

# Magneto-transport and Glassiness at Nanoscale Coexistence

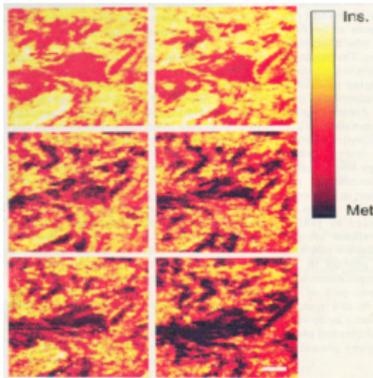
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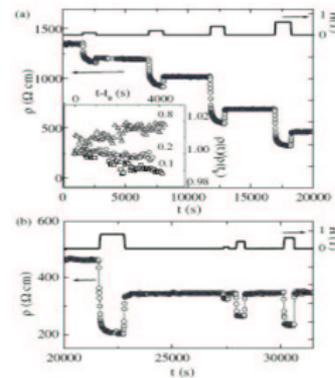
# Outline

- 1 Motivation
  - Phase Separated Manganites: Experiments
  - Theory Efforts
- 2 Model and Method
  - Competing Interactions and Disorder
  - Self Consistent Renormalisation(SCR)
- 3 Results
  - Magneto-transport
  - Glassiness

# Inhomogeneities and Slow Relaxation



Fath *et al.* (1999)



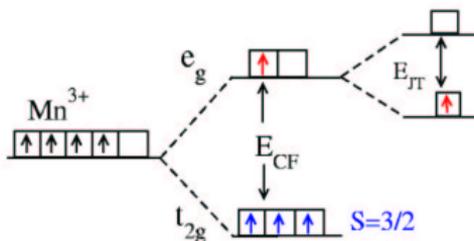
Levy *et al.* (2002)

- Glassiness in  $Pr_{0.7}Ca_{0.3}MnO_3$ . Deac *et al.* (2001)

# Understanding the Phase Coexistence Regime

- Difficulty: Inhomogeneous structure.
- Real space monte-carlo methods.  
Moreo *et al.* (2000)
- Resistor network theory for studying transport.  
Mayr *et al.* (2000)
- Very few theory efforts to understand the slow relaxation, glassiness or history dependence.

# Double Exchange vs. Superexchange



Our focus is on phase competition:

$$H = -t \sum_{\langle ij \rangle, \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + h.c.) + \sum_i (\epsilon_i - \mu) n_i - J_H \sum_i \mathbf{S}_i \cdot \sigma_i + J_S \sum_{\langle ij \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$

$J_S$ : AF coupling,  $\Delta$ : disorder,  $n$ : electronic density

# The Double Exchange Limit

$$J_H \rightarrow \infty \quad \Rightarrow \quad \mathbf{C}_i \rightarrow \gamma_i$$

Electronic spin slaved on to the core spin.

$$\begin{aligned} H_{el} &= -t \sum_{\langle ij \rangle} (g_{ij} \gamma_i^\dagger \gamma_j + h.c) + \sum_i (\epsilon_i - \mu) n_i \\ &= -t \sum_{\langle ij \rangle} \sqrt{(1 + \mathbf{S}_i \cdot \mathbf{S}_j)/2} (e^{i\Phi_{ij}} \gamma_i^\dagger \gamma_j + h.c) + \sum_i (\epsilon_i - \mu) n_i \end{aligned}$$

$$g_{ij} = \cos(\theta_i/2) \cos(\theta_j/2) + \sin(\theta_i/2) \sin(\theta_j/2) e^{i(\phi_i - \phi_j)}$$

# Effective Hamiltonian and EDMC

## The Partition Function

$$Z = \int \mathcal{D}\mathbf{S} \text{Tr} e^{-\beta H(\{\mathbf{S}\})} \equiv \int \mathcal{D}\mathbf{S} e^{-\beta H_{\text{eff}}(\{\mathbf{S}\})}$$

$$H_{\text{eff}}(\{\mathbf{S}\}) = -\frac{1}{\beta} \log \text{Tr} e^{-\beta H(\{\mathbf{S}\})}$$

$\text{Tr} e^{-\beta H(\{\mathbf{S}\})}$  can not be calculated analytically for arbitrary  $\{\mathbf{S}\}$

- Use Exact Diagonalisation to compute the trace.  $\Rightarrow$  EDMC
- EDMC is computation intensive.  $N \sim 100$

# Self Consistent Renormalisation

- The electronic part of the Hamiltonian:

$$H_{el} = -t \sum_{\langle ij \rangle} \sqrt{(1 + \mathbf{S}_i \cdot \mathbf{S}_j)/2} (e^{i\Phi_{ij}} \gamma_i^\dagger \gamma_j + h.c.) + \sum_i (\epsilon_i - \mu) n_i$$

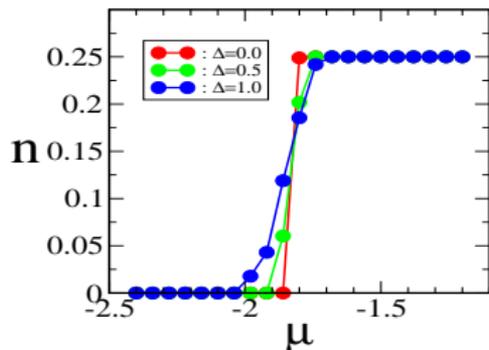
- The effective spin Hamiltonian:

$$H_{eff}(\{\mathbf{S}\}) \approx -t \sum_{\langle ij \rangle} D_{ij} \sqrt{(1 + \mathbf{S}_i \cdot \mathbf{S}_j)/2} + J_s \sum_{\langle ij \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$

- Parameters for the effective spin Hamiltonian:

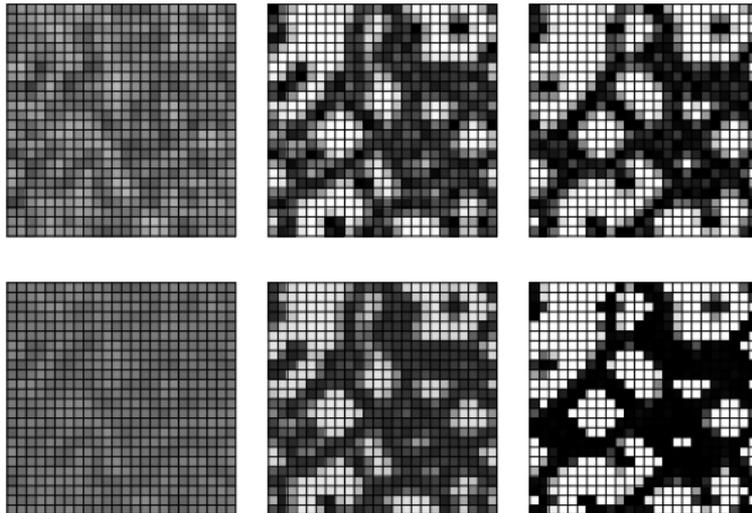
$$D_{ij} = \int \mathcal{D}\mathbf{S} e^{-\beta H_{eff}(\{\mathbf{S}\})} \langle (e^{i\Phi_{ij}} \gamma_i^\dagger \gamma_j + h.c.) \rangle$$

# Effect of Disorder on Phase Separation



- 1st order transition from  $n = 0$  AF-I to  $n \sim 0.2$  FM-Metal.
- Disorder smooths out the  $n - \mu$  discontinuity.

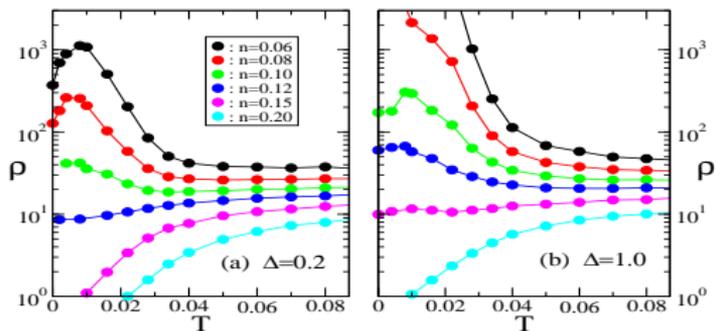
# Coexisting FM-M and AF-I Clusters



- $\langle n_i \rangle$  (top row) and  $\langle \mathbf{S}_i \cdot \mathbf{S}_{i+\delta} \rangle$  (bottom row) on cooling.

# Transport in the Coexistence Regime

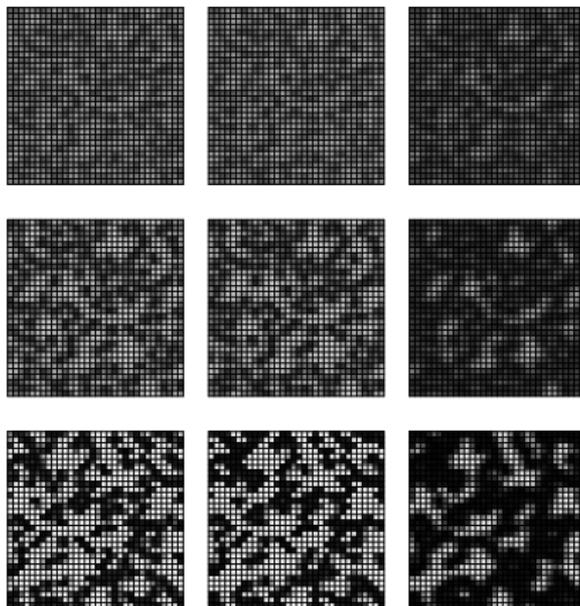
- Resistivity using Kubo formula (*cond-mat / 0504656*)



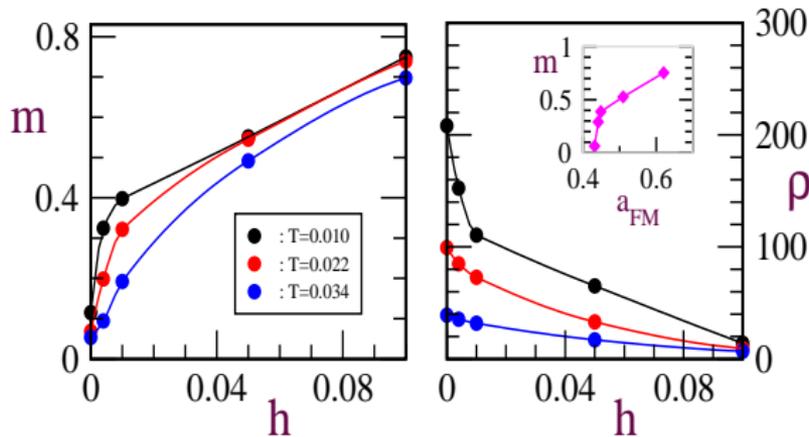
- Density driven MIT. Percolation?
- Hint for a thermally driven MIT.

# Effect of External Magnetic Field

Including external magnetic field:  $H' = H - h \sum_i \mathbf{S}_i^z$



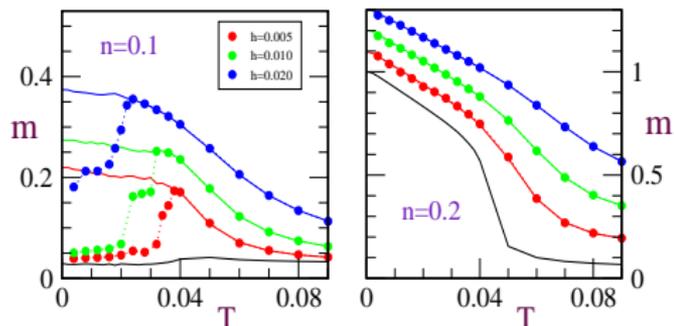
# Magnetization and Resistivity: response to $h$



- Low fields: Alignment of *cluster* magnetic moments
- High fields: Expansion of FM regions.

## Field Cooling and Zero Field Cooling

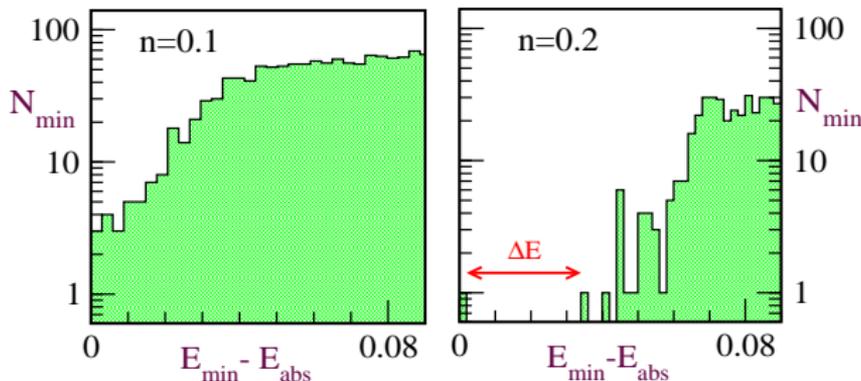
- No Spin-Glass behaviour for O(3) spin model in 2d.
- Weak local anisotropy to lift the O(3) symmetry.



- FC magnetisation differs from ZFC for  $n = 0.1$  at low fields.

# Density of Local Minima

- Minimize  $E(\{\mathbf{S}\})$  using Conjugate-Gradient Method.



- $n = 0.1$ : High density of local minima near  $E = E_{\text{abs}}$ .
- $n = 0.2$ : Gap at low energy.

# Summary

- Transport beyond the simple percolation scenario.
- Low field response: alignment of FM clusters.
- Spin glass behaviour and non-trivial energy landscape.

## Outlook:

- 2-band model with JT coupling.
- Structural glass  $\Leftrightarrow$  spin glass.

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