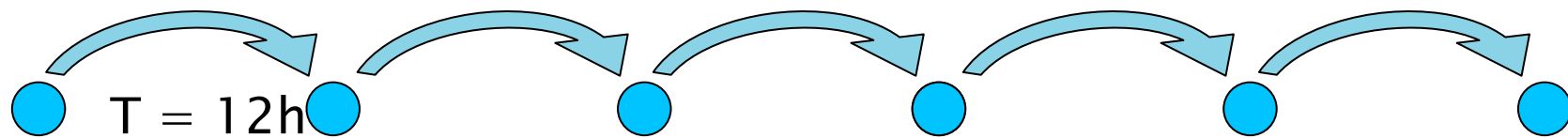


$$\ln(\rho) = 0$$
$$\omega^2 = 5$$



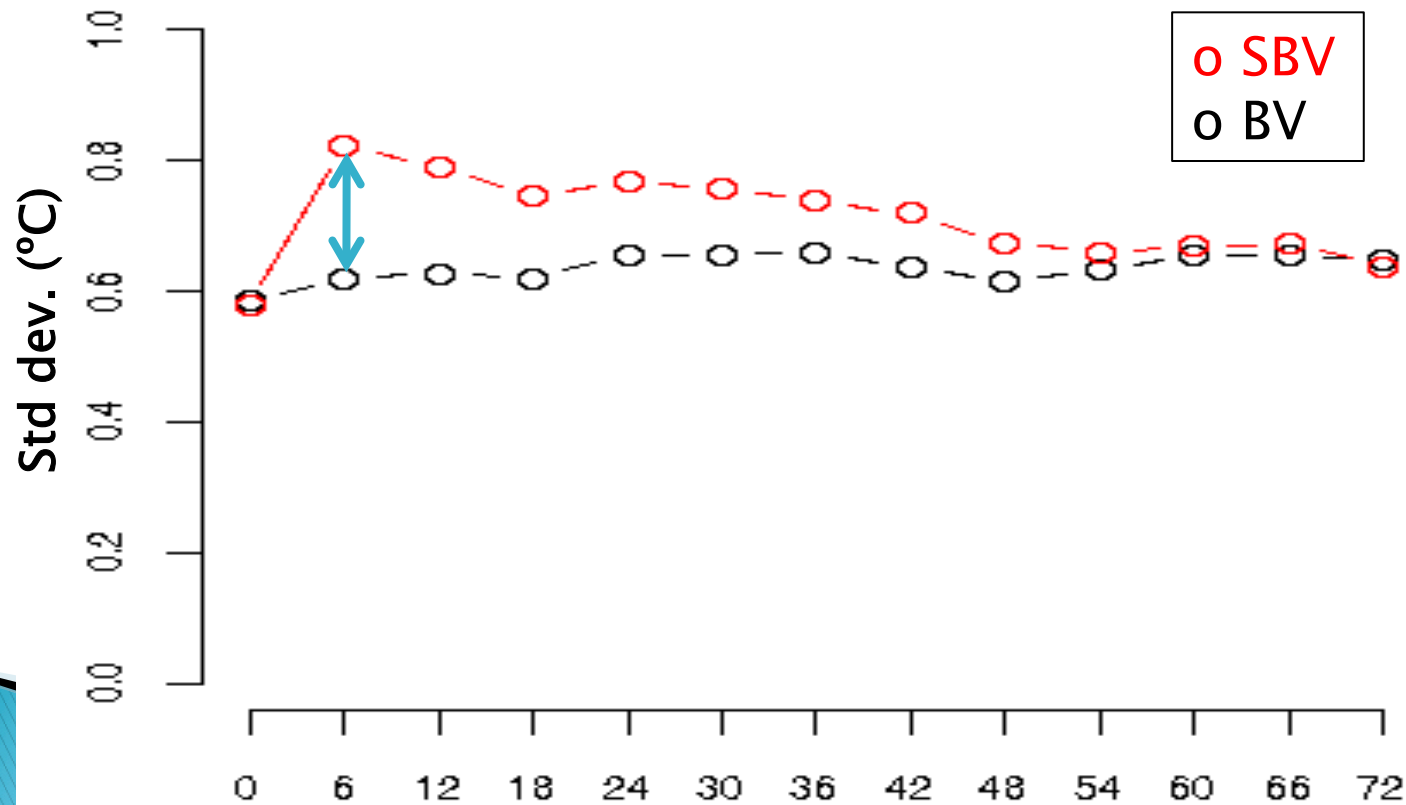
# New generation method

- ▶ A full ensemble can be generated from (even) a single bred cycle:



# New generation method

- ▶ Comparing this “scaled bv” with standard bv:
  - Test over 30 cycles (15 days) with convective activity over the Western Mediterranean
  - Low mesoscale and convective scale perturbations are generated here

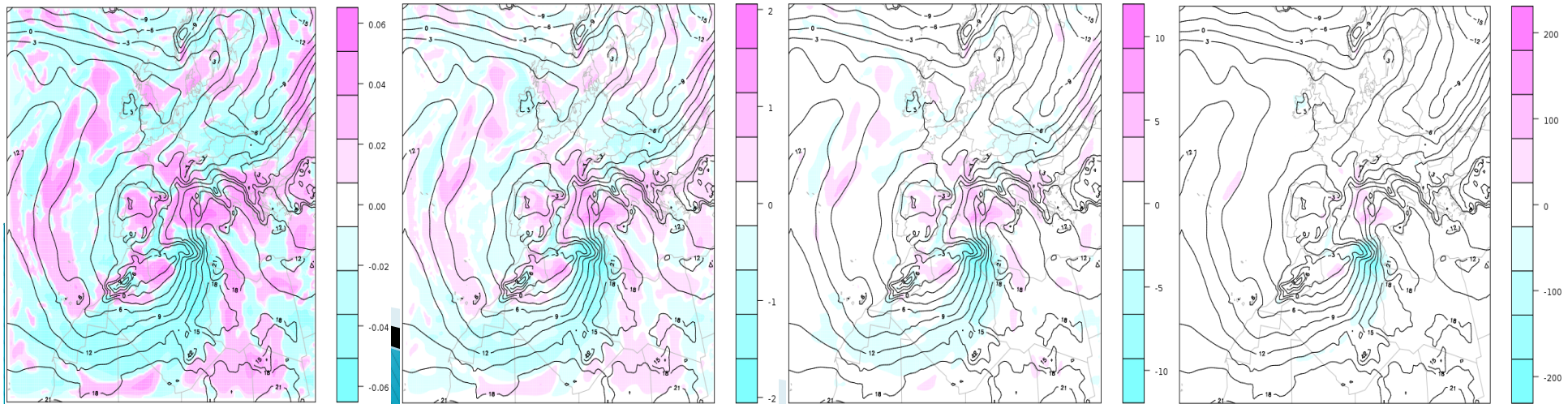




# ‘À la carte’ perturbations

- ▶ One step further consists in adding diversity to the ensemble by mixing bred cycles to build the set of IC

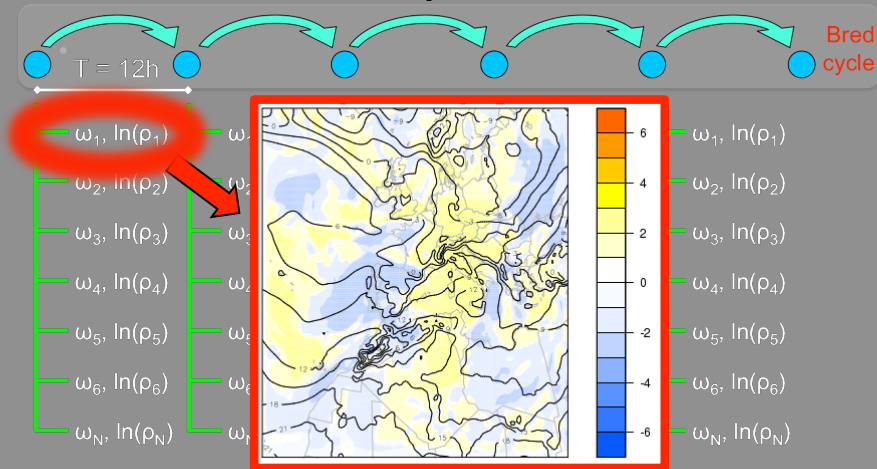
$$ICP_i = \sum_j \gamma_j \overrightarrow{sbv}_j = \sum_j \gamma_j \frac{\overrightarrow{\delta x}_j^{1/\beta_j}}{\alpha_j} ; \text{ where } j \text{ determines BC and } sbv$$



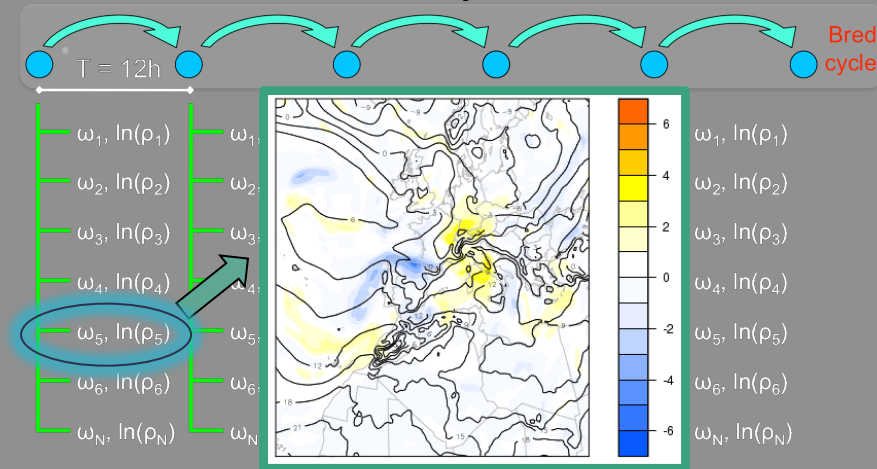
# 'À la carte' perturbations

- Using various bred cycles, a number of different IC perturbations can be computed:

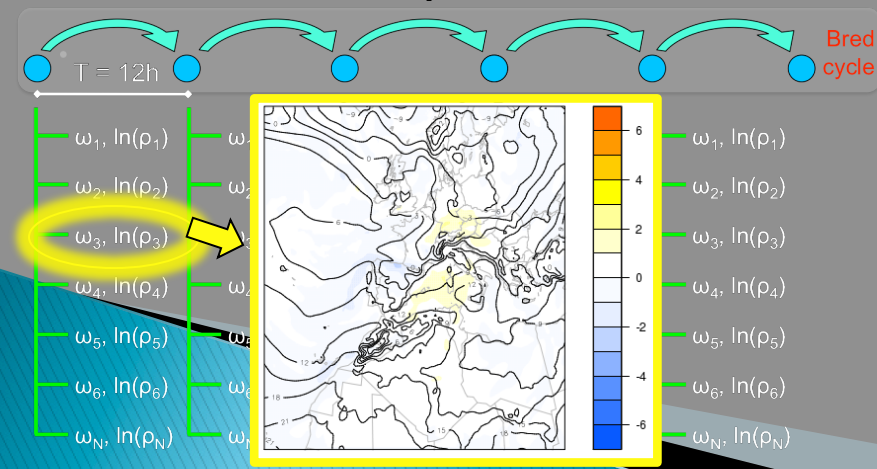
Bred Cycle A



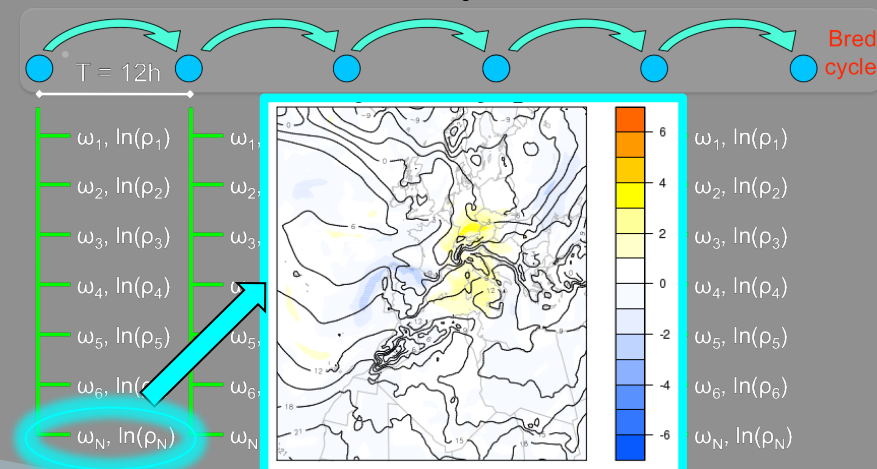
Bred Cycle B



Bred Cycle C

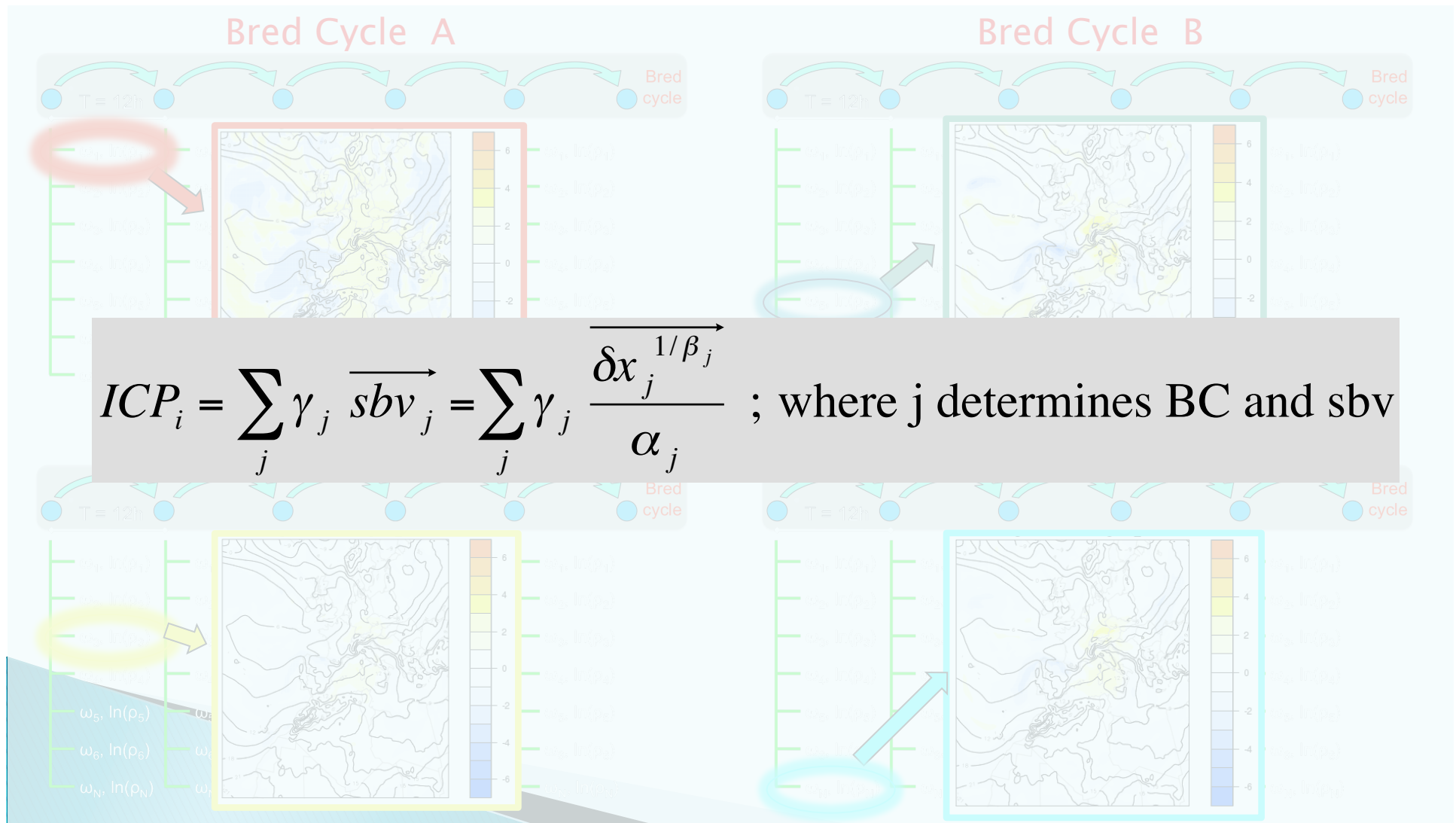


Bred Cycle D



# 'À la carte' perturbations

Using various bred cycles, a number of different IC perturbations can be computed:

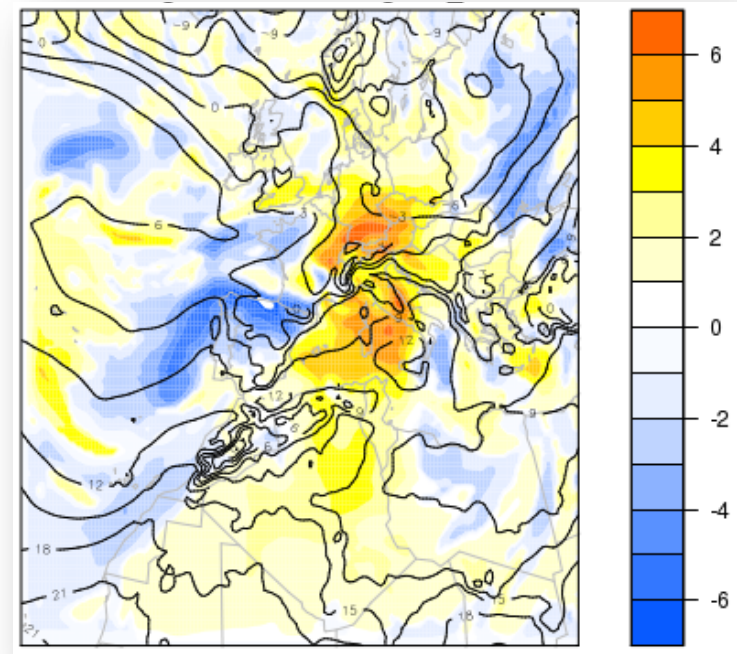
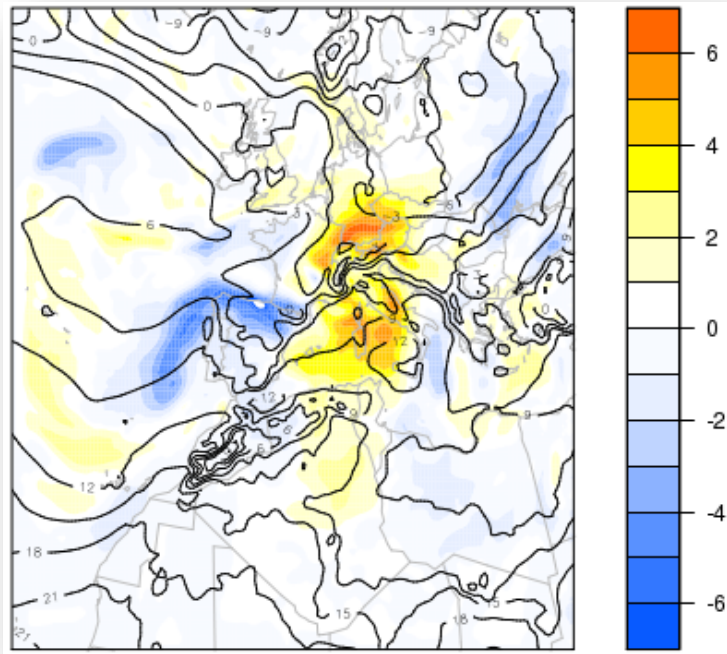




# ‘À la carte’ perturbations

Currently defining global rescaling coefficients ( $\gamma$ )

ICP examples:



# SUMMARY

- ▶ What is *extreme weather*?
  - Not strictly defined. Practical definitions used.
- ▶ Why is it *extreme*?
  - Ingredients coincide rarely
- ▶ Is it predictable? Why?
  - Not within useful lead-times. Very sensitive to poorly observed scales
- ▶ How is extreme weather forecast nowadays?
  - Ensemble methods. Not yet solutions for extreme (HR).  
Still working on it...








Thanks!

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# Definition of predictability

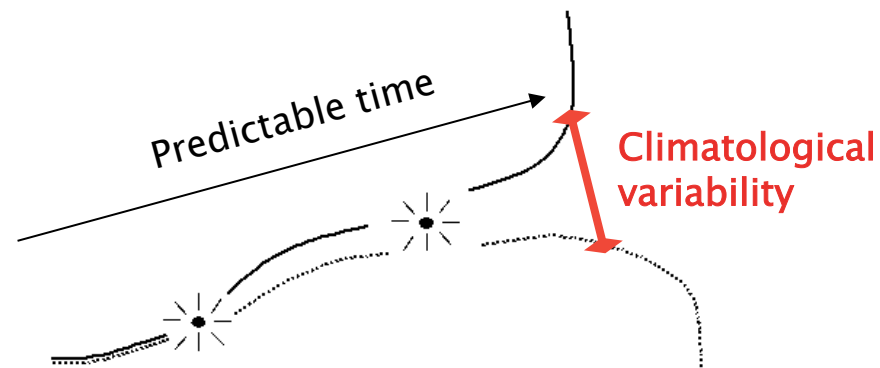
- ▶ *Predictability: the quality of being predictable*  
“The predictability of *<something>* ...”

*This quality refers to a certain forecast entity, and by defining one, we are implicitly setting a space-temporal scale, which sets its predictability limit.*



# Definition of predictability

- ▶ Predictability time: time at which two solutions obtained from slightly differing initial states are as different from each other as two random states of the system (Lorenz 1963).



Predictability time depends, besides growth, on how “differing” the initial states are. The attribution of indistinguishable states might be simply assigned by technical limitations.

# Definition of predictability

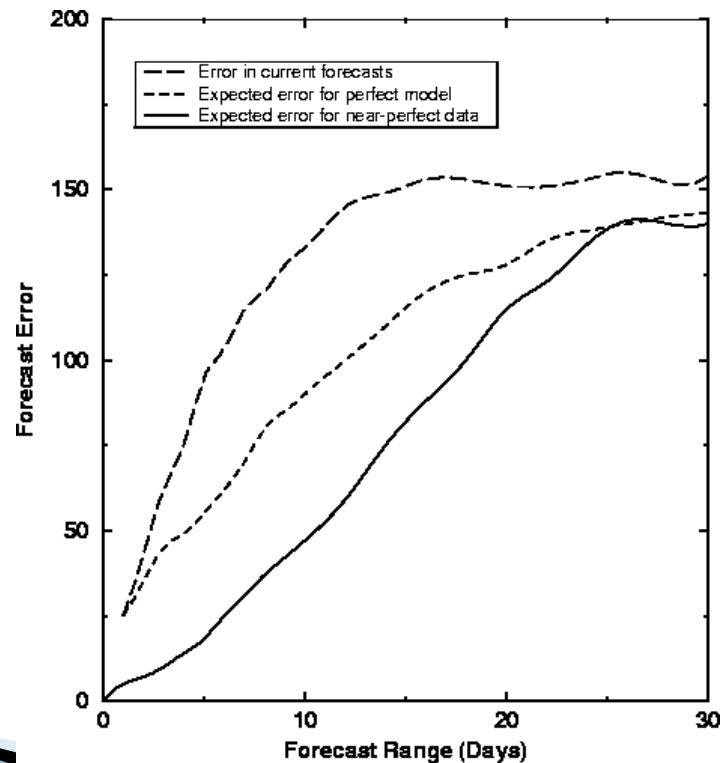
- ▶ Predictability time: time at which initial conditions error is doubled [Smagorinsky (1963), Mintz(1964), Leith (1965)]

Predictability time not really informative about predictive capability of the system



## (practical) Definition of predictability

- ▶ Predictability time: time at which two solutions compatible with “best guess uncertainty” become intolerably different



Predictability time depends on how “tolerant” the end-user is



# (Dyn Sys) Definition of predictability

- ▶ Predictability time: time at which the system asymptotically evolves into its (strange) attractor

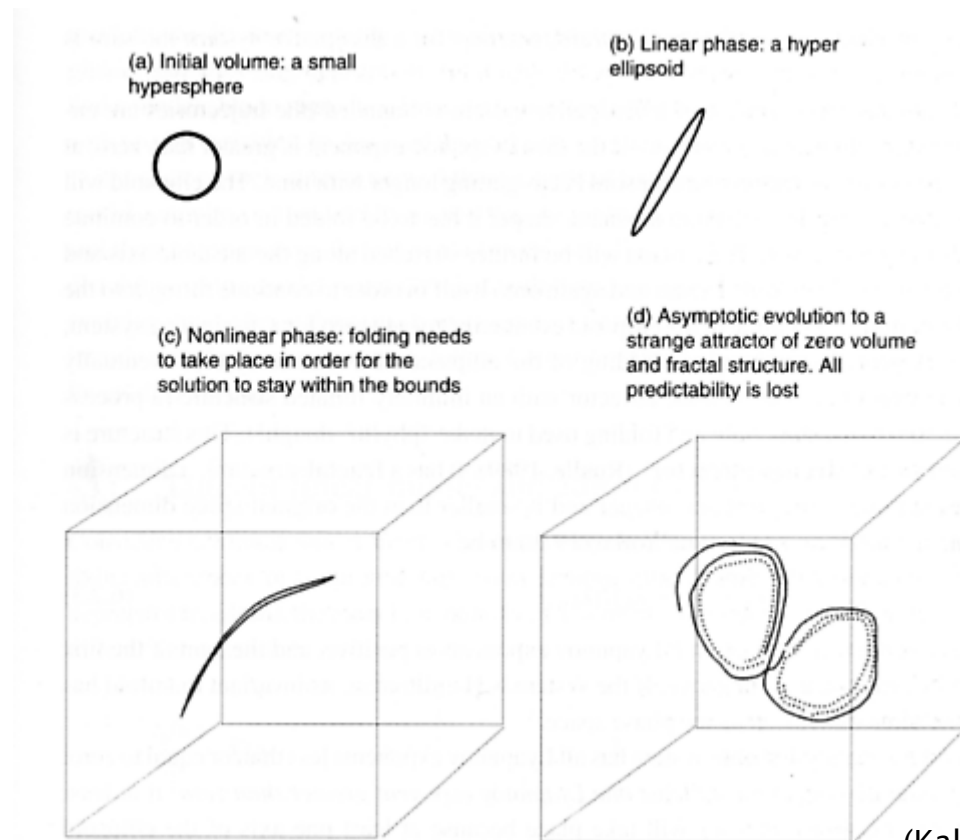
Error growth in a dynamical system:

$$|\delta(t)| = \delta_0 e^{\lambda_L t}$$

Predictability time:

$$t^* \approx \frac{1}{\lambda_L} \ln \frac{\Delta}{\delta_0}$$

(May not be appropriate for high-dimensional finite systems)



(Kalnay 2003)

## (Dyn Sys) Definition of predictability

- ▶ Predictability time: time at which a system trajectory is attracted to the neighborhood of a statistically stationary solution

Let us consider some ensemble (distribution) of initial states  $P_0$  and its evolution  $P(t)$ .

If the system has the invariant (mixing) measure

$$P(t) = G(t)(P_0) \xrightarrow{t \rightarrow \infty} P_{st}, \quad \psi(t) = G(t)(\psi_0).$$

where  $P_{st}$  is the stationary distribution of points in the system phase space (e.g climatology).

When  $P(T) \approx P_{st}$  all information about the initial distribution  $P_0$  is lost.

Let us call  $T$  as the **predictability limit** (Dymnikov, Izvestiya, 2004).

# Conventions

- ▶ “Kinds of predictability”: attribute the predictability limits to sources of errors (infinitesimal)
  - **Predictability of 1st kind**: limited by the errors in the estimate of the state of the system (initial and boundary conditions)
  - **Predictability of 2nd kind**: limited by the errors and deficiencies in the model (errors *per se*, resolution, discrete nature, parameterizations)

