

# The nodal-antinodal dichotomy and competing orders in high temperature superconductors

Dung-Hai Lee, Berkeley



## STM

J. C. Davis (Cornell)  
J.E. Hoffman (Harvard)  
K. McElroy (Berkeley)

## ARPES

Z.-X. Shen (Stanford)  
X.-J. Zhou (LBNL)

## ARPES

A. Lanzara (Berkeley)  
G.H. Gweon (LBNL)

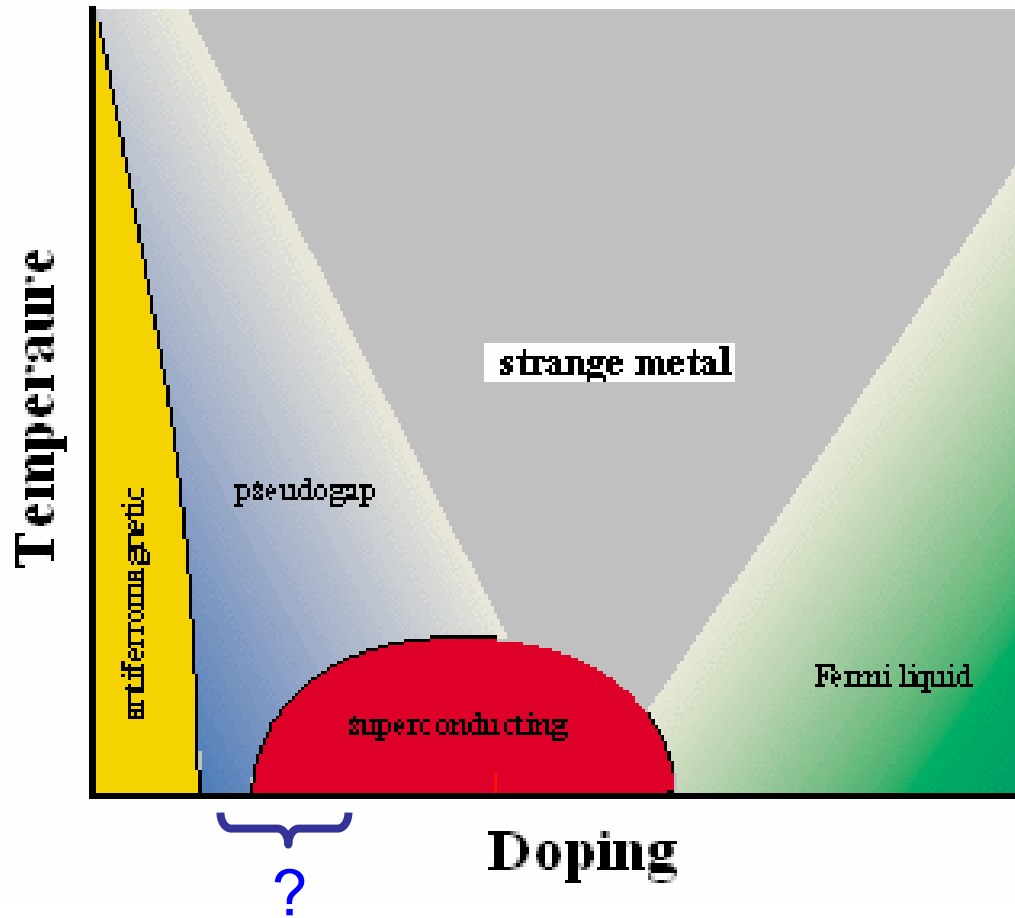
## Theory

H. Fu (Berkeley)  
C. Honerkamp (Max Plank)  
Q.H. Wang (Nanjing Univ.)

# Outline

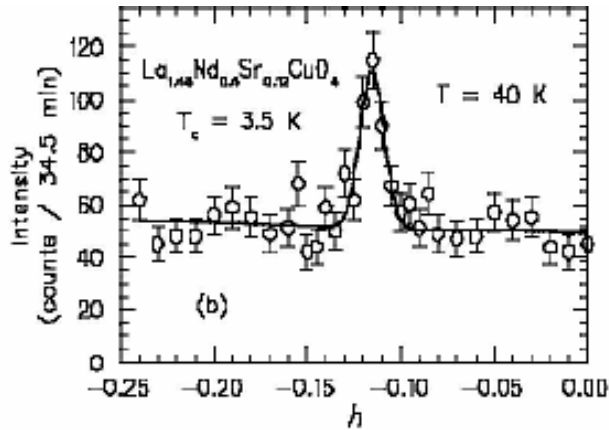
- Some background knowledge.
- The nodal-antinodal dichotomy in ARPES.
- Effect of disorder on nodal/antinodal excitations.
- The coupling of N/AN excitations to phonons.
- The coupling between N/AN excitations to charge order.
- Theoretical discussions
- Conclusion

# Competing order

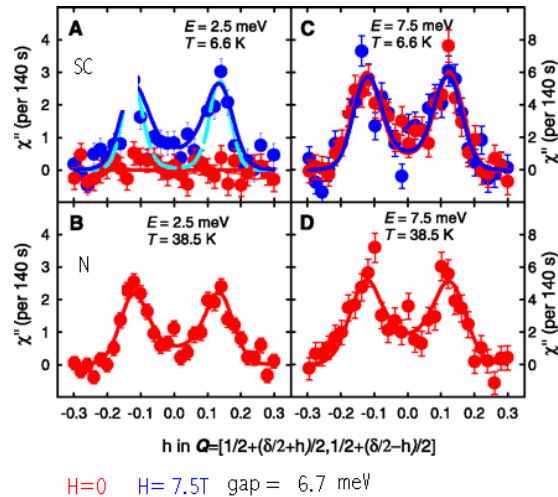


# The incommensurate magnetism

Tranquada *et al*  
Nature, (1995)

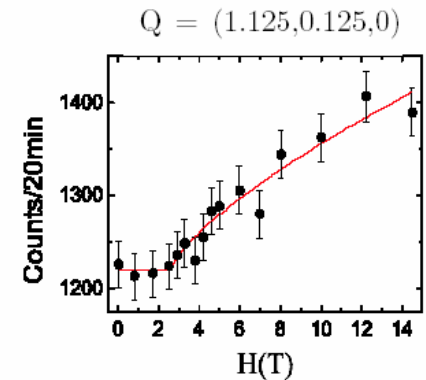


Lake et al, Science, (1999)  
Enhanced SDW fluctuation  
in the vortex cores



Khaykovich et al,  
cond-mat/0411355

B-induced SC  $\rightarrow$   
SC+SDW phase  
transition

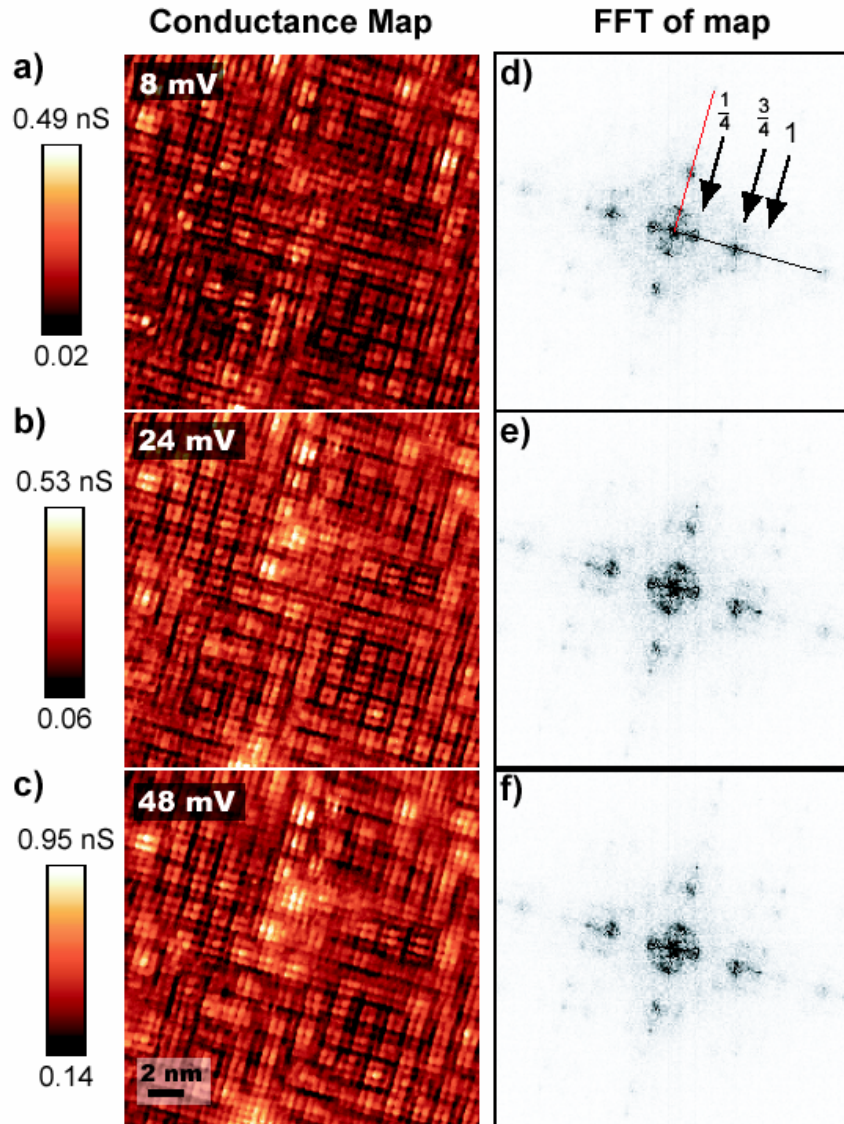


Stripe interpretation  
Zaanen & Gunnarsson, PRB (89).  
Emery & Kivelson, Physica C (93).

*Competitive* nature of SC and  
SDW



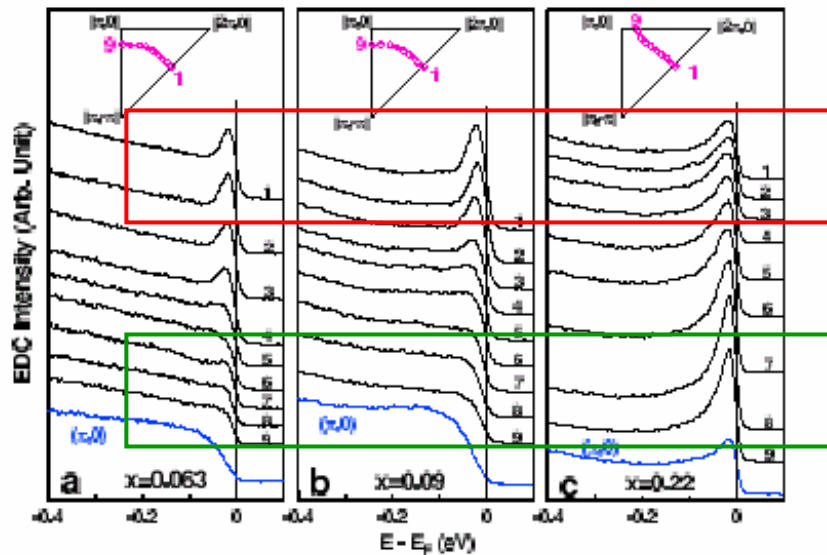
Hanaguri *et al*, *Nature* (2004)



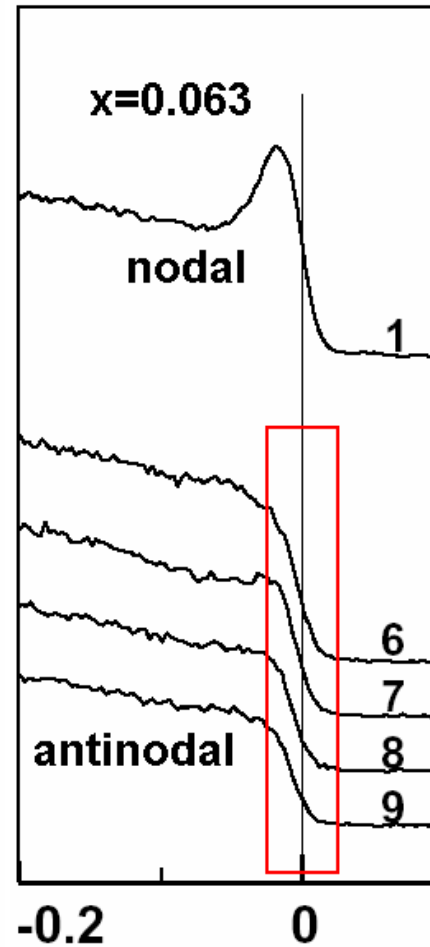
- No bias dependent modulation is observed. → quasiparticle interference is different from static ordering.
- Commensurate  $4a$ .
- Checkerboard pattern independent of doping → lattice pinning.

# The nodal and antinodal dichotomy in ARPES spectra

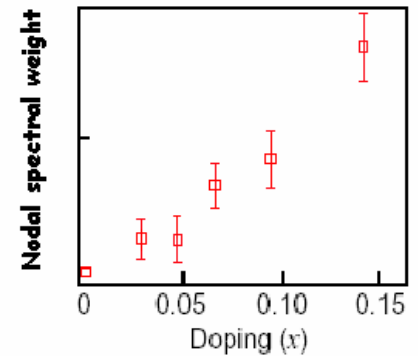
# The nodal-antinodal dichotomy



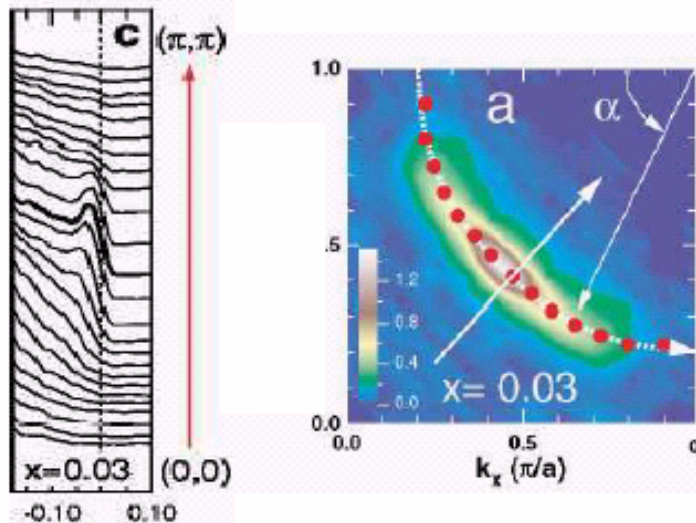
X.J. Zhou *et al*, PRL. 92 187001, (2004).



Tiny pseudogap !



Nodal  $Z \rightarrow 0$  as  $x \rightarrow 0$ .

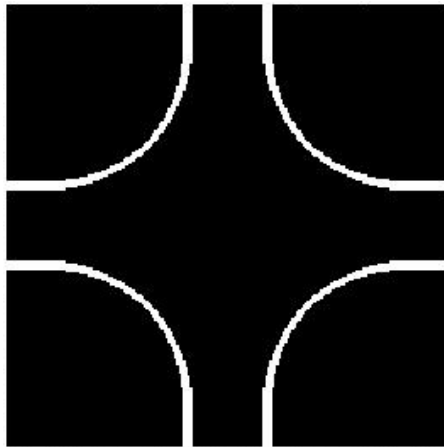


$E - E_F$

T. Yoshida *et al*, PRL. 91 027001, (2003).



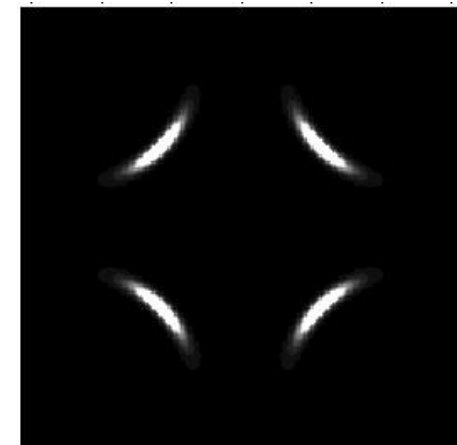
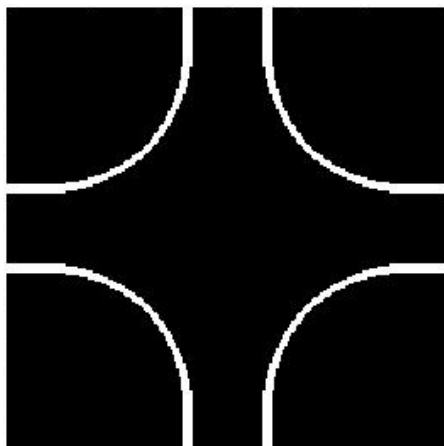
Prediction from theories that take the electronic correlation in a mean-field fashion



Decreasing doping  $\rightarrow$

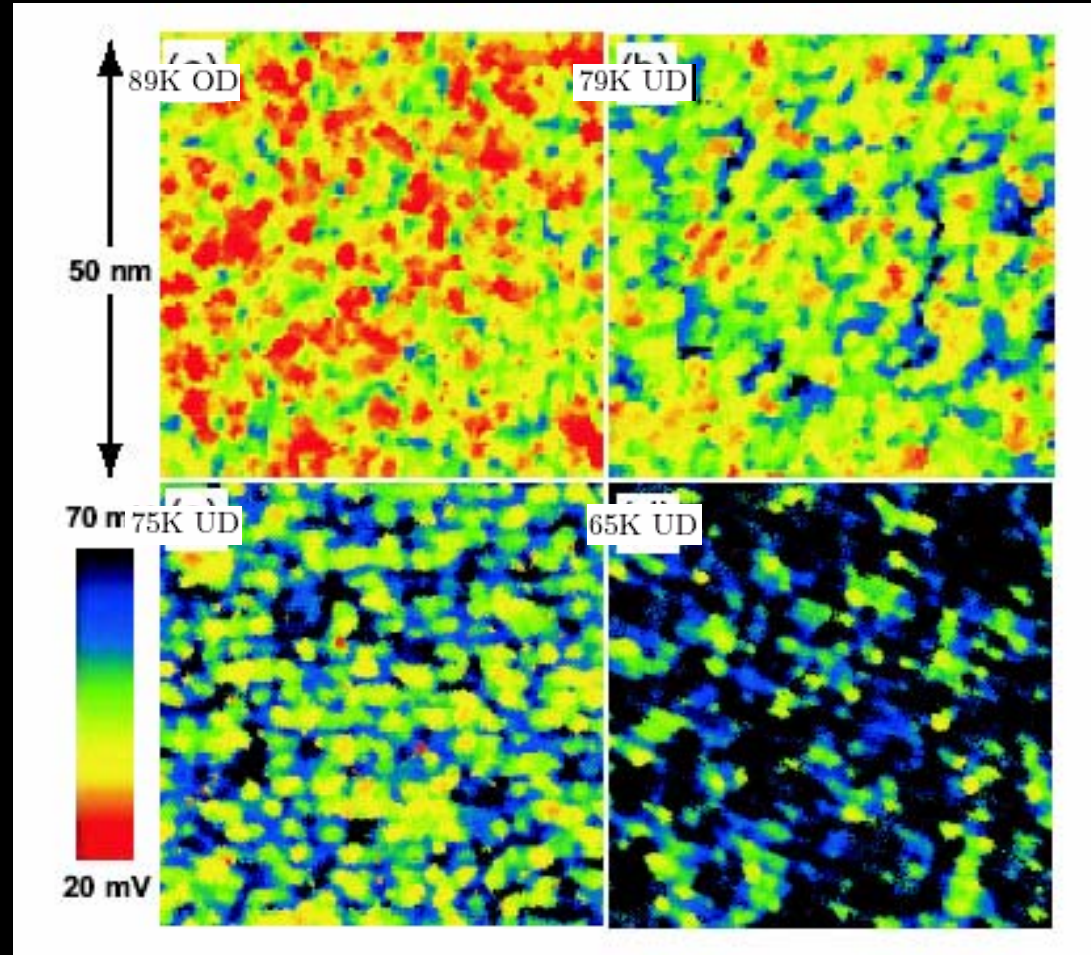
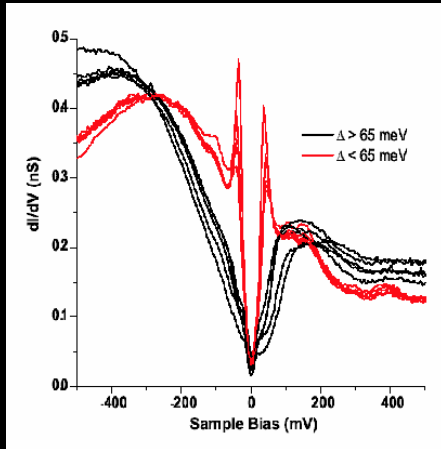
Anderson, Science (86), Kotliar & Liu PRB (88), Suzumura et al, J. Phys. Soc. Jpn. (88), Anderson *et al*, J. Phys. Cond. Mat. (04), Randeria *et al*/Cond-mat/0412096

Reality



The coupling of nodal and antinodal  
excitations to disorder

# Bi-2212 Gap inhomogeneity

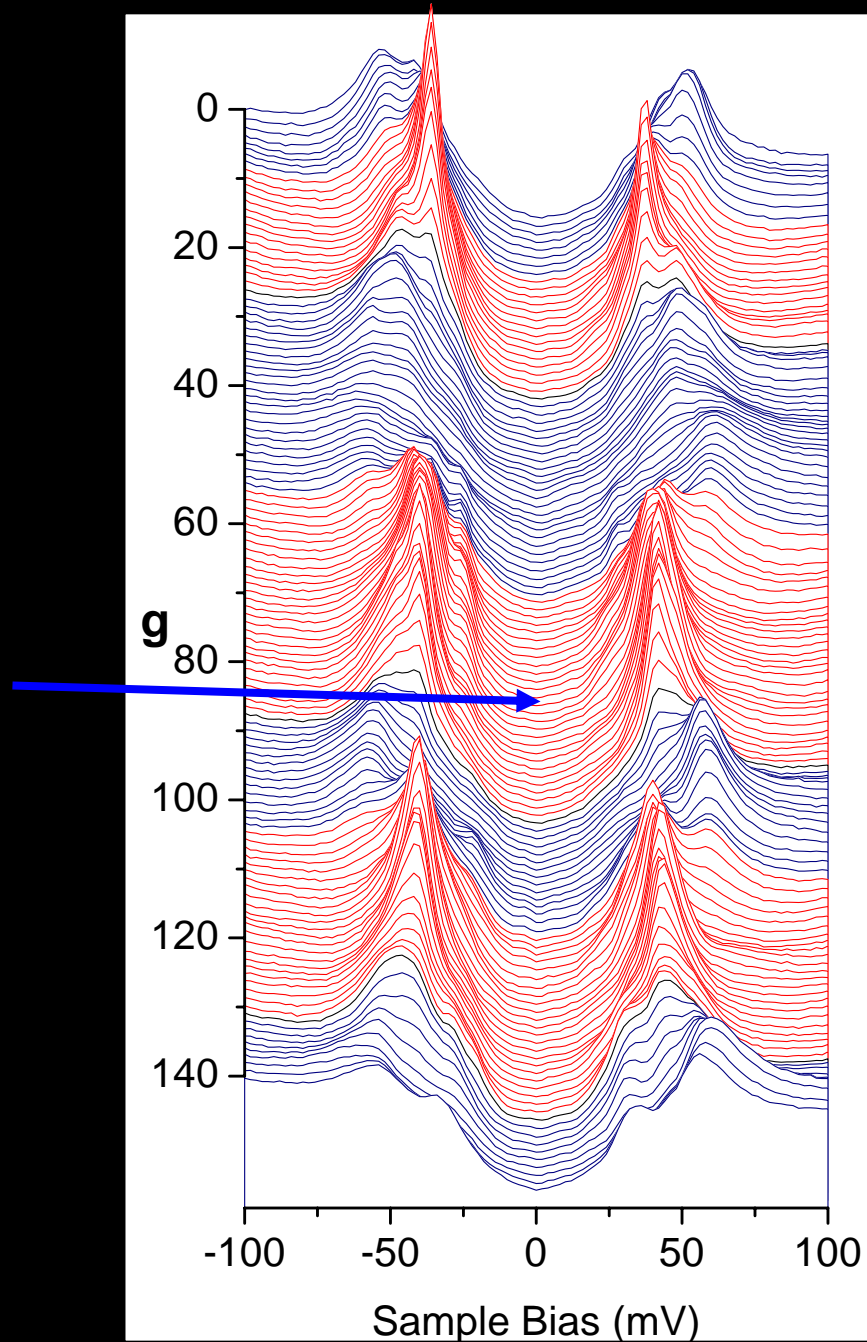


Liu et al, *PRL* (91)  
Chang et al, *PRB* (92). Howald  
*et al.*, *PRB* (01). Cren et al,  
*Eu.Phys.Lett.* (01)  
Matsuda *et al.* *J. Chem. Phys.*  
*Solids* (01).  
Pan et al, *Nature* (01).  
Lang et al, *Nature* (02).  
McElroy et al, *cond-mat*  
0404005, 0406491.

Bi-2212  $T_c = 75\text{K}$

homogeneous sub-gap  
conductance

Howald *et al.*, *PRB* (01).  
Pan *et al.*, *Nature* (01).  
Lang *et al.*, *Nature* (02)

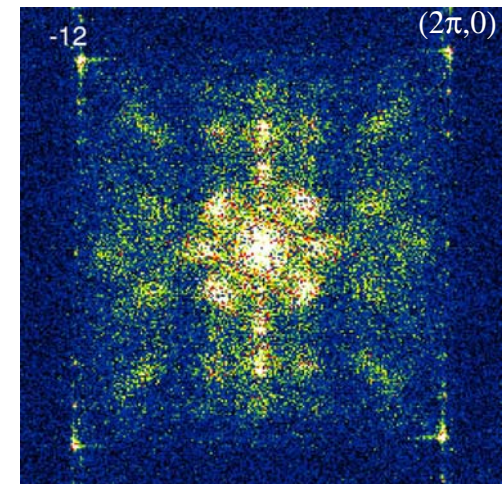
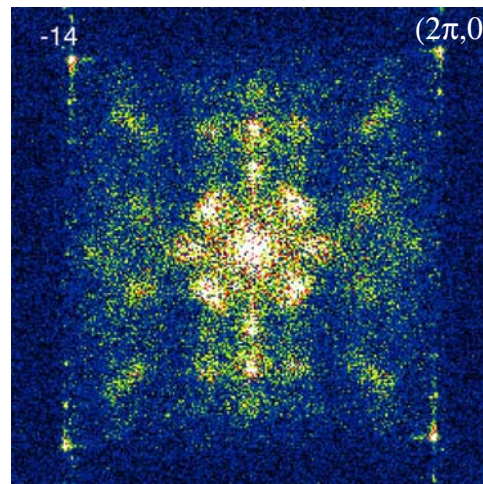
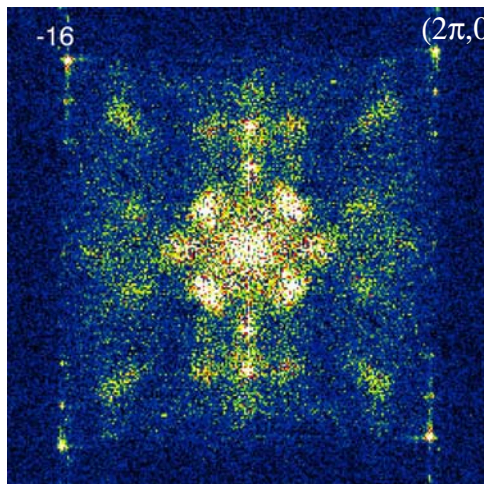
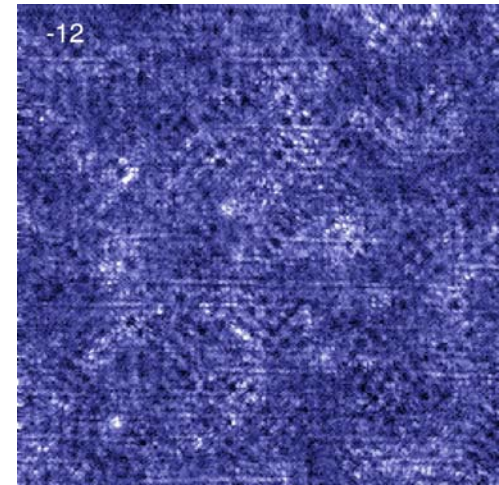
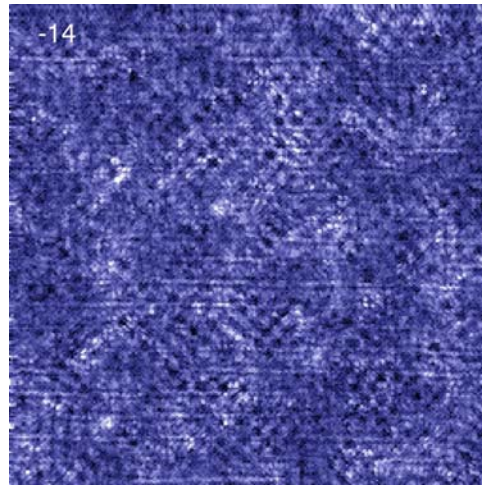
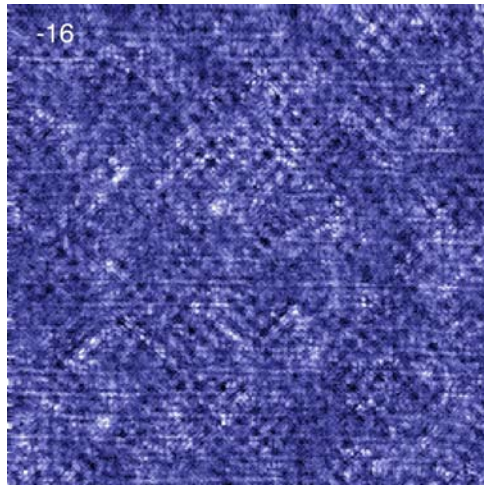


# Quasiparticle interference

Bi-2212

$T_c = 76\text{K}$

Measured @ 4.2 K



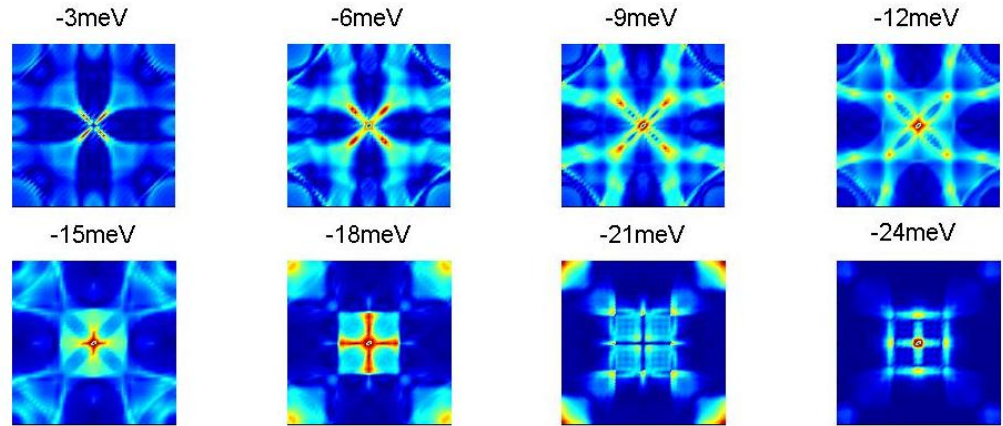
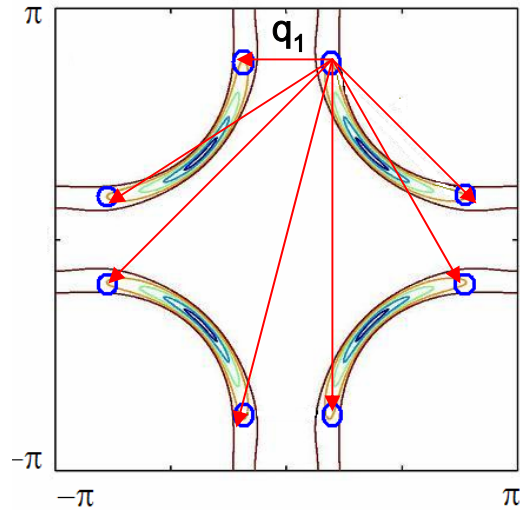
1. Exists for *subgap* energies.
2. Peak positions change with bias voltage.

Hoffman *et al*, *Science* (2002)

McElroy *et al*, *Nature* (2003)

# The quasiparticle interference model

A toy model: Wang, Lee PRB (03)



$$\text{LDOS} \sim |\Psi_1 + \Psi_2 + \dots + \Psi_8|^2$$

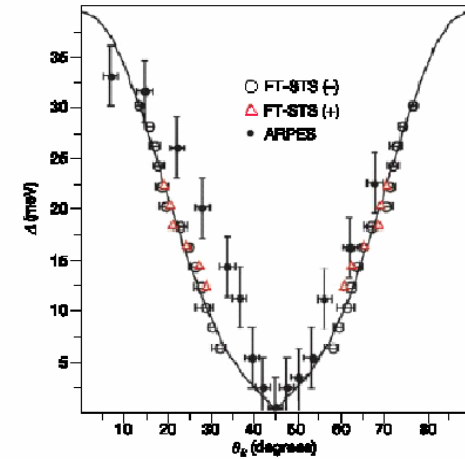
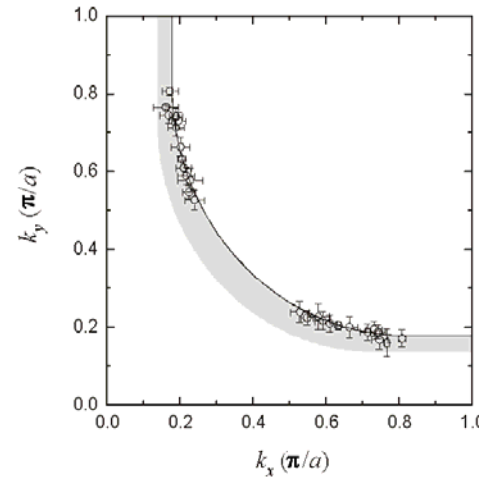
32 different vectors

Problem:  $q_1$  modulation at low bias is too weak.

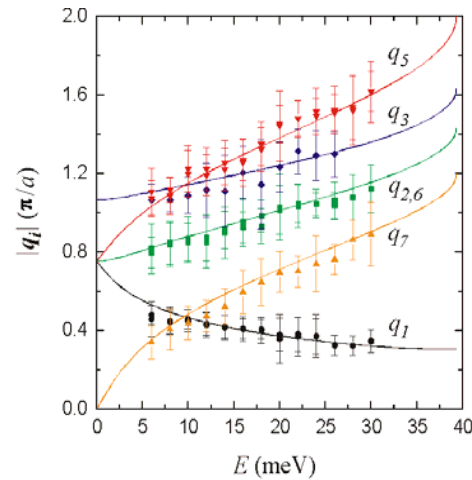
# The Octet model

Hoffman et al, Science (2002)  
McElroy et al, Nature (2003)

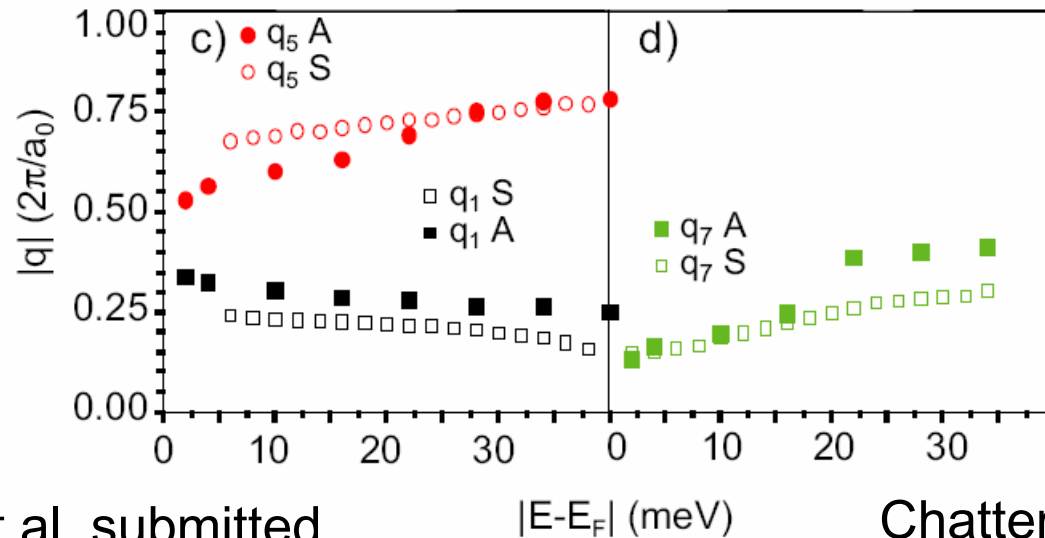
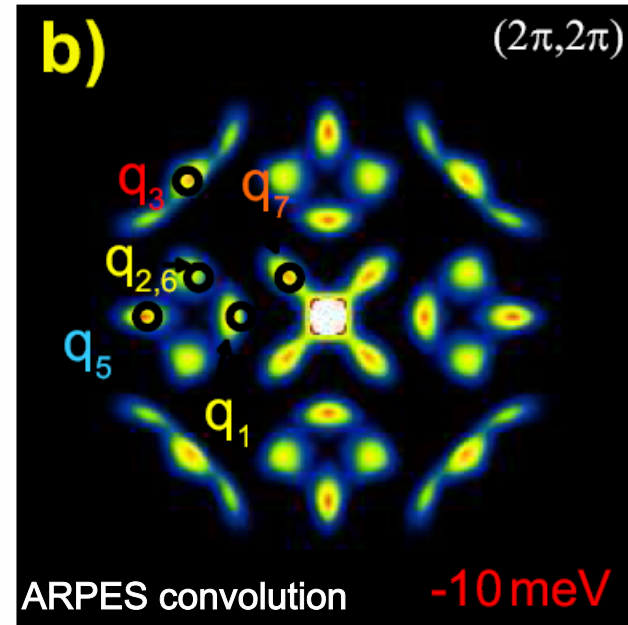
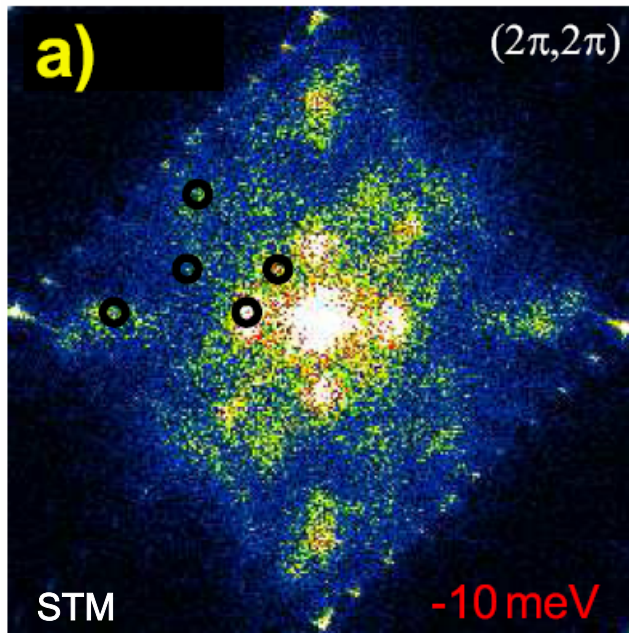
Fit data to model  $\rightarrow$



Quality of the (*extremely over-constrained*) fit



# Comparison between FTSTS and convolution of ARPES spectra



McElroy et al, submitted

$|E-E_F|$  (meV)

Chatterjee et al, submitted

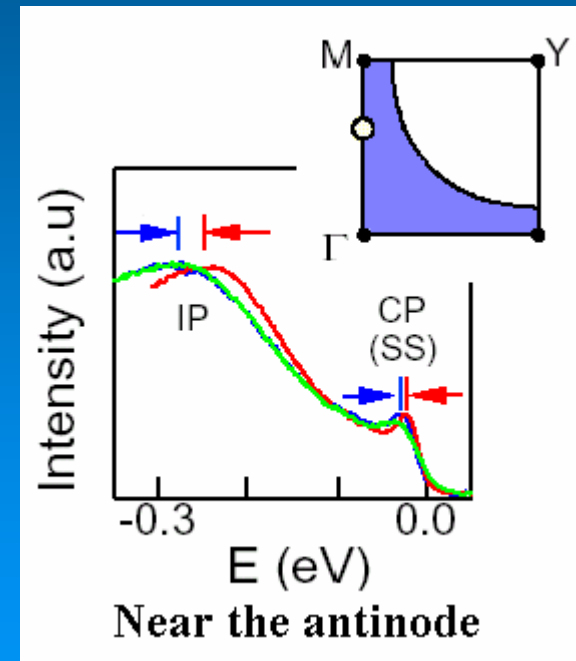
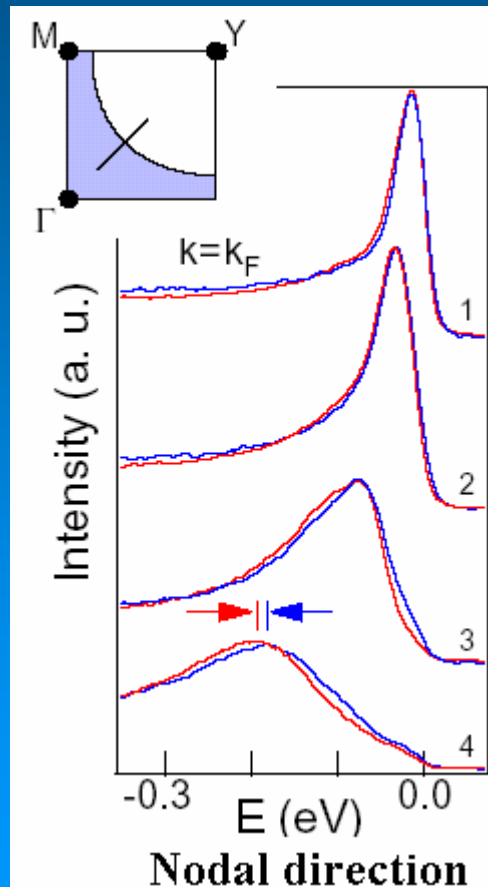


# The coupling of N/AN excitations to lattice vibration

# Nodal and antinodal excitations couple to lattice differently

Isotope dependence Bi-2212,  $T_c = 90$  K

Measured @ 25K

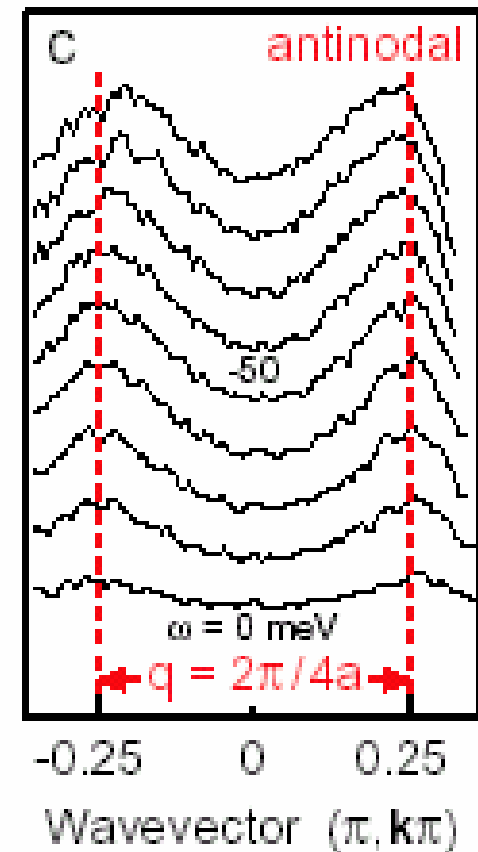
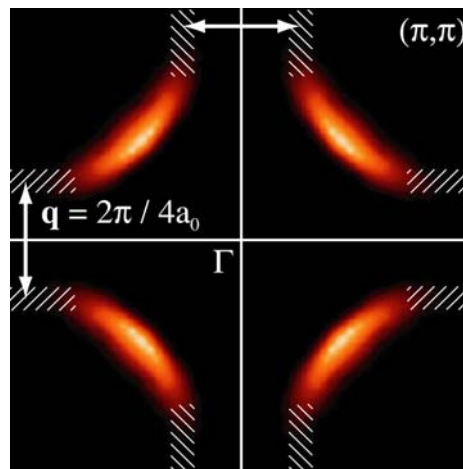
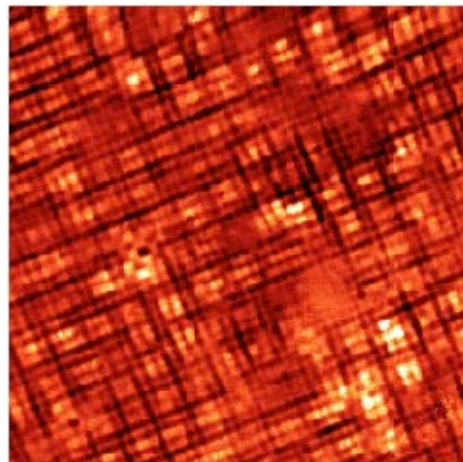
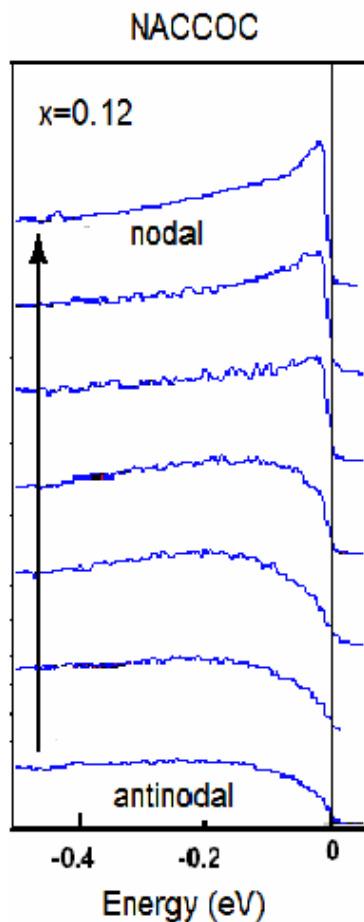


Gweon *et al*, *Nature* (04)

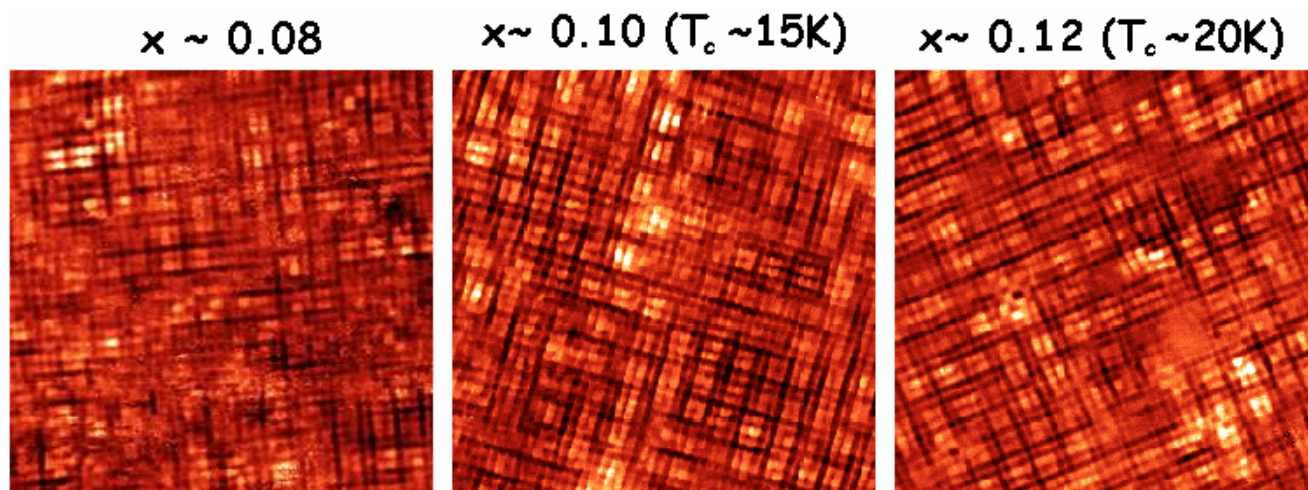
The coupling of N/AN excitations to  
charge order

# ARPES of checkerboard ordered $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$

K. Shen *et al* Science (04).



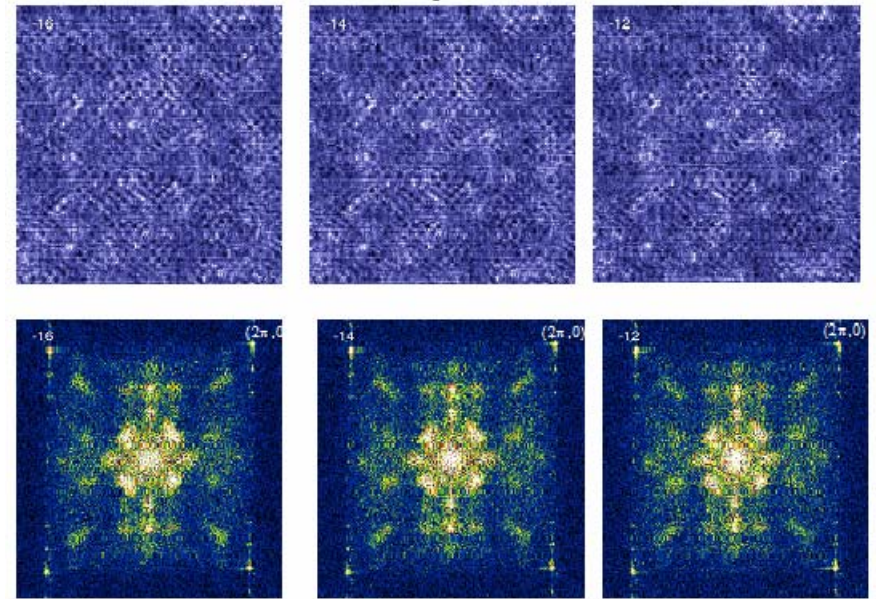
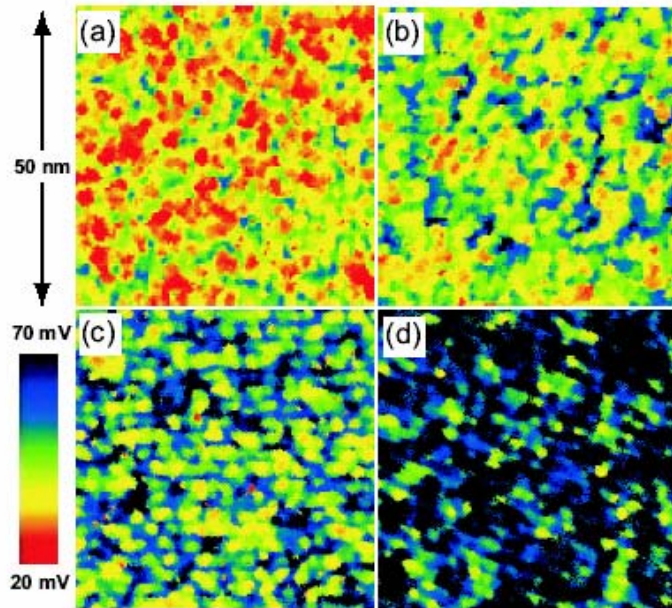
Nodal quasiparticle excitations coexists with charge order. Clearly, we do not have a simple charge insulator.



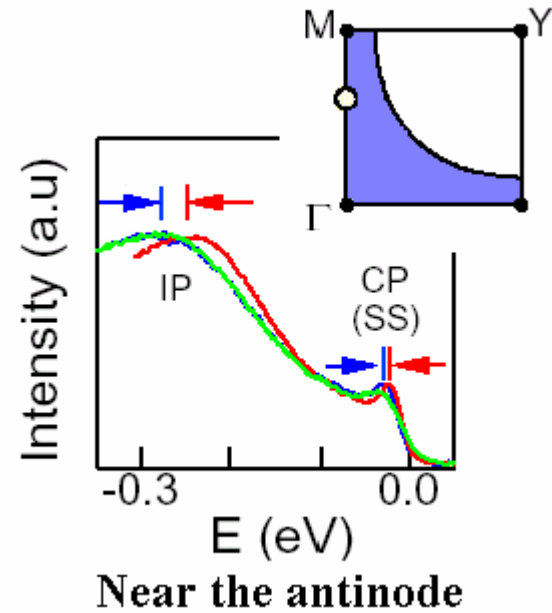
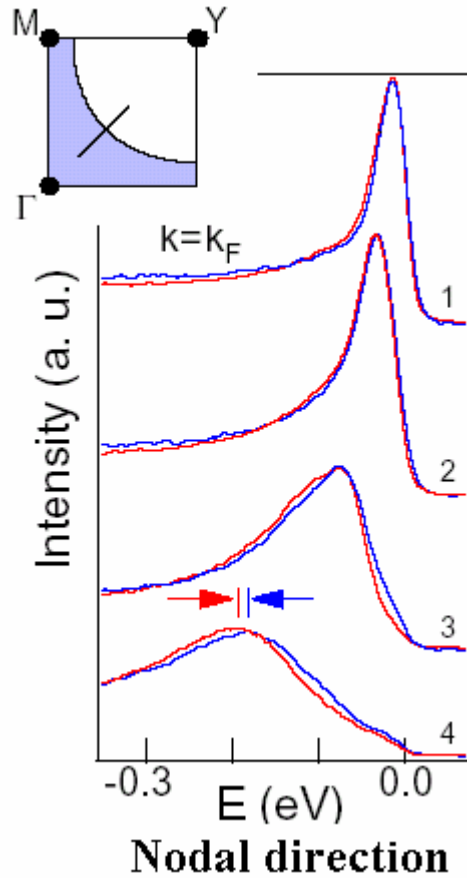
The same periodic pattern is seen for a range of doping  
→ lattice pinning plays an important role.

# Summary

# Effect of (oxygen dopant) disorder

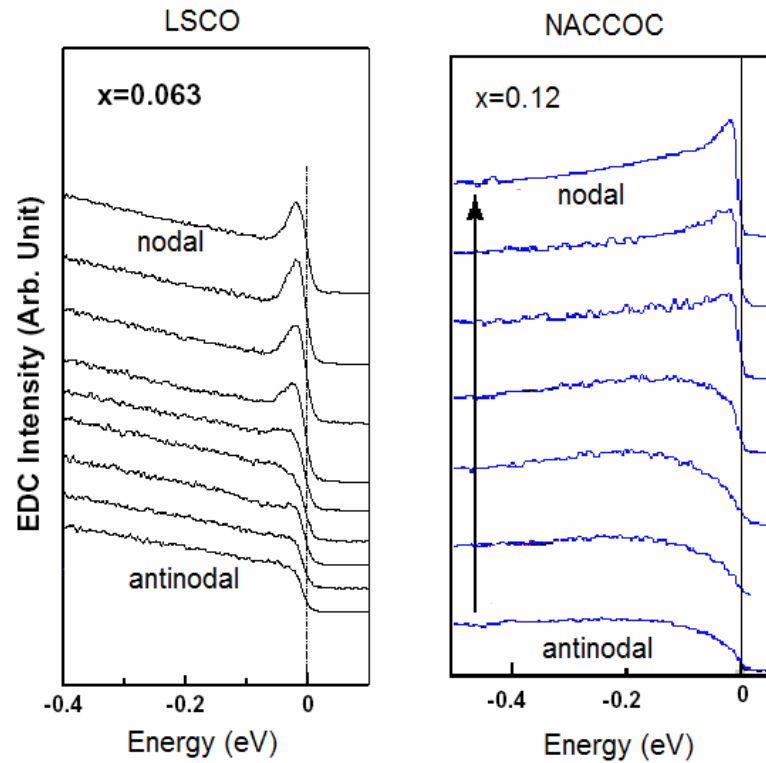


# Effect of lattice vibration



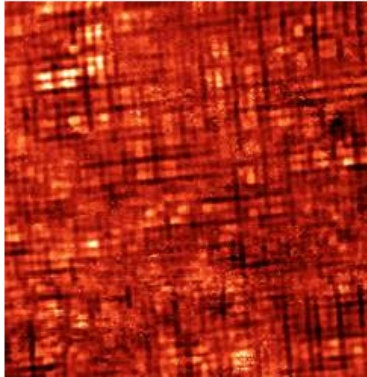


# The nodal-antinodal dichotomy in ARPES spectra.

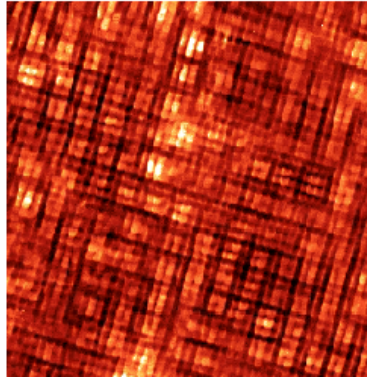


# Coupling to charge order

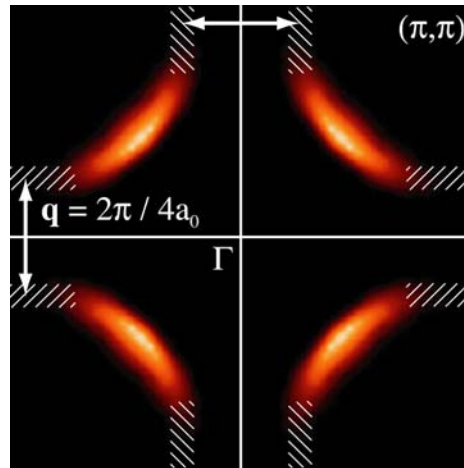
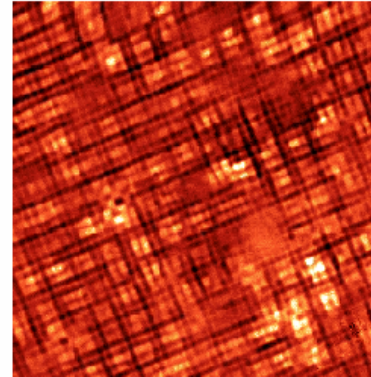
$x \sim 0.08$



$x \sim 0.10$  ( $T_c \sim 15\text{K}$ )

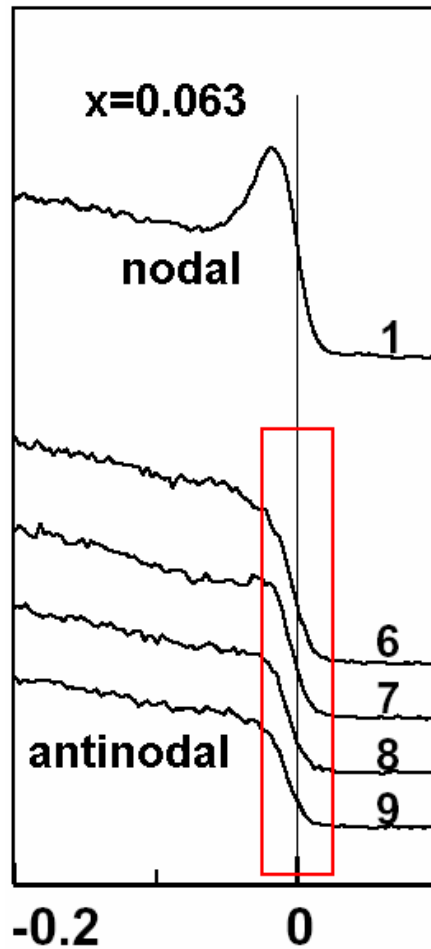


$x \sim 0.12$  ( $T_c \sim 20\text{K}$ )



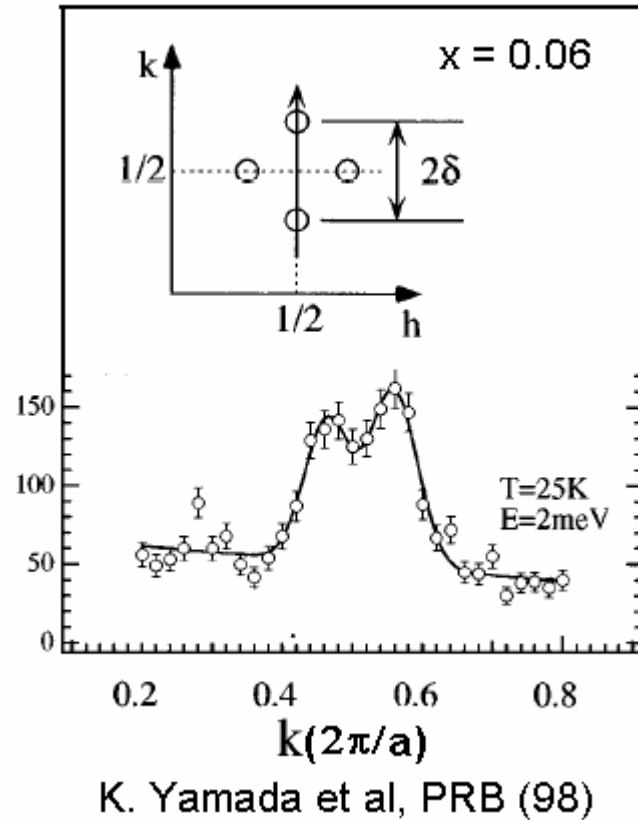
# Theoretical discussions

What causes the antinodal decoherence ?  
Why is the pseudogap so small ?

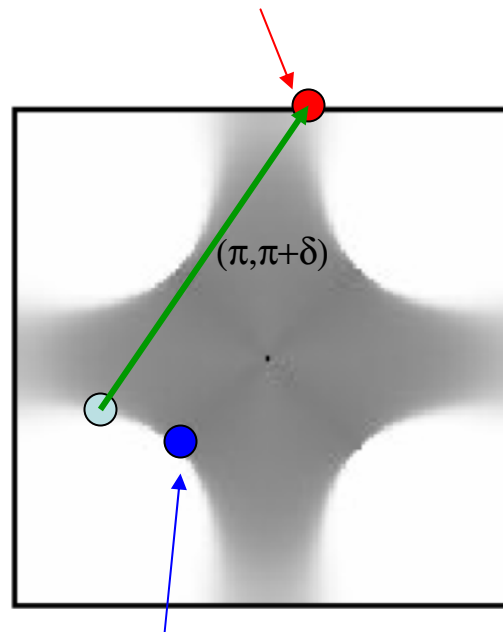


# The cause of antinodal (single-particle) decoherence

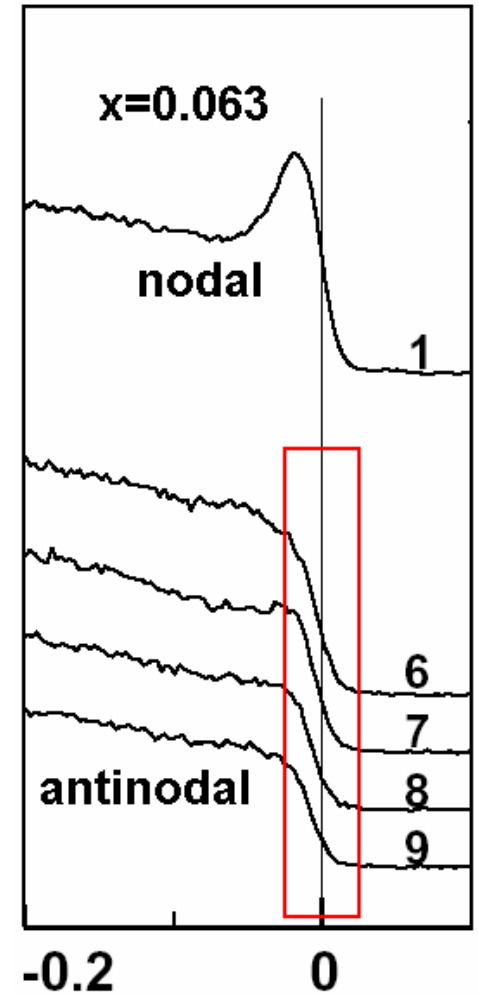
The existence of low-energy incommensurate spin excitations.



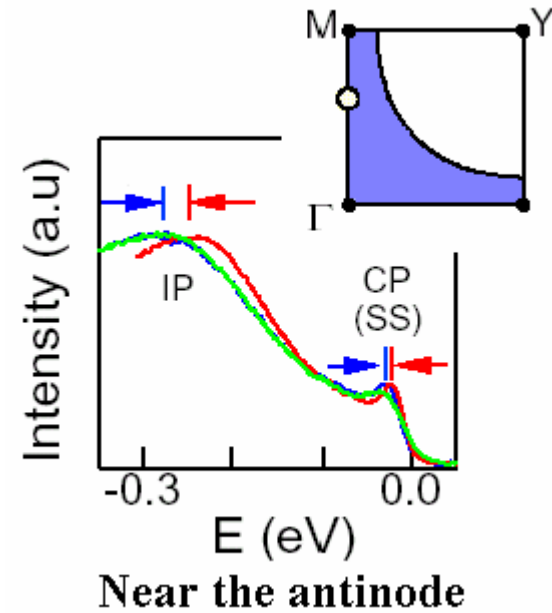
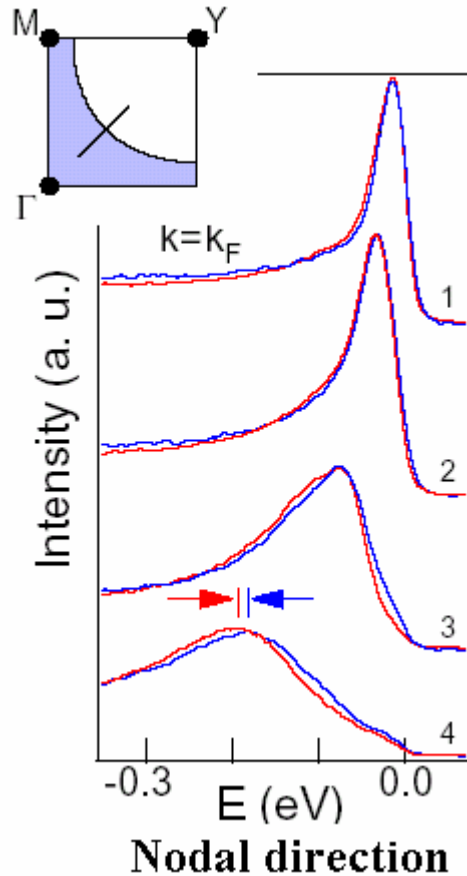
Lowest E excitation is Multi-particle-like



Lowest E excitation = quasiparticle

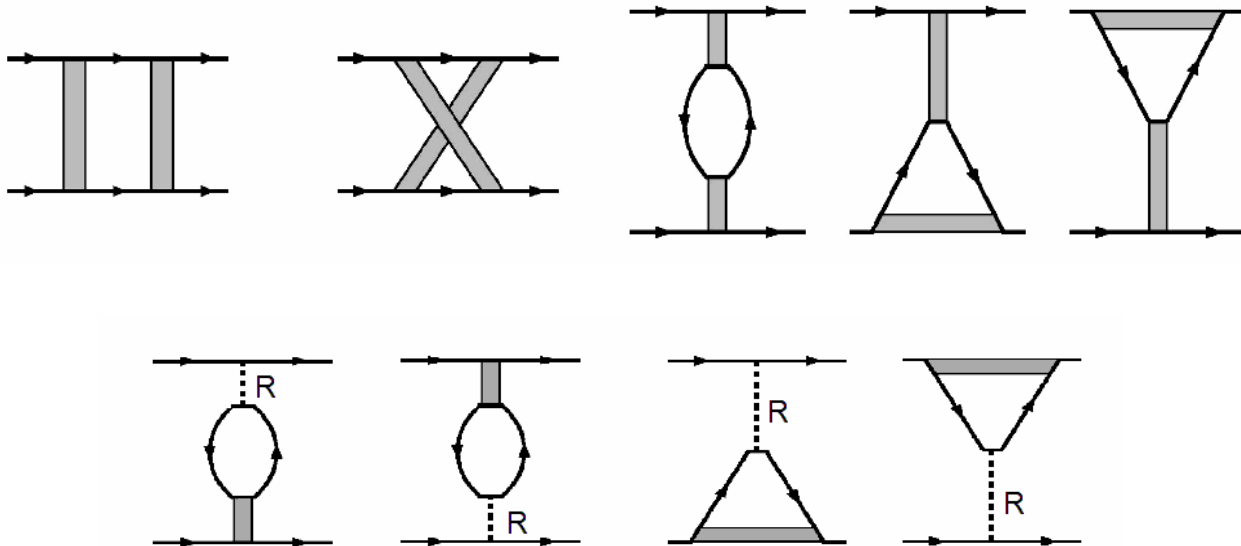


Why is the electron-phonon coupling stronger for antinodal excitations ?



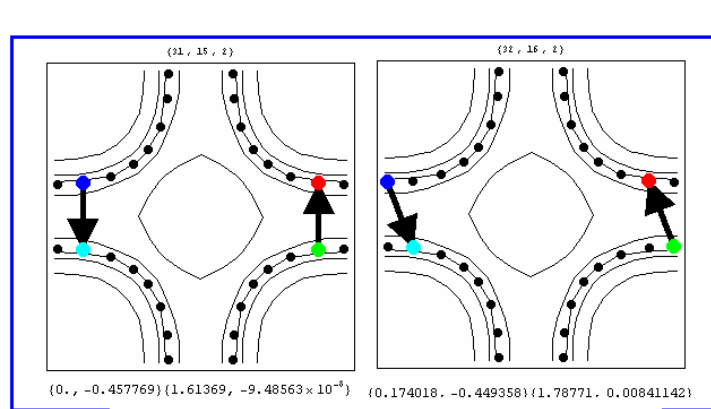
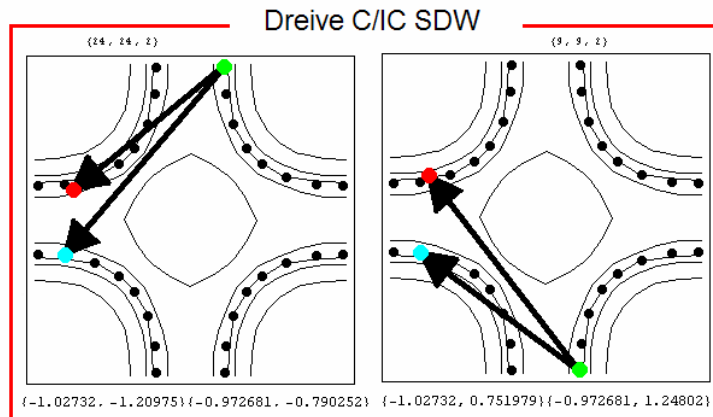
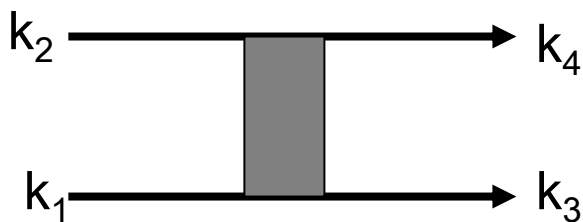
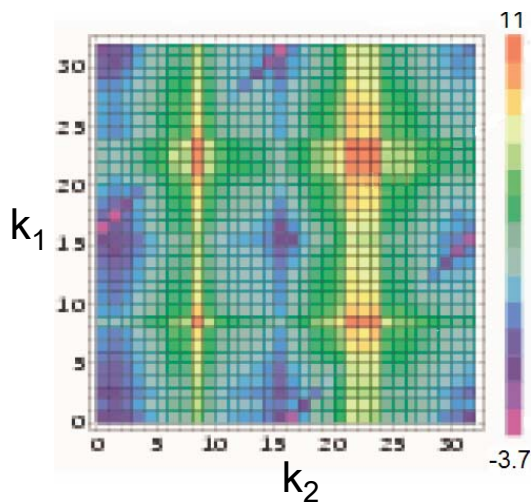
# One-Loop renormalization group study

$$H = \sum_{ij\sigma} t_{ij} [c_{i\sigma}^\dagger c_{j\sigma} + h.c.] + U \sum_i n_{i\uparrow} n_{i\downarrow} + \text{coupling to phonons}$$

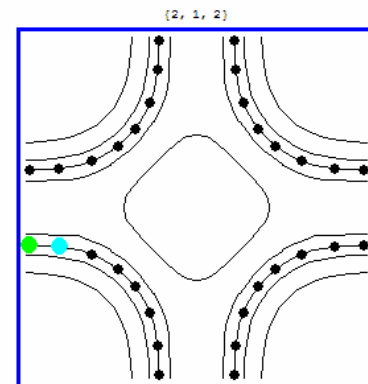


# Electron-electron interaction

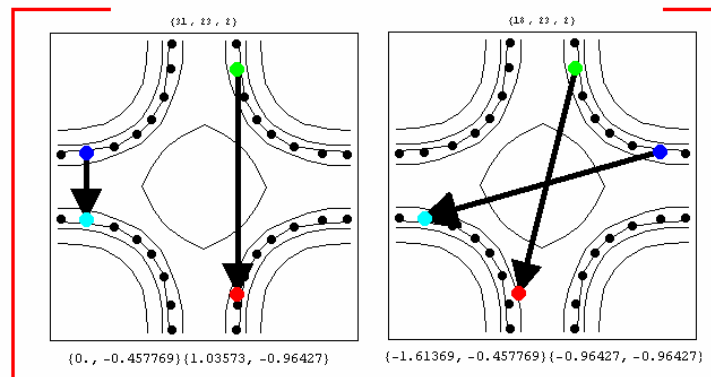
Honerkamp *et al*, *PRB* (2003)



Drive C/IC SDW, dSC and dCDW



Drive the Pomeranchuk instability



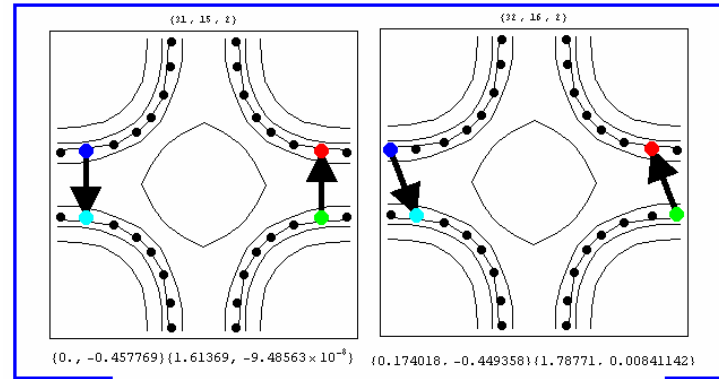
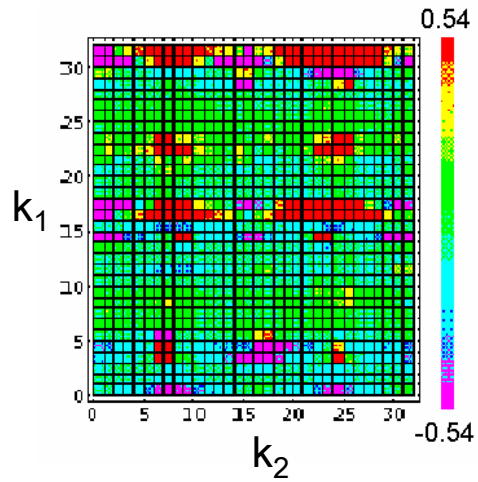
dCDW order parameter

$$\sum_{\mathbf{k}\sigma} (\cos k_x - \cos k_y) c_{\mathbf{k}+\mathbf{q}\sigma}^+ c_{\mathbf{k}\sigma}$$

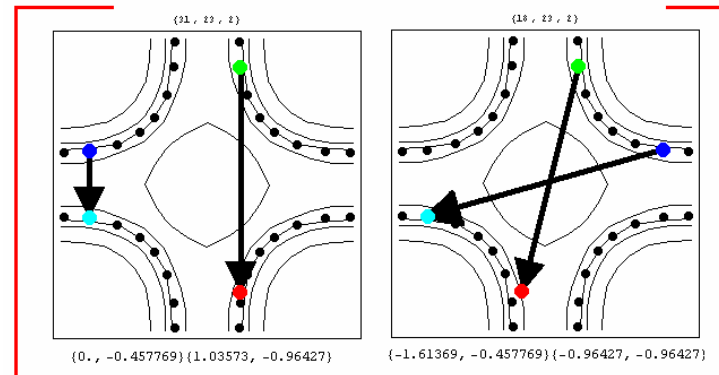


# Retarded coupling

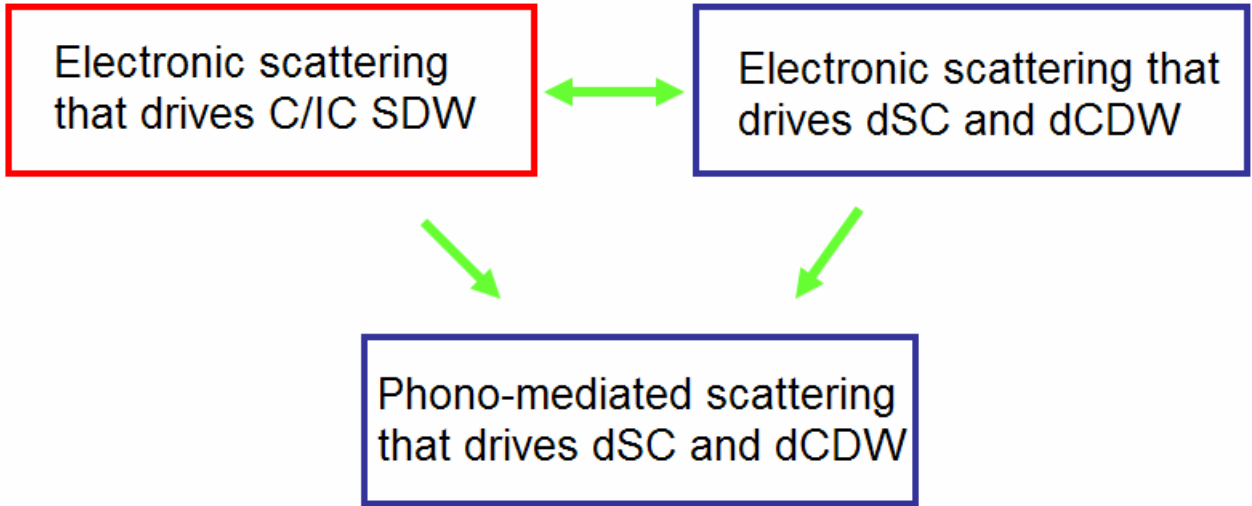
Fu *et al*, to be submitted



Drive C/IC SDW, dSC and dCDW

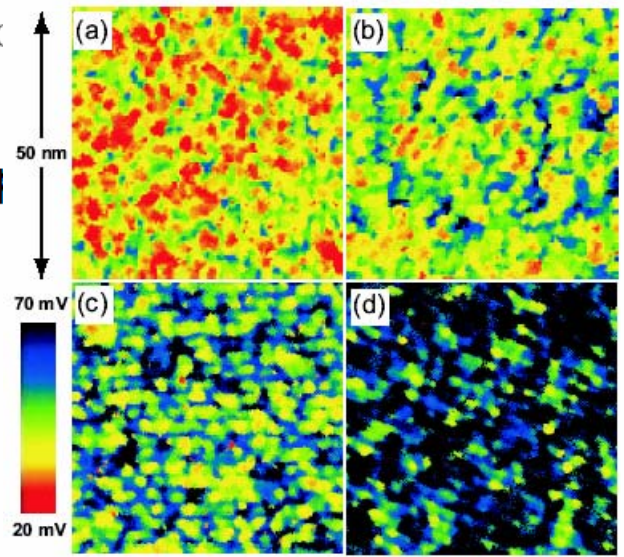
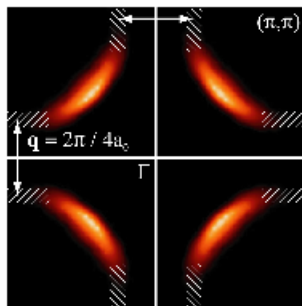


# Growing antinodal scattering processes upon RG

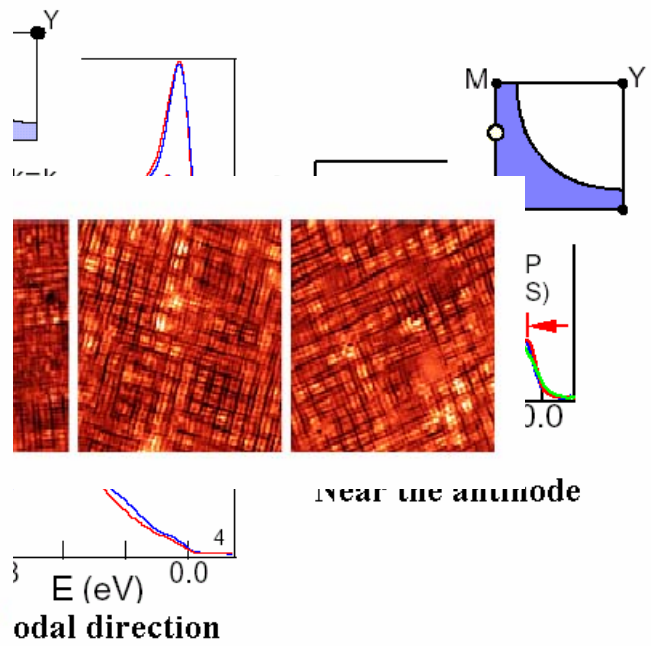


$$dCDW = \sum_{\mathbf{k}\sigma} (\cos k_x - \dots)$$

does not affect nodal  $q_{||}$



Due to local Lattice distortion ?



# Conclusion

