

Electron Self-Organization and Insulating Ground State of Cuprate Superconductors

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Outlines

- Brief History of Superconductivity
- Basics of High-Tc Cuprates
- Electron Self-Organization in High-Tc Cuprates inferred through
 - Unusual Metallic Transport
 - Peculiar Localization Behavior

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Superconductivity

- **1911**: Discovery of zero resistivity in mercury by H. Kamerlingh-Onnes

(1913 Nobel Prize)



- **1957**: Bardeen, Cooper and Schrieffer explained the superconductivity in metals (BCS theory)



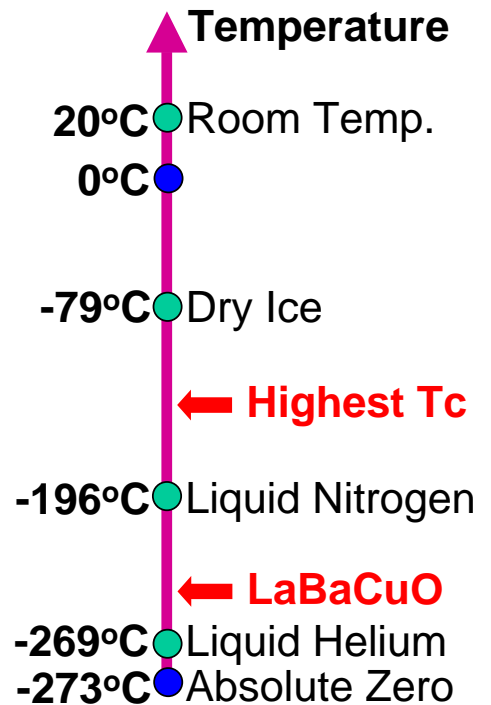
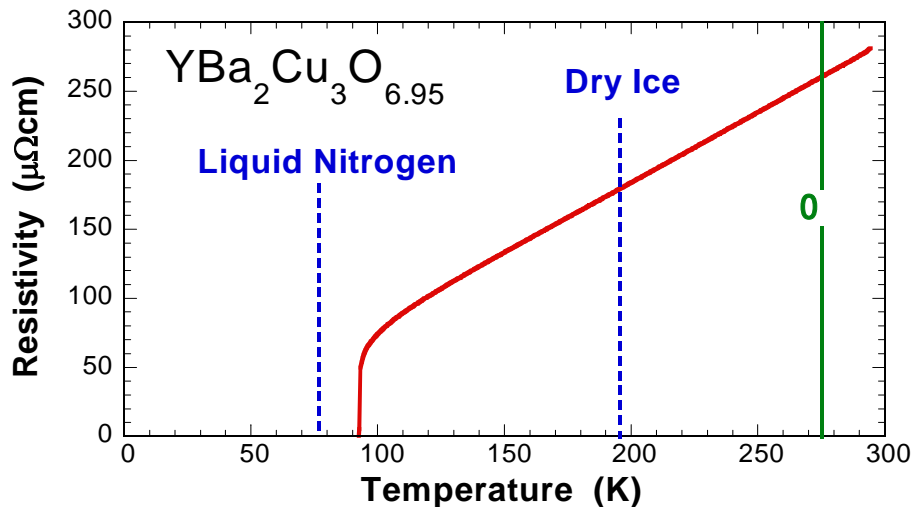
(1972 Nobel Prize)

High-Temperature Superconductivity

- Discovered by Bednorz and Müller in a **copper oxide** (cuprate) in **1986**



(1987 Nobel Prize)



Transition Temperature T_c

- BCS superconductors

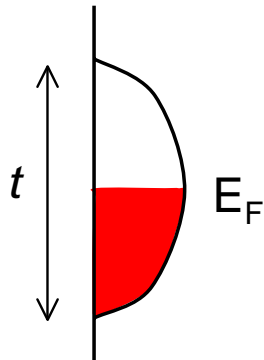
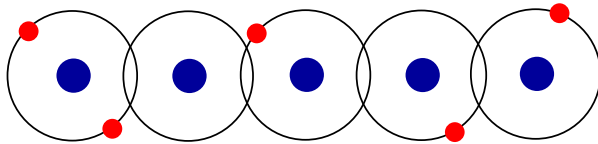
$$k_B T_c = 1.13 \hbar \omega_D \cdot e^{-\frac{1}{N(0)|V|}}$$

- Higher T_c is achieved with:
 - Larger ω_D → lighter elements
 - Larger $N(0)$ → van Hove singularity *etc.*
 - Larger $|V|$ → stronger electron-phonon int.
- What about copper-oxide superconductors?
 - ***Need to understand the HTSC mechanism!***

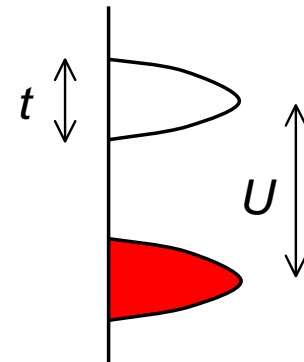
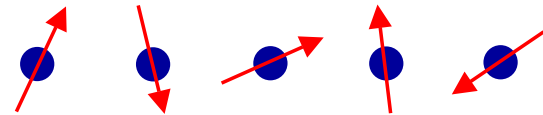
High-Temperature Superconductor

- Parent Cuprate La_2CuO_4 : **Mott Insulator**

Conventional Metal



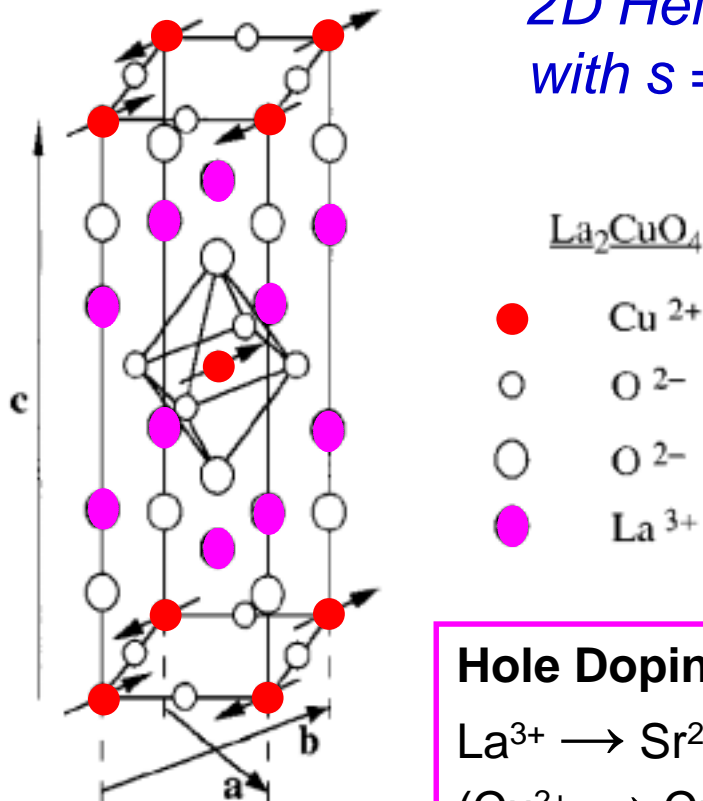
Mott Insulator



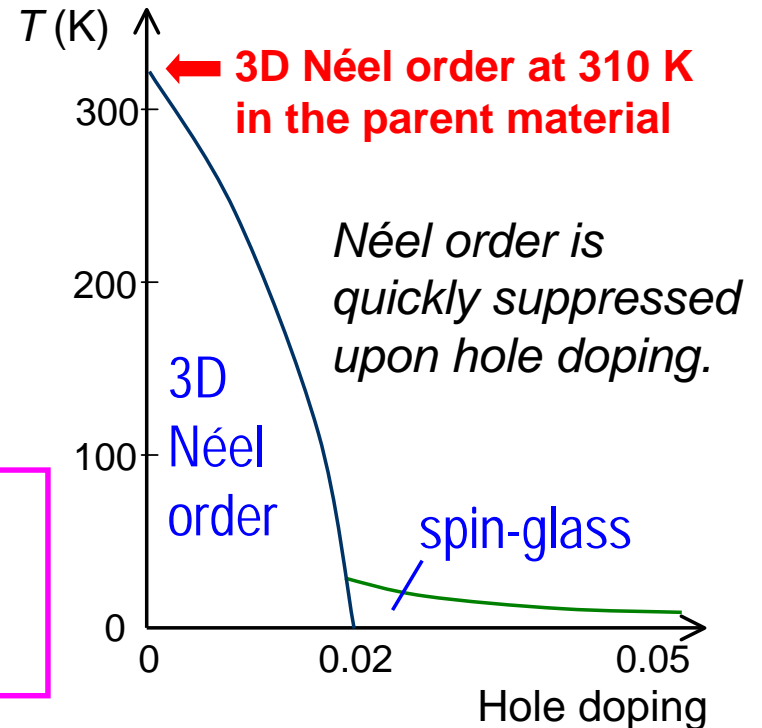
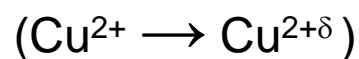
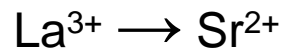
High-Temperature Superconductor

- Parent Cuprate La_2CuO_4 : **Mott Insulator**

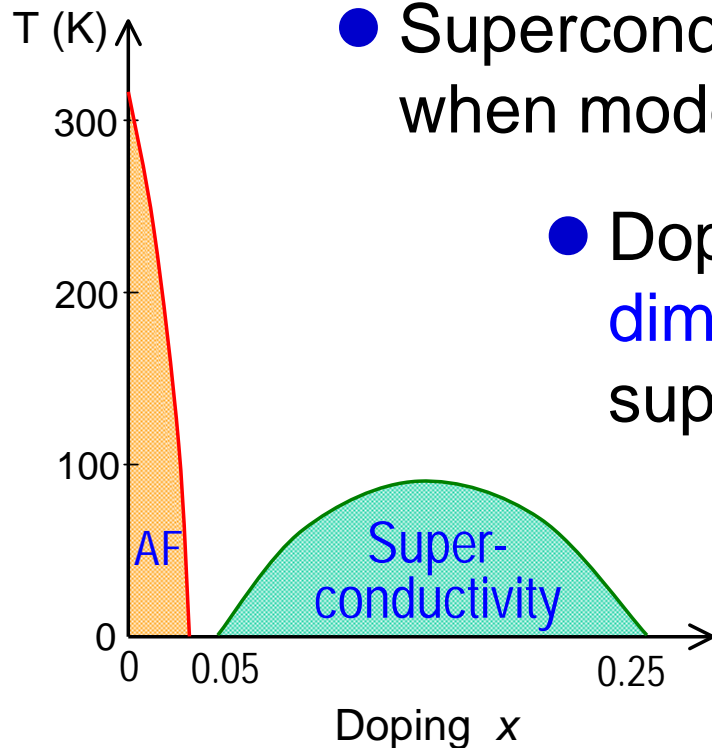
*2D Heisenberg Antiferromagnet
with $s = 1/2$ on a square lattice*



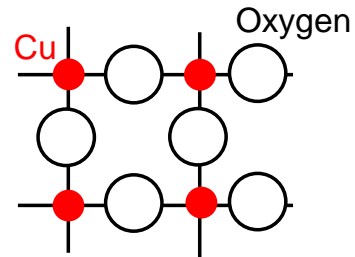
Hole Doping:



Further Doping



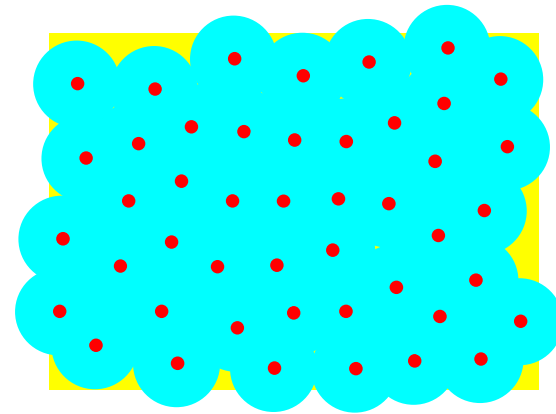
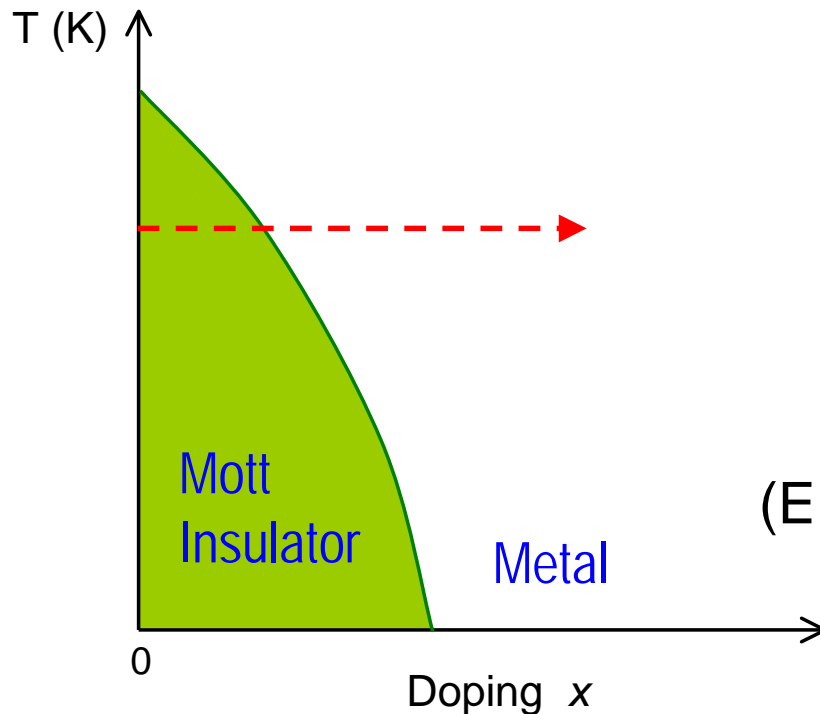
- Superconductivity shows up when moderately doped.
- Doped holes go into the **two-dimensional CuO_2 planes**, which support metallic transport.



How does the **metallic transport** emerge in the CuO_2 planes when holes are doped?

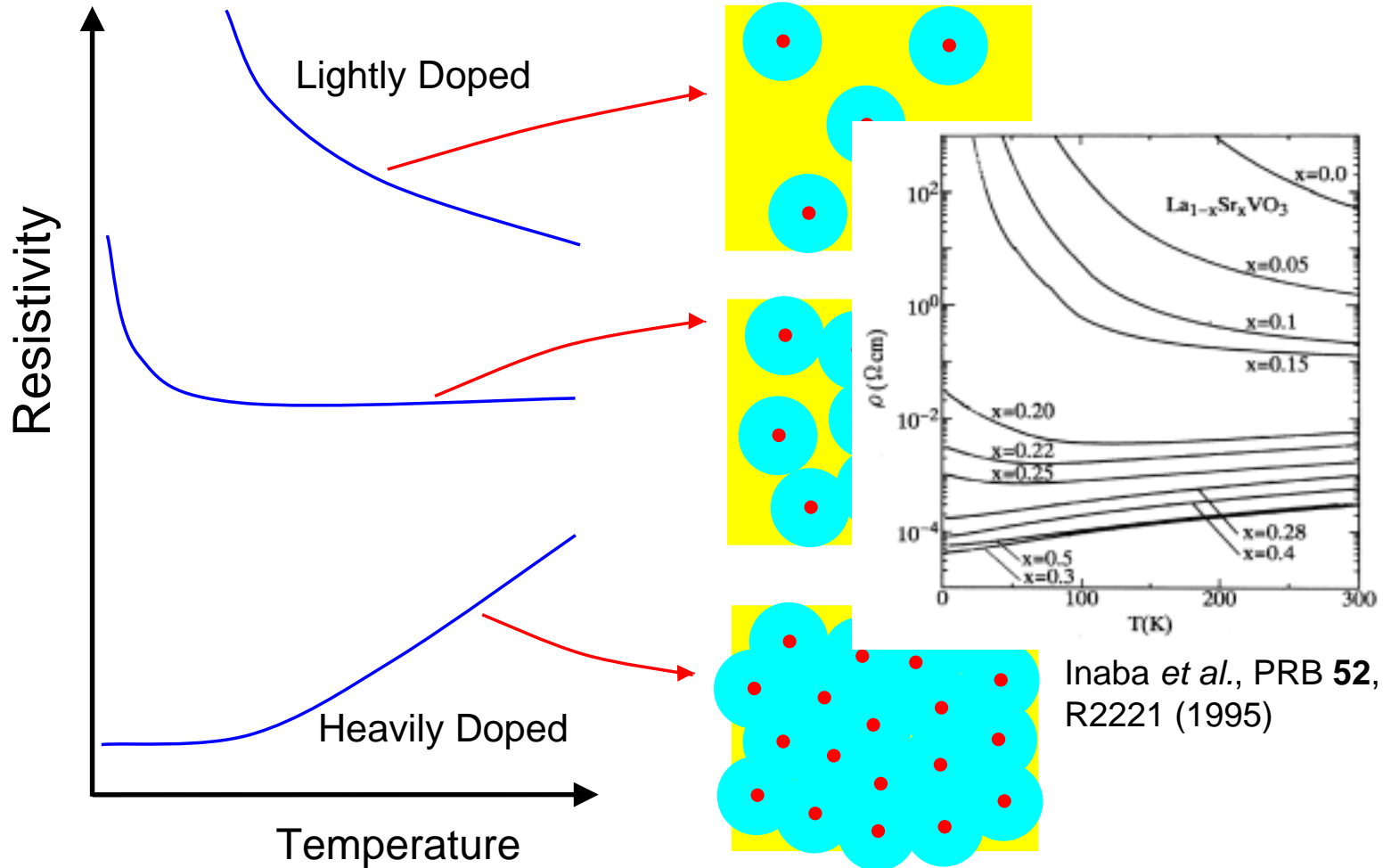
Ordinary Insulator-Metal Transition

- Carrier Doping to Mott Insulator

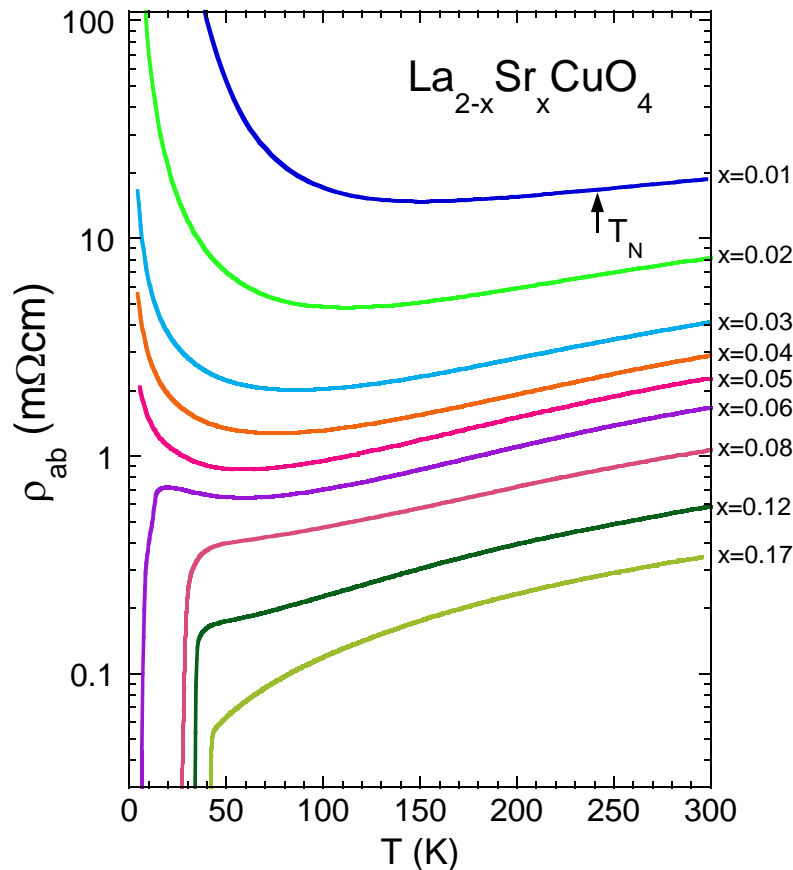


Metallic State
(Electrons form Bloch waves)

Ordinary Insulator-Metal Transition



Unusual Metallic Transport in LSCO

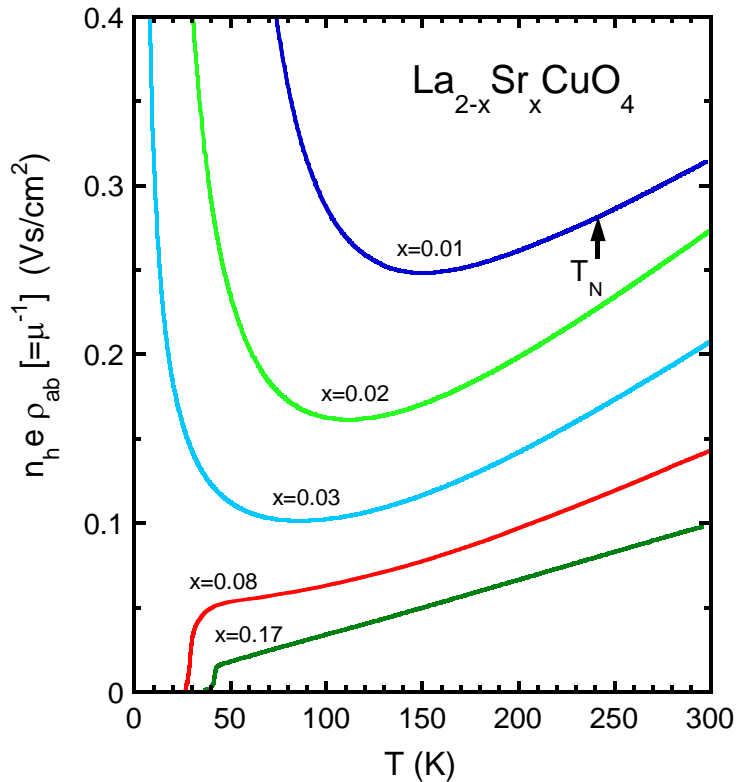


- Metallic behavior is observed at only 1% doping.
- Magnitude of ρ_{ab} at $x = 0.01$ is *too large* for a 2D metal.

(Electron mean free path would be *shorter* than their de Broglie wave length.)

Y. Ando *et al.*, PRL **87**, 017001 (2001)

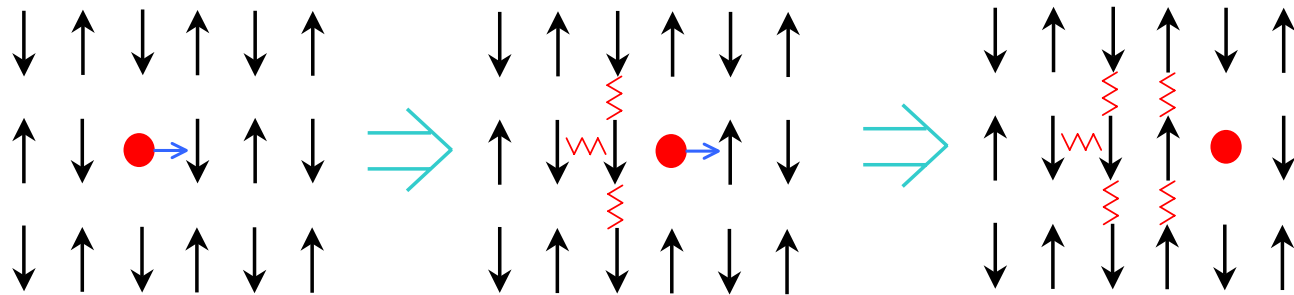
Mobility of Holes



- The mobility of doped holes in the Néel state (at $x = 0.01$) is not much different from that at optimum doping.

Motion of a Hole in an Antiferromagnet

Motion of a single hole frustrates the AF bonds.

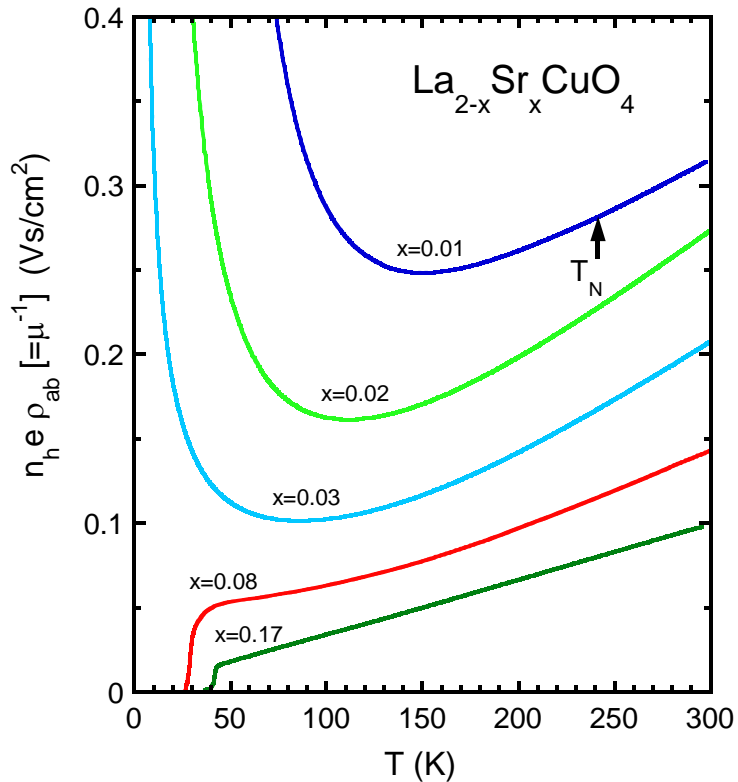


⚡: frustrated bond

⇒ Antiferromagnetic order should impose a **large effective mass** on doped holes.

cf. E. Dagotto, RMP **66**, 763 (1994)

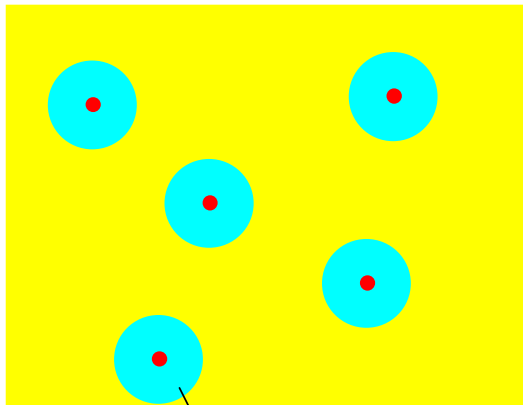
Mobility of Holes



- “High” mobility in the Néel state is unusual.

*Mobility in LSCO (3-10 cm²/Vs) is comparable to that in Pb (2.5 cm²/Vs) at 300 K.

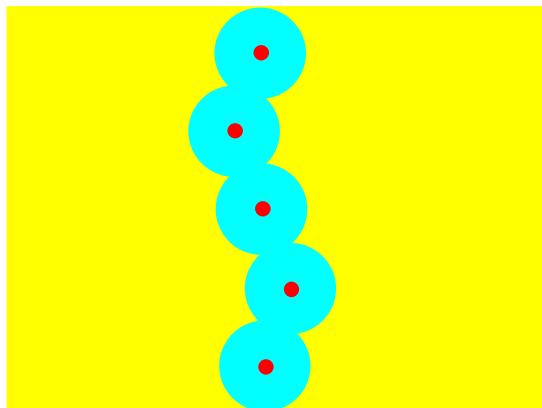
Transport Mechanism (simple picture)



electron wave function

Random Distribution

⇒ **Localize**

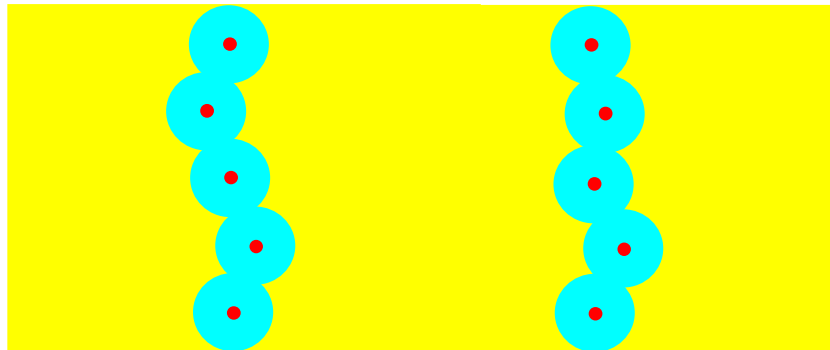


Electron Self-Organization
(Stripe Formation)

⇒ **Metallic Transport**

Transport through Stripes

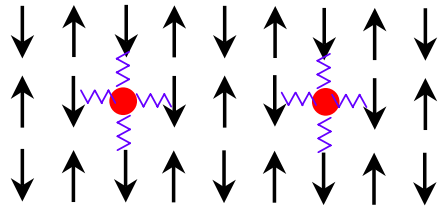
- Self-organization picture naturally explains ...
 - Insensitivity of the metallic transport to the Néel ordering
 - Too large bulk resistivity
 - Weak doping-dependence of the mobility



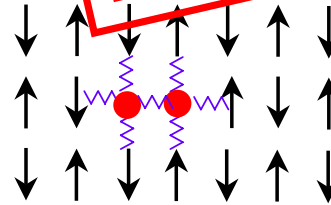
Why Stripes are Formed?

- Antiferromagnets tend to **expel** holes.

⚡: broken bond



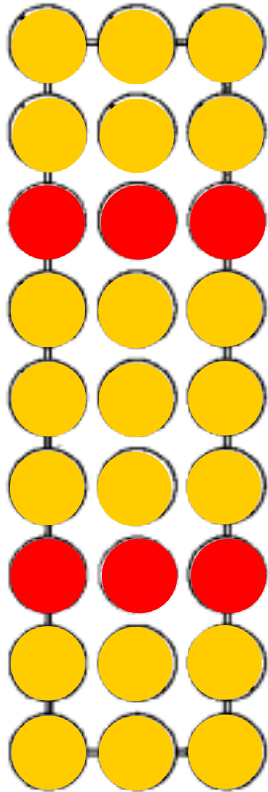
8 broken bonds
(Energy increase is $8J$)
 J : exchange int. energy



7 broken bonds
(Energy increase is $7J$)

- Holes tend to segregate, but *macroscopic* phase segregation will increase Coulomb energy and is prohibited.
- Kinetic energy can be lowered by forming stripes.

Stripes Seen in LSCO Family

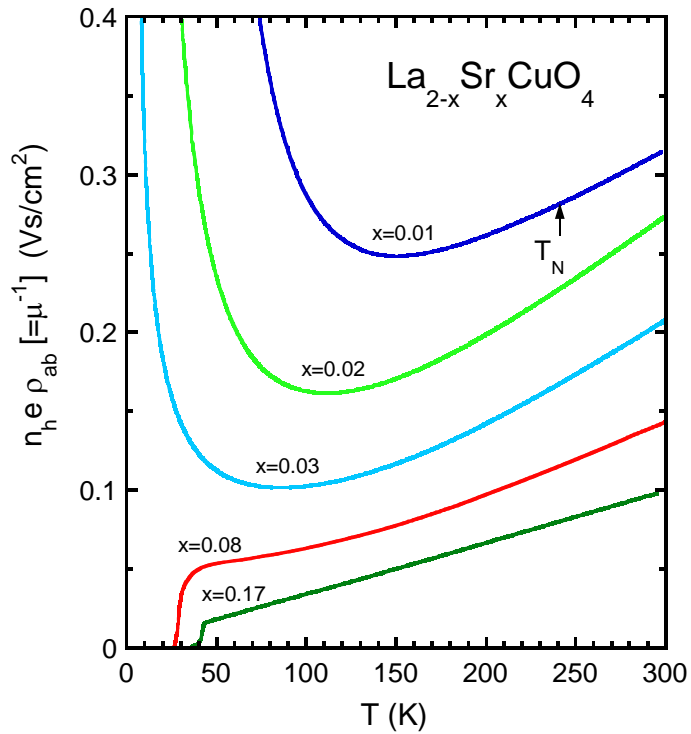


- Stripe order has been actually observed by neutron and X-ray scattering experiments.

J. M. Tranquada *et al.*,
Nature **375**, 561 (1995)

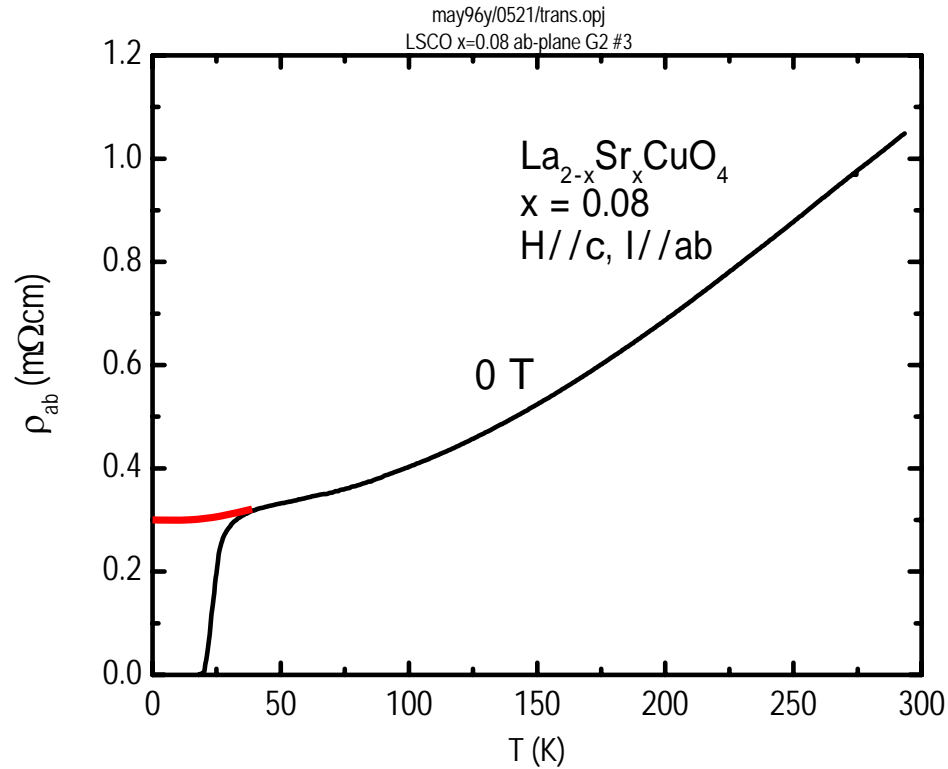
Peculiar Localization

We have seen ...

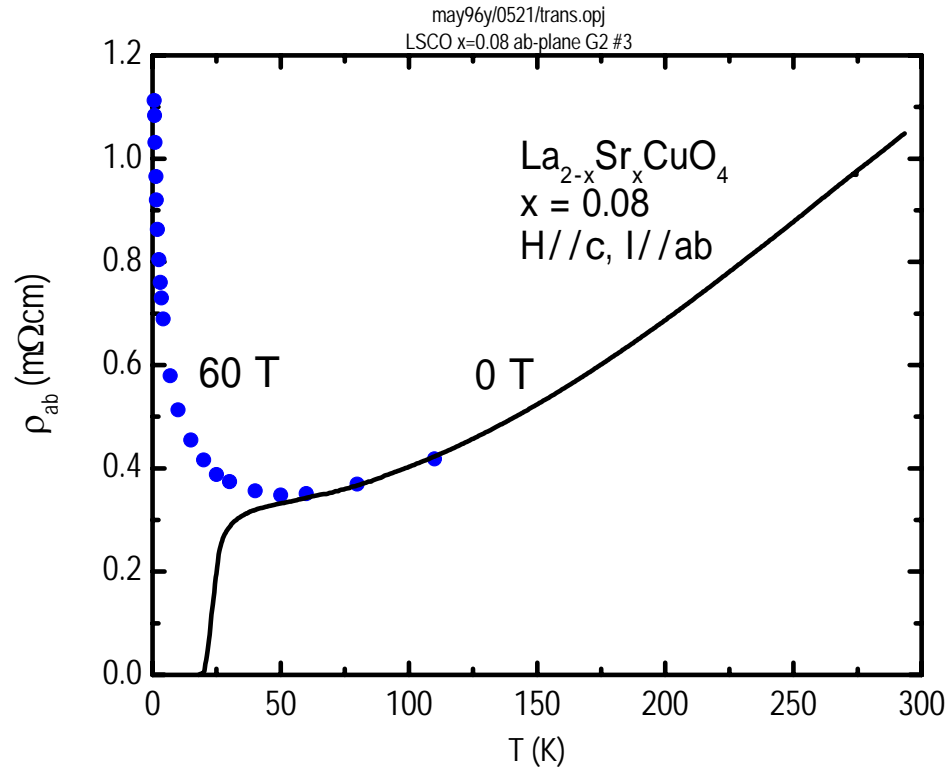


“Anomalous Metal” at moderate temperature down to very low doping.

However, that's not the whole story ...



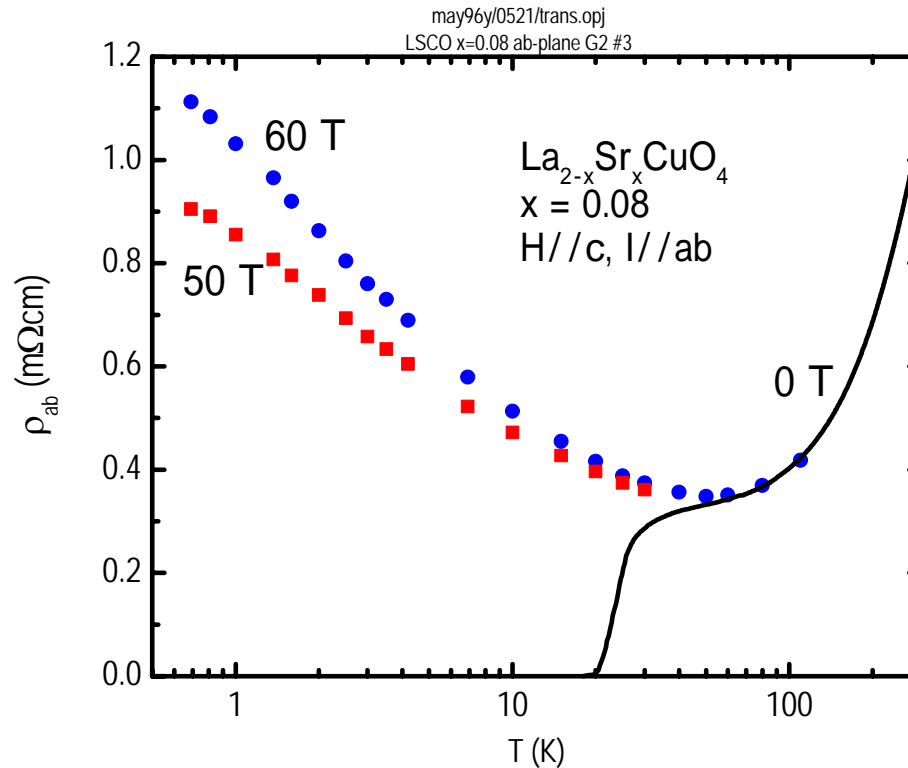
However, that's not the whole story ...



Pronounced **insulating behavior** shows up when superconductivity is suppressed by 60-T pulsed magnetic field.

Ando-Boebinger Experiment, 1995-1996

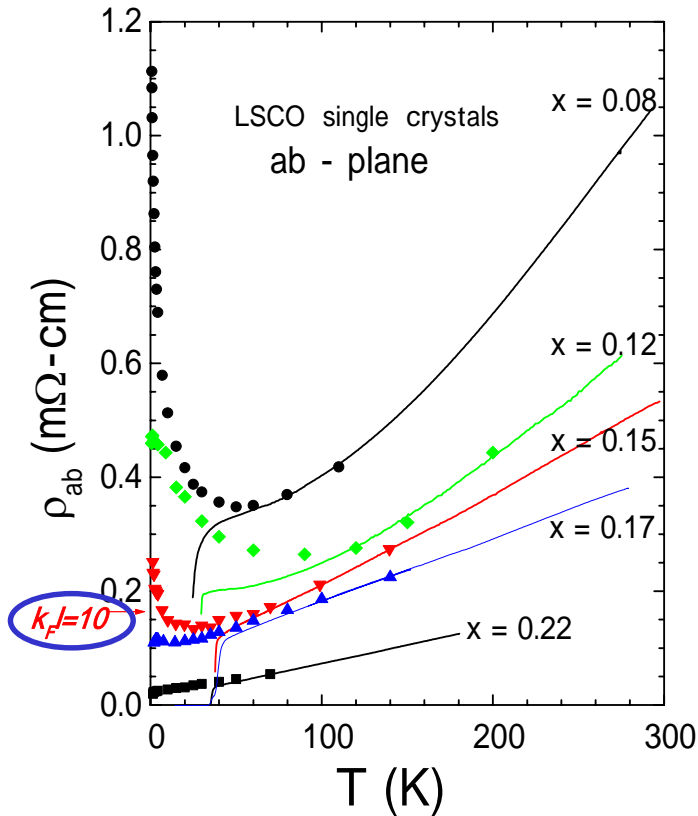
However, that's not the whole story ...



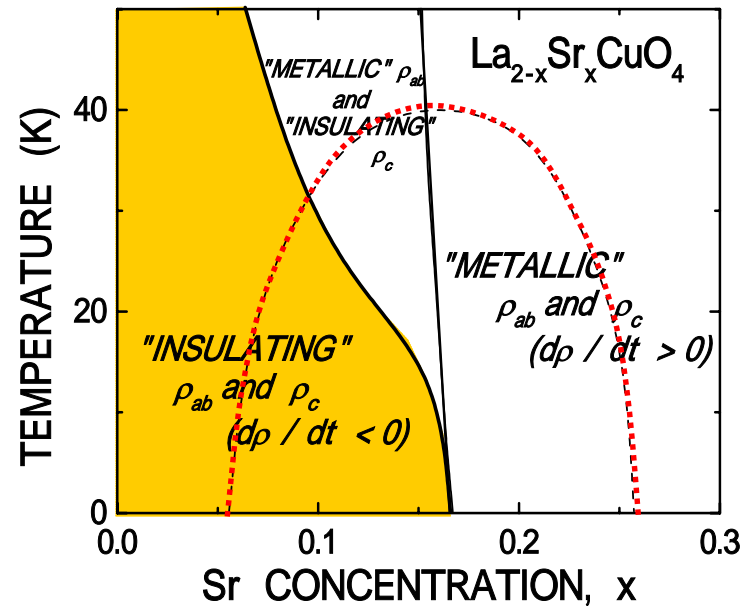
$\log(1/T)$ divergence of resistivity at low temperature

Y. Ando *et al.*, PRL **75**, 4662 (1995)

Metal-Insulator Crossover under 60 T

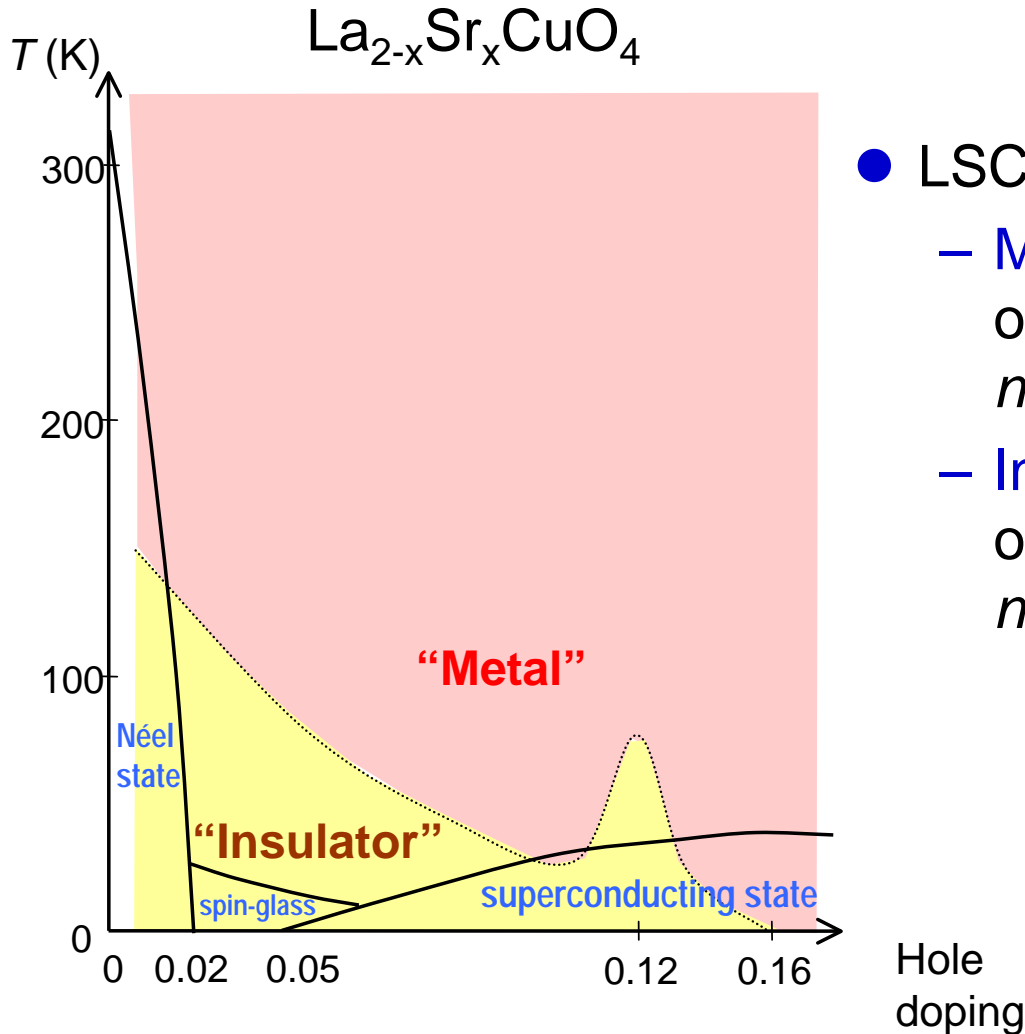


G. S. Boebinger, Y. Ando *et al.*,
PRL **77**, 5417 (1996)



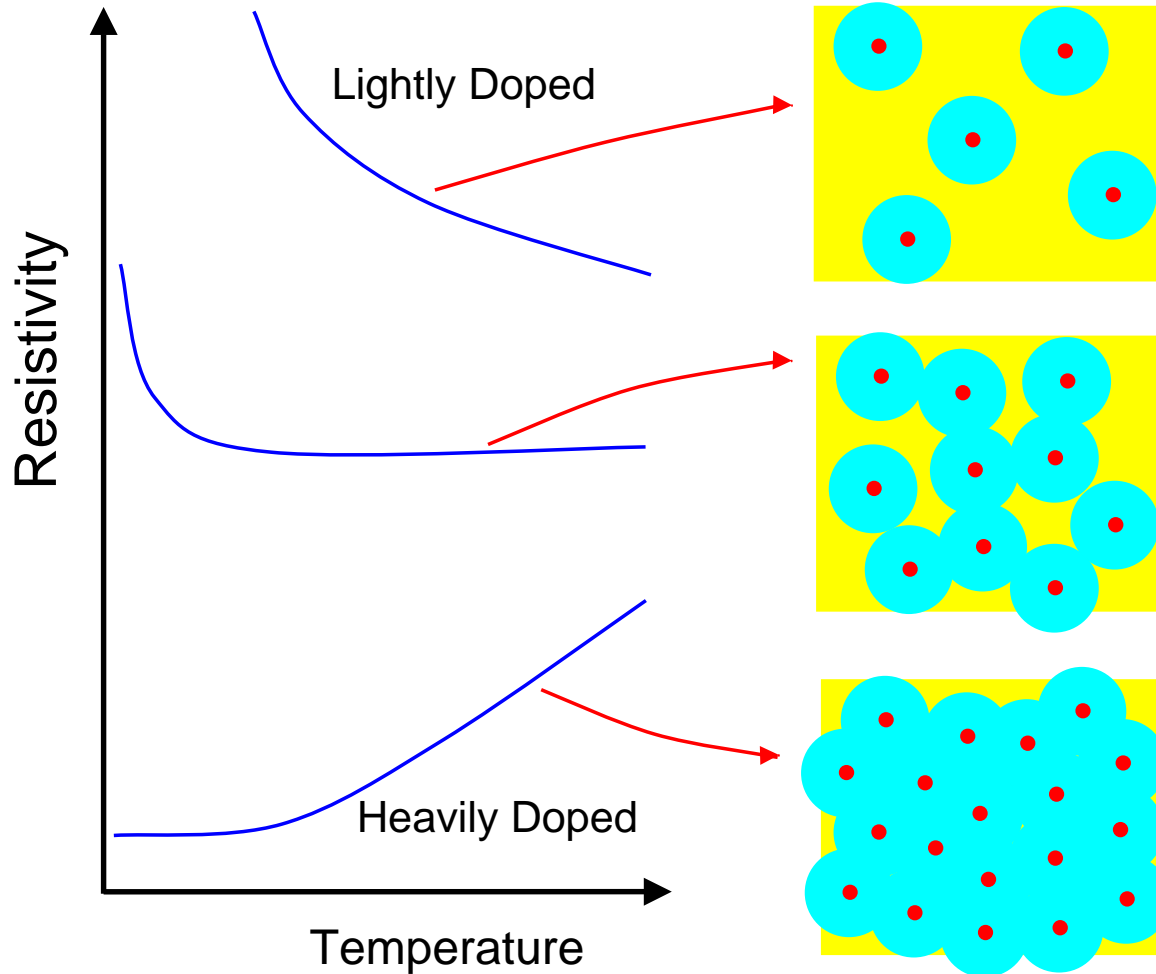
"Anomalous Insulator" at low temperature
(ρ_{ab} is too small for a 2D electron-localized system.)

Phase Diagram

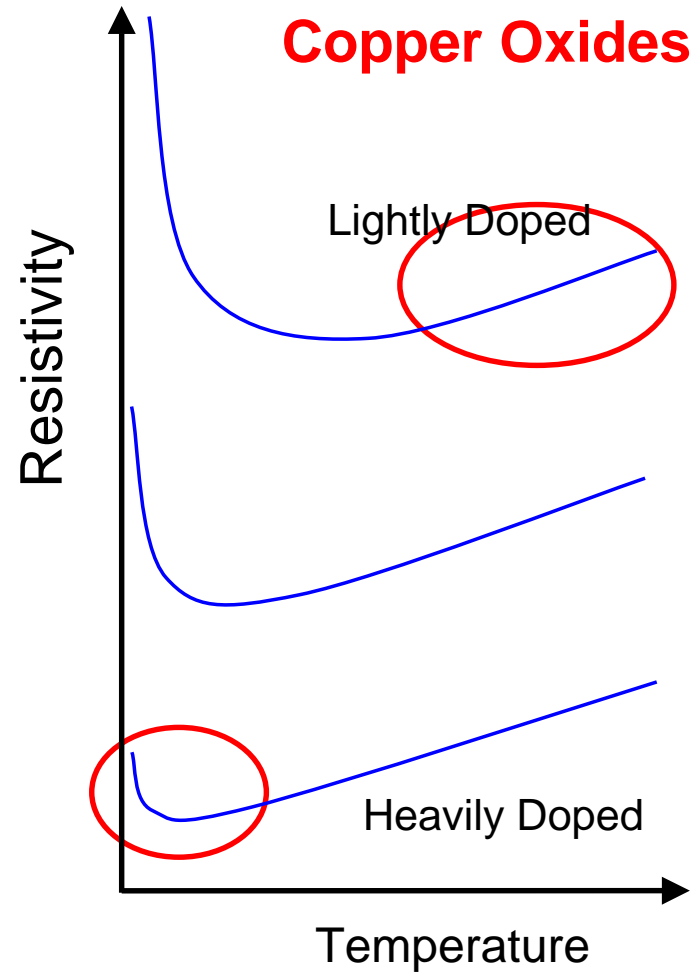
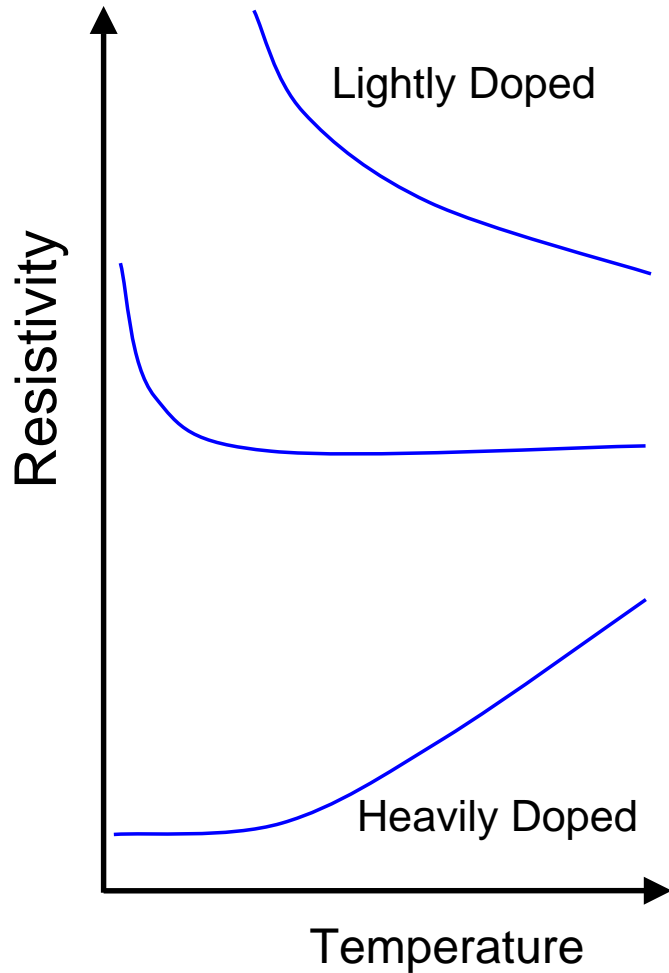


- LSCO is peculiar in that:
 - **Metallic behavior** is observed when it should *not* be a metal.
 - **Insulating behavior** is observed when it should *not* be an insulator.

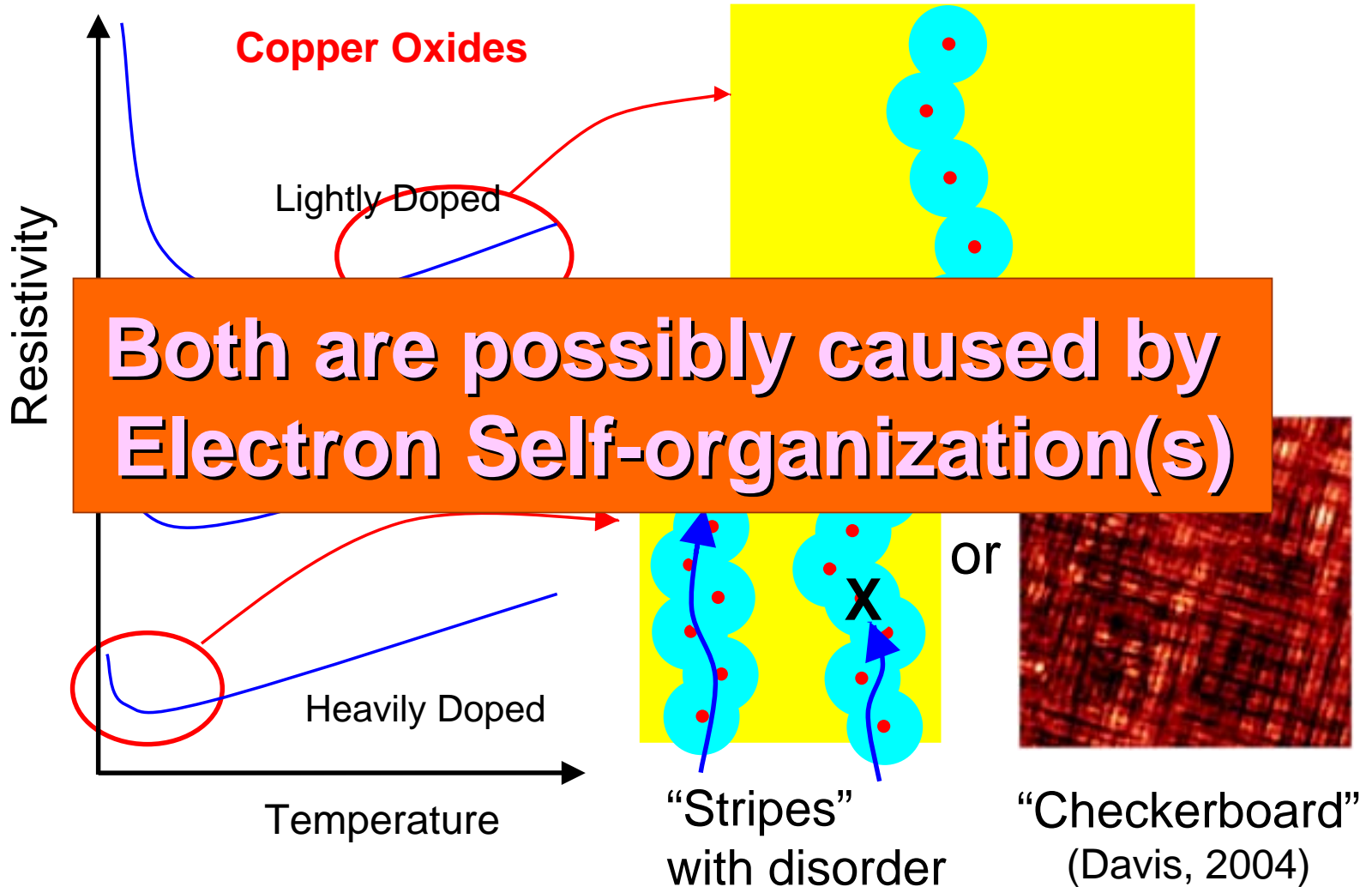
Ordinary Materials



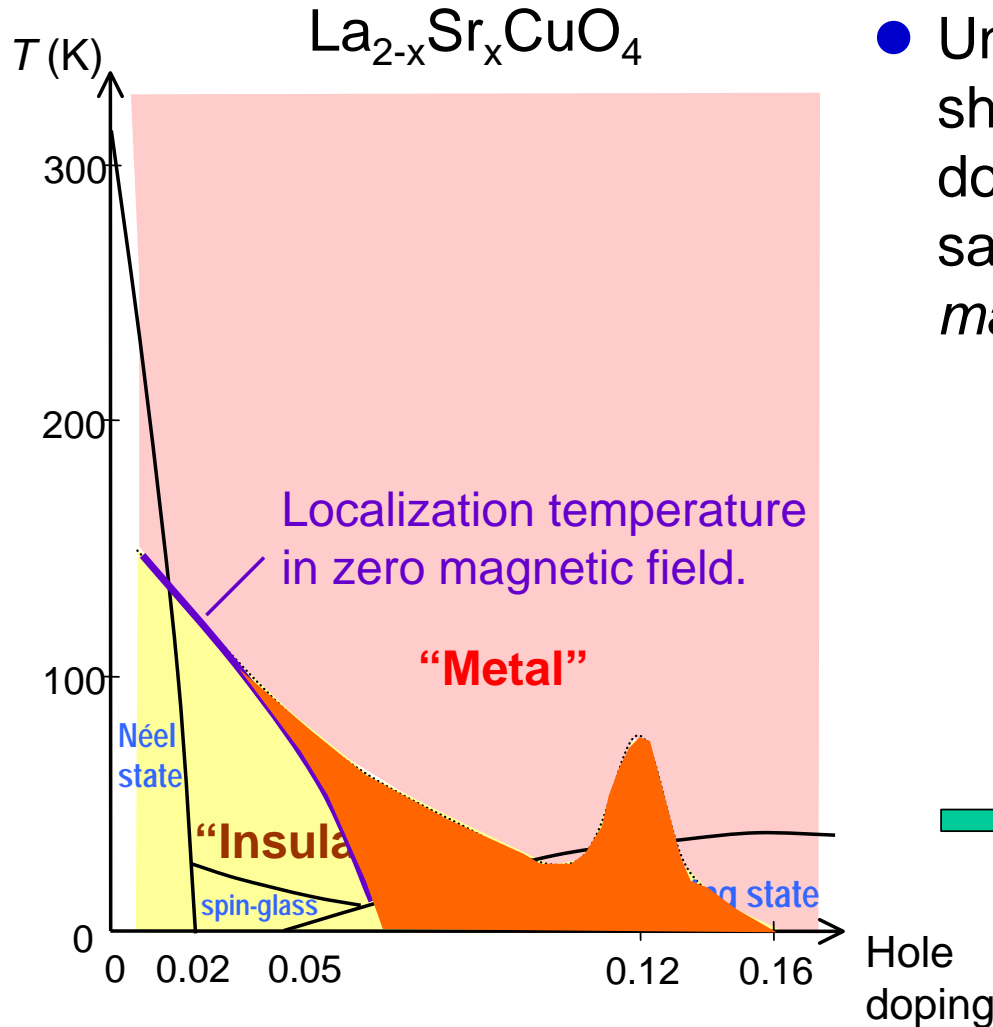
Comparison



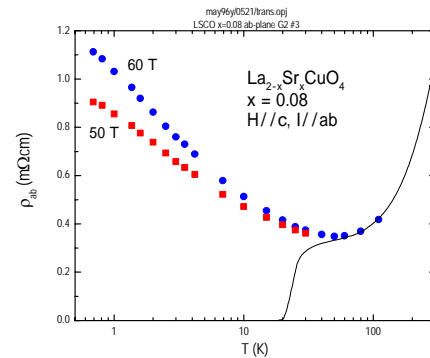
Copper Oxides



Phase Diagram (reprise)

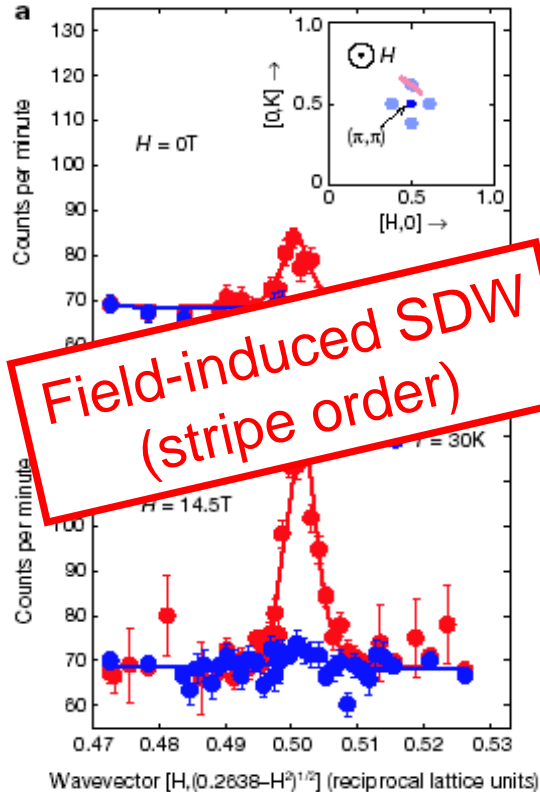


- Unusual Insulating state shows up under the SC dome in underdoped samples *when the magnetic field is applied.*

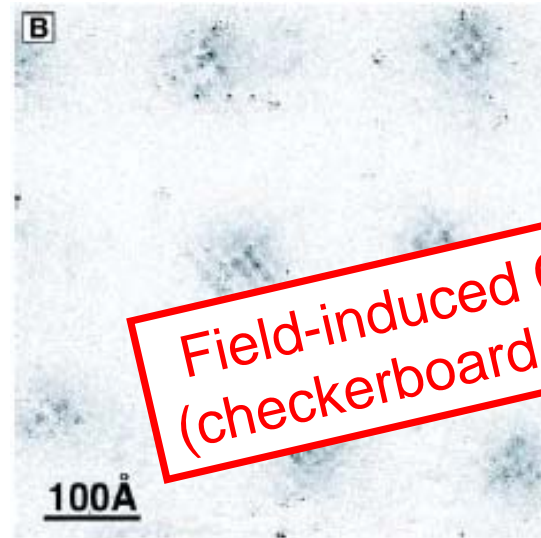


"Insulating State"
is caused by the magnetic field?

Magnetic-Field-Induced SDW/CDW



Field-induced SDW
(stripe order)



Field-induced CDW
(checkerboard order)

J. E. Hoffman *et al.*, Science **295**, 466 (2002)

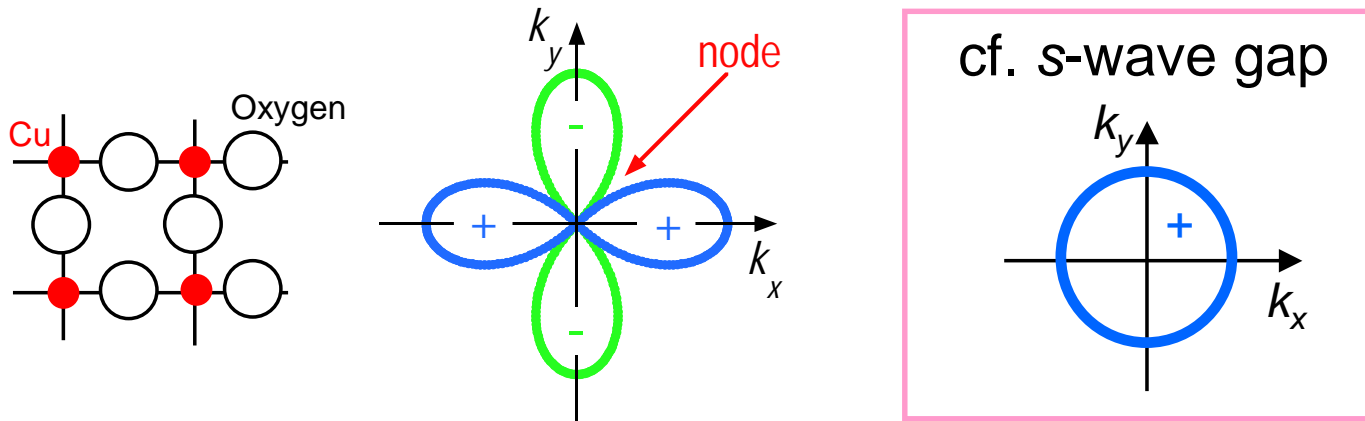
B. Lake *et al.*, Nature **415**, 299 (2002)

It is possible that these orders in the SC state are responsible for the localized state under 60 T.

Let's sort out the magnetic-field effect
in the superconducting state.

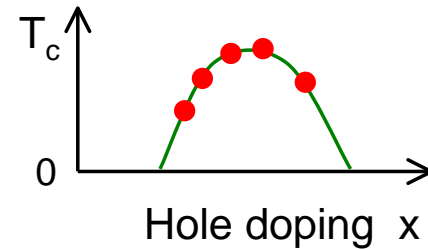
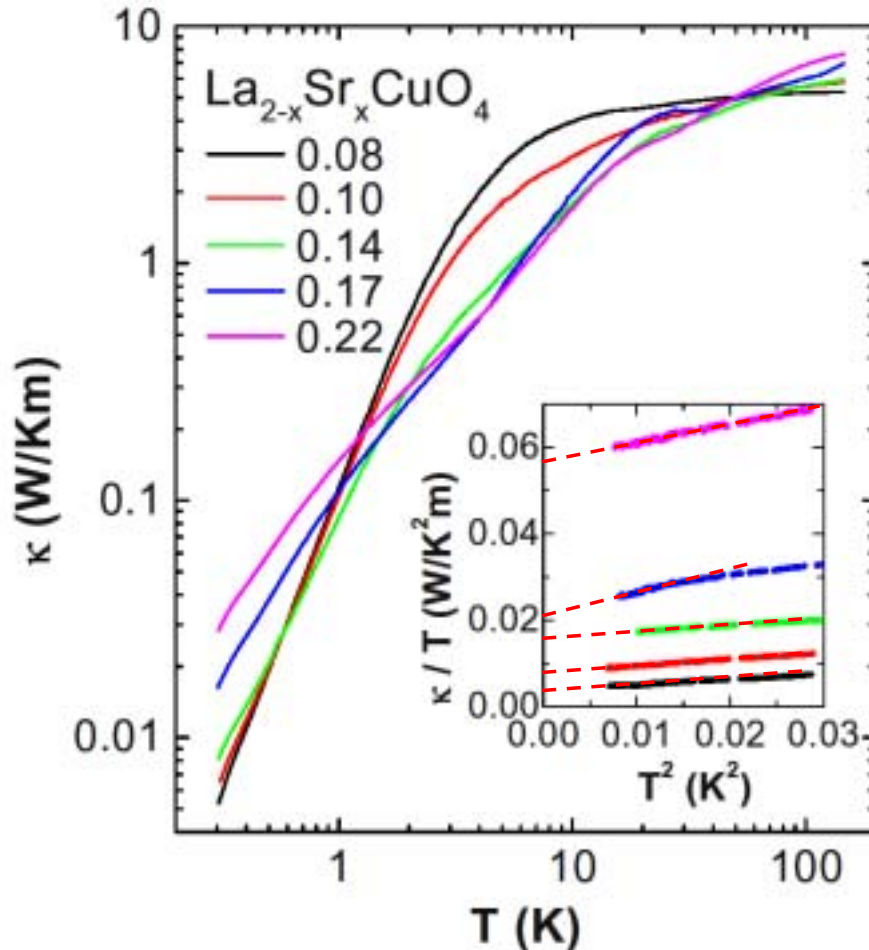
Heat Transport in the SC State

- Cuprates have a “*d*-wave” superconducting gap.



- Zero-energy quasiparticles exist near the **nodes** and carry heat in the *d*-wave SC state down to low T .

Quasiparticle Heat Transport at low T



Zero intercept of the κ/T vs. T^2 plot gives a measure of the QP transport at 0 K.

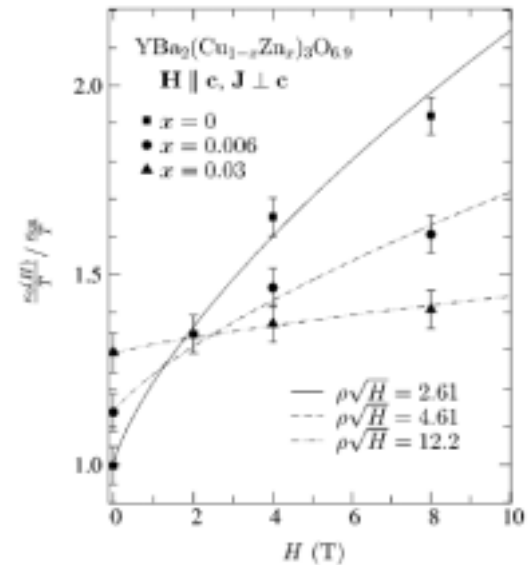
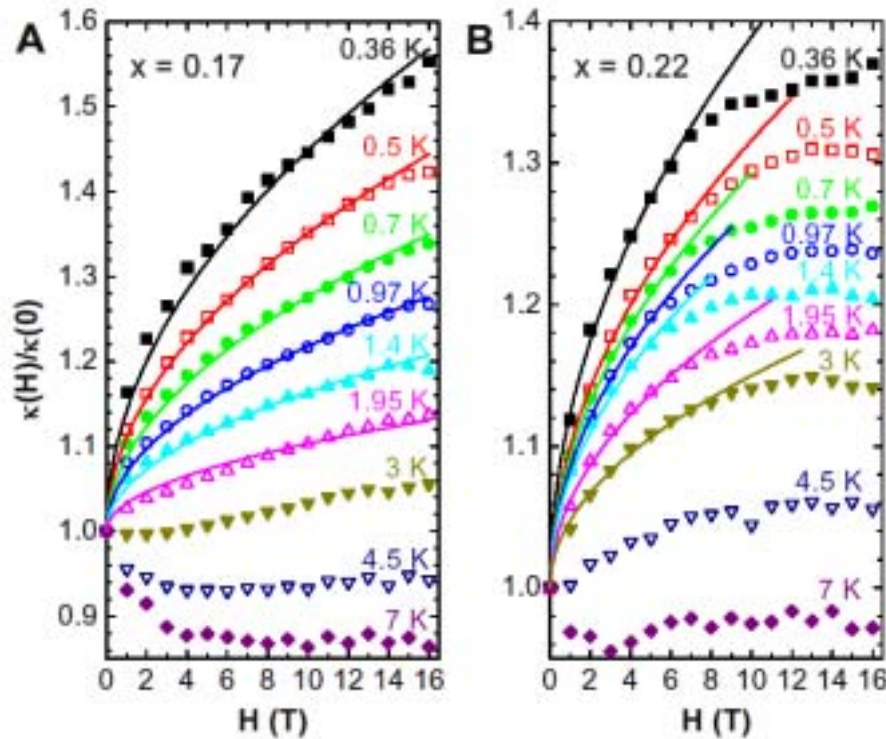
⇒ In all these samples, there are delocalized QPs that carry heat.

⇒ All the samples are “conductive” in 0 T.

Magnetic-Field Dependence (1)

Optimum and Overdoped

cf. $\text{YBa}_2\text{Cu}_3\text{O}_{6.9}$



M. Chiao *et al.*, PRL **82**, 2943 (1999)

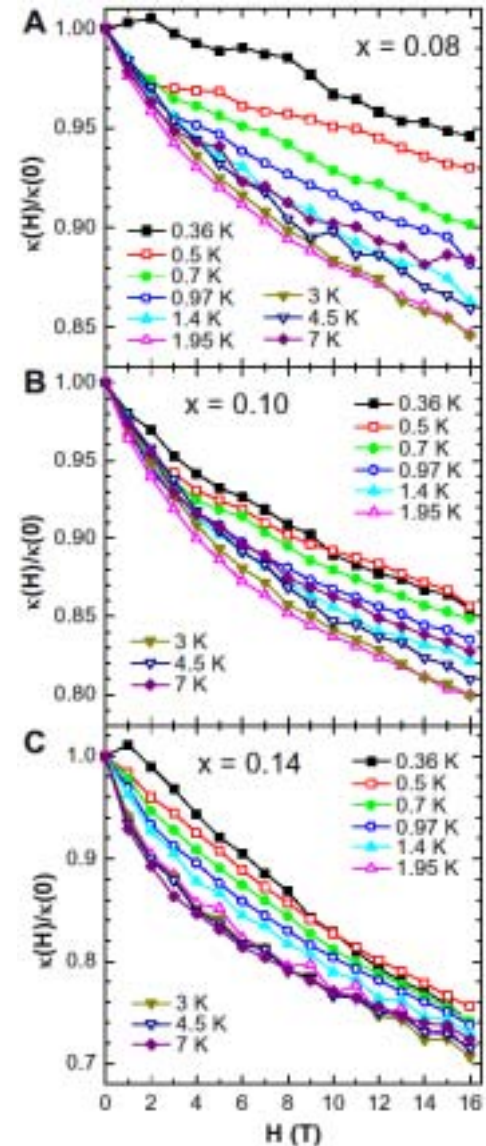
Magnetic-Field Dependence (2)

Underdoped LSCO

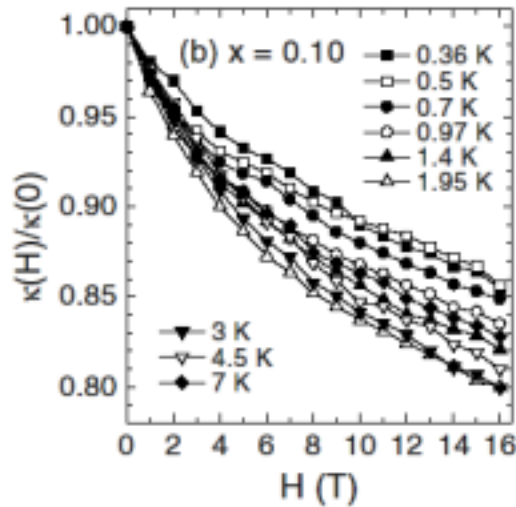
➔ No increase in κ with magnetic field

Specific heat shows QPs are created with magnetic field.

➔ QPs do *not* contribute to the transport, which means they are **localized**.



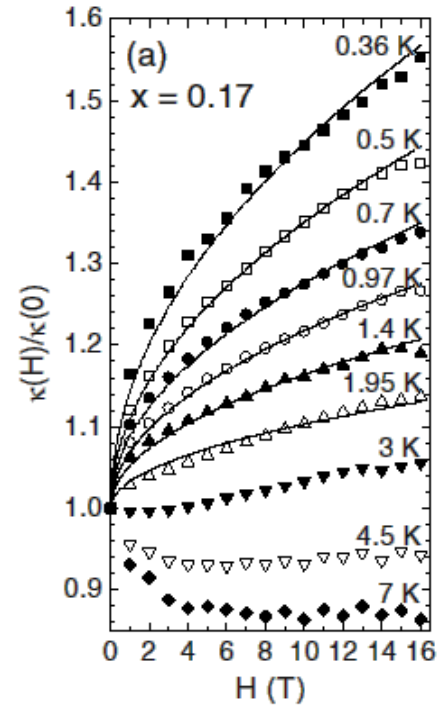
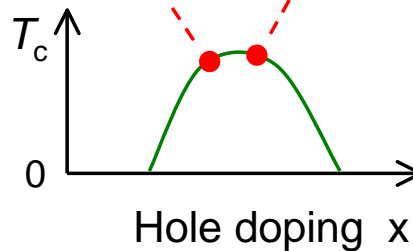
Magnetic-Field Dependence of κ



localized

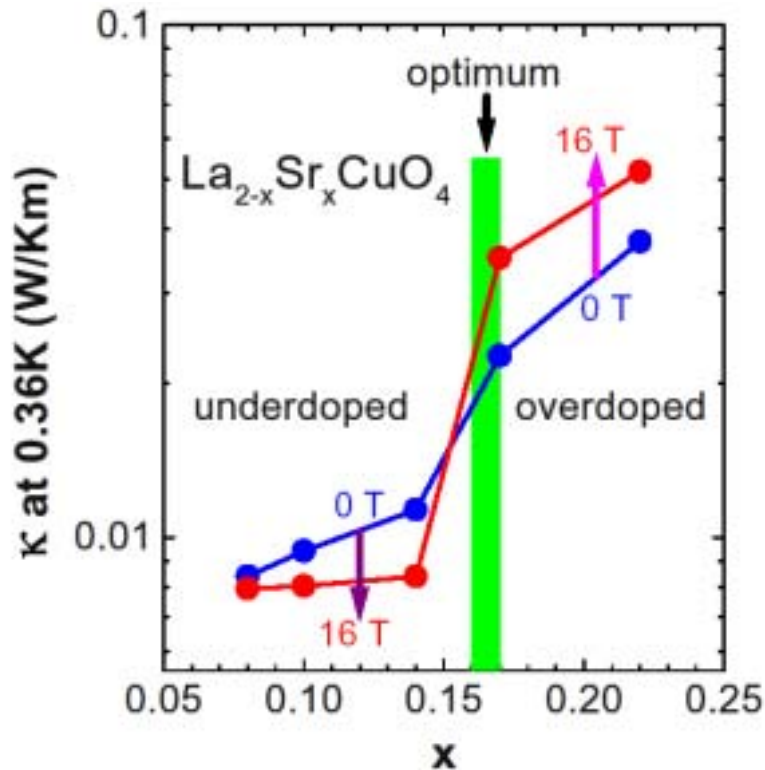
under-doped

optimally-doped

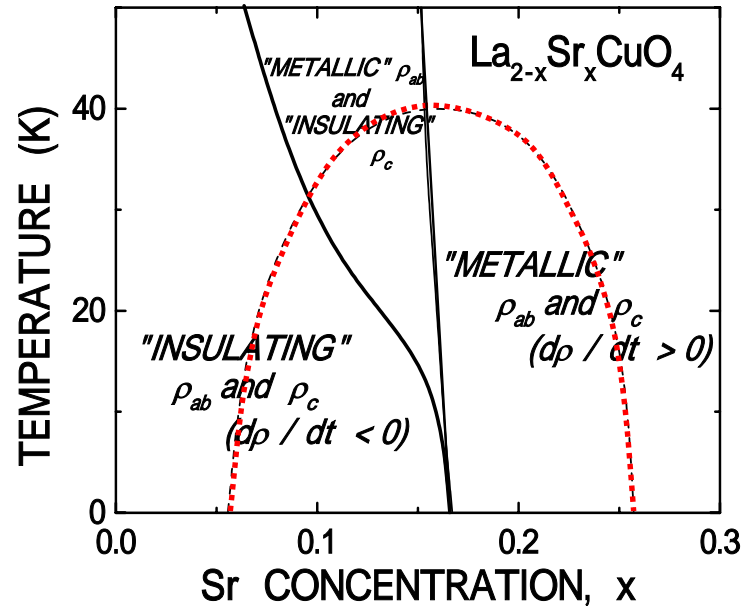


conductive

Magnetic-Field-Induced Localization



X. F. Sun *et al.*,
PRL **90**, 117004 (2003)



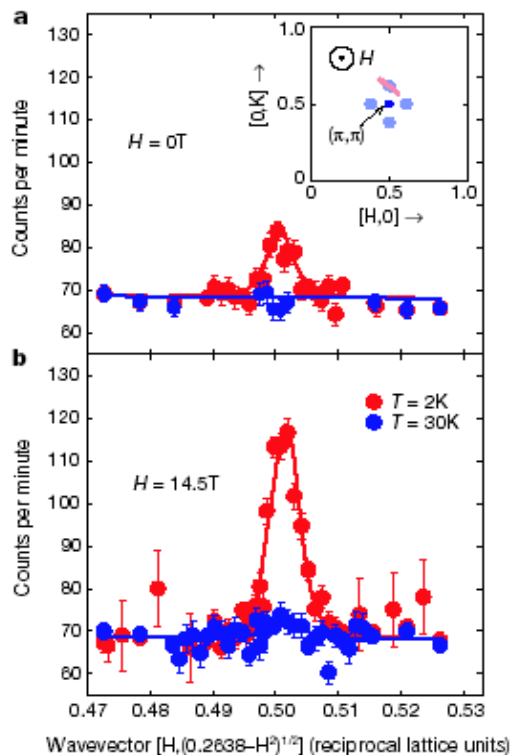
G. S. Boebinger *et al.*,
PRL **77**, 5417 (1996)

Thus, magnetic field is actually causing a
quasiparticle localization
in the underdoped SC state.

Field-Induced Incommensurability

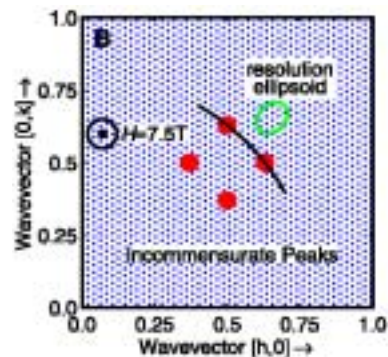
$x = 0.10$ (underdoped)

$x = 0.16$ (optimally-doped)

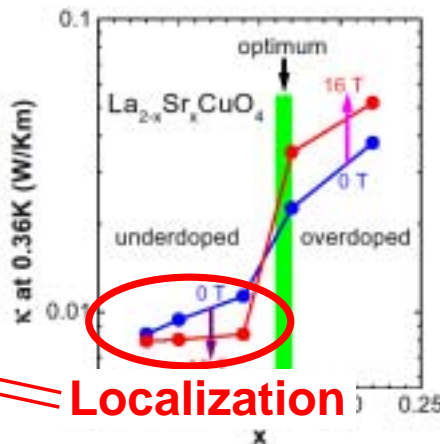
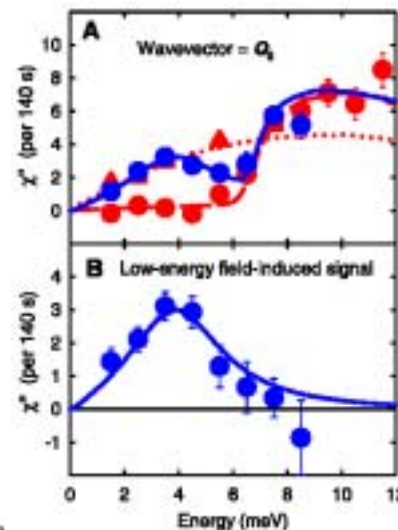


B. Lake *et al.*, Nature **415**, 299 (2002)

Field-induced *static* stripes



B. Lake *et al.*, Science **291**, 1759 (2001)



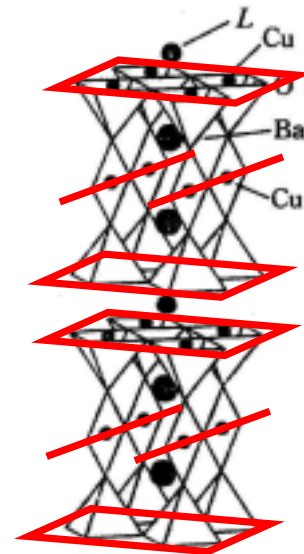
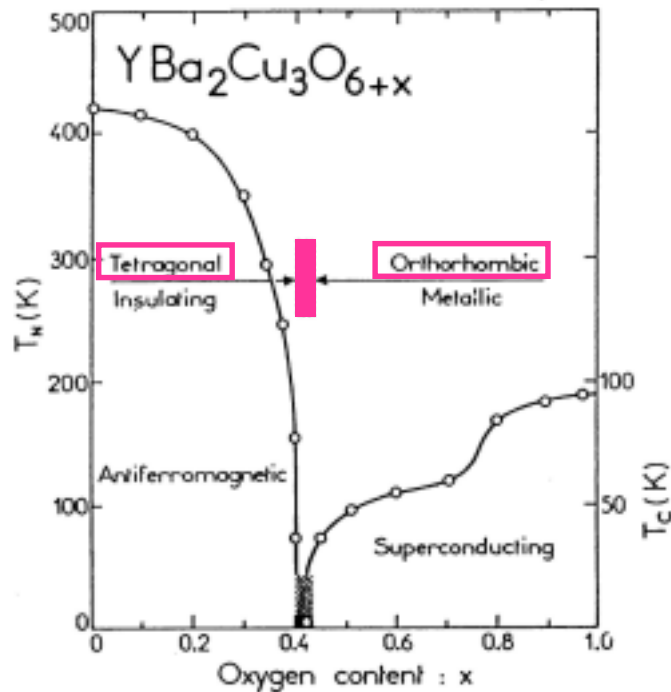
Localization

No static stripes, only *dynamical* stripes

How about the cleanest cuprate, YBCO?

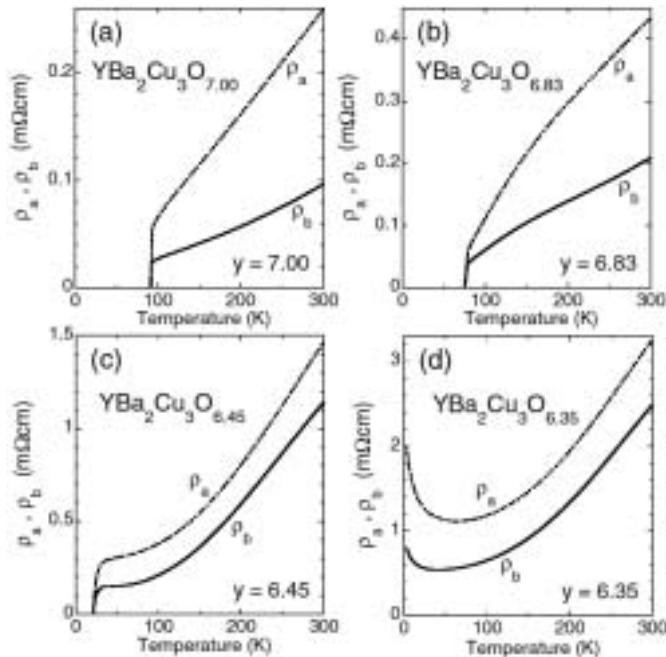
YBa₂Cu₃O_y

- Phase diagram of YBCO

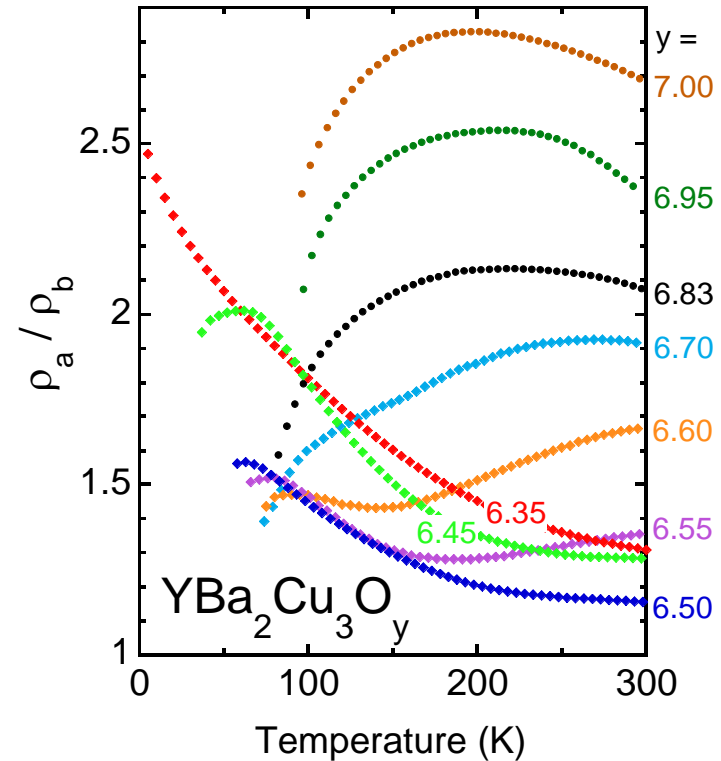


J. Rossat-Mignod *et al.*, Physica B **169**, 58 (1991)

Resistivity Anisotropy in YBCO

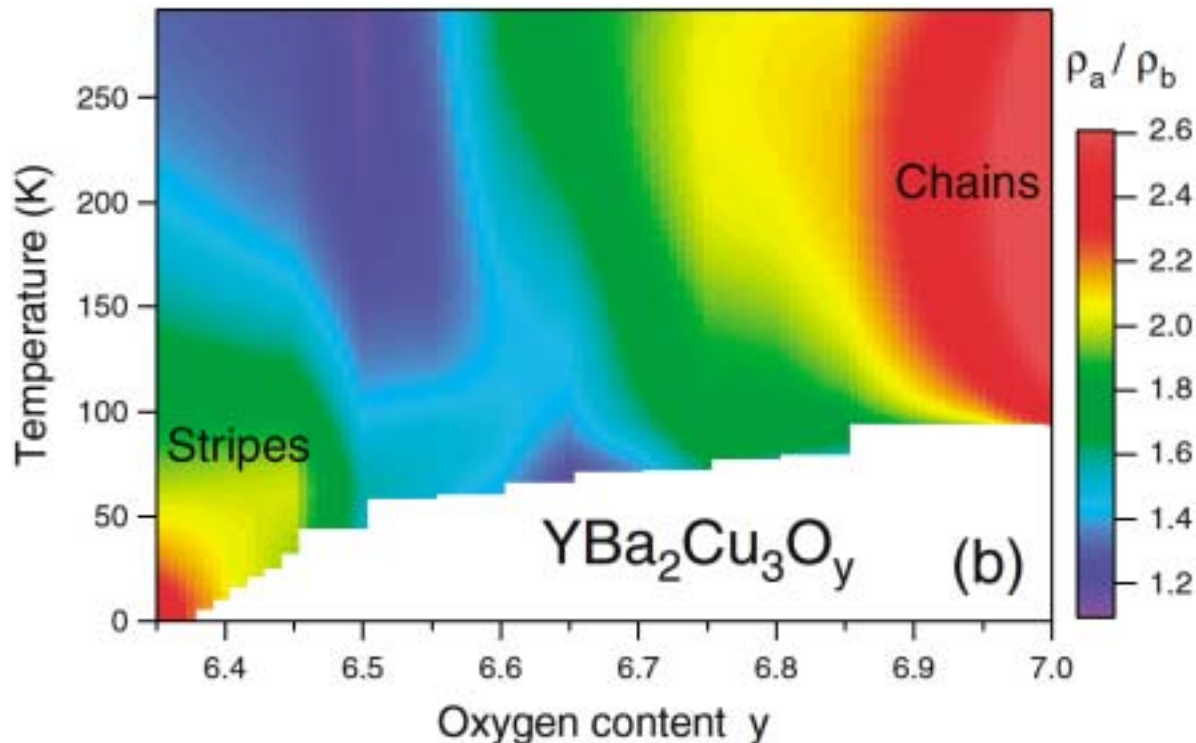


Y. Ando *et al.*, PRL **88**, 137005 (2002)



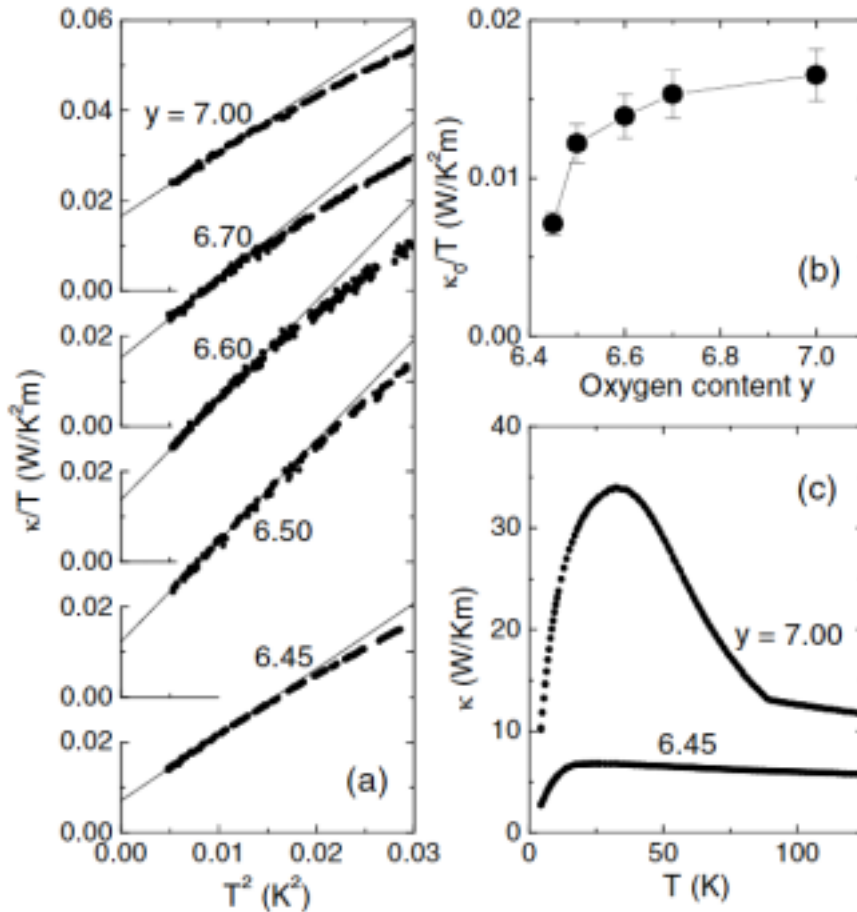
- At low doping, anisotropy tends to grow with lowering T.

Resistivity Anisotropy Mapping for YBCO



Clear sign of electron self-organization for $y < 6.55$

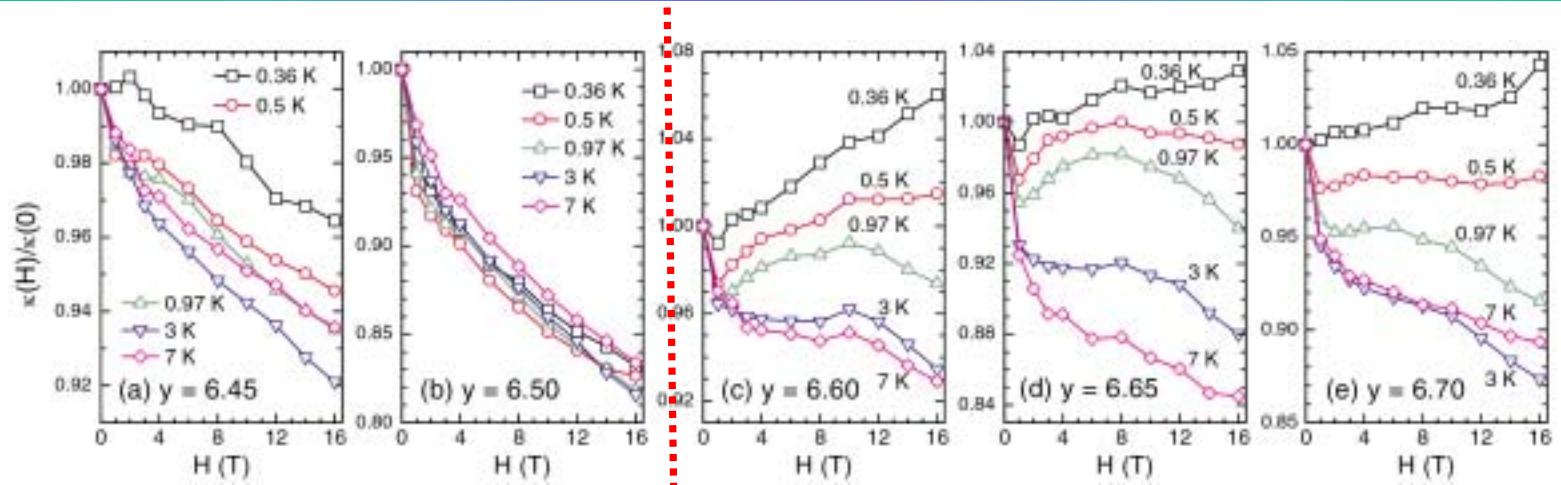
QP Heat Transport in YBCO at $H = 0$



\Rightarrow As in LSCO, there are delocalized QPs in all the SC samples.

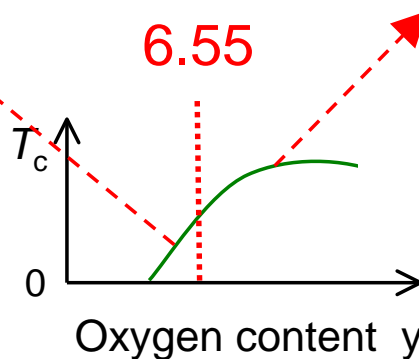
\Rightarrow All these samples are “conductive” in 0 T.

Magnetic-Field Dependence of κ

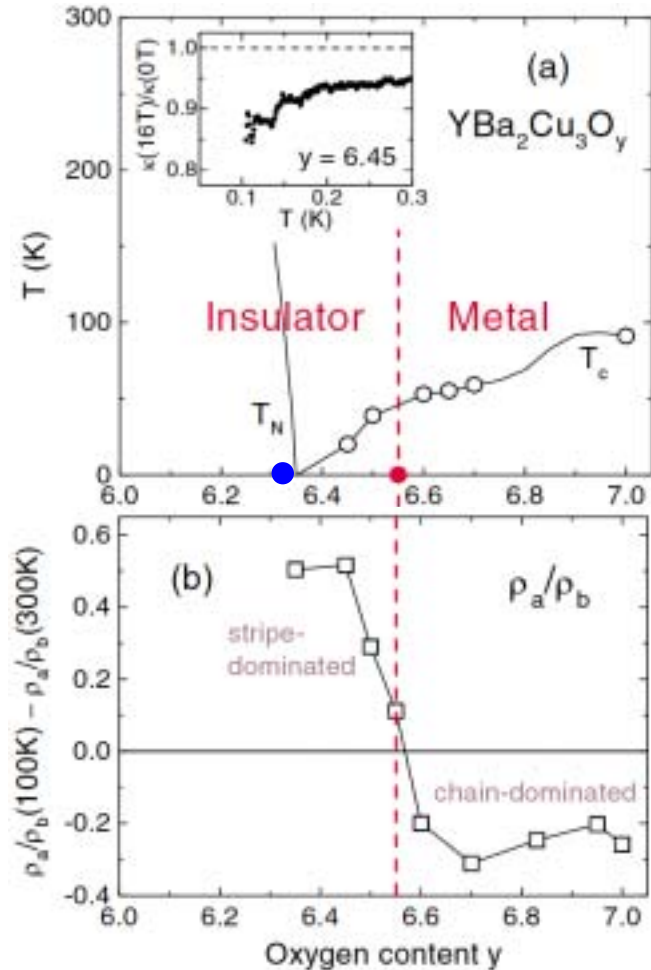


localized

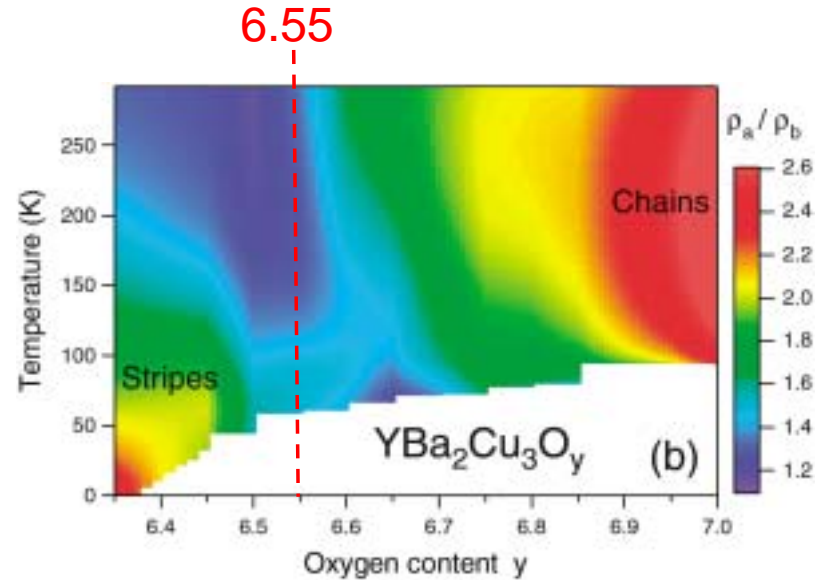
conductive



Localization and Self-Organization



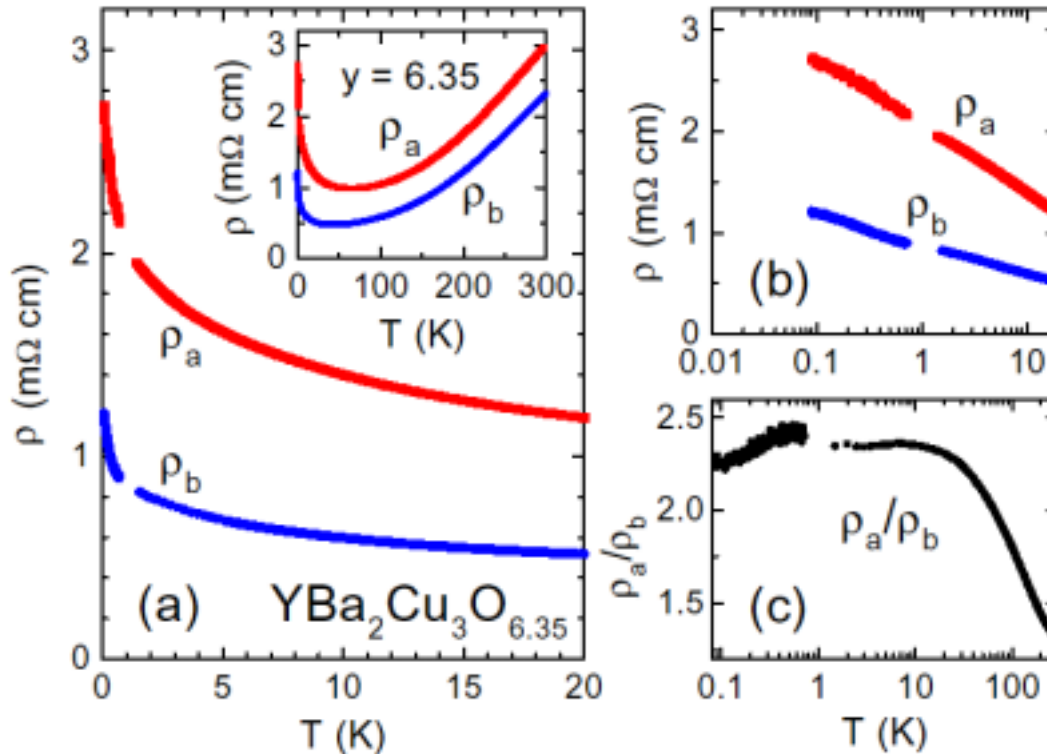
X. F. Sun *et al.*,
PRL **93**, 107001 (2004)



Y. Ando *et al.*, PRL **88**, 137005 (2002)

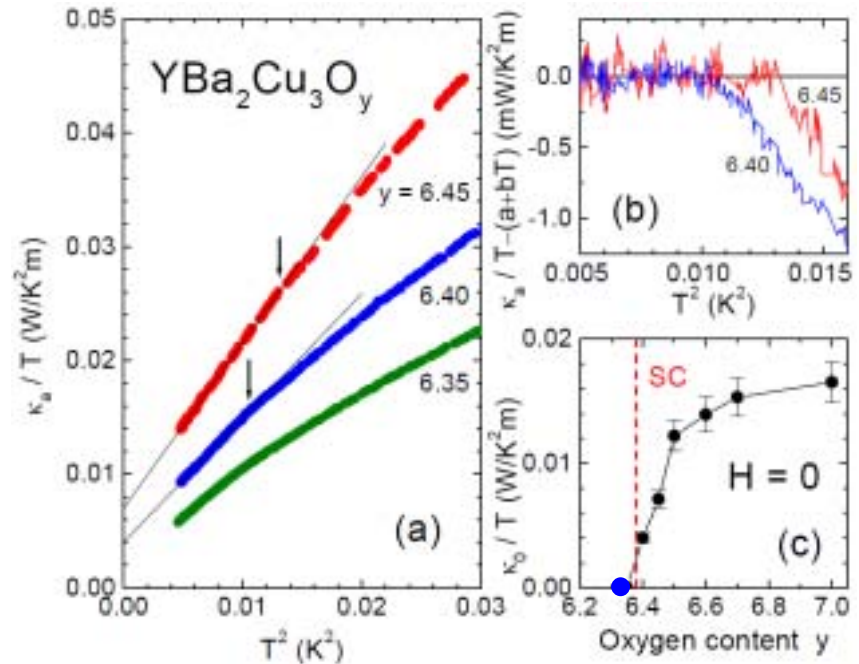
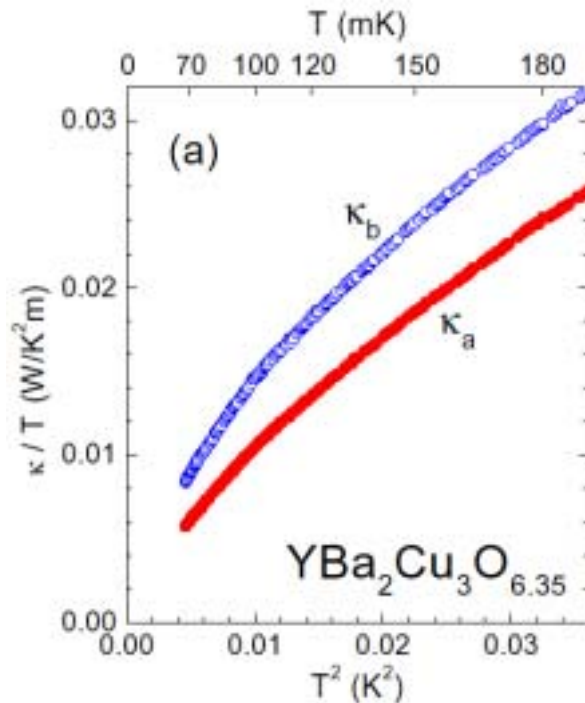
Non-superconducting YBCO

In-Plane Resistivity for $y = 6.35$



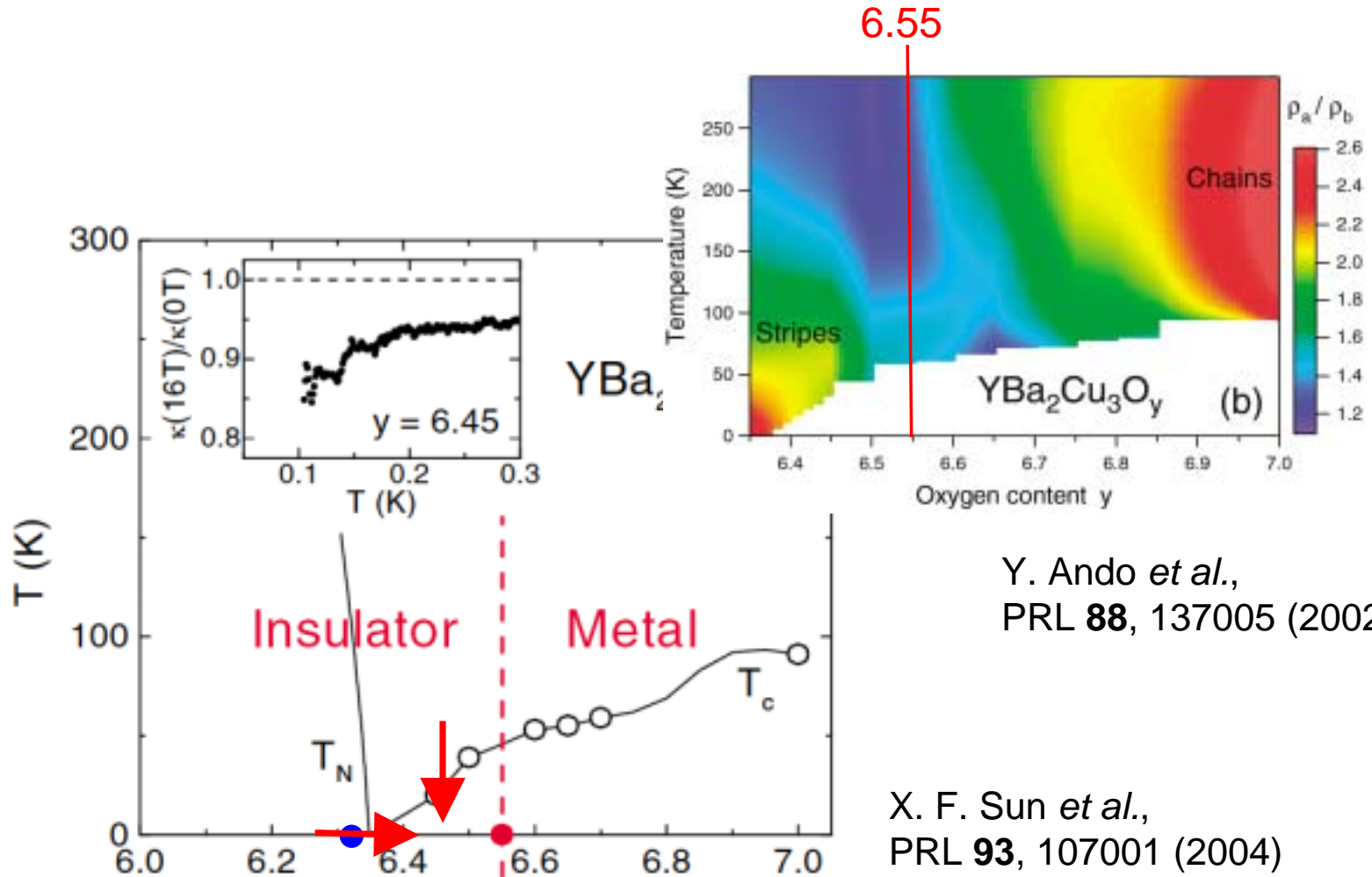
Non-superconducting YBCO

In-Plane Thermal Conductivity



Quasiparticles are localized for $T \rightarrow 0$ in the *absence* of SC even in the cleanest cuprate, YBCO, at $H = 0$.

Kinetic-Energy-Driven Superconductivity?



Y. Ando *et al.*,
PRL **88**, 137005 (2002)

X. F. Sun *et al.*,
PRL **93**, 107001 (2004)

Conclusions

- Self-organization of electrons in high- T_c cuprates seems to be responsible for the emergence of a metallic transport.
- At the same time, the electron self-organization seems to be responsible for the unusual localization behavior that is not well understood.
- Relevance of the electron self-organization to the occurrence of HTSC is obviously a key issue.

Key Issues (in my opinion)

- Electron Self-Organizations
- Insulating Normal State under the SC Dome
- Pseudogap and “Fermi arc” in the Normal State
(*d*-wave SC and the Associated Nodal Structure)
- Peculiar Spin Dynamics and the Resonance Mode
- Unusual Roles of Phonons
- Quantum Phase Transition and Criticality

Thank you !