# Charge Instabilities At The Metamagnetic Transition

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1 Layered Sr-Ruthenates

2 Stoner and Pomeranchuk scenarios for the metamagnetic transition

**3** 2D Hubbard model perspective: mechanisms?

4 Micro phase separation?

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#### Layered Strontium-Ruthenates Sr<sub>n+1</sub>Ru<sub>n</sub>O<sub>3n+1</sub> Ruddlesden-Popper Series





Single layer:  $Sr_2RuO_4$ Triplet superconductor,  $T_c=1.5K$ , expanding FS volume: strong increase of  $\chi$ 

Double layer: Sr<sub>3</sub>Ru<sub>2</sub>O<sub>7</sub> close to ferromagnetism, metamagnetic transition

## Electronic Structure: Single Layer Sr<sub>2</sub>RuO<sub>4</sub>

- 3 t<sub>2g</sub> bands (d<sub>xy</sub>,d<sub>xz</sub>,d<sub>yz</sub>) cross Fermi level, almost 2D band structure
- LDA, dHvA and ARPES agree on Fermi surfaces
- Van Hove singularity near Fermi level



#### Doping La<sup>3+</sup> For Sr<sup>2+</sup>: Pushing The FS Closer To Van Hove Points & Ferromagnetism

- Sr<sub>2-y</sub>La<sub>y</sub>RuO<sub>4</sub>: y>0 adds electrons, expands all Fermi surfaces
- Spin susceptibility χ increases (FM tencencies!)
- FS pushed toward van Hove points
- Multi-layer splittings push FS closer to VH points (Sigrist)



#### Double-Layer Sr<sub>3</sub>Ru<sub>2</sub>O<sub>7</sub>: Metamagnetic Transition



- Sharp increase of magnetization in magnetic field around 7.8T
- Feature in resistivity, anomalous T-dependence:  $\rho = \rho_0 + A T^x$  with  $x \neq 2$  in critical region.

#### **Stoner Picture**

• Mean field theory for local repulsion U: metamagnetic transition near van Hove filling





- Ultraclean samples ( $\rho_0$ =0.4  $\mu\Omega$ cm) show two or three peaks in low frequency susceptibility  $\chi$
- peaks in Im  $\chi$  interpreted as hysteretic signals of two 1st order transitions

## **Resistivity Anomaly**



- Cleaner samples develop big (×2) resistivity anomaly at the metamagnetic transition
- In anomalous B-field range: no significant increase of  $\rho$  with T  $\rightarrow$  elastic scattering
- Domains of something sensitive to impurities???

#### d-Pomeranchuk Scenario



#### Proposal: d-wave 'Pomeranchuk' Fermi surface deformation

- increases magnetization
- makes domains responsible for resistivity anomaly
- should be sensitive to sample quality

## d-Wave FS Deformation In 2D Hubbard Model

- RG in Hubbard model near half filling:
  - tendencies toward d-wave FS deformation (e.g. Halboth&Metzner 2000)
  - typically not strongest instability (CH et al. 2001), but generic tendency
- Effective interaction

$$H_{dPom}^{eff.} = -g \sum_{\vec{k}, \vec{k}', s, s'} f(\vec{k}, \vec{k}') c_{\vec{k}, s}^{+} c_{\vec{k}, s} c_{\vec{k}', s'}^{+} c_{\vec{k}', s'}$$





forward scattering needs this form with g>0  $\rightarrow$  calculate f<sub>kk</sub> with RG

## Effective Interactions From Functional RG

Momentum-shell RG: integrate out shell around FS at decreasing energy scale  $\Lambda$ 

 $\rightarrow$  low energy interactions

**Temperature flow:** follow flow of vertex functions down to low

 $\rightarrow$  effective low-T interactions



#### RG: Triplet Superconductivity Near Ferromagnetism

• Temperature RG flow *p*-wave instability near FM regime at van Hove filling (CH & Salmhofer 01, Katanin 03,04)



#### Forward Scattering In Hubbard Model



- RG finds contradiction: d-wave FS deformations unfavorable (no attractive coupling constant) in FM regime!
- Alternative explanations?

## Similarity To Liquid-Gas Transition



Liquid gas transition:

- Jump in entropy S vs. T at T<sub>c</sub>
- Also feature in F as function of V

Regions with negative curvature wrt
 V → phase coexistence

Analogue for metamagnetic transition?

## Unstable Density Regions Near MM Transition



- Gibbs potential G(T,h,n) in Binz-Sigrist mean-field model has negative curvature wrt density n
- $\rightarrow$  Coulomb-frustrated phase separation?



#### Maxwell Destruction Of Magnetization Jump?



• Does phase separation wipe out magnetization-step?

#### **Coulomb & Interface Energies**

Coulomb energy frustrates phase separation

- $\rightarrow$  micro phase separation on nanoscale
- $\rightarrow$  interfaces between high- and low-density phases cost additional energy  $G_{I}$
- $\rightarrow$  not all mixing ratios p energtically favorable, very thin stripes don't pay



#### Two Jumps



Length Scale Of Domains



• stripes in metals (Lorenzana et al.):

size of domains ~ screening length ~ lattice distance

$$l_s^2 = \mathcal{E}_0 / (4\pi e^2 \kappa)$$
  $\kappa = \text{compressibility}$ 

Is our description sensible? BUT:

- only one Fermi surface (of 6) near VH points, other FS are spectators
- mutual screening by other FS reduces effective charge of domains → screening length increases

$$l_s^2 = \mathcal{E}_0 / (4\pi e^2 Z^* \kappa)$$
  $Z^* < 1$  charge reduction

- Strontium-Ruthenates are good test case for understanding of correlation effects
- Scenarios for resistivity anomaly at metamagnetic transition
  - Pomeranchuk FS deformation hard to reconcile with FM tendencies and Hubbrd-type models
  - MM transition invites micro phase separation,
    Coulomb+interface energies might create two magnetization jumps
  - Alternative: uncharged Condon domains due to demagnetization (Binz, Sigrist et al.)

Possible experimental test: STM (Cornell group)