

**REVIEW *and* EFFECTS OF COMPETING  
FERRO- AND ANTI-FERROMAGNETIC INTERACTIONS IN  
MAGNETIC SEMICONDUCTORS**

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# FERROMAGNETIC DMS

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collaborators:

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*J. Cibert, D. Ferrand, S. Tatarenko – Grenoble*

*T. Jungwirth, J. König, A. MacDonald – Prague/Bochum/Austin*

*K. Edmonds, C.T. Foxon, B.L. Gallagher, K.Y. Wang – Nottingham*

*L.W. Molenkamp, G. Schmidt – Wuerzburg*

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reviews: *MRS Bulletin, October 2003, p. 714*

*Europhys. News 34 (2003) 216; cond-mat/0408561*

support: *FENIKS, AMORE -- EC projects; Polonium Project*

*Ohno Semiconductor Spintronics ERATO Project of JST*

*Humboldt Foundation*

# OUTLINE / ISSUES

1. **Why ferromagnetic semiconductors?**
2. **Understanding of carrier-controlled diluted ferromagnetic semiconductors**
3. **Nanoscale fluctuations**
  - electrostatic disorder
  - magnetic disorder
4. **Nanoscale phase separations**

# ICT - ways to go

- **improving existing technologies**
- **disruptive technologies**

*many ideas around ....  
which will win – unknown ...*

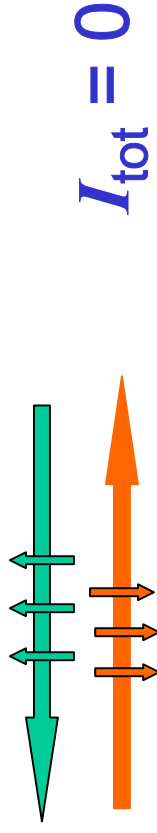
# SPINTRONICS

*exploiting spin, not only charge*

- Storing *and* processing and transferring of classical information
  - manipulation with magnetization
- Storing *and* processing and transferring of quantum information
  - manipulation with single spins

**electronic and/or nuclear spins**

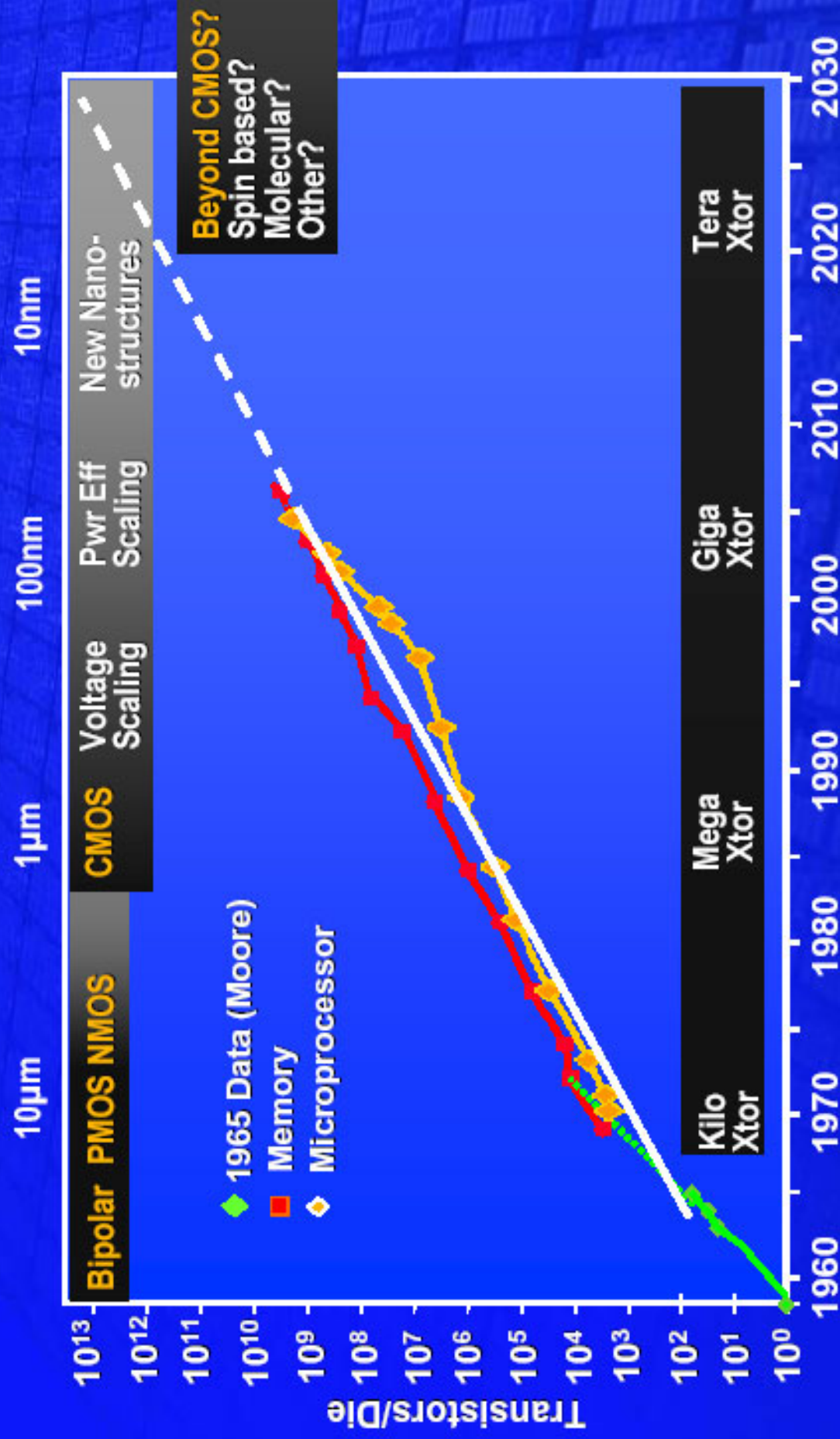
→ Low power memories, processors, and interconnects



**dissipation less currents**

*cf. John Schliemann*

# Moore's Law Will Outlive CMOS



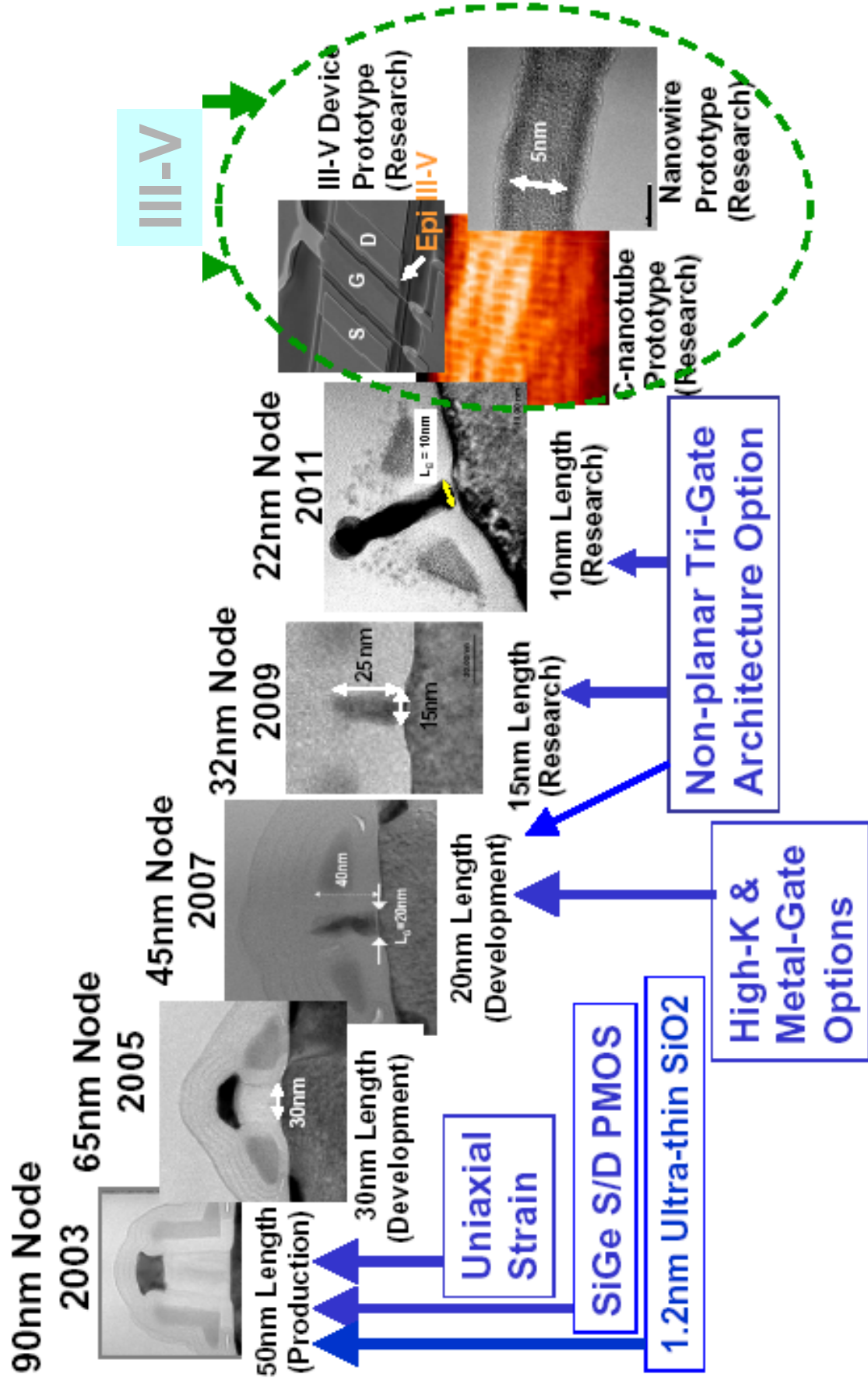
**Sunlin Chou**

Technology and Manufacturing Group  
Intel Corporation

International Solid-State Circuits Conference  
February 2005

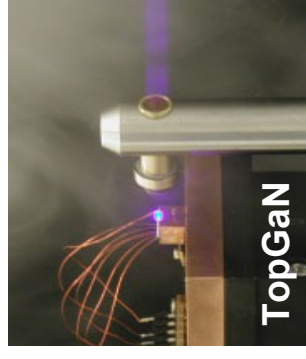
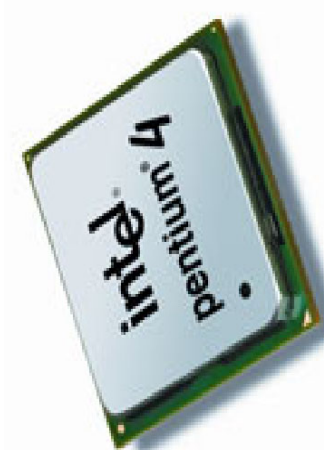
# Materials

*strain* → *new oxides* → *new channels*



# Spintronics -- materials aspect

*Why to do not combine complementary resources of ferromagnets and semiconductors?*



- ferromagnetic metal / semiconductor hybrid structures
- ferromagnetic semiconductors – multifunctional materials

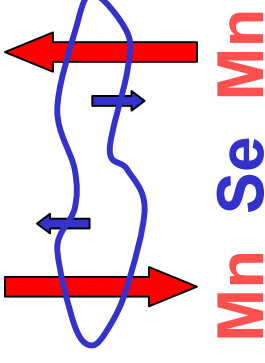


# Search for ferromagnetic semiconductors

- **Antiferromagnetic superexchange dominates**  
in magnetic insulators and semiconductors

→ **no spontaneous magnetisation**

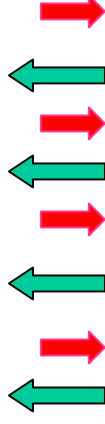
NiO, MnSe, EuTe, ...



- **Exceptions**

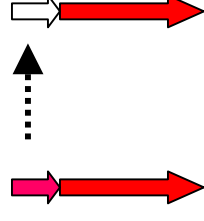
-- ferrimagnets (two ions or two spin states co-exist)

NiO(Fe<sub>2</sub>O<sub>3</sub>), Mn<sub>4</sub>N, ...



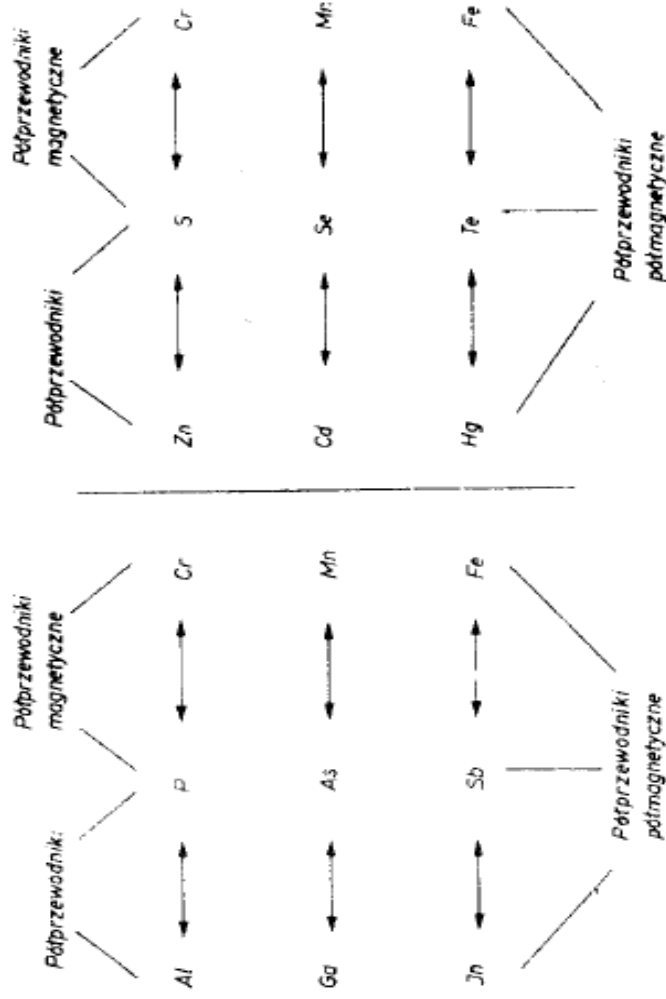
-- double exchange (two charge states co-exist)

LaMnO<sub>3</sub> → La<sub>1-x</sub>Sr<sub>x</sub>MnO<sub>3</sub> (holes in d band)



-- ferromagnetic superexchange dominates

EuO, ZnCr<sub>2</sub>Se<sub>4</sub>, ...  $T_C \approx 100$  K **IBM, MIT, Tohoku, ... '60-'70**



Robert R. Galazka

Instytut Fizyki PAN  
Warszawa

Rys. 2. Przykład jak można tworzyć półprzewodniki półmagnetyczne. Oczywiście można również tworzyć skośne połączenia np GaMnSb, ZnFeSe...

### Semimagnetic Semiconductors

## now: Diluted Magnetic Semiconductors (DMS)

*Abstract:* The paper considers a new group of solid states — alloys between semiconducting and magnetic compounds. The materials conserve main properties characteristic for semiconductors (doping in wide range of concentration on *n* and *p* type, well defined band structure *E(k)*) but contain strong localized spins introduced by transition elements. New physical phenomena are observed mainly at low temperatures and in the presence of magnetic field. Experimental results are presented for HgMnTe and CdMnTe type of mixed crystals.

# Diluted magnetic semiconductors (DMS)

III-V

Al ↔ P ↔ Cr

Ga ↔ As ↔ Mn

In ↔ Sb ↔ Fe

II-VI

Zn ↔ S ↔ Cr

Cd ↔ Se ↔ Mn

Hg ↔ Te ↔ Fe

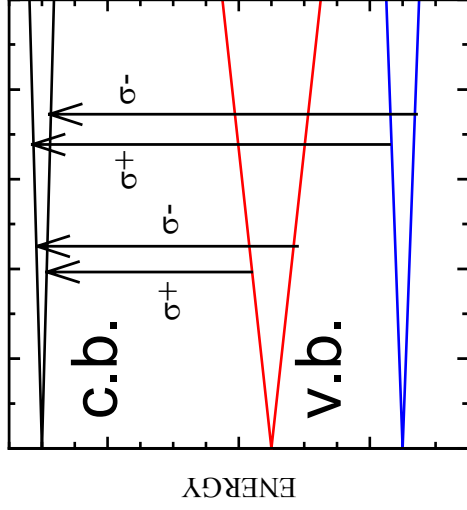
*Gałązka (Warsaw) ICPS'78*

- Large solubility of Mn in II-VI's
- AF superexchange in (II,Mn)VI  
→ random antiferromagnets

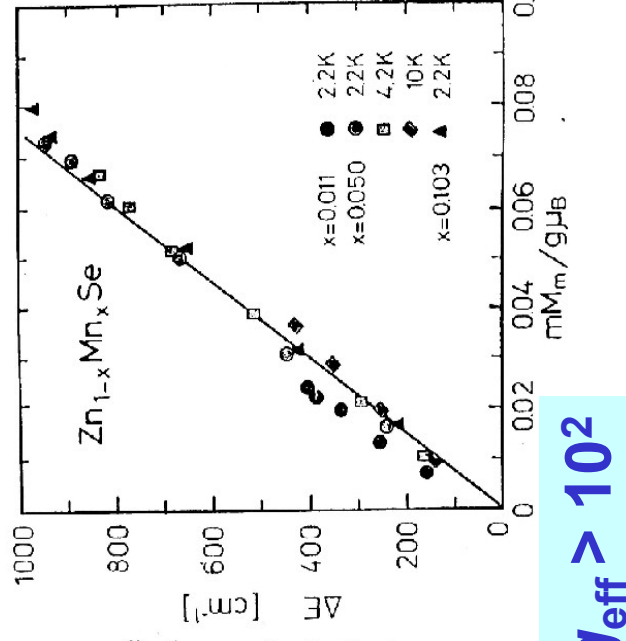
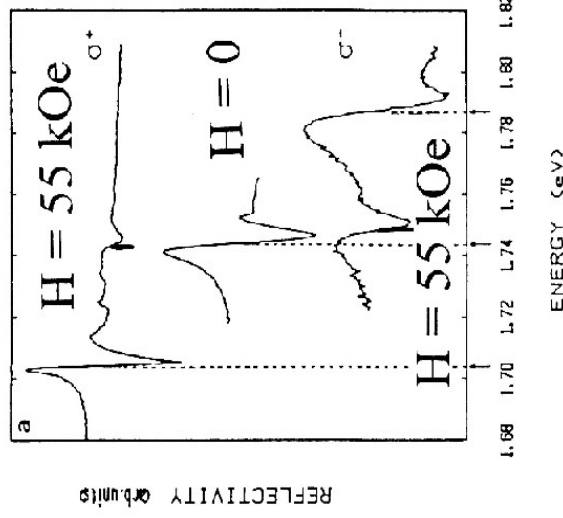
# Determination of sp-d exchange integrals $I$

## - giant splitting of exciton states

$$\Delta E \sim M \sim B_S(H)$$



$\text{Cd}_{0.1}\text{Mn}_{0.9}\text{Te}$   
 $T = 4.5 \text{ K}$



*Gaj et al.; Twardowski et al. (Warsaw)*

--- p-d:  $I_{pd} \equiv \beta N_o \approx -1.0 \text{ eV}$

large p-d hybridization and large intra-site Hubbard  $U \Rightarrow$   
 kinetic p-d exchange (*T.D. '80, ..., P. Kacman, SST'01*)

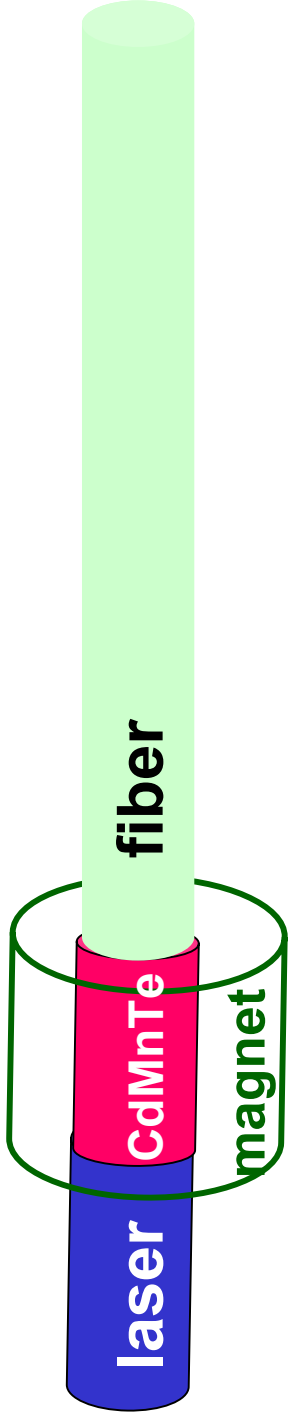
--- s-d:  $I_{sd} \equiv \alpha N_o \approx 0.2 \text{ eV}$

no s-d hybridization  $\Rightarrow$  potential s-d exchange

# Hybrid optical isolators of DMS

- absorption  $\alpha(\sigma^+) > \alpha(\sigma^-) \rightarrow$  magnetic circular dichroism  $\rightarrow$  large Faraday rotation
- optical isolators:

Gaj et al. (Warsaw) SSC'78



$$\Theta_F = \pi/4$$

*Puremat (A. Mycielski) – world-wide monopole on pure Mn*

# Making DMS ferromagnetic

long-range **carrier**-mediated ferromagnetic exchange

**IV-VI:** p-Pb<sub>1-x-y</sub>Mn<sub>x</sub>Sn<sub>y</sub>Te Story et al. (Warsaw) PRL '86

**III-V:** In<sub>1-x</sub>Mn<sub>x</sub>As Ohno et al. (IBM) PRL '92

Ga<sub>1-x</sub>Mn<sub>x</sub>As Ohno et al. (Tohoku) APL '96

**$T_C \approx 100$  K for  $x = 0.05$**

**II-VI:** p-Cd<sub>1-x</sub>Mn<sub>x</sub>Te/Cd<sub>1-x-y</sub>Zn<sub>x</sub>Mg<sub>y</sub>Te:N QW

*Haury et al. (Grenoble, Warsaw) PRL '97*

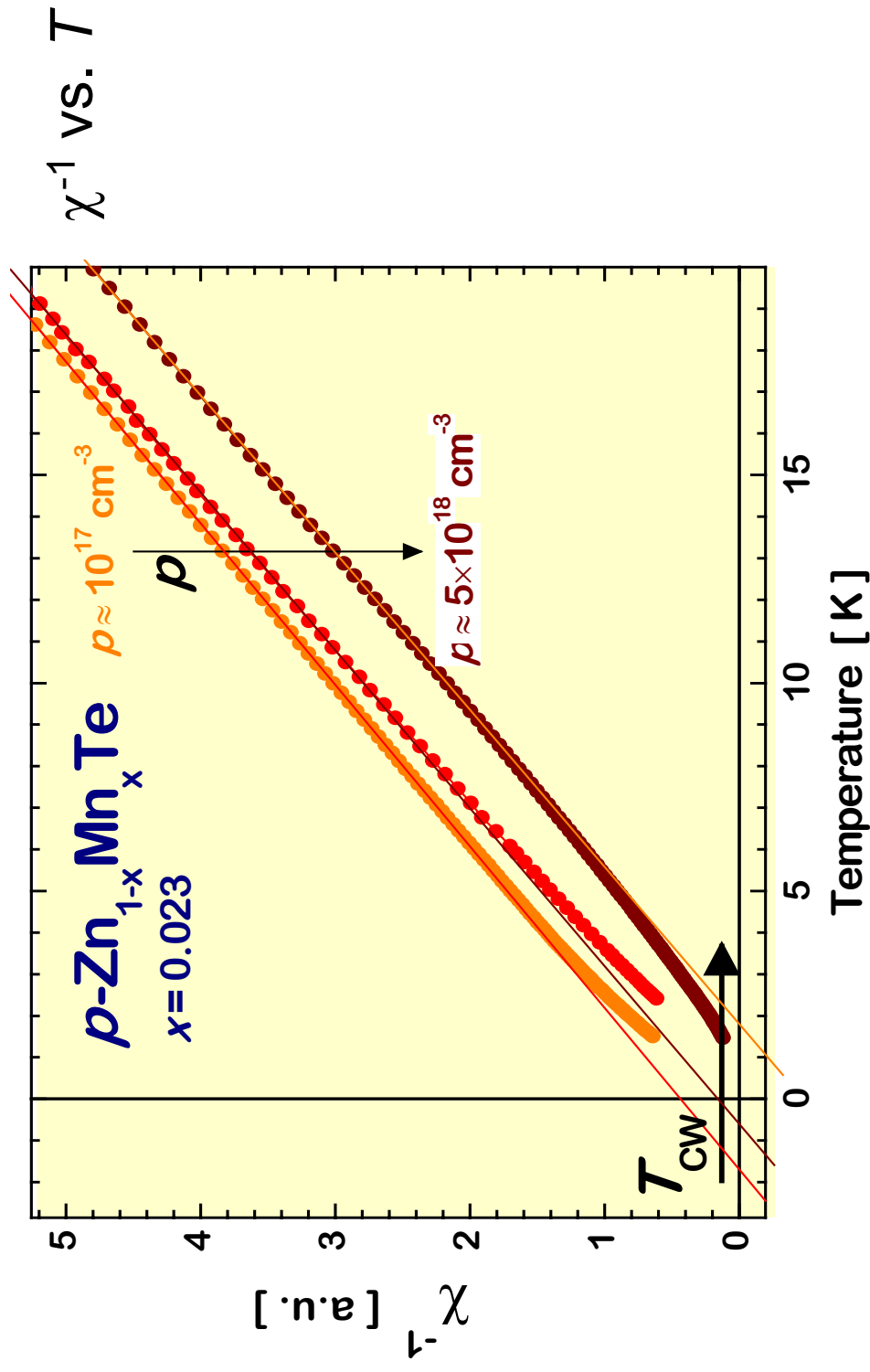
p-Zn<sub>1-x</sub>Mn<sub>x</sub>Te:N Ferrand et al. (Grenoble, Warsaw) PRB '01

p-Be<sub>1-x</sub>Mn<sub>x</sub>Te:N Hansen et al. (Wuerzburg, Warsaw) APL '01)

**III-V and II-VI DMS:**

**quantum nanostructures and ferromagnetism combine**

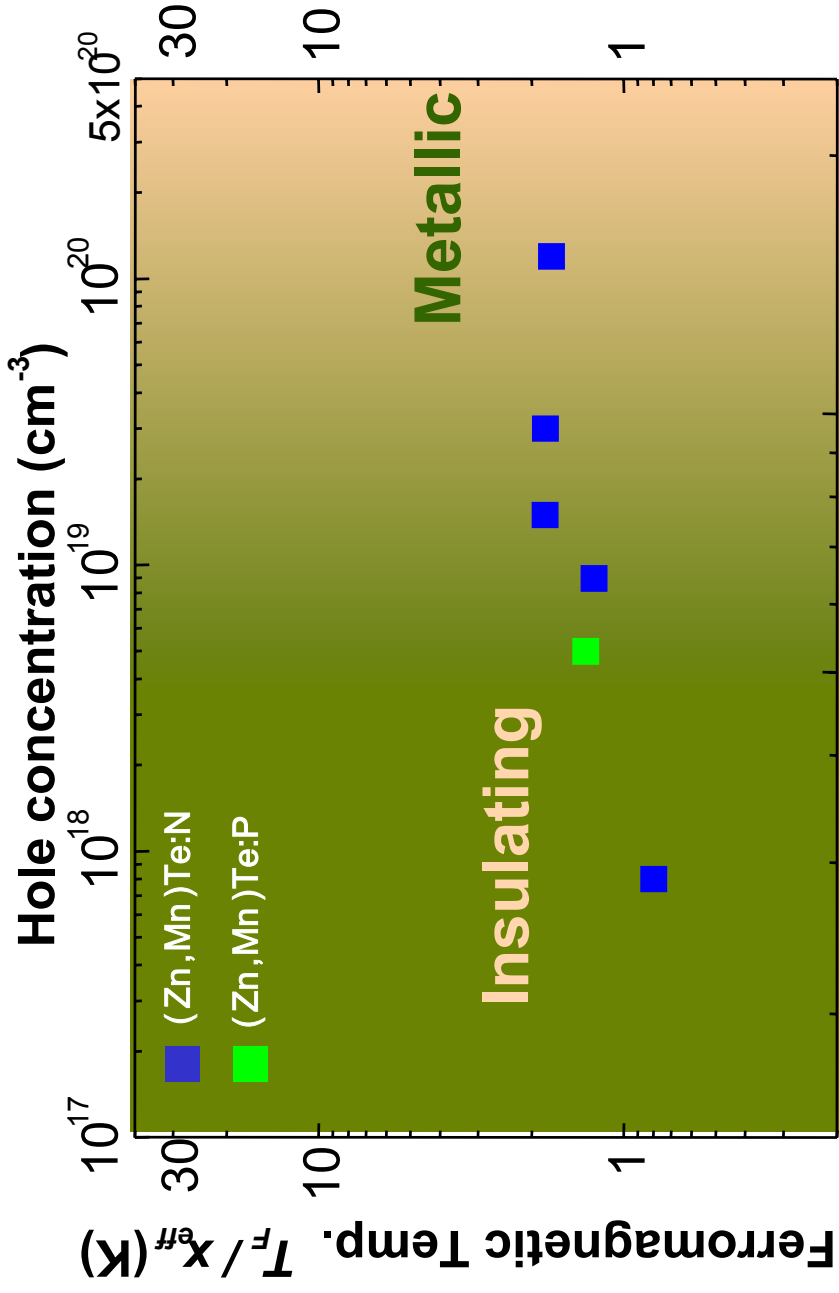
# Effect of acceptor doping on magnetic susceptibility in $\text{Zn}_{1-x}\text{Mn}_x\text{Te:P}$



Sawicki et al. (Warsaw) pss'02

Kępa et al. (Warsaw, Oregon) PRL'03

# Ferromagnetic temperature in p-(Zn,Mn)Te



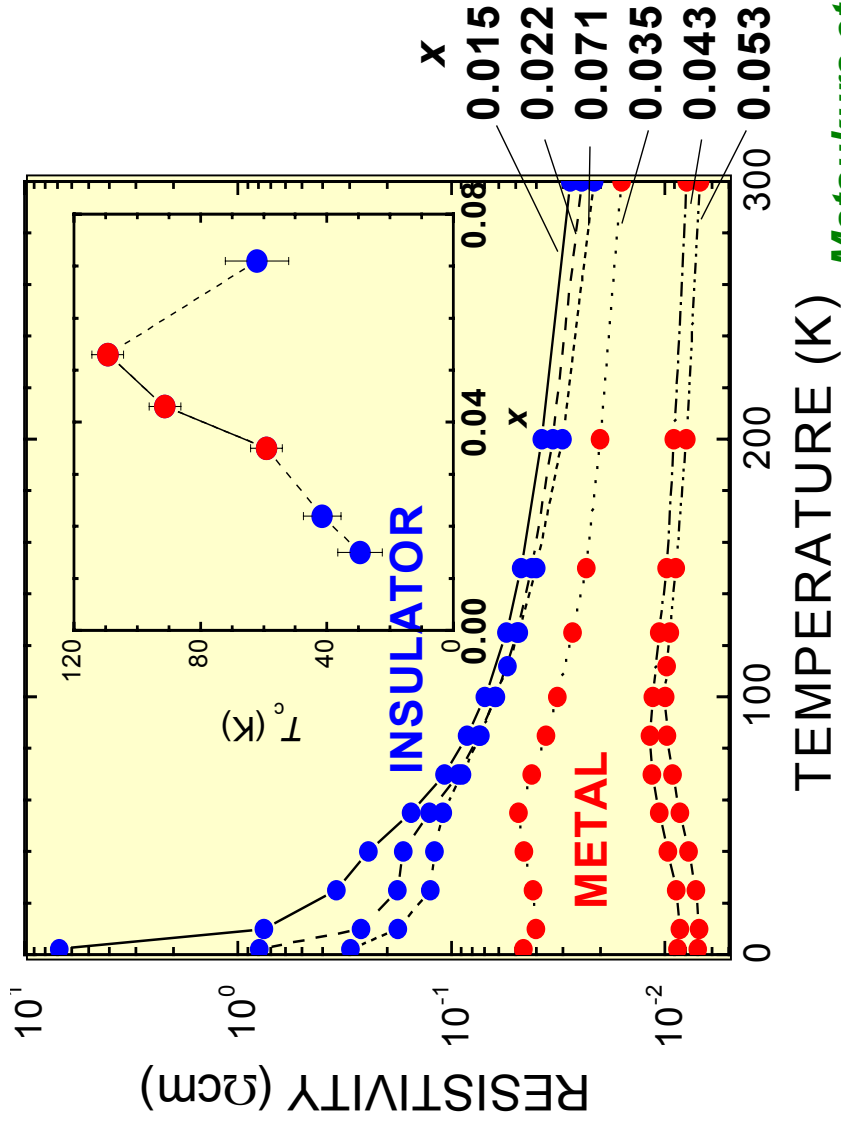
- ferromagnetism disappears in the absence of holes
- ferromagnetism on both sides of metal-insulator transition

Ferrand et al. (Grenoble, Warsaw) PRB'01

Sawicki et al. (Warsaw) pss'02



# $\text{Ga}_{1-x}\text{Mn}_x\text{As}$ : resistance vs. temperature and Curie temperature vs. x



*Matsukura et al. (Tohoku) PRB'98*

- ferromagnetism on both sides of metal-insulator transitions
- ferromagnetism disappears in the absence of holes

# Carrier-induced ferromagnetism in DMS

- ferromagnetism on both sides of metal-insulator transitions
- coexistence of physics of:
  - strongly correlated metals
  - disordered magnetic insulators
  - highly doped semiconductors(Anderson-Mott localization, self-compensation)

*A number of theoretical proposals ....*

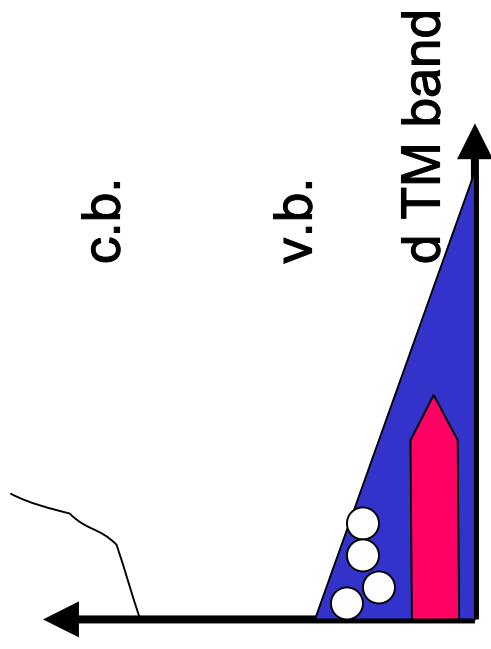
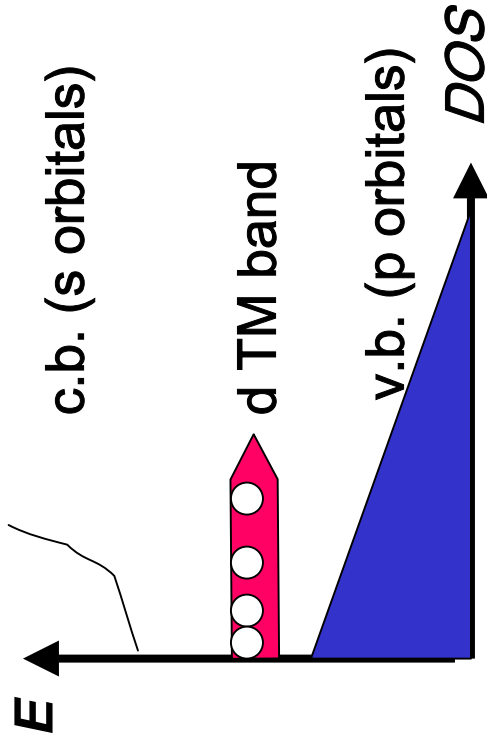
**Where do Mn d levels and holes reside?**

# Where do Mn d levels and holes reside?

## Two possibilities:

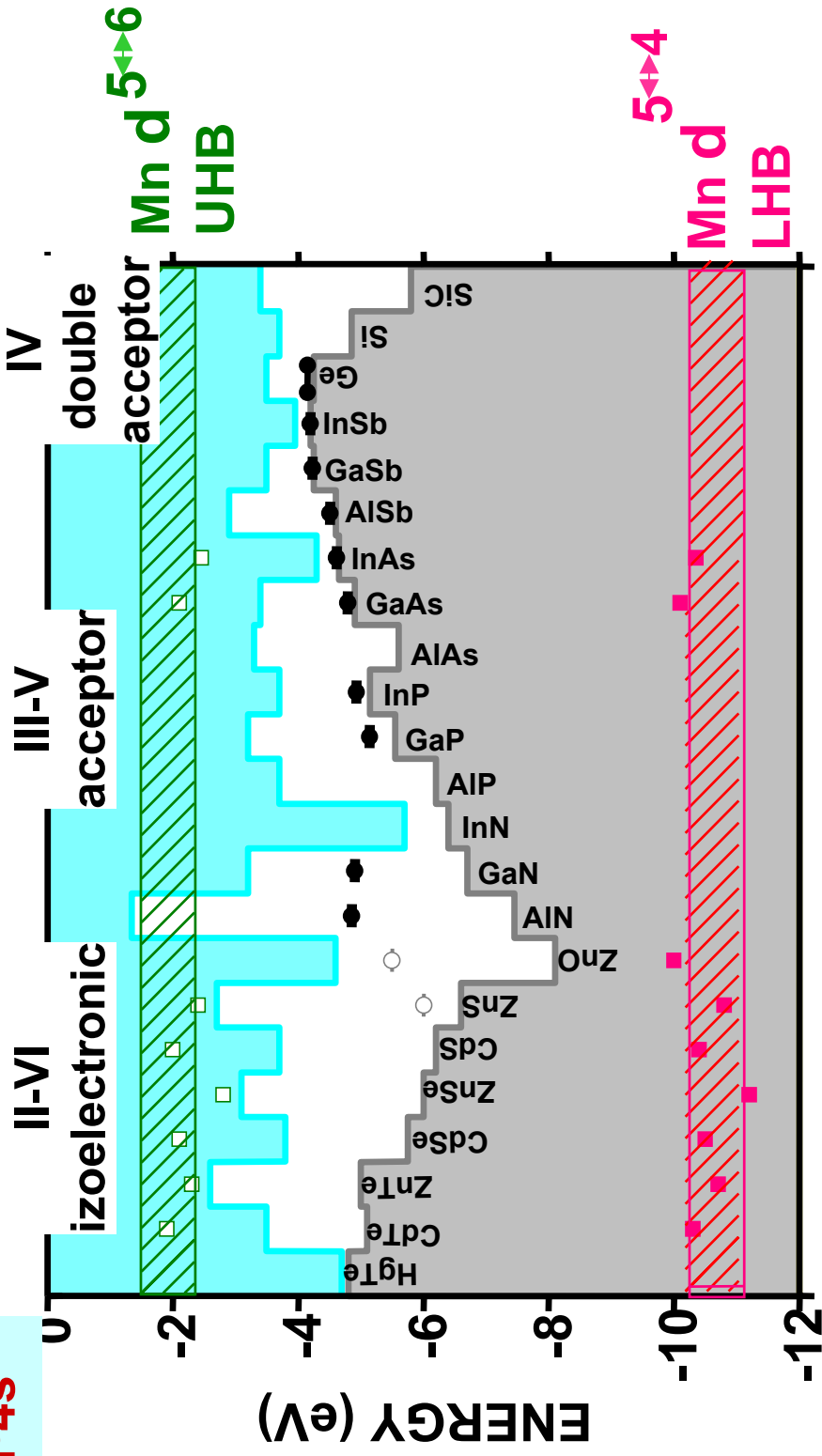
-- Mott-Hubbard insulator  
[manganides  $\text{La}_{1-x}\text{Sr}_x\text{MnO}_3$ ]

-- charge transfer insulator  
[cuprates  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ ]



# Mn-derived states in semiconductors

**Mn:  $3d^5 4s^2$**



Photoemission: Fujimori et al. (Tokyo), PRB'02, PRB'04

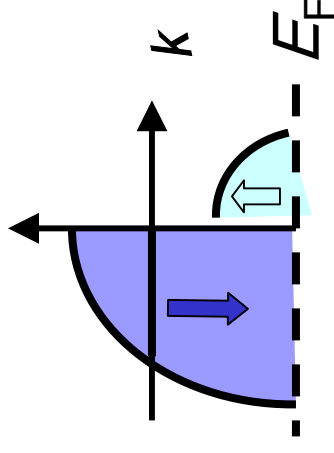
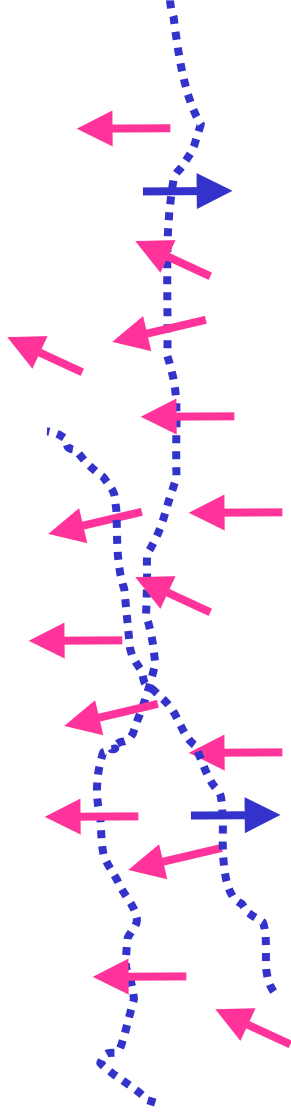
Band edges compile by: Van de Walle (UCSB) Neugebauer (Dusseldorf), Nature'04

Band-gap states compile by: T.D. et al., PRB'02 **cf. Paul Koenraad**

**Contradicts LSDA  $\rightarrow$  SIC, LSDA +U, ...**

# Modelling of carrier-controlled ferromagnetism in DMS

# Mean-field Zener/RKKY model of hole-controlled ferromagnetism in DMS



*Driving force:*

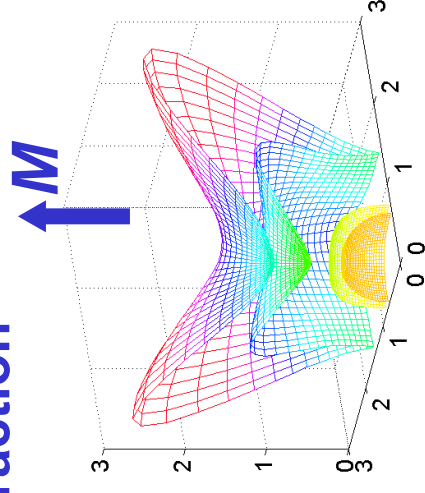
lowering of the hole energy due to redistribution between hole spin subbands split by p-d exchange interaction

*Essential ingredient:*

Complexity of the valence band structure has to be taken into account

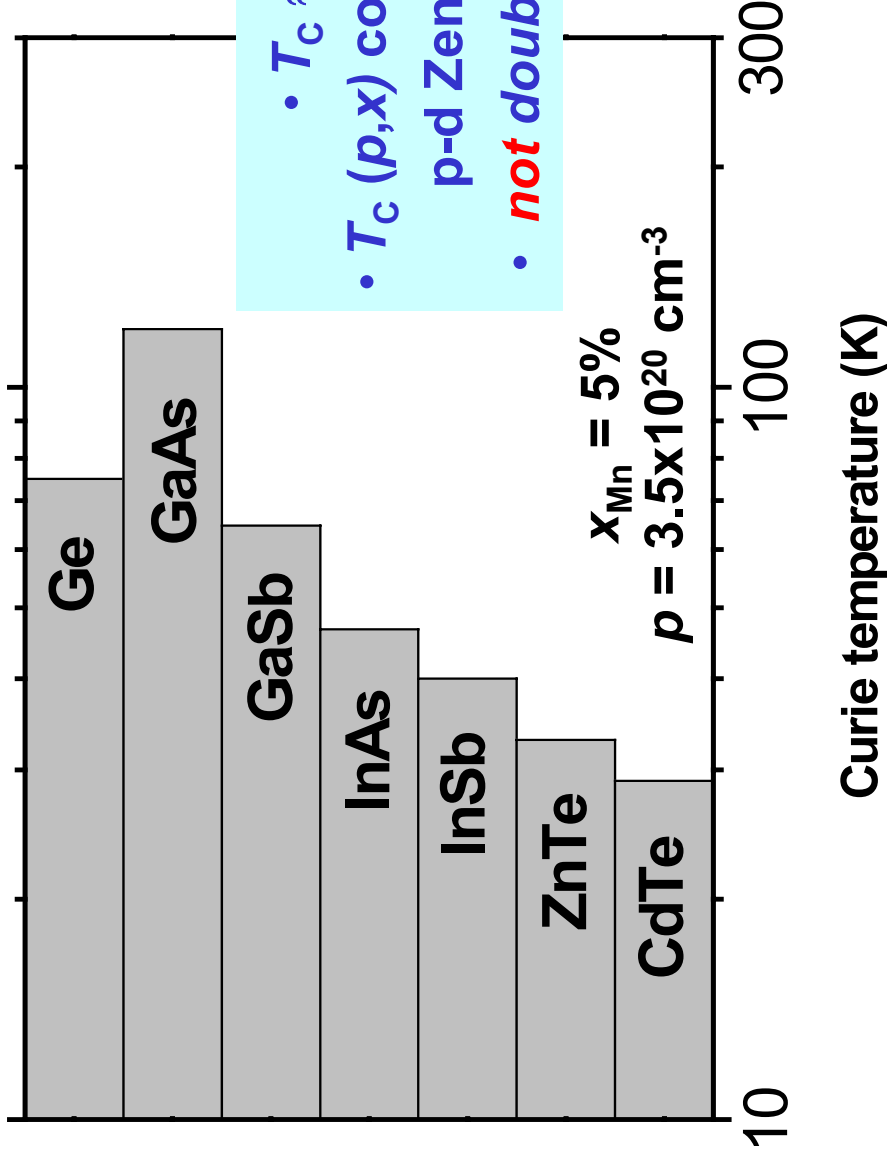
**No adjustable parameters**

$$T_C = T_F - T_{AF}; \quad T_F \sim I_{pd}^2 \rho^{(s)}_{DOS}$$



T.D. et al., '97-  
MacDonald et al. (Austin) '99-

# Mn-based p-type DMS to which p-d Zener model has been found to apply



Theory: T. D et al. (Warsaw, Tohoku, Grenoble) Science'00, PRB'01

Jungwirth et al. (Austin, Prague, PRB'02), also UCSD, NRL, ...

Support LSDA+U, LSDA+SIC (Osaka, Juelich, Uppsala, Prague, Golden, Oak Ridge ....)

Expl.: Tohoku, Kanagawa, Tokyo, Grenoble, PSU, NRL, Notre Dame, UCSB, Nottingham, ...



# p-d Zener model for p-type DMS

- ***the model explains/predicts:***
  - $T_C(x, p, n)$ , spin polarization,  $M(T, H)$ , magnetic anisotropy
  - magnetic stiffness (domain width, spin wave spectrum)
  - anomalous Hall effect
  - a.c. conductivity and magnetic circular dichroism
  - magnetoresistance (WLR) and anisotropic magnetoresistance
  - ...

*T.D. et al., '97-*

*A.H. MacDonald et al. '99-*

*cf. Carsten Timm*

- (Ga,Mn)As, p-(Cd,Mn)Te, ... emerge as model ferromagnets
- basis for magnetisation manipulation

*cf. Hideo Ohno*

# Examples of effects of nanoscale fluctuations in ferromagnetic DMS

- **(III,Mn)V**  
electrostatic disorder caused by ionised Mn acceptors  
and compensating donors
- **(II,Mn)VI**  
magnetic disorder caused by competing AF and FM  
interactions

*cf. Georges and Richard Bouzerar*

# Electrostatic disorder

# s-d exchange energy $\propto N_o$ in (III,Mn)V

## Experimental values of s-d exchange energy

- Mn<sup>+1</sup> free ion:  $\alpha N_o = 396$  meV
- in (II,Mn)VI:  $\alpha N_o = 220 \pm 50$  meV

## Experimental values in (III, V)Mn

- n-Ga<sub>1-x</sub>Mn<sub>x</sub>N

$$\alpha N_o = |14 \pm 4| \text{ meV} \quad 0.01\% < x < 0.2\%$$

EPR- Korringa *Wolos et al. (Warsaw) APL'03*

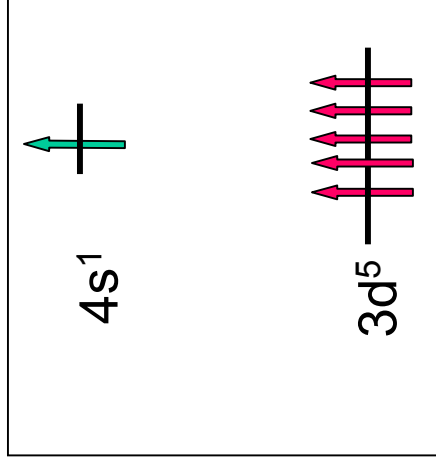
- Ga<sub>1-x</sub>Mn<sub>x</sub>As

$$\alpha N_o = 23 \text{ meV} \quad x = 0.1\%$$

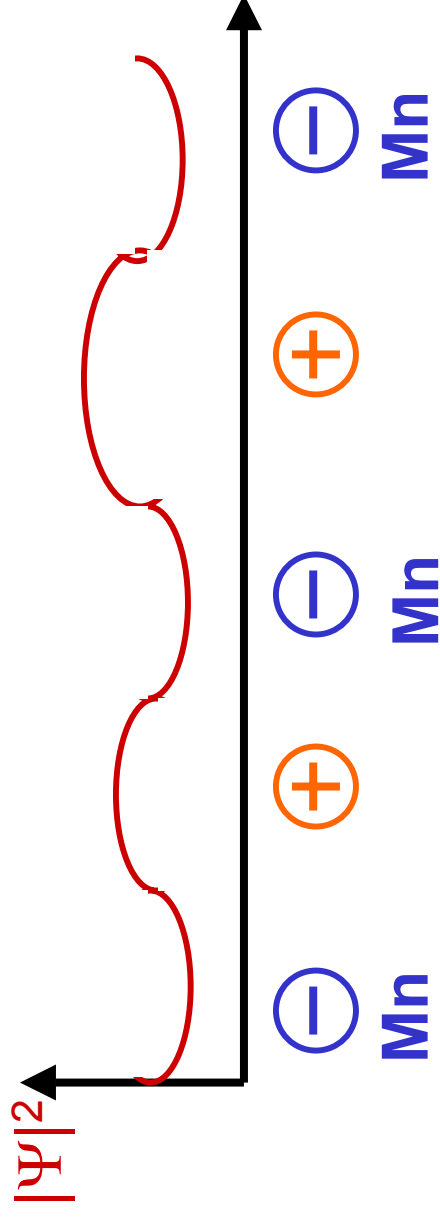
SFRS *Heimbrodt et al. (Marburg) Physica E'01*

$$\alpha N_o = -90 \pm 30 \text{ meV} \quad x < 0.03\%$$

Time-resolved Kerr *Myers et al. (St. Barbara) cond-mat/0502115*



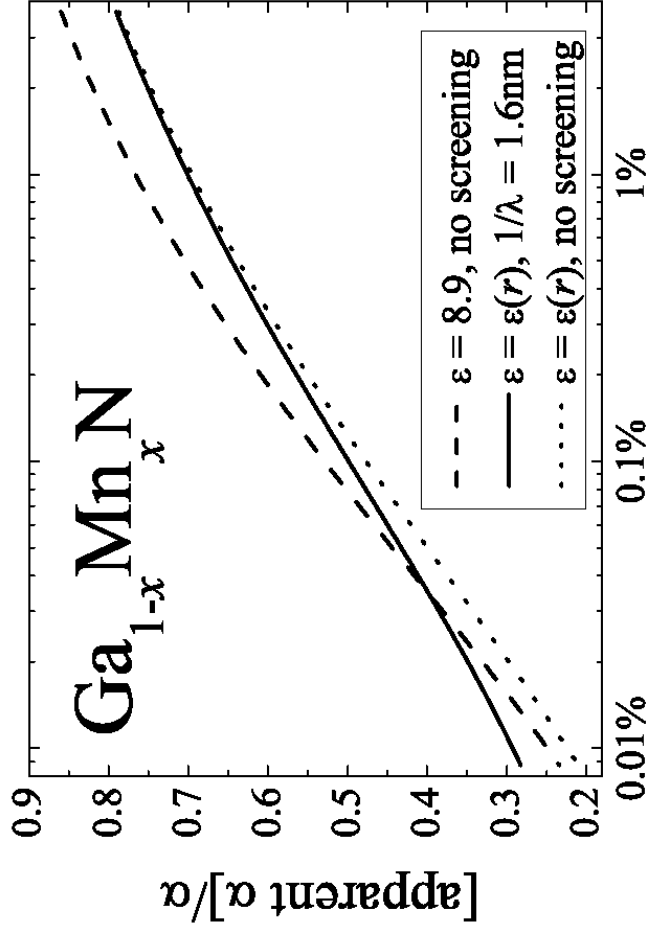
# Model for *apparent* s-d exchange energy $\propto N_o$ in (III,Mn)V



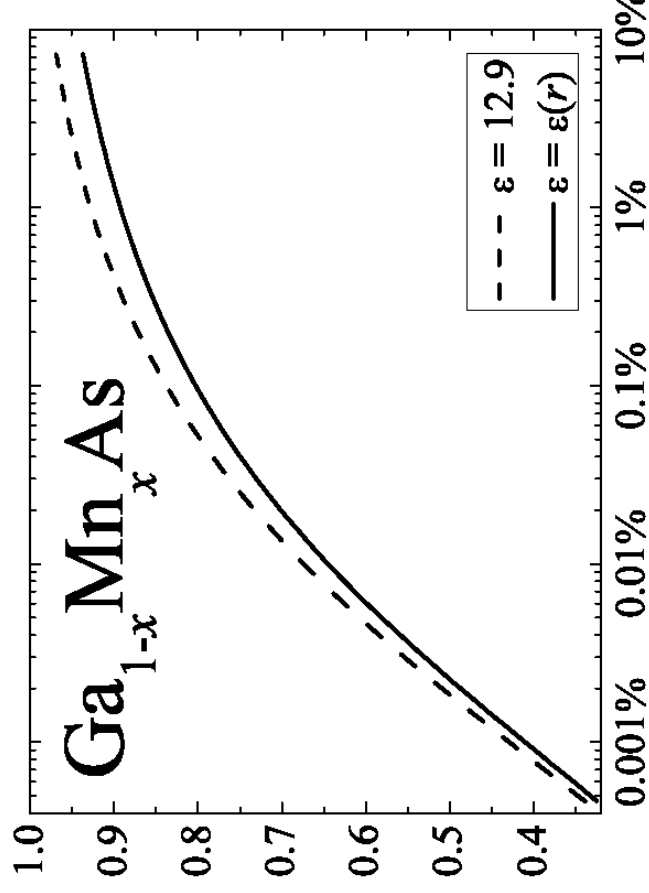
Electron repulsion by Mn acceptors and attraction by donors:

- reduces:  $|\Psi|^2$  at Mn → spin-splitting → apparent  $\propto N_o$
- effect large at small  $x$

# Reduction of *apparent* $\alpha N_0$ taking into account Coulomb repulsion by Mn acceptors



Mn concentration  $x$



Mn concentration  $x$

C. Śliwa, T.D. (Warsaw) cond-mat/0505126

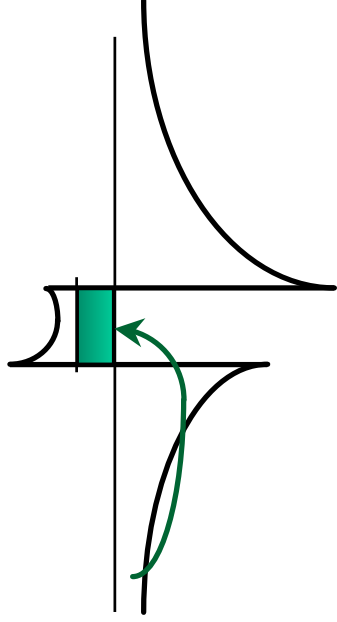
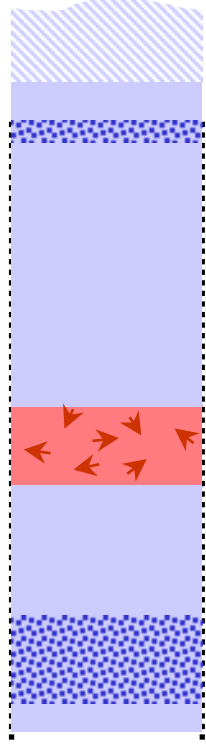
# Magnetic disorder

# Modulation-doped (Cd,Mn)Te quantum wells

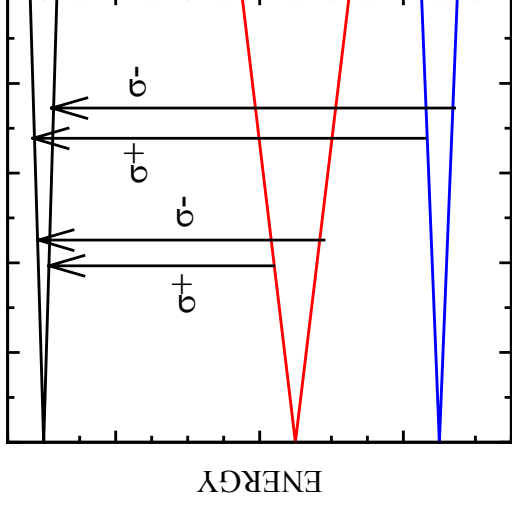
(Cd,Mg)Te:N

(Cd,Mg)Te:N

(Cd,Mn)Te



cf. Joël Cibert

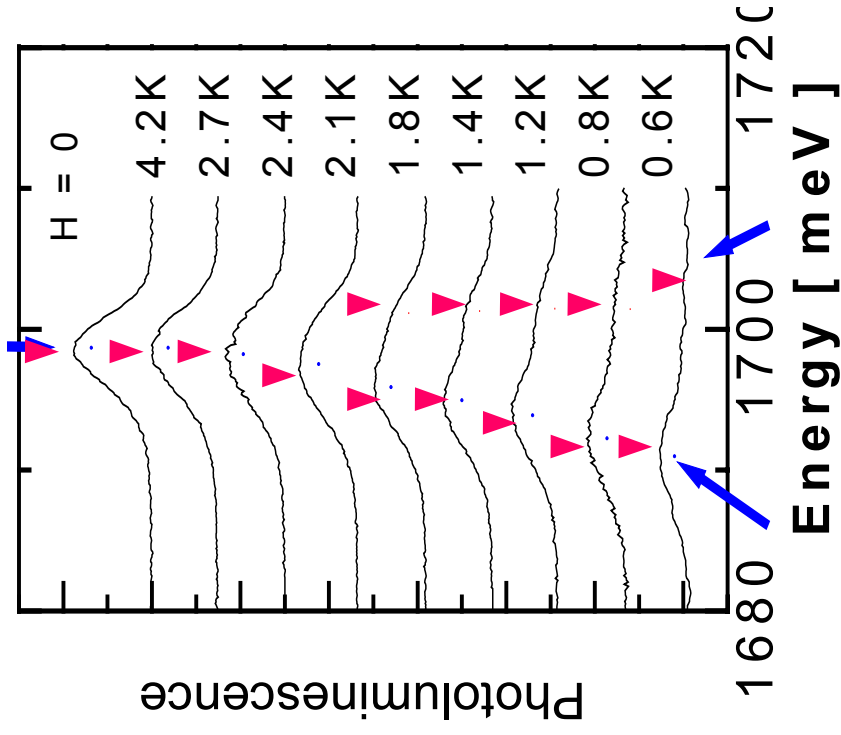


$$\Delta E \sim M$$

- weak disorder
- Ising system

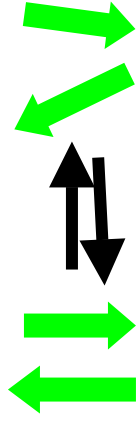


# Spontaneous splitting of PL line in p-(Cd,Mn)Te QW



*Kossacki et al. (Warsaw, Grenoble) Physica E'00*

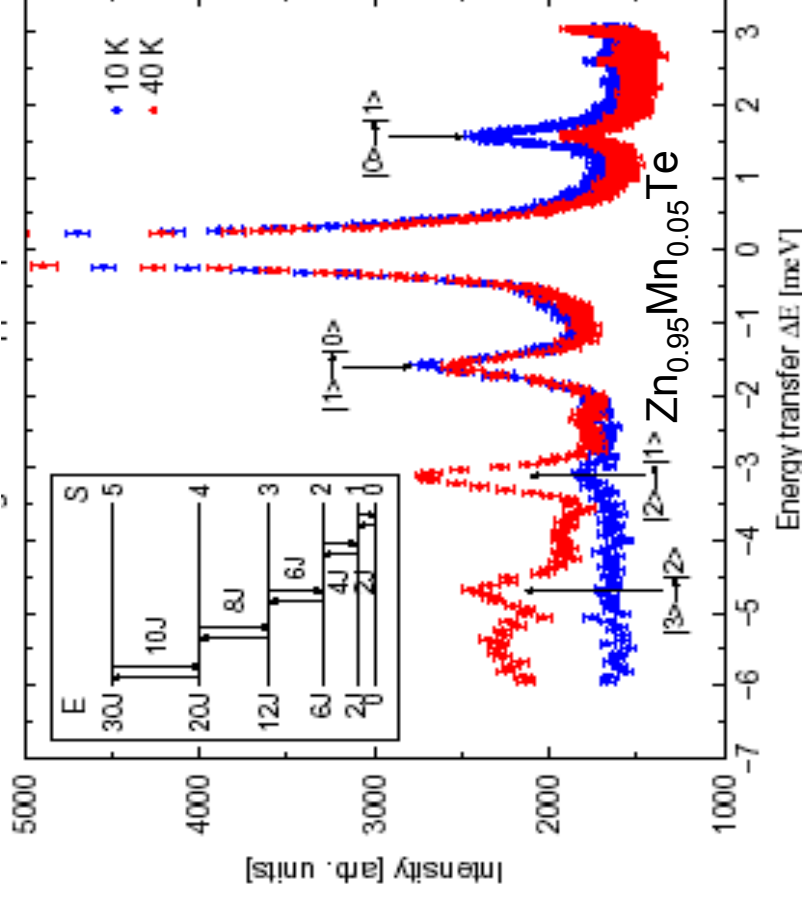
# Probing competing AF and FM interactions by inelastic neutron scattering in p-(Zn,Mn)Te



inelastic neutron scattering of n.n. Mn pairs

large single crystals of  $\text{Zn}_{0.95}\text{Mn}_{0.05}\text{Te:P}$

$\rho = 5 \times 10^{18} \text{ cm}^{-3}$ ,  $T_{\text{CW}} = 2 \text{ K}$   
Insulator side of the MIT



$$H_{\text{int}} = -2(J_{\text{AF}} + J_{\text{h}})S_i S_j$$

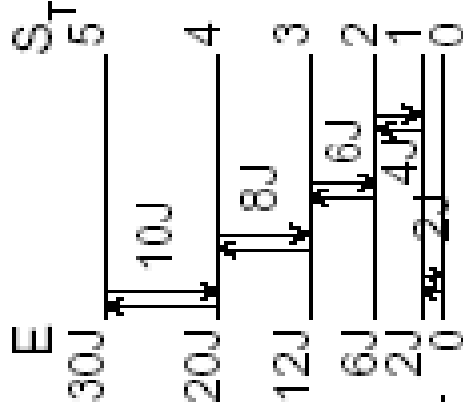
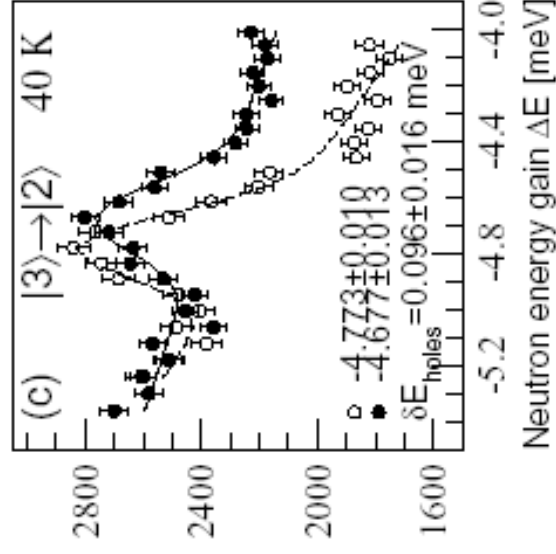
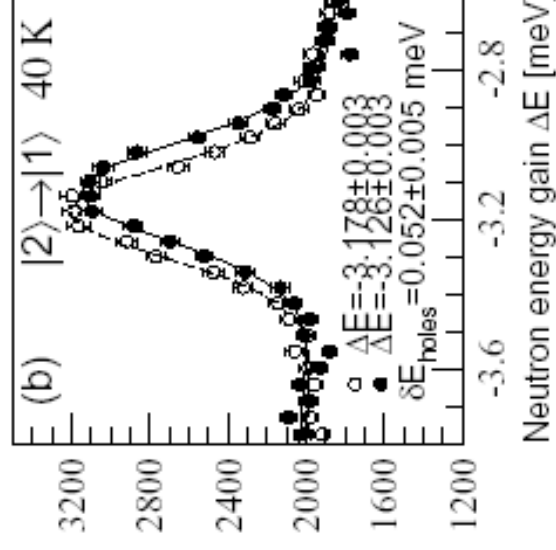
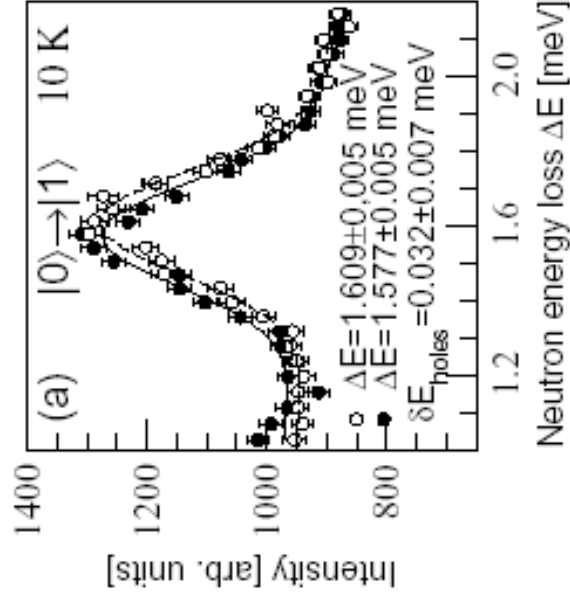
$J_{\text{AF}} < 0$  super-exchange

$J_{\text{h}} > 0$  hole-induced

*Kępa et al. (Warsaw, Oregon) PRL '03*

# Hole induced contribution

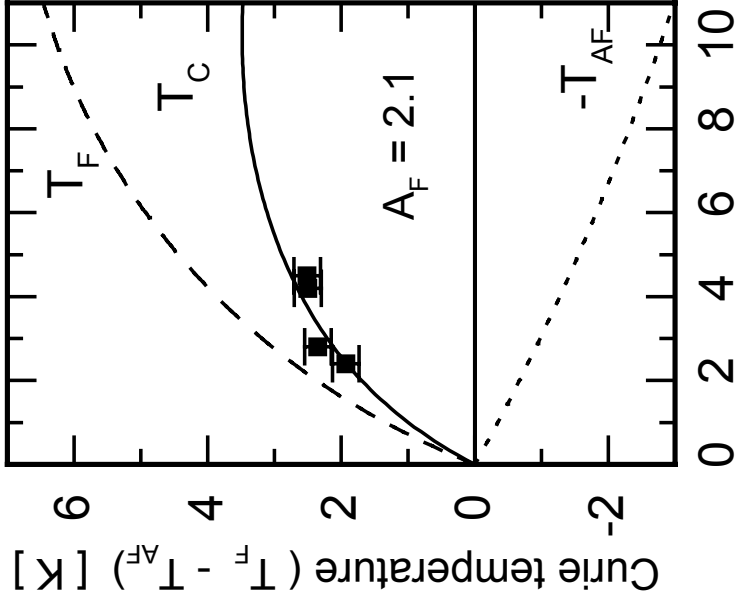
empty dots - no holes, full dots - with holes



$$\delta E = 2J_h = 0.03 \pm 0.006 \text{ meV}$$

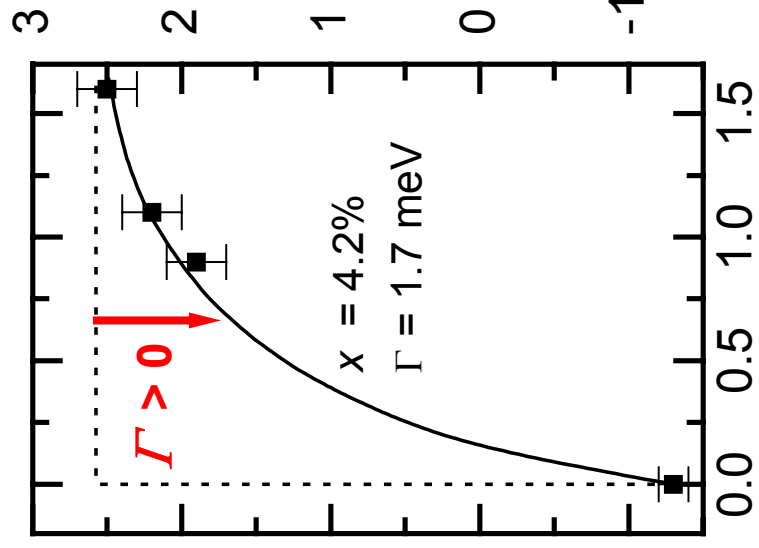
$$2J_h^{\text{RKKY}} = 0.020 \text{ meV}$$

# Mean field $T_C = T_F - T_{AF}$ vs. $x$ and $p$ in $p\text{-Cd}_{1-x}\text{Mn}_x\text{Te}$ QW



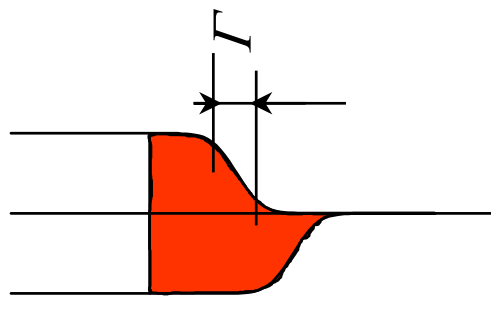
Mn content  $x$  [%]

Boukari et al. (Grenoble, Warsaw) PRL '02



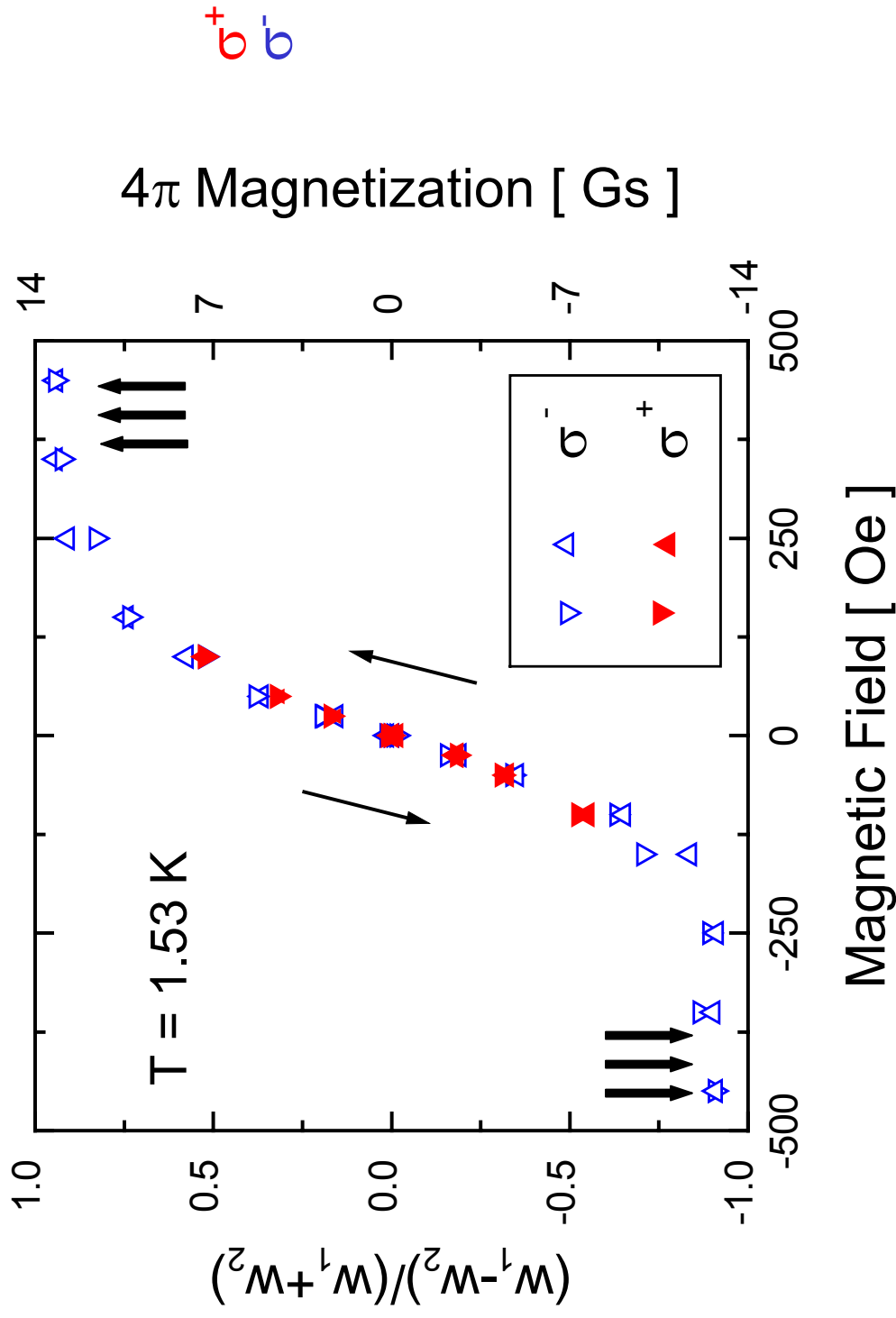
Hole density [ $10^{11} \text{ cm}^{-2}$ ]

role of disorder:



MFA describes  $T_C$  but ....

# Optically determined $M(H)$ for $H$ along easy axis



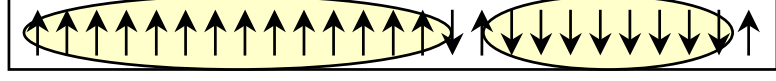
Kossacki et al. (Warsaw, Grenoble)  
 Physica E'02

- no hysteresis
- large saturation field

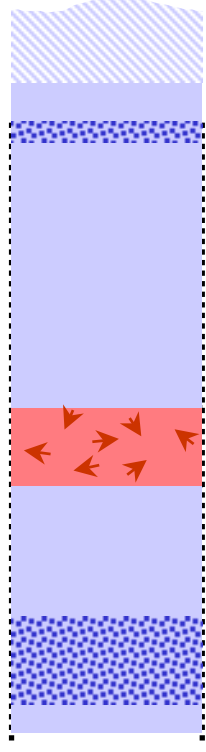
# Model and approach

**Competing long-range  
FM and short-range AF  
produces nanoscale  
180° domains**

*Dechrakos et al. (Athens, Warsaw) PRL '05*



**Monte Carlo simulations  
of coupled hole  
and Mn spin systems  
in (Cd,Mn)Te QW**

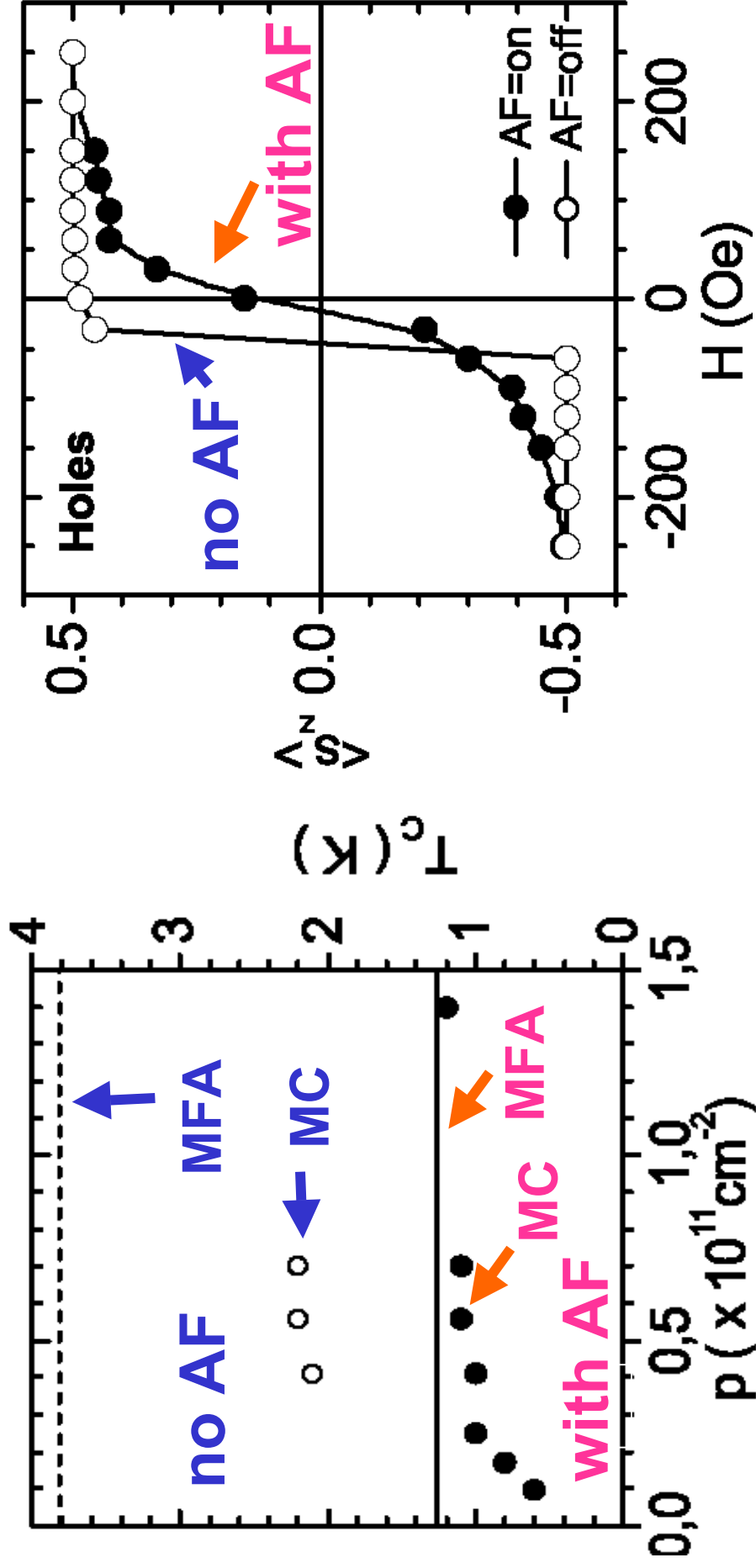


- *hole energies calculated at each Monte Carlo sweep*
- *AF interactions taken into account* "

*previous MC simulations of DMS:*

*J. Schliemann et al., E. Dagotto et al., L. Brey et al., ...*

# Comparison of MFA and Monte Carlo results with AF and with no AF interactions



Dechrakos et al. (Athens, Warsaw) PRL '05

- ordering temperature  $T_C > T_F - T_{FA}$
- macroscopic spontaneous magnetisation reduced

# Nanoscale fluctuations - summary

- (III,Mn)V  
electrostatic disorder caused by ionised Mn acceptors and compensating donors reduces *apparent s-d* and enhances *apparent p-d* exchange integral at low  $x$
- (II,Mn)VI  
magnetic disorder caused by competing AF and FM interactions increases  $T_C = T_F - T_{FA}$  and diminishes spontaneous magnetisation



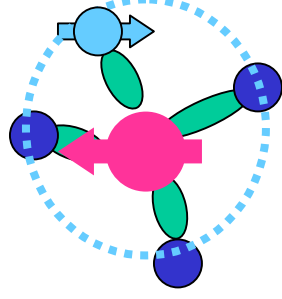
**Nanoscale phase separation**  
**Can we push  $T_c$  higher?**

# Strategies

- **Two strategies for increasing  $T_c$** 
  - increasing  $p$  and/or  $x$  in existing ferromagnetic DMS
  - searching for DMS with greater coupling constant  $\beta^2\rho(E_F)$

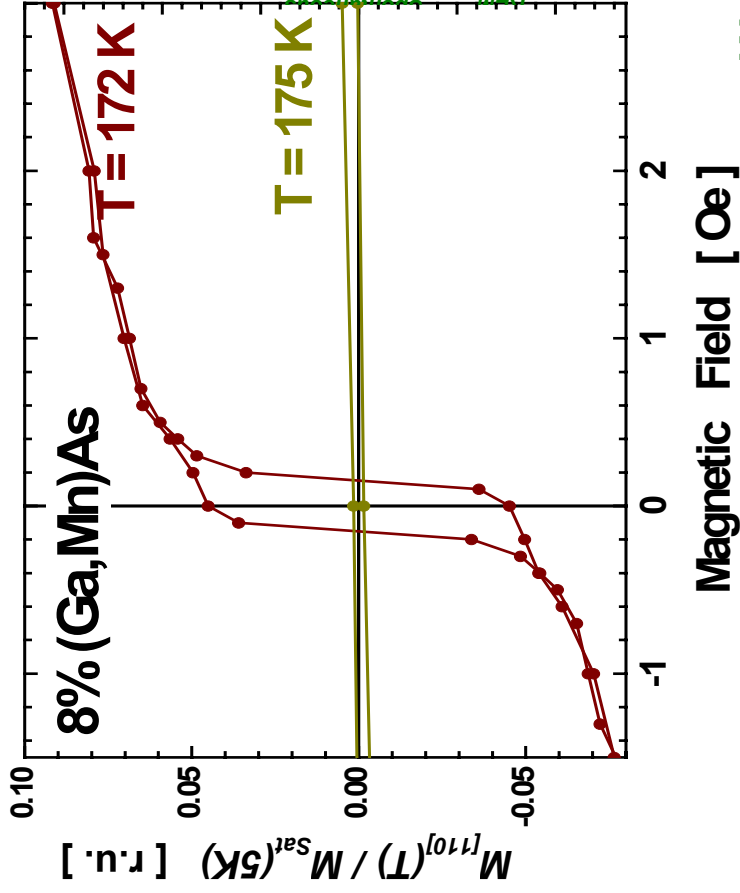
# Strategies

- **Two strategies for increasing  $T_c$** 
  - increasing  $p$  and/or  $x$  in existing ferromagnetic DMS
  - searching for DMS with greater coupling constant  $\beta^2\rho(E_F)$   
→ *nitrides and oxides*
- **Obstacles**
  - self-compensation
  - solubility limits
  - tight binding of holes by TM ions (Zhang-Rice polaron)

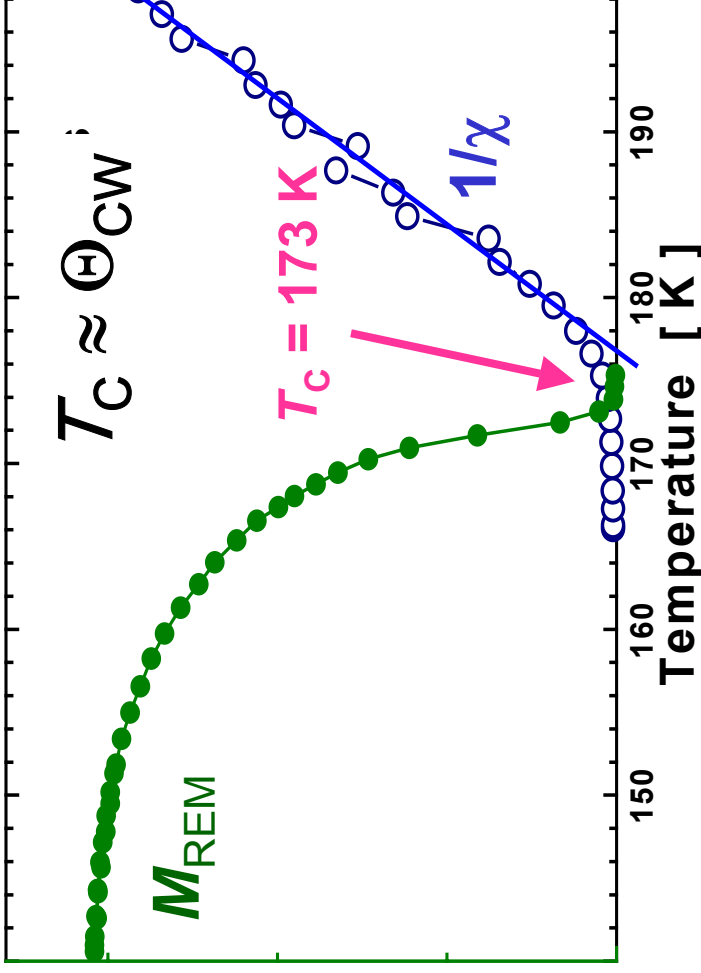


# Where do we stand?

hysteresis loops



remanent magnetisation and  $1/\chi$  vs.  $T$

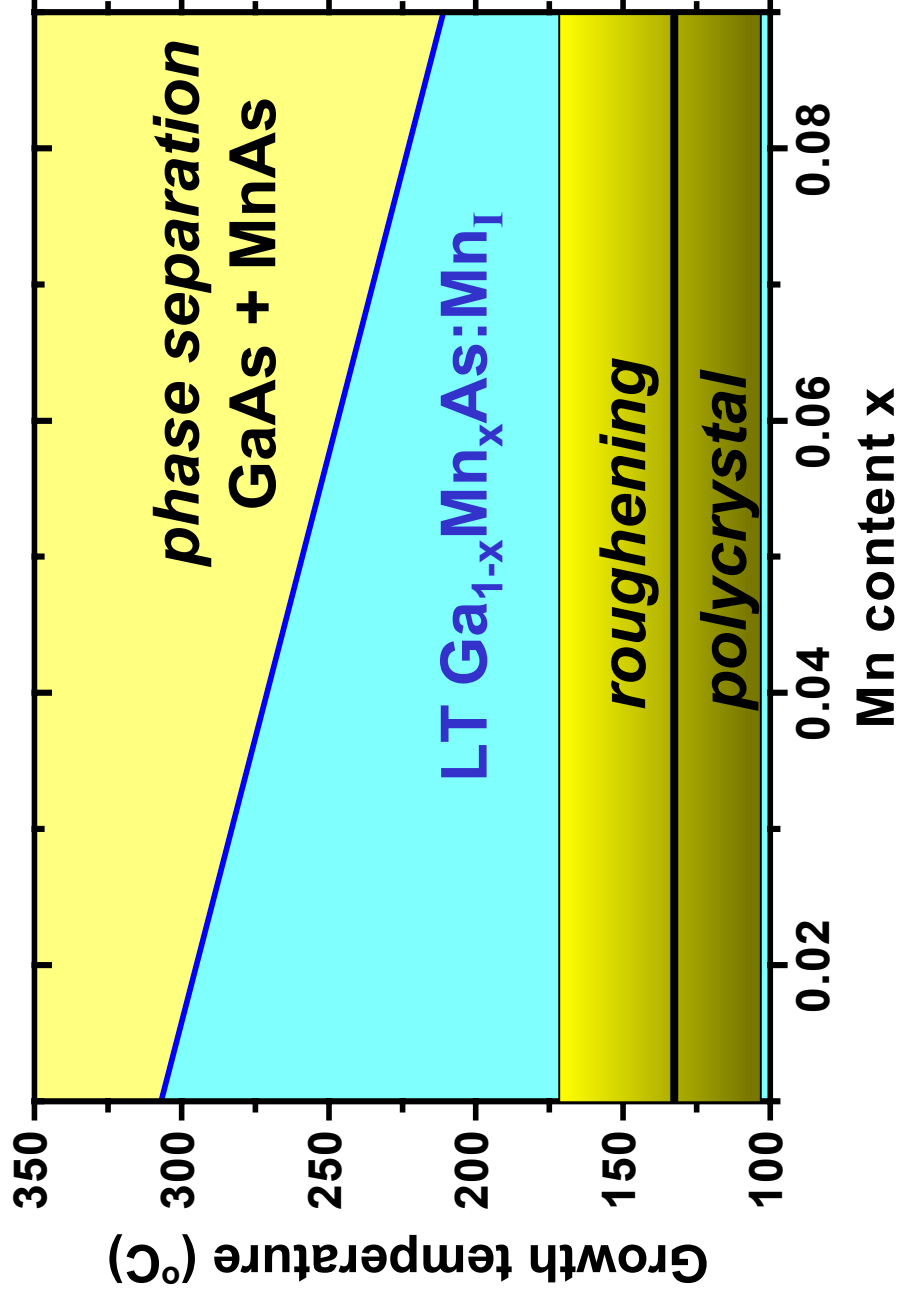


Wang et al. (Nottingham, Warsaw)

Progress due to control over self-compensation

cf. Nitin Samarth

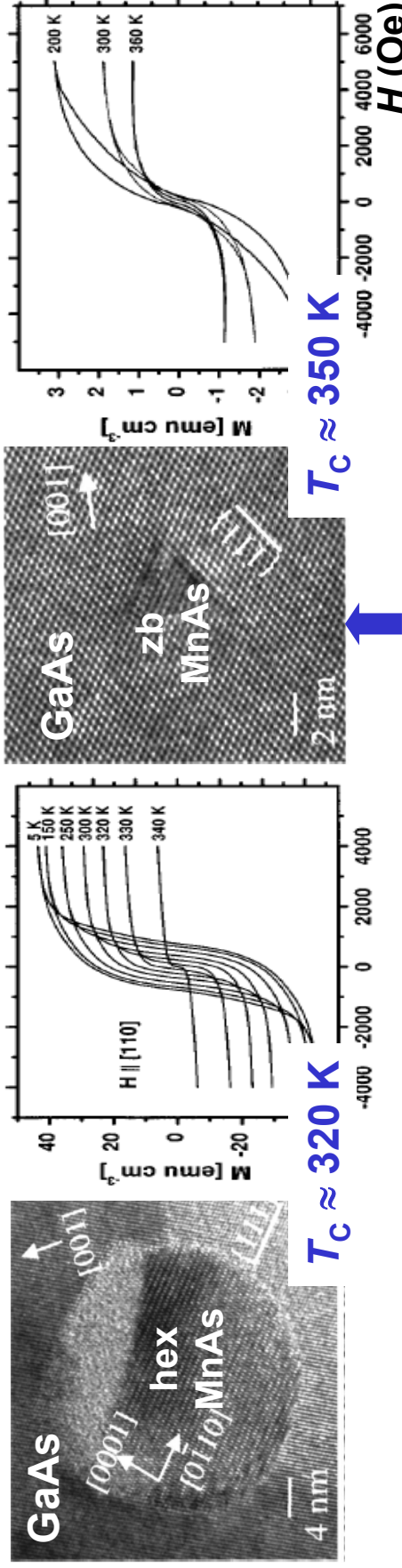
# (Ga,Mn)As – growth phase diagram



after Matsukura and Ohno (Tohoku)

# GaAs + MnAs precipitates

- size and structure determined by growth conditions
- control magnetic properties *De Boeck et al. (IMEC) APL'96*

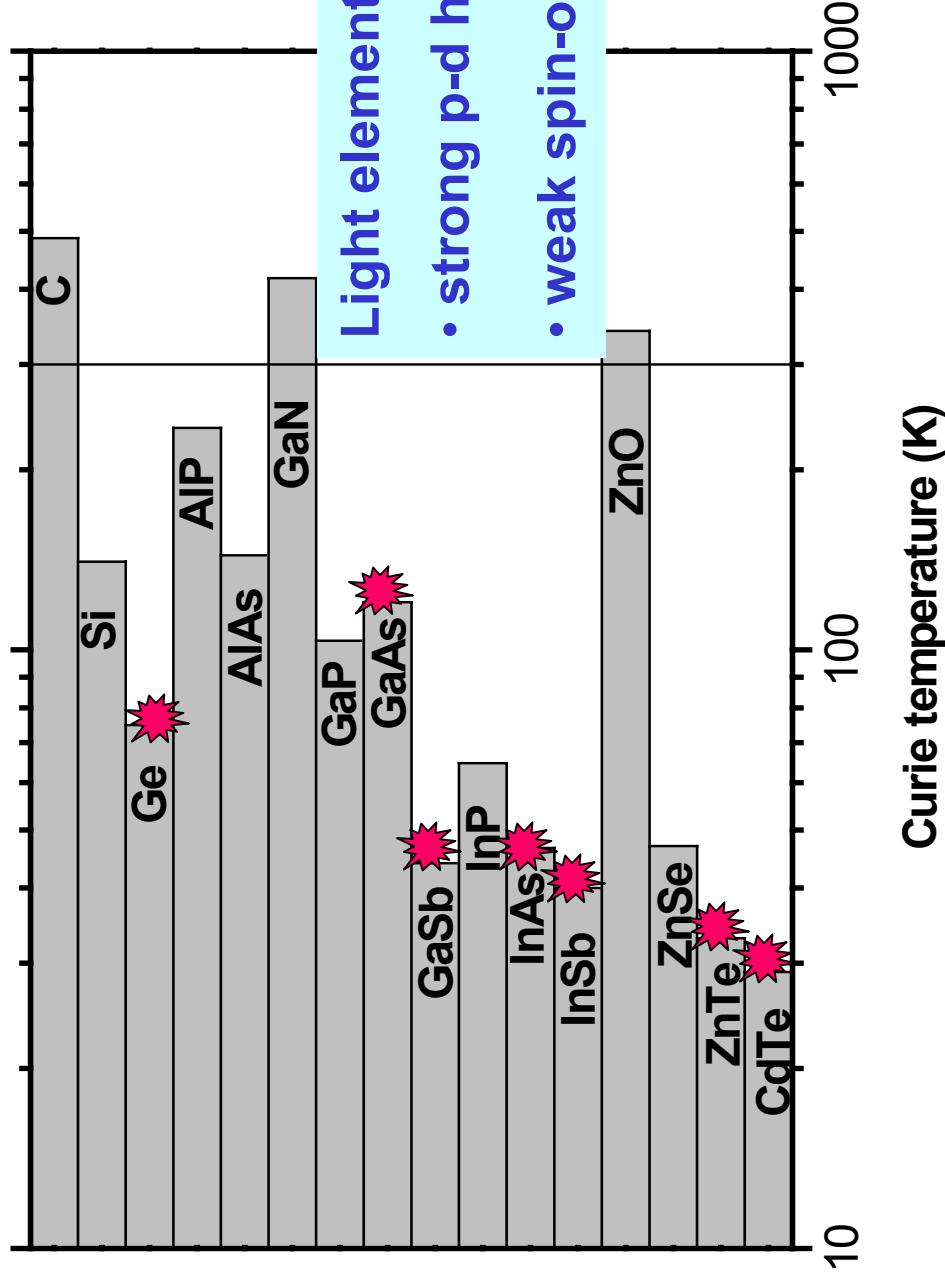


- spinodal decomposition
- superparamagnetic limit not reached

*Moreno et al. (Berlin) JAP'02*

# Other systems

# Zener model prediction of $T_C$ for semiconductors containing 5% Mn d<sup>5</sup>, $\rho = 3.5 \times 10^{20} \text{ cm}^{-3}$



*T. D. et al. (Warsaw, Tohoku, Grenoble) Science'00, PRB'01*



# Semiconductor materials showing hysteresis and spontaneous magnetisation at 300 K

wz-c-(Ga,**Mn**)N, (In,**Mn**)N, (Al,**Mn**)N, (Ga,**Cr**)N, (Al,**Cr**)N, (Ga,**Gd**)N,

(Ga,**Mn**)As, (In,**Mn**)As, (Ga,**Mn**)Sb, (Ga,**Mn**)P:C

(Zn,**Mn**)O, (Zn,**Ni**)O, (Zn,**Co**)O, (Zn,**V**)O, (Zn,**Fe**,**Cu**)O

(Zn,**Cr**)Te

(Ti,**Co**)O<sub>2</sub>, (Ti,**V**)O<sub>2</sub>, (Sn,**Co**)O<sub>2</sub>, (Sn,**Fe**)O<sub>2</sub>, (Hf,**Co**)O<sub>2</sub>

(Cd,Ge,**Mn**)P<sub>2</sub>, (Zn,Ge,**Mn**)P<sub>2</sub>, (Cd,Ge,**Mn**)As<sub>2</sub>, (Zn,Sn,**Mn**)As<sub>2</sub>

(Ge,**Mn**), (Ge,**Mn**,**Fe**)

(La,Ca)B<sub>6</sub>, C, C<sub>60</sub>, HfO<sub>2</sub>, ...

cf. Klaus Ploog

In many cases high  $T_c$   
consistent with  
*ab initio* computations  
within LSDA

# High $T_c$ ferromagnetic semiconductors

- Growth phase diagrams unknown

- Microscopic mechanism underlying ferromagnetic response unknown

*LSDA largely overestimates tendency towards ferromagnetism*

- Each system brings new challenges

- new uniform ferromagnetic semiconductor?

  - *long-range ferromagnetic coupling with no band carriers?*

- nanoscale phase separation?

  - *structural*: precipitates of known or new ferro/ferrimagnets?

  - *atomic*: magnetic atom segregation (spinodal decomposition)?

    - *electronic*?

    - *magnetic*?

- role of defects and contamination?

# CONCLUSIONS AND OUTLOOK

- **(Ga,Mn)As, p-(Cd,Mn)Te, ... emerge as the best understood model ferromagnets**
- **Beginning of the road for high temperature ferromagnetic semiconducting systems**
  - nanoscale phase separations?
- **Is high temperature ferromagnetism without magnetic ions possible? (low  $T_C$ : QHFM, organic materials)**
  - defects bands, zinc-blende metals (CaAs, ...), ...?