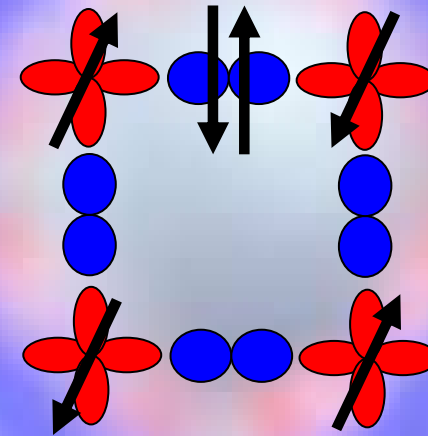
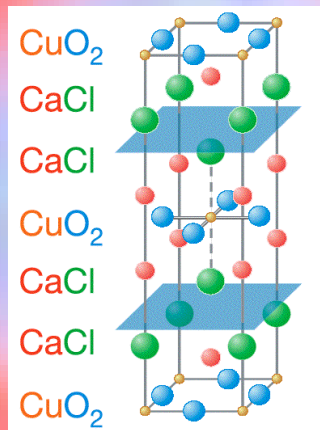
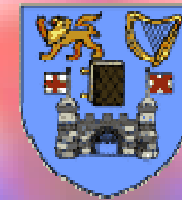


Nature of Striped Phases in Cuprates with $x \sim 1/8$



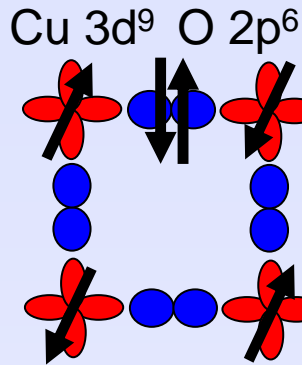
Charles H. Patterson
School of Physics
Trinity College Dublin



Summary

- Hybrid DFT calculations for $\text{Ca}_2\text{CuO}_2\text{Cl}_2$
 - Electronic structure
- Magnetic anti-phase boundaries in $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/8$
 - Electronic structure
 - STM and STS data
- Small polarons in low-doped $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/32$
 - Polaron distortions
 - Electronic structure
 - Photoemission

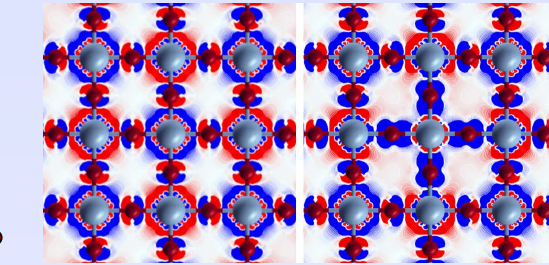
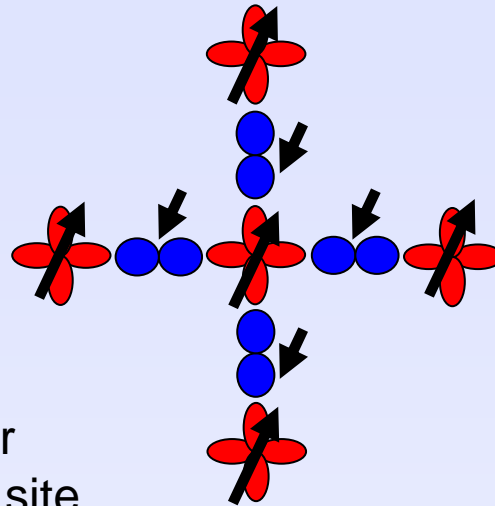
Electronic and Crystal Structures



Undoped cuprate

Anti-ferromagnetic insulator

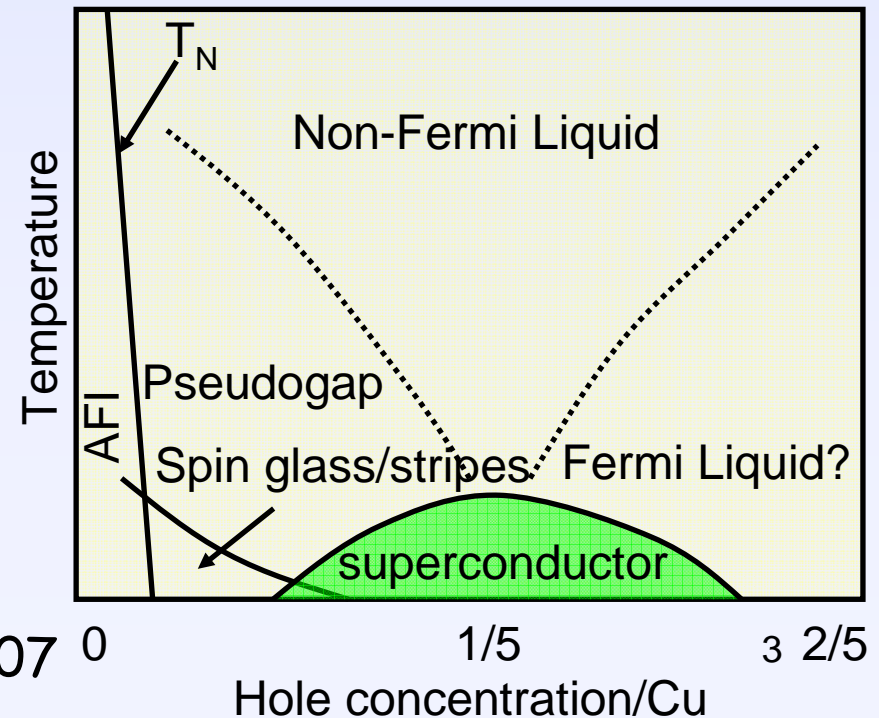
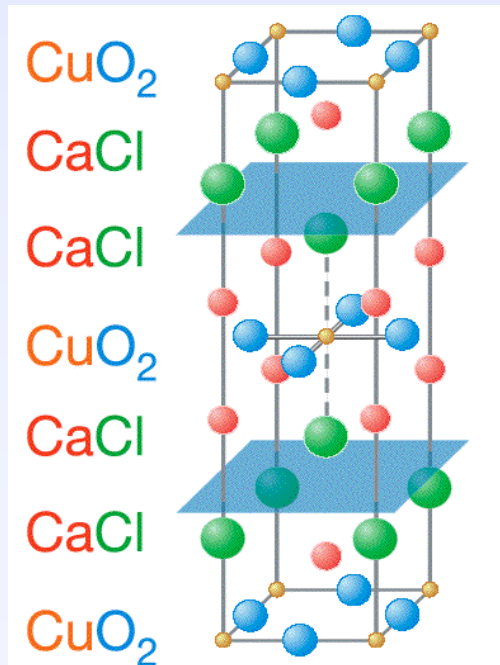
Half-filled 3d x²-y² on each site



Single hole doping

Zhang and Rice PRB (1988)

$$\Psi_{ZRS} = (\phi(\alpha)d(\beta) - \phi(\beta)d(\alpha))$$



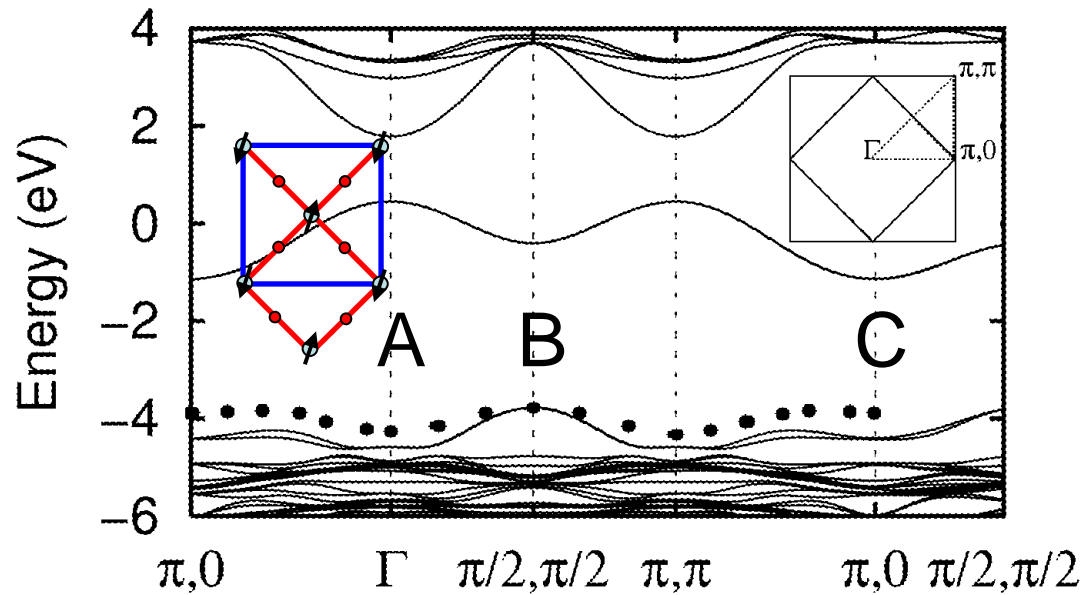
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Hybrid DFT $\text{Ca}_2\text{CuO}_2\text{Cl}_2$

$$E_{xc} = (1-A)(E_x^{LDA} + BE_x^{Becke}) + AE_x^{HF} + (1-C)E_C^{VWN} + E_C^{LYP}$$

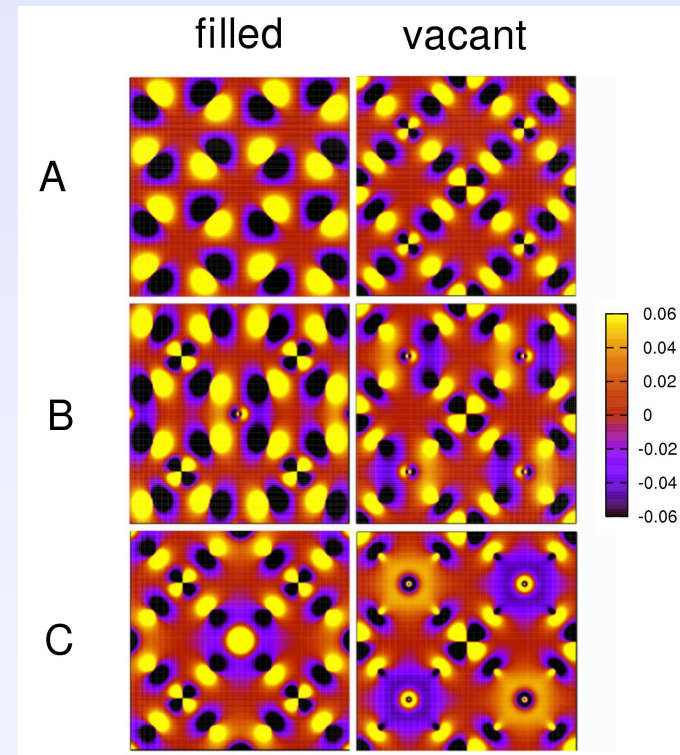
B3LYP: $A = 0.2, B = 0.9, C = 0.81$

Becke (1993), Stephens (1994)



Dots = t - J model
 $J/t = 0.4$
 $t = 0.5$ eV
 Dagotto (1994)

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Cuprate stripe history

Incommensurate Magnetic Fluctuations in $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$,
S. W. Cheong *et al.*, *Phys. Rev. Lett.* **67**, 1791-1794 (1991)

Incommensurate Magnetic Fluctuations in $\text{La}_{2-x}\text{Sr}_x\text{NiO}_4$,
S. M. Hayden *et al.*, *Phys. Rev. Lett.* **68**, 1061 (1992)

Evidence for stripe correlations of spins and holes in copper oxide superconductors
J. M. Tranquada, B. J. Sternlieb, J. D. Axe, Y. Nakamura, S. & Uchida, *Nature (London)* **375**, 561 (1995)

A 'checkerboard' electronic crystal state in lightly hole-doped $\text{Ca}_{2-x}\text{Na}_x\text{CuO}_2\text{Cl}_2$,
T. Hanaguri *et al.*, *Nature* **430**, 1001 (2004).

Quantum magnetic excitations from stripes in copper oxide superconductors,
J. M. Tranquada *et al.*, *Nature* **429**, 534 (2004).

The structure of the high-energy spin excitations in a high-temperature superconductor,
S. M. Hayden, H. A. Mook, P. Dai, T. G. Perring and F. Dogan, *Nature* **429**, 531 (2004).

Computation of stripes in cuprates within the LDA + U method,
V. I. Anisimov *et al.*, *Phys. Rev. B* **70**, 172501 (2004).

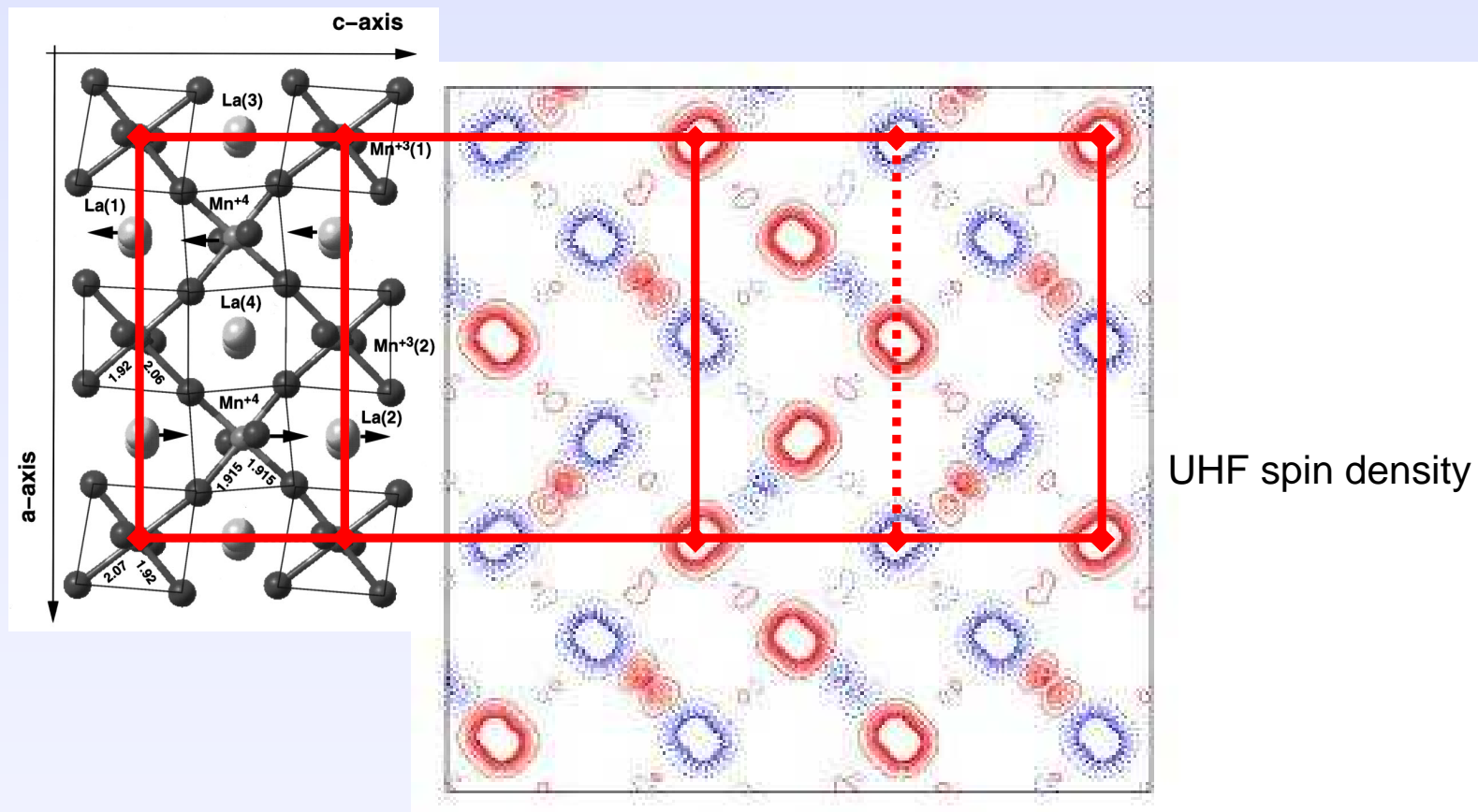
Electron-phonon coupling reflecting dynamic charge inhomogeneity in copper oxide superconductors,
D. Reznik *et al.*, *Nature*, **440**, 1170 (2006).

An Intrinsic Bond-Centered Electronic Glass with Unidirectional Domains in Underdoped Cuprates,
Y. Kohsaka, *et al.*, *Science* **315**, 1380 (2007).

Angle-resolved photoemission studies of lattice polaron formation in the cuprate $\text{Ca}_2\text{CuO}_2\text{Cl}_2$,
K. M. Shen *et al.*, *Phys. Rev. B* **75**, 075115 (2007)

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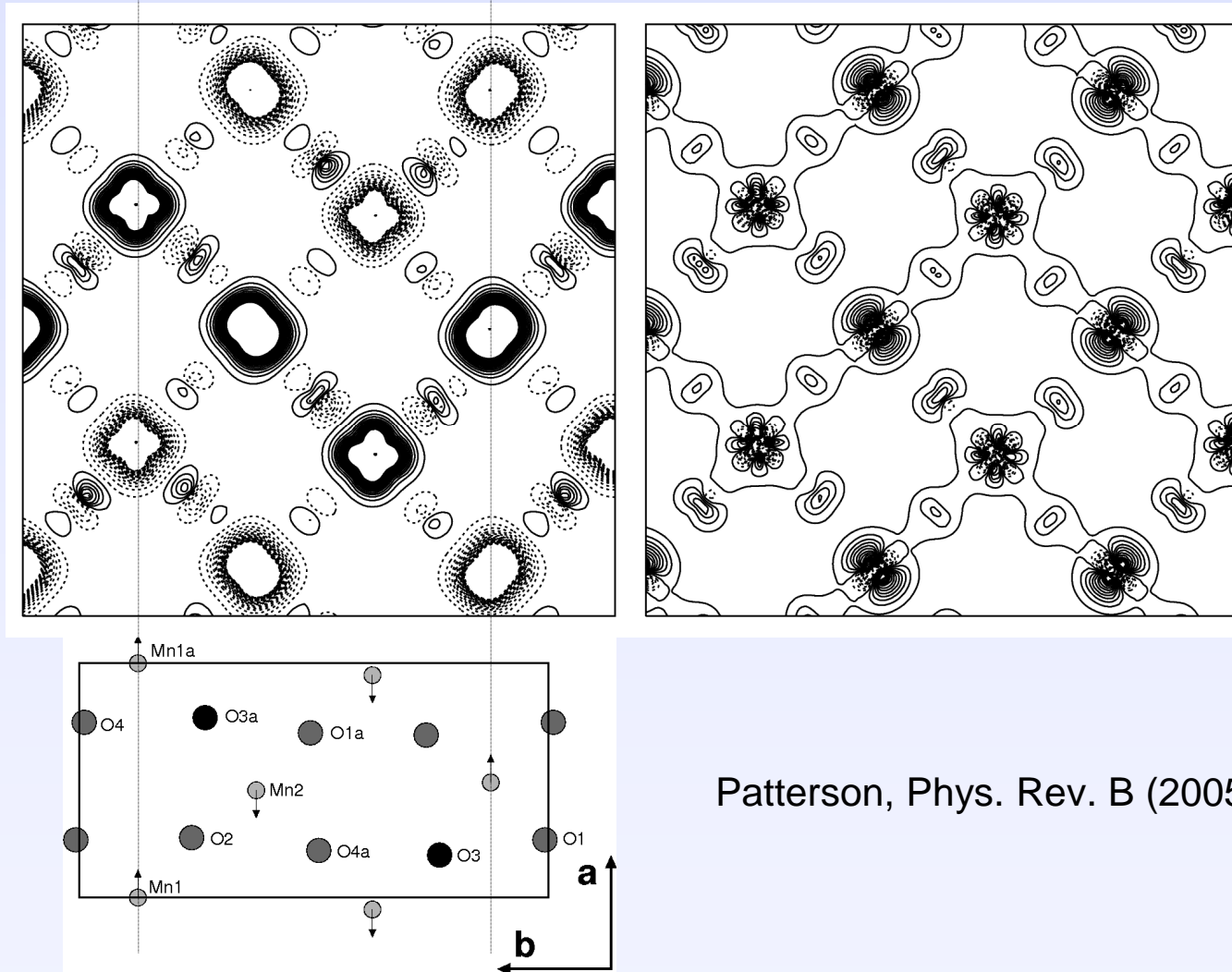
Zener Polaron Electronic Structure of $\text{La}_{1/2}\text{Ca}_{1/2}\text{MnO}_3$



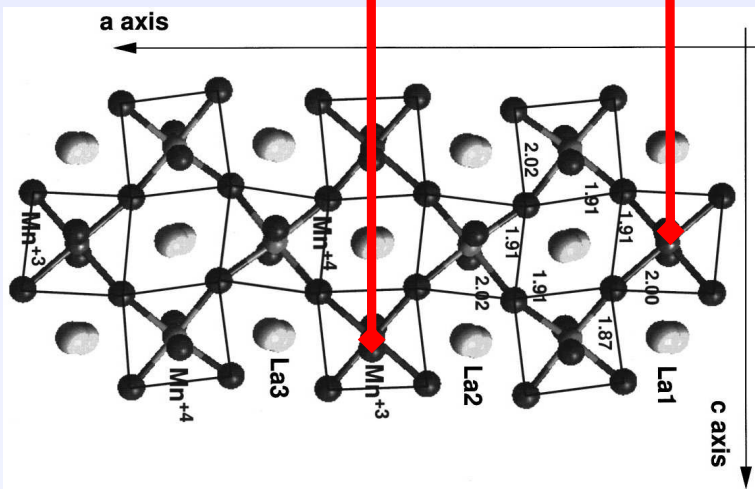
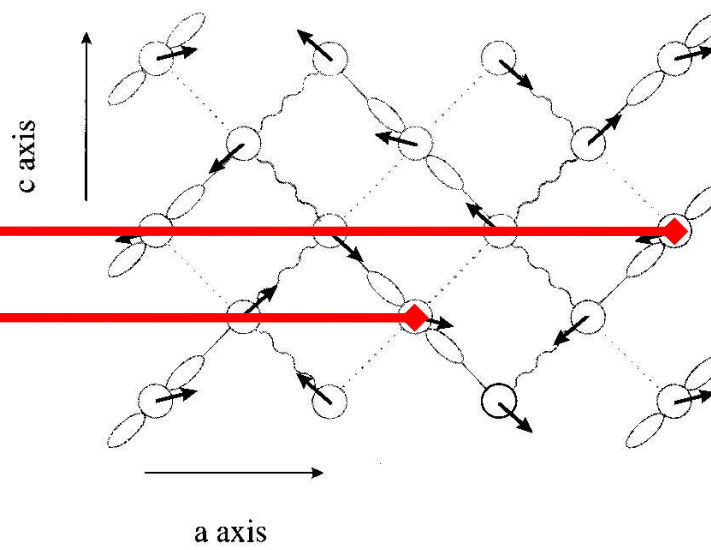
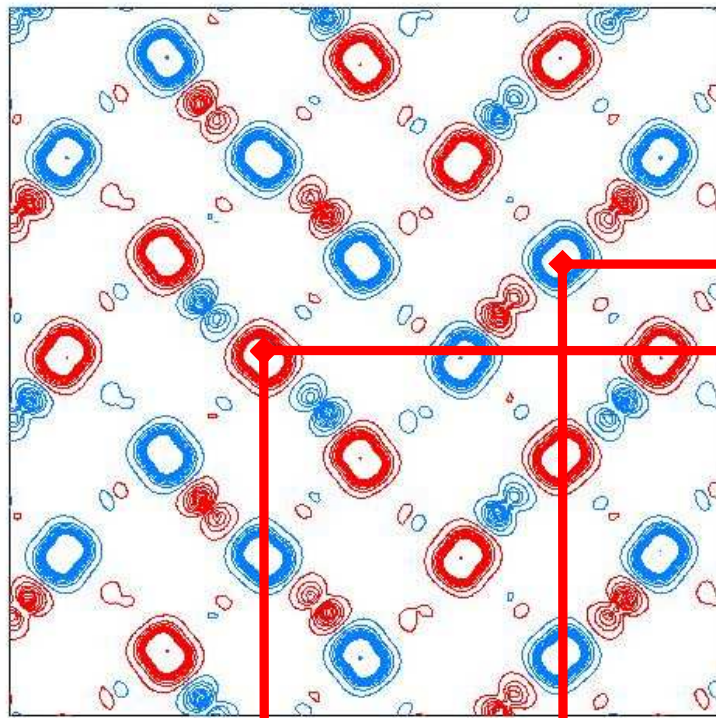
Zheng and Patterson, Phys. Rev. B (2003)

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CE-type phase of $\text{La}_{1/2}\text{Ca}_{1/2}\text{MnO}_3$



Patterson, Phys. Rev. B (2005)

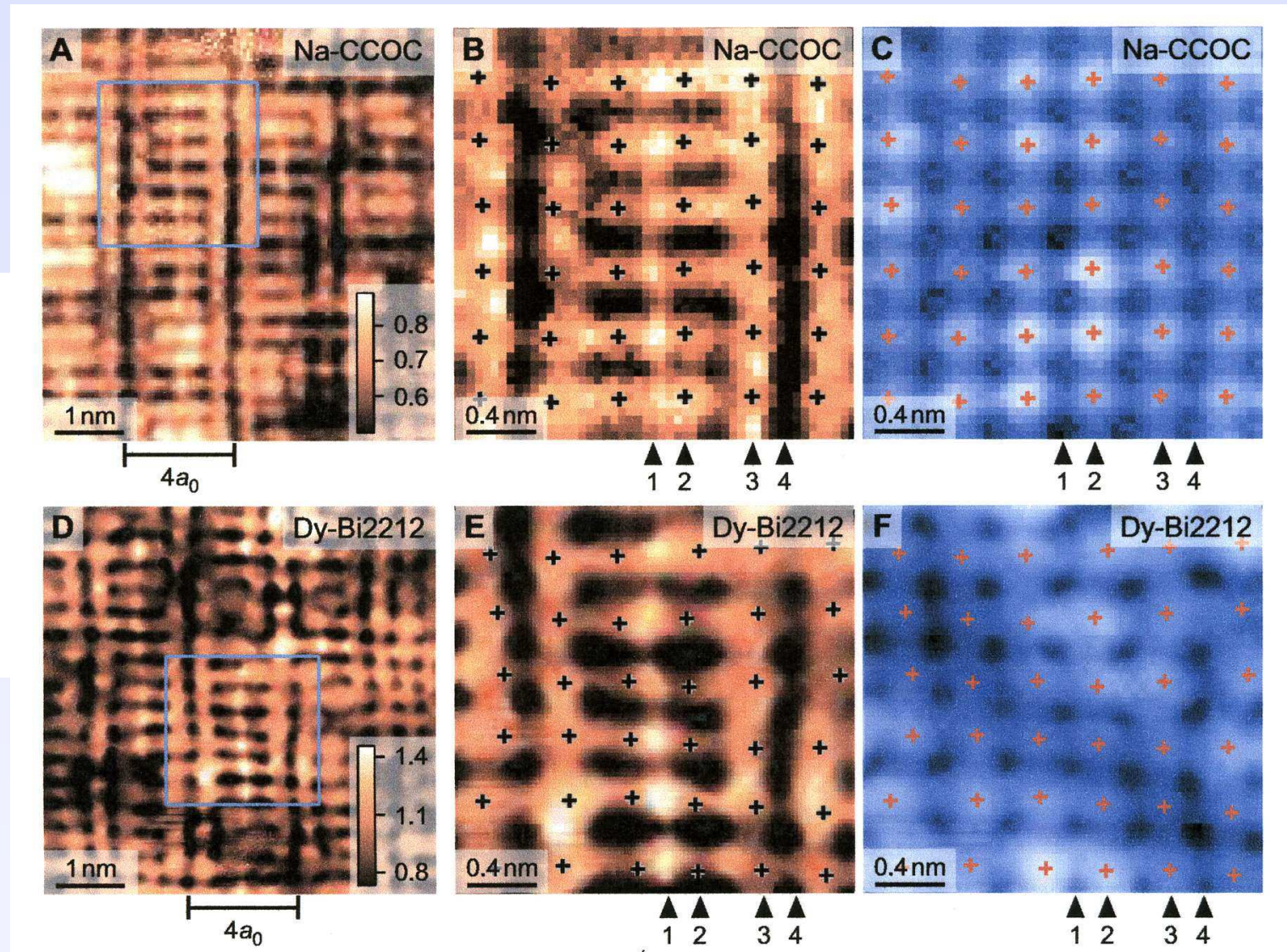
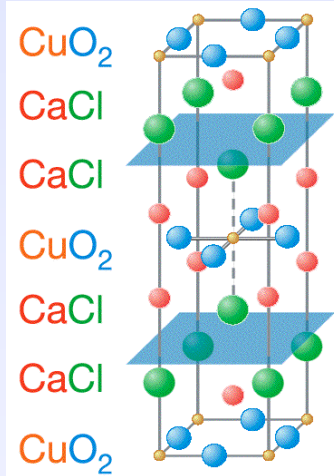


$La_{1/3}Ca_{2/3}MnO_3$ UHF spin density
CO on O ions not Mn ions!

Zheng and Patterson,
 Phys. Rev. B (2003)

Neutron powder crystal structure
 P. Radaelli *et al.*
 Phys. Rev. B (1999)

1-D Stripes $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/8$

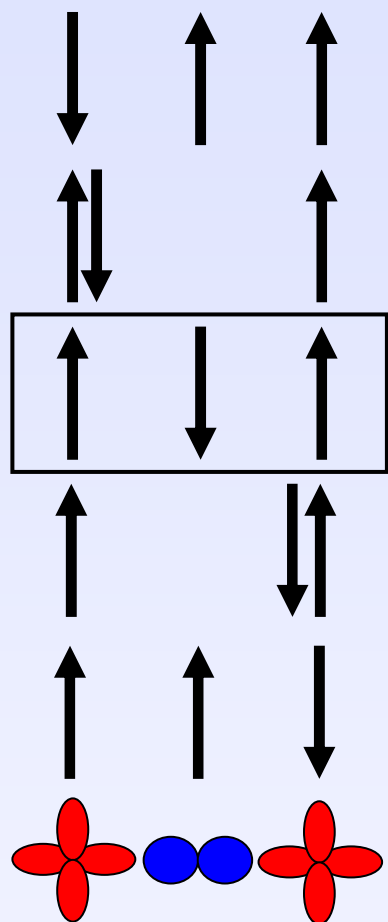


Y. Kohsaka et al. Science (2007)

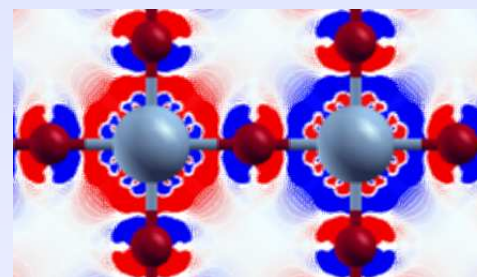
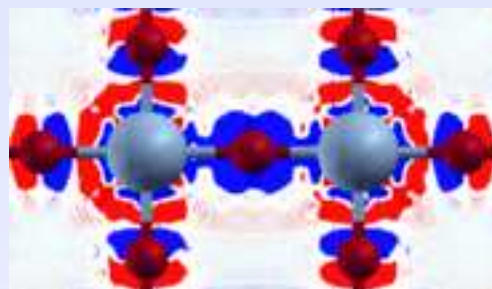
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O Cu Cu \ominus



Double and Superexchange

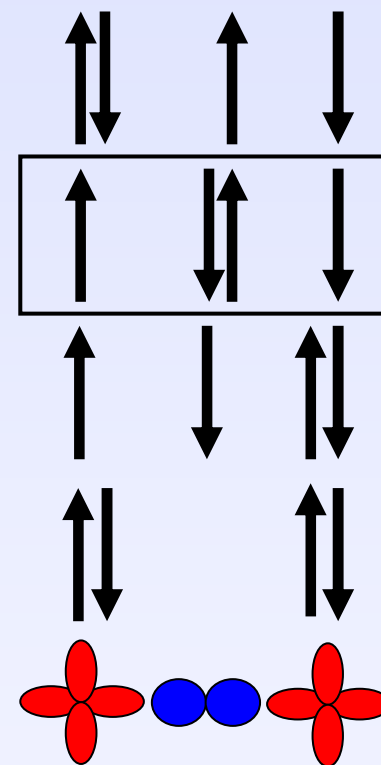


Double Exchange
Localised hole
Zener (1955)



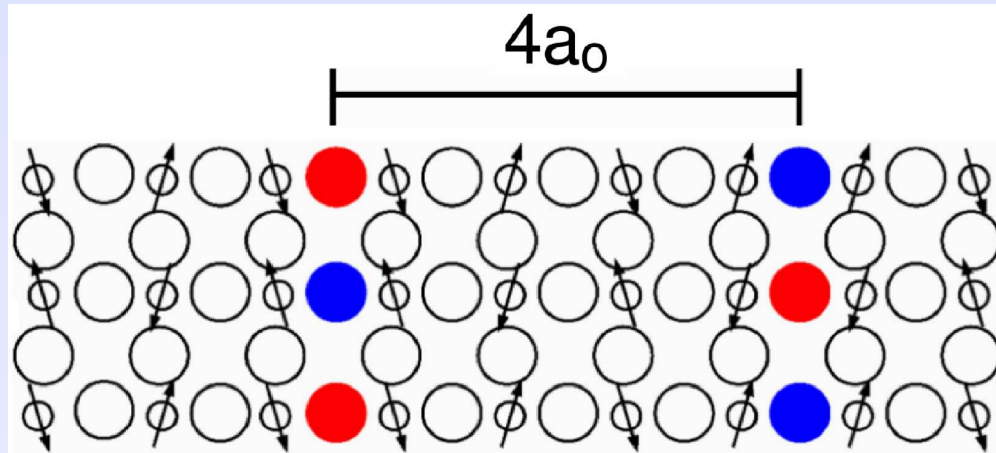
Cu  O 

 Net spin up
 Net spin down

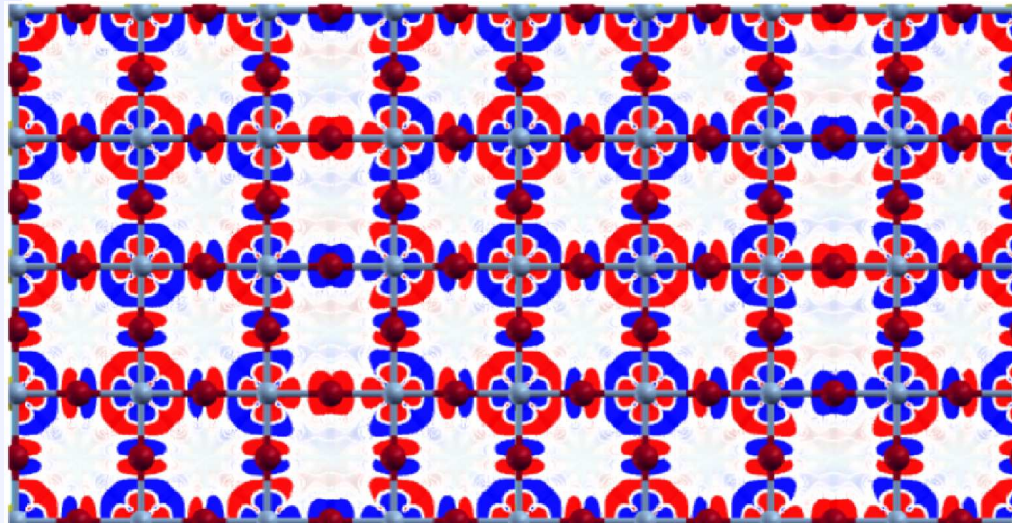


Superexchange
No localised hole
Anderson (1969)

Hybrid DFT: $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/8$

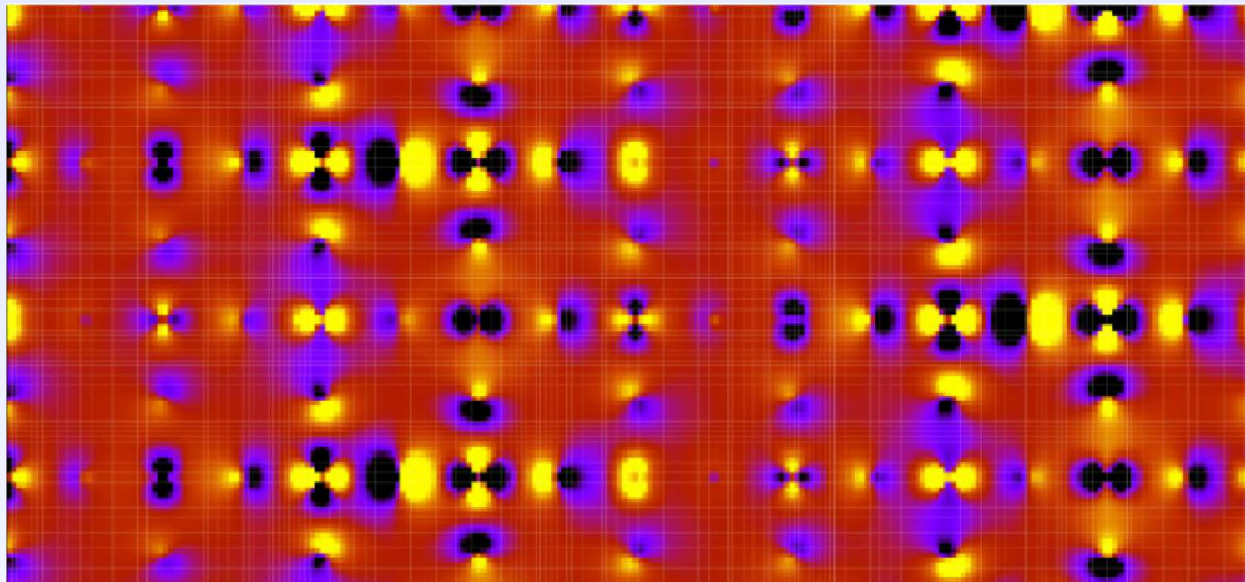
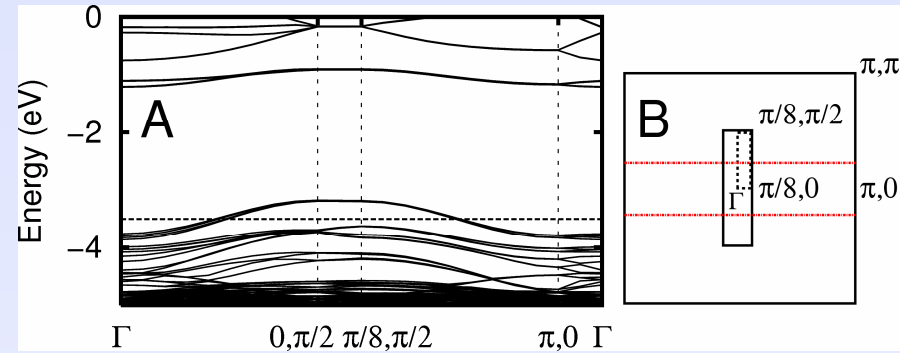


Magnetic Anti-Phase Boundaries



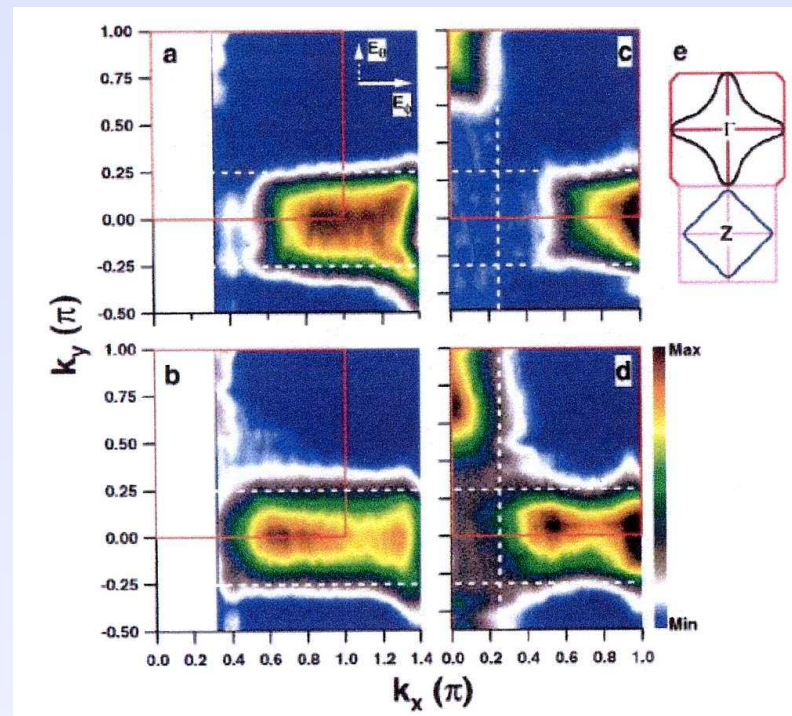
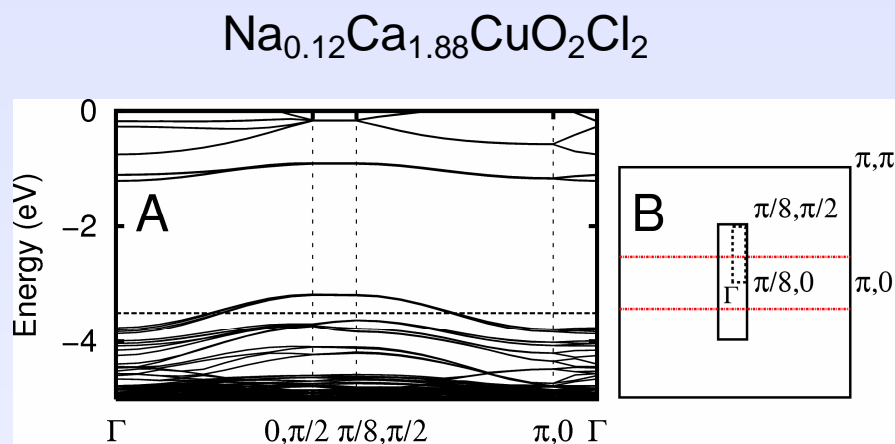
Spin Density

Hybrid DFT: $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/8$



Stripe Band Wave Function Amplitude (Γ point)

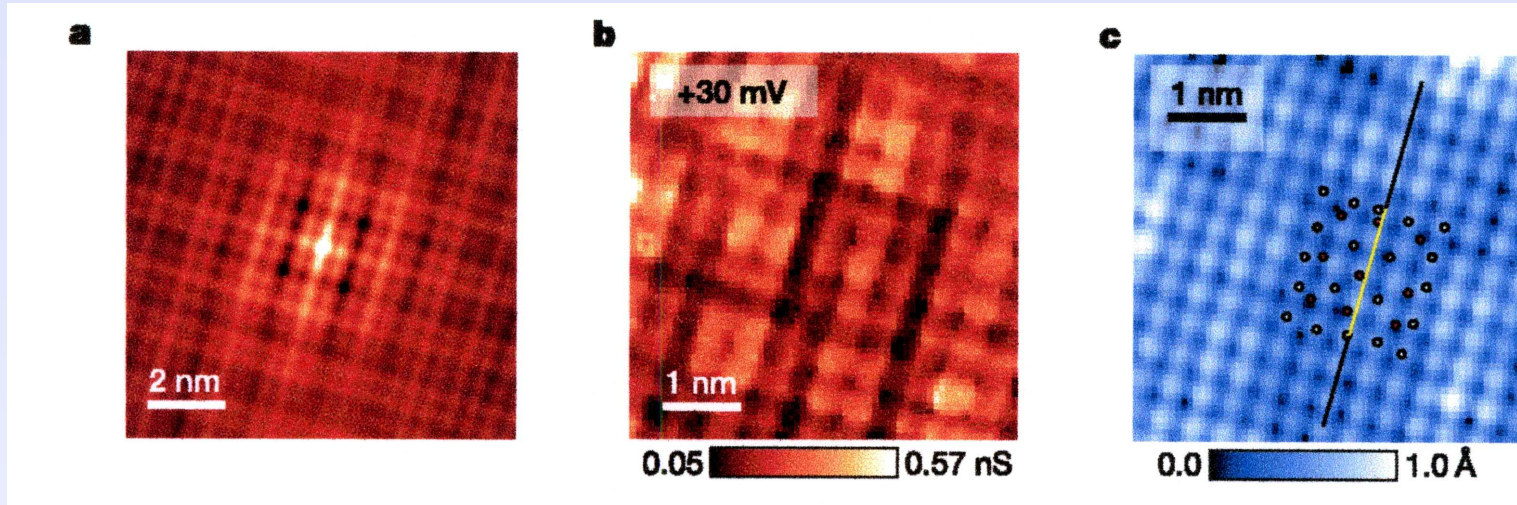
Spectral weight of Nd-LCSO near ε_f



Zhou et al. Phys. Rev. Lett. (2001)

- (a) $x=0.10$, 30 meV
- (b) $x=0.10$, 300 meV
- (c) $x=0.15$, 30 meV
- (d) $x=0.15$, 300 meV

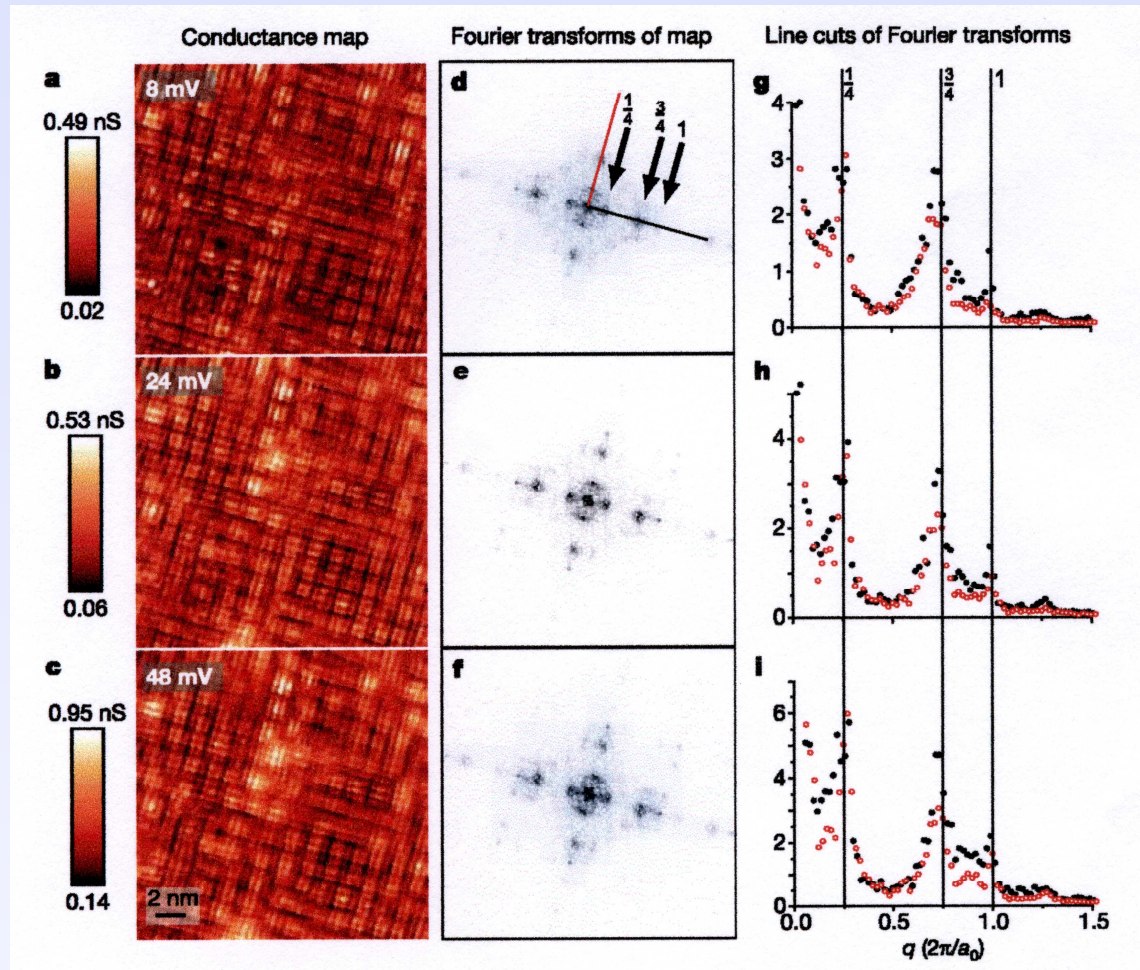
4x4 'Tile' Phase in $\text{Na}_{0.1}\text{Ca}_{1.9}\text{CuO}_2\text{Cl}_2$



autocorrelation dI/dV topographic
conductance \propto PDOS

Hanaguri *et al.* Nature (2004)

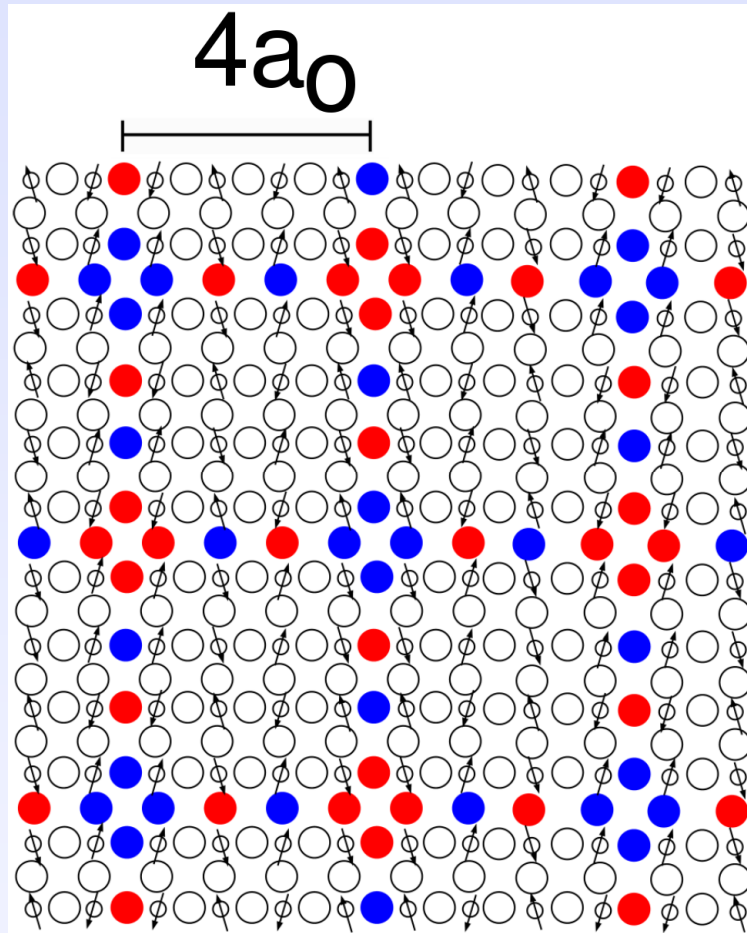
4x4 'Tile' Phase in $\text{Na}_{0.1}\text{Ca}_{1.9}\text{CuO}_2\text{Cl}_2$



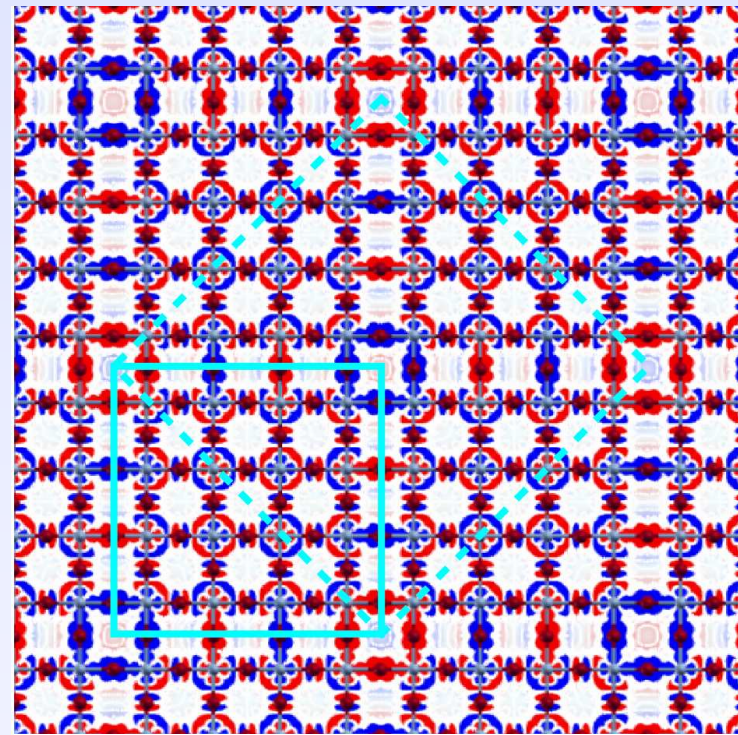
Hanaguri *et al.* Nature (2004)

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Hybrid DFT: $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/8$

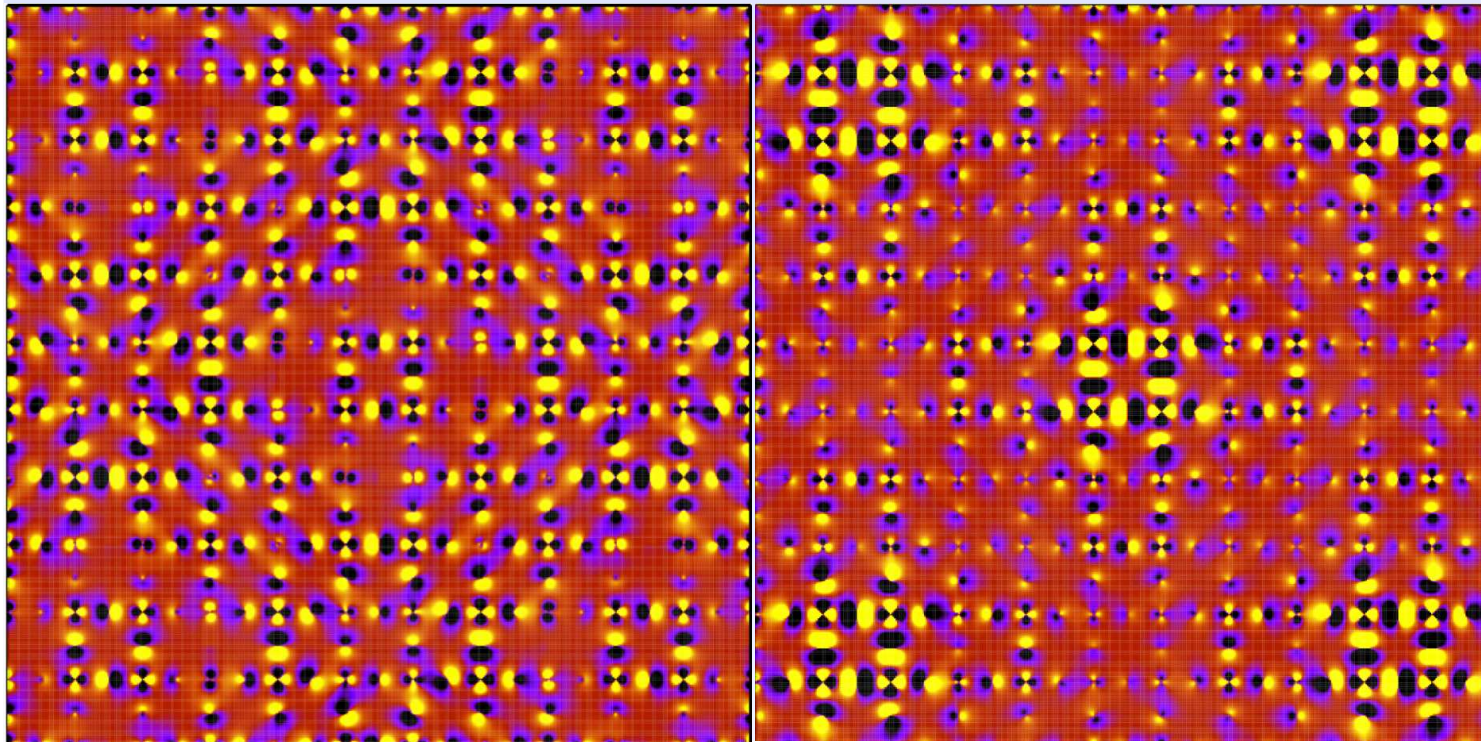


Magnetic Anti-Phase Boundaries



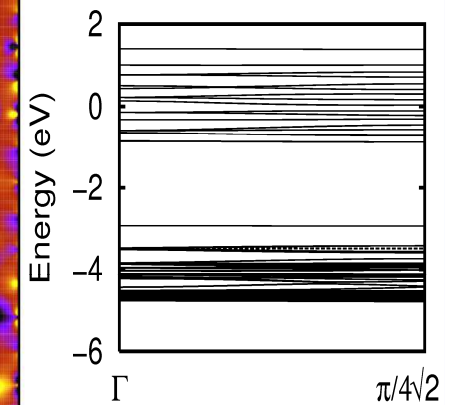
Spin Density

Hybrid DFT: $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/8$

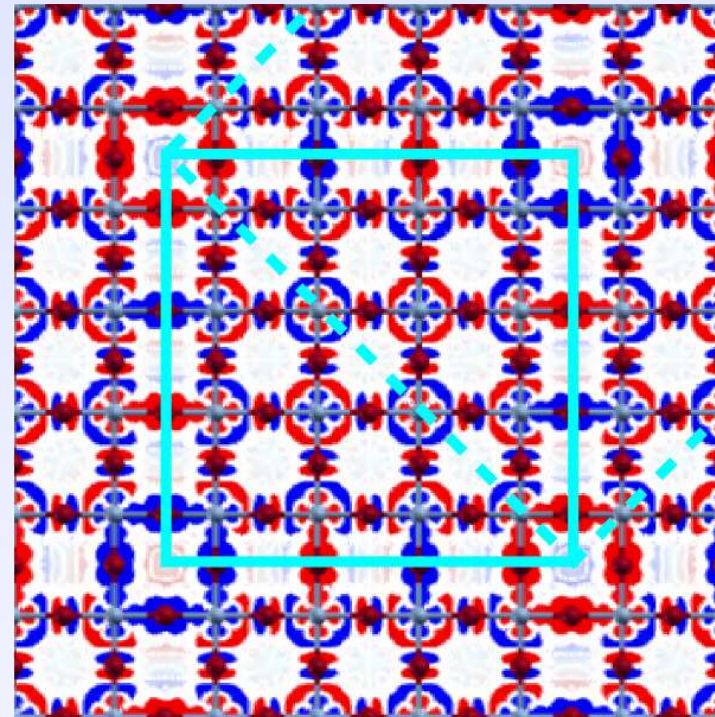
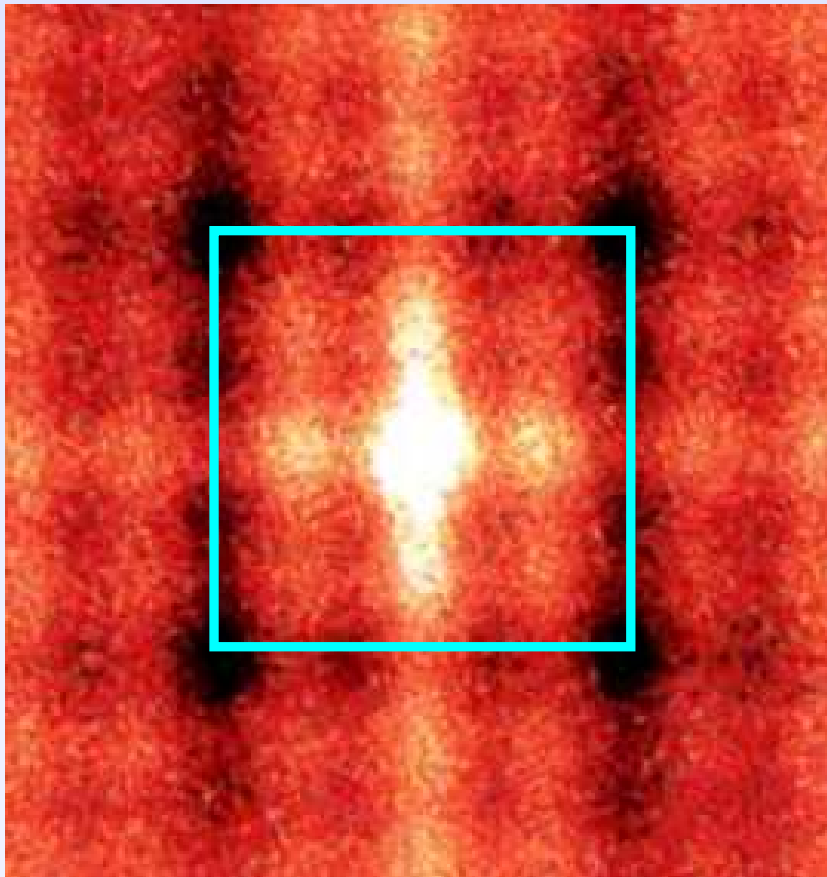


Ψ Amplitude (Γ point, occupied)

Ψ Amplitude (Γ point, band gap)

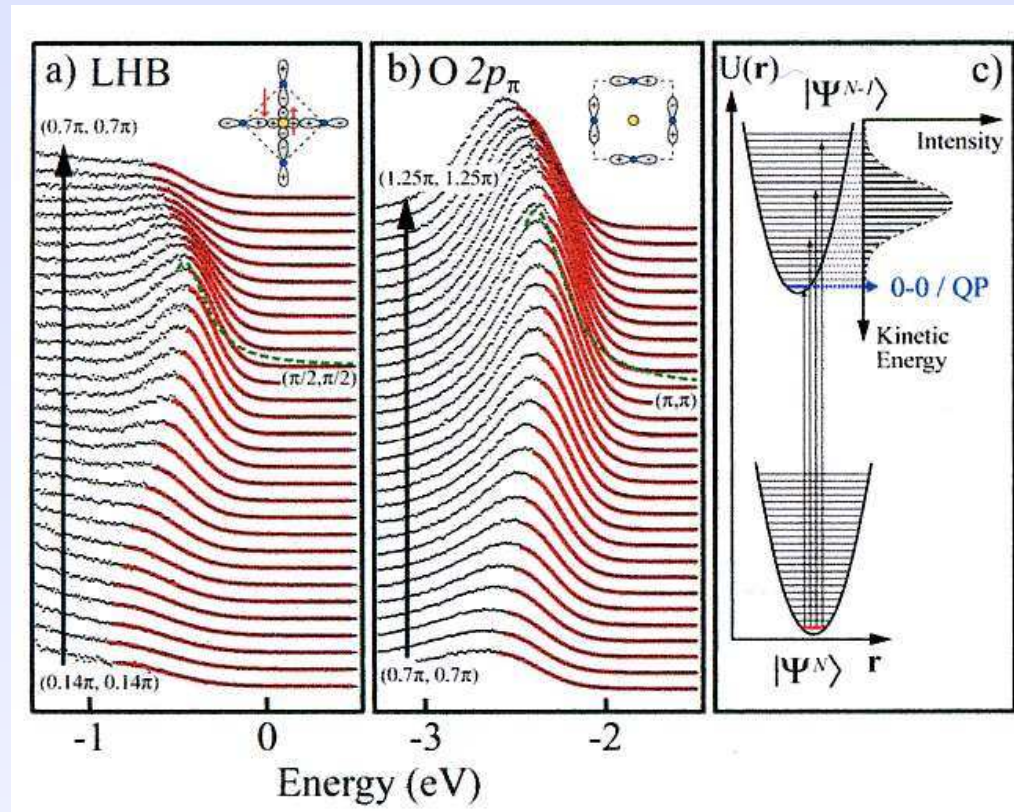


$4\sqrt{2} \times 4\sqrt{2}$ Magnetic Supercell



- Charge unit cell
- - - Magnetic unit cell

Recent Photoemission $\text{Ca}_2\text{CuO}_2\text{Cl}_2$



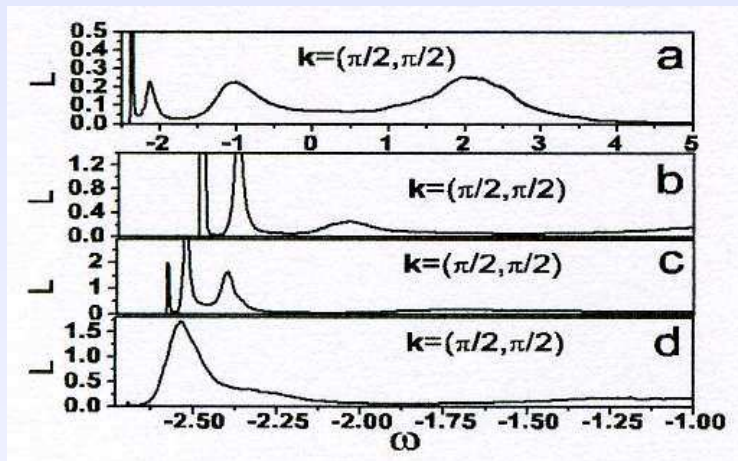
Photoemission lineshapes well fitted by Gaussian profile
Both LHB and O $2p_\pi$ states broadened into Gaussian
Broadening mechanism is phonon, not magnon
Photo-holes are small polarons

t - J + electron-phonon coupling

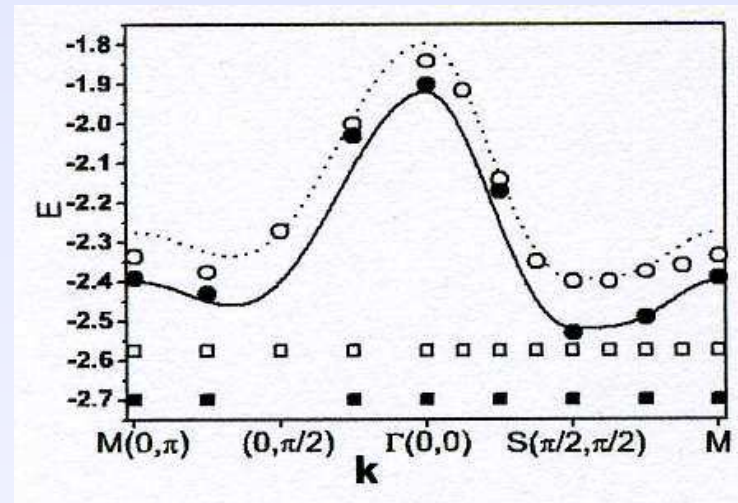
$$H = H^{t-J} + H^{e-ph}$$

$$H^{e-ph} = \Omega \sum_k b_k^\dagger b_k + \frac{\gamma}{N} \sum_{k,q} [h_k^\dagger h_{k-q} b_k + H.c.]$$

$$g = \frac{\gamma^2}{8t\Omega}$$

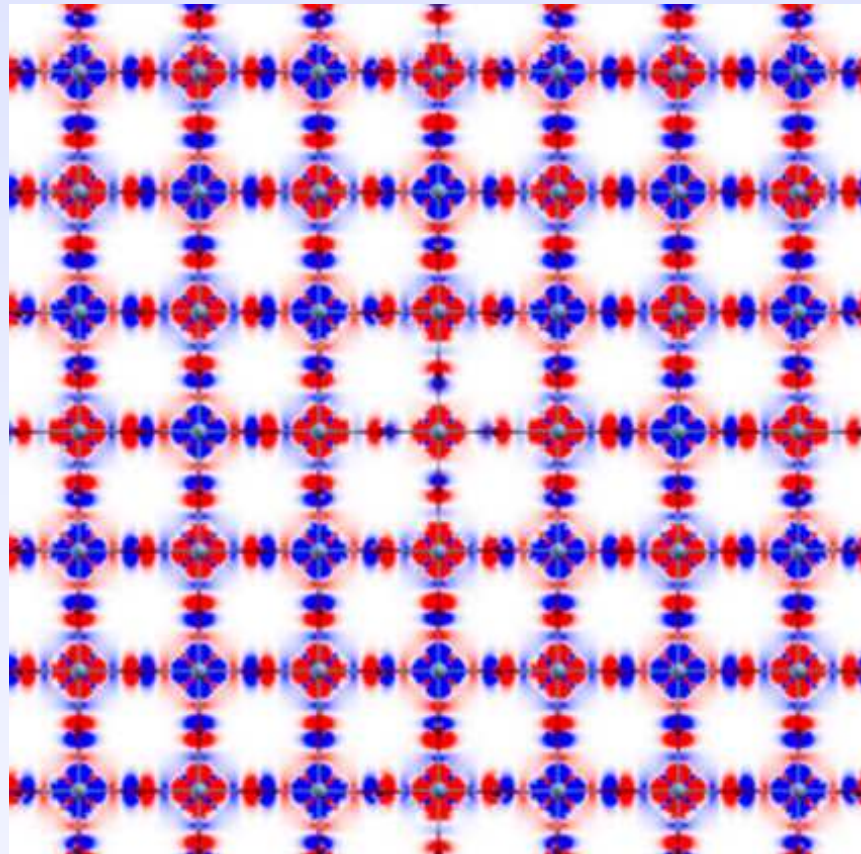


- (a) $g = 0$
- (b) $g = 0.14$ $\gamma = 0.34$
- (c) $g = 0.20$ $\gamma = 0.40$
- (d) $g = 0.23$ $\gamma = 0.43$



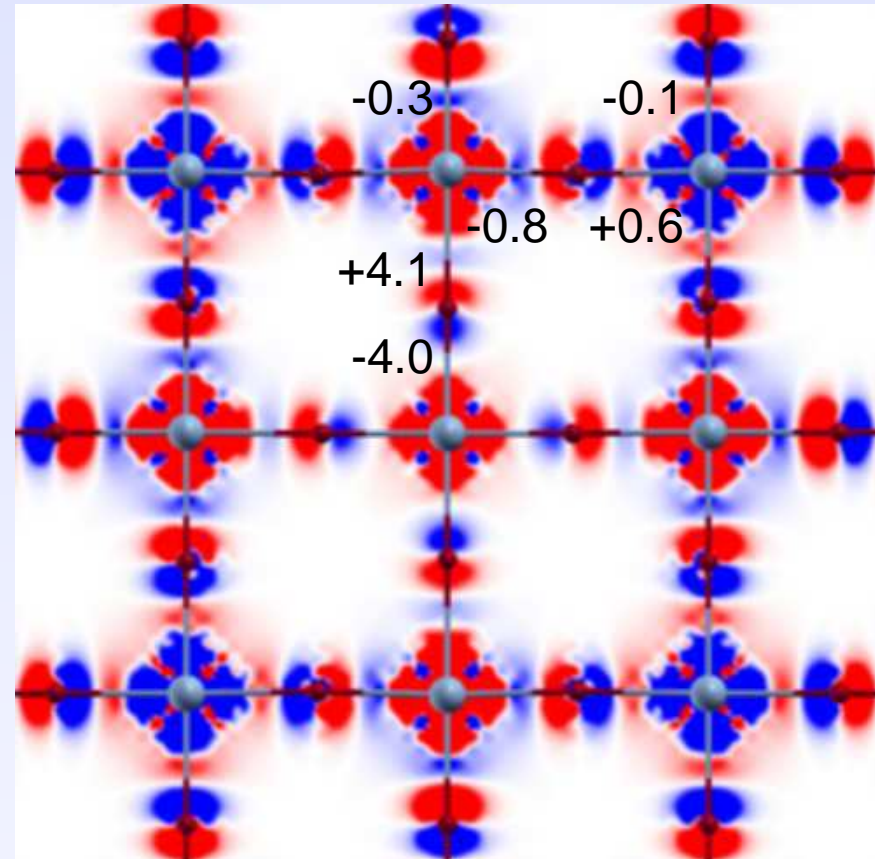
Spectral function consists of self-trapped quasi-particle state with vanishing spectral weight plus 'broad feature' which tracks t - J dispersion

Small polarons: $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ $x=1/32$



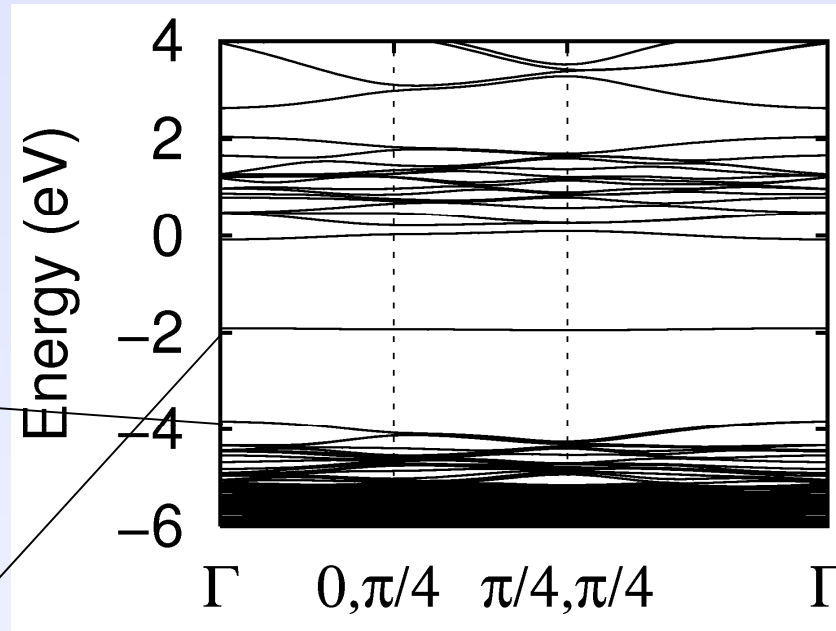
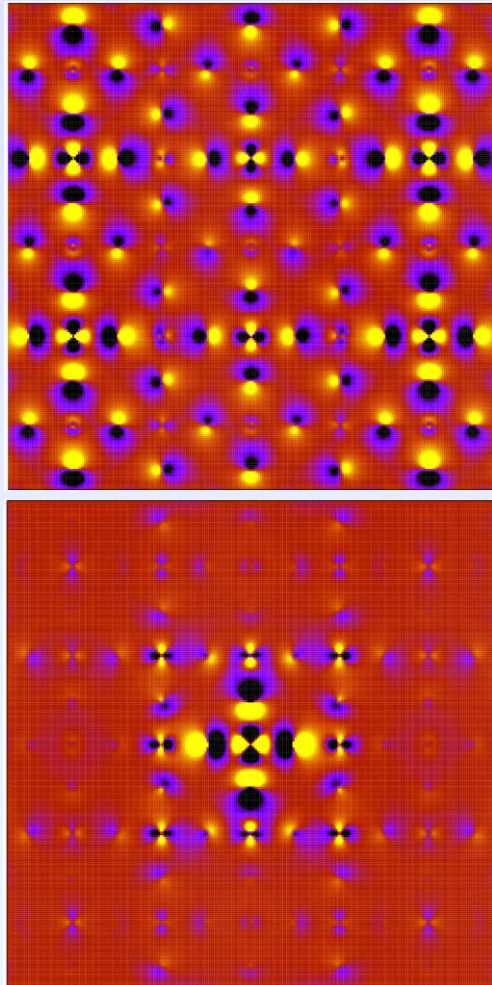
B3LYP A = 0.3

Bond length changes (%)



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Small polaron band structure



Polaron band structure

Calculation performed in 4x4 cell
Hole localises for $A = 0.3$
Vacant state formed at mid-gap

Conclusions

- Polarons key to understanding doped oxides
- Local charge order on O ions
- How do stripes/polarons affect T_c in CMR, HTS, DMS oxides?
- Hybrid DFT
 - short range properties need more exchange
 - Long range properties need less exchange

Acknowledgements

Coworkers

Dr. Guang Zheng

Dr. Nikos Konstantinidis

Marco Nicastro

Andrew Rowan

Funding

HEA PRTL I cycle III IITAC2 project

Enterprise Ireland