

Nanostructures and molecular devices

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Image: J.W. Ciszek



Outline

- Preliminaries and background
- 2-terminal single-molecule measurements
- Single-electron devices Single-molecule transistors vs. semiconductor dots
- Inelastic processes
- Kondo physics nanostructures for quantum impurity problems
- Noise
- Optics in the mix

Themes: Model systems for quantum impurities + nonequilibrium response



Semiconductor quantum dots (gate-defined)



Semiconductor QD (nanocrystals)



Schoenenberger, Basel





Gudiksen et al., Nano Lett., 5, 2257 (2005)



Semiconductor QD (nanowires)



Lu et al., PNAS 102, 10046 (2005)



Doh et al., Science 309, 272 (2005)



Carbon nanotubes

Schoenenberger group, Basel



Molecular junctions (large area)



Preiner and Mellosh, APL 92, 213301 (2008)

Single-molecule junctions (2 terminal)





0

Dadosh et al., Nature **436**, 677 (2005).



Single-molecule transistor (3 terminal)



Liang et al., Nature **417**, 725 (2002).



Albrecht *et al.*, Nano Lett. **5**, 1451 (2005)



Champagne et al., NL 5, 305 (2005).



Chen et al., Nano Lett. 5, 503 (2005)



Single-atom transistor (3 terminal)



Sellier et al., PRL 97, 206805 (2006)

Transport measurements have been made through individual dopant atoms.



Energy scales – quantum confinement

- Confined electrons can only have certain energies.
- Smaller system = larger energy spacing of allowed states.



- This matters when energy intervals are big compared to available energies (e.g. eV or $k_{\rm B}T$).
- For (3 nm)³ of sodium, level spacing $\Delta E \sim 3 \text{ meV} \sim 35 \text{ K}$
- For 1-2 nm molecule, $\Delta E \sim 100 \text{ meV} \sim 1160 \text{ K}$
- Important at room temperature for electrons in small molecules!



- A great "miracle" of condensed matter physics: often we can get away with ignoring electron-electron interactions.
- Classically, capacitive charging. (A simplifying approximation!)



Can make systems where charging energy is larger than $k_{\rm B}T$. Room temperature $\rightarrow C \sim 3 \times 10^{-18}$ F. For vacuum, $\rightarrow a \sim 28$ nm



- Coupling a quantum system w/ the "outside world" perturbs states.
- Shift of energy levels + lifetime broadening



• Characteristic energy scale = $\Gamma = \hbar/\tau$



Acoustic phonons – gapless!



Typical sound speed ~ 8 km/s (Si), 5 km/s (GaAs) Energy = $h c_s / \lambda$

For λ = 100 nm, energy in Si = 0.3 meV

Timescale ~ 10⁻¹² s

• Optical phonons – tens of meV. Ex.: Gold optical phonon ~ 11 meV.



Local (within a unit cell) motion for k = 0.

Similar energy scale for local molecular vibrations





35 meV



- Consequence of Coulomb interaction.
- Aligning spin lowers overall energy by forcing electrons to stay far apart.
- "Hund's rule"
- Can be very important in transition metal atoms.



In GaAs dots, e.g., exchange effects are typically smaller (fractions of a meV).



Energy scales – crystal/ligand fields



Interactions w/ neighboring atoms break degeneracy of singleelectron orbitals.

Splittings ~ 0.1 eV.

Not relevant in semiconductor/nanotube dots.



Energy scales – valley splittings



In semiconductors, conduction band often has valley degeneracy.

Degeneracy may be split by strain, interface effects ~ meV scale.



Energy scales





Energy scales

D. Berman, PhD thesis, MIT (1998)



Goldhaber-Gordon et al., Nature 391, 156 (1998)





Single-molecule transistor

Aluminum SET

 $\Delta \sim 5.9 \times 10^{-8} \text{ eV}$ $E_c \sim 4 \times 10^{-4} \text{ eV}$ GaAs/AlGaAs SET $\Delta \sim 4 \times 10^{-4} \text{ eV}$ $E_c \sim 2 \times 10^{-3} \text{ eV}$

 $\Delta > 0.1 \,\mathrm{eV}$ $E_c > 0.1 \,\mathrm{eV}$



Transport regimes

Strong coupling (coherent)

 $\Gamma > \Delta$

Landauer-Buttiker

Best to think about electronic states that span from one lead to the other, through the device.



From van Wees, Groningen



"Weak" coupling (coherent)

- Single barrier
- Off-resonant transport
- Conductance (per channel)
 2e²/h



- Transmission exponentially suppressed with length and barrier height
- Most relevant these days in molecular devices (back to this in a couple of slides!).
- Some subtle issues at work screening, timescales.
- (Charging effects = dynamical Coulomb blockade)



Transport regimes

"Weak" coupling

- Two barriers
- Sequential vs. resonant tunneling
- Coulomb charging very important!



- Gate electrode can discrete shift level spectrum relative to source and drain
- Relevant in semiconductor structures + some molecular junctions.



Transport – what can happen?



- "Hot" electrons in the metal leads.
- Molecular vibrations.
- Vibrations in the electrodes.
- Electronic transitions in the molecule
- Chemical reactions
- Quantum entanglement.



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Transport – importance of coherence



τ = transmission probabilityfor each barrier, individually

Sequential tunneling:

Conductance ~ $\tau \times \tau$

Resonant tunneling:

Conductance ~ 1 (consequence of constructive interference)



Temperature:

down to 4.2-1.6 K easily (LHe)300 mK (3He refrigerators)~ 50 mK (dilution refrigerator)

Challenges:

Cooling the electrons. Measuring the temperature.

Frequency:

DC to tens of kHz – standard for V and I

measurements

100 kHz-hundreds of MHz – "RF" GHz and higher – microwave Challenges:

Noise vs. bandwidth. Impedance matching.

Voltage:

pV to V; supplies via programmable source, fn gen, batteries + op-amps Detection via amplifiers (differential; single-ended) Tradeoff: noise, input impedance

Current:

fA to A; supplies via programmable source (can be V + series R)Detection usually via transimpedance amplifiers (not differential)Tradeoff: noise, input impedance, output impedance



Lock-in amplifier

Lock-in amplifiers allow us to recover small (known ω) ac signals from noise at other ω .



A lock-in amplifier multiplies the two sinusoids, and then low-pass filters to get rid of ac components.

$$V_{\rm psd} = V_{\rm sig} V_{\rm L} \sin(\omega_0 t + \phi_{\rm sig}) \sin(\omega_{\rm L} t + \phi_{\rm ref})$$

= (1/2) $V_{\rm sig} V_{\rm L} \cos([\omega_0 - \omega_{\rm L}]t + \phi_{\rm sig} - \phi_{\rm ref})$
- (1/2) $V_{\rm sig} V_{\rm L} \cos([\omega_0 + \omega_{\rm L}]t + \phi_{\rm sig} + \phi_{\rm ref})$

DC only: $V_{\rm psd} = (1/2)V_{\rm sig}V_{\rm L}\cos(\phi_{\rm sig}-\phi_{\rm ref})$



Measuring conductance





Atomic-scale contacts

Simplest nano"device": atomic-scale metal contact.

Make by breaking a wire.

I-V essentially linear, but preferred values of conductance show up.



From van Wees, Groningen





People had seen something similar in semiconductor structures:



- How much can a single electronic mode conduct?
- Conductance is *quantized*.
- A single, perfect electronic channel has conductance $2e^2/h$.



Van Wees et al., PRL 60, 848 (1988)



Consider two macroscopic leads, connected by small number of quantum "channels".

(EM analogy: big cavities connected by piece of waveguide) Assumes noninteracting, independent particles, no inelastic scattering.



Landauer (1959) did general case:



 $G = \frac{e^2}{h} \sum_{i,\sigma} \tau_{i,\sigma}$ Here $\tau_{i,\sigma}$ is the transmission probability for the *i*th channel, spin σ .



Atomic-scale contacts

Landauer formula is *suggestive*, but is it really applicable here?

What about chemistry? Are peaks in histogram just signs of particular atomic configurations?



From van Wees, Groningen



How can we tell? *Noise!*







What do we want to know here?

- Is this simple effective barrier picture valid?
- Can we infer the barrier height from measurements?
- Are the carriers "electron"-like or "hole"-like?



General thinking: $G = G_* \exp(-\beta L)$, where G_* is related to the molecule-metal contact, and β is the decay constant,

 $\beta = \sqrt{\frac{2m\varphi_B}{h^2}}$ for *e*-like carriers at the Fermi level.

Things we can measure:

Conductance (low-bias) for transmission coefficient; higher bias to infer barrier heights, etc.; length-dep?





Venkataraman et al., Nano Lett. 6, 458 (2006)

- Conductance decreases exponentially with length of molecule (effective barrier picture), decay constant = β .
- With appropriate end groups (-NH₂ here), well-defined peak in conductance histograms are obtained.
- Extrapolation to zero length should tell us something about the contacts and the matrix element there.





Venkataraman et al., Nature 442, 904 (2006)

- Can fix the end groups and vary the molecule.
- Here, looking at effect of breaking the molecular "conjugation" by varying degrees.



- Conjugated molecules (polyphenylenes) have a smaller decay constant that saturated molecules (alkanes).
- Consistent with conjugated molecules having smaller
 HOMO-LUMO gaps, and therefore smaller barrier heights.
- With appropriate quantum chemistry calculations, theory captures trends well.



Hybertsen et al., J. Phys.: Condens. Matter 20, 374115 (2008)

Very crude effective barrier model seems to do surprisingly well (near zero bias). Can we learn more?



Transition voltage spectroscopy

Beebe *et al.* suggested a way to infer more information from *I-V* characteristics.



Simmons model of (low bias) tunneling J. G. Simmons, J. Appl. Phys. **34**, 1793 (1963).

$$I = \frac{qA}{4\pi^2\hbar d^2} \left(\left(\phi - \frac{qV}{2}\right) \exp\left(-\frac{2d\sqrt{2m_e}}{\hbar}\sqrt{\phi - \frac{qV}{2}}\right) - \left(\phi + \frac{qV}{2}\right) \exp\left(-\frac{2d\sqrt{2m_e}}{\hbar}\sqrt{\phi + \frac{qV}{2}}\right) \right)$$

.ow bias limit:
$$I \propto V \exp\left(-\frac{2d\sqrt{2m_e\phi}}{\hbar}\right)$$

 $\ln\left(\frac{I}{V^2}\right) \propto \ln\left(\frac{I}{V}\right) - \frac{2d\sqrt{2m_e\phi}}{\hbar}$

Beebe et al., PRL 97, 026801 (2006)



Transition voltage spectroscopy

At high bias, crossover to Fowler-Nordheim tunneling.

Effective triangular barrier, tuned by bias.

$$I \propto V^2 \exp\left(-\frac{4d\sqrt{2m_e\phi^3}}{3\hbar qV}\right)$$
$$\ln\left(\frac{I}{V^2}\right) \propto -\frac{4d\sqrt{2m_e\phi^3}}{3\hbar q}\left(\frac{1}{V}\right)$$

V



Idea: Plotting data as $\ln(I/V^2)$ vs. (1/V) should show the crossover, at a voltage V_{trans} that should be related to ϕ .

Beebe et al., PRL 97, 026801 (2006)


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Beebe et al., PRL 97, 026801 (2006)



Transition voltage spectroscopy





- Electron-electron interactions can dominate transport properties.
- $\Delta =$ single-particle level spacing, lowest energy of e-h excitation
- *E*_c = Coulomb charging energy (constant interaction model)





- Data usually presented as *differential conductance*.
- Can overcome blockade with source-drain bias.





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- $\Delta =$ single-particle level spacing, lowest energy of e-h excitation
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Weak coupling limit: No current flows unless bias is sufficient to bring level into alignment.

"Coulomb blockade"



In metal islands + early semiconductor dots, E_c dominates – hence the name.



Single-electron devices – Stability diagrams



Depending on gate + source-drain bias, can stabilize different numbers of electrons on the island.



- Data usually presented as *differential conductance*.
- Gate shifts levels, discretely changes avg island charge.





- Data usually presented as *differential conductance*.
- Gate shifts levels, discretely changes avg island charge.





Semiconductor (vertical) dot example





One molecule-specific feature:







35 meV

Vibrational resonances





One molecule-specific feature:

Vibrational resonances





One molecule-specific feature:

Vibrational resonances



Scott and Natelson, ACS Nano 4, 3560 (2010)



One molecule-specific feature:

Vibrational resonances





Qiu et al., PRL 92, 206102 (2004)



Similar signatures in semiconductor dots:



Sellier et al., PRL 97, 206805 (2006)



The Zeeman effect provides a convenient way to track single-particle levels.



Hanson et al., Rev. Mod. Phys. 79, 1217 (2007)

B in plane of 2deg = (nominally) pure Zeeman.

B normal to plane of 2deg = Zeeman + orbital effects (via Aharonov-Bohm phase)



Zeeman + orbital response are a convenient way to track single-particle levels.





Kouwenhoven *et al.*, Science **278**, 1788 (1997).



- In 2nd order, can have virtual transitions.
- Virtual state violates energy conservation....







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- Virtual state violates energy conservation....



- Nonzero conduction in "blockade".
- Physicist: "Elastic cotunneling"
- Chemist: "superexchange"
- This is the **off-resonant** tunneling routinely seen in, *e.g.*, alkyl SAMs.



M. A. Ratner, J. Phys. Chem. 94, 4877-4883 (1990)



Inelastic cotunneling

• Can also have virtual transitions that leave system excited....





• Can also have virtual transitions that leave system excited....





• Can also have virtual transitions that leave molecule excited....



- Inelastic Electron Tunneling Spectroscopy!
- As shown, peak in 2nd derivative.



Inelastic cotunneling – semiconductor dot

GaAs dot embedded in an interferometer (!).

Clear step-like discontinuity in conductance in middle of blockaded regime.



Sigrist *et al.*, PRL **96**, 036804 (2006)



Coherence of the inelastic cotunneling process demonstrated by looking at interference fringes (source-drain conductance vs. external magnetic field while in inelastic cotunneling-dominated regime).



Inelastic electron tunneling spectroscopy (IETS)

• Discovered in 1966: tunneling electrons can vibrationally excite molecules embedded in a tunnel barrier.



Hipps, J. Chem. Phys. 97, 7803 (1997).



Inelastic electron tunneling spectroscopy (IETS)





IETS challenges

Challenges:

- Data acquisition can be slow.
- Signals generally weak....
- Most big vibrational features at quite high energies.
- Broadening of lines is significant (~ 5.4 $k_{\rm B}T$, + 1.22 $V_{\rm ac}$). •
- Line shapes can be distorted.



Song et al., J. Phys. Chem. C, 114, 20431 (2010)



IETS in SMTs?

• Definitely see features in the blockaded regime that look like inelastic cotunneling.





IETS in SMTs?

• Definitely see features in the blockaded regime that look like inelastic cotunneling.



- Energies are far too low to be electronic excitations.
- Lineshapes aren't simple, and lines shift near electronic levels!





How we make single-molecule devices



- Analogous to STM:
- Conduction dominated by tunneling volume ~ 1 molecule.
- Every device is different!
- Can't "see" what's going on!
- Vibrational fingerprint?





Tunneling conductances depend exponentially on geometry....

Statistical approach and systematic characterization are essential!

- Effects only present in samples with molecules?
- Charging energy and charge states sensible?
- Molecule-specific features?
- Optical measurements! (*new!*)

Example of a potential pitfall: metal blob from breaking process.



20



Many junction configurations are possible!

In general, in electromigrated junctions, we **don't** have the idealized situation.





ρ

- "Standard model" of normal metals: resistivity to *decrease* as *T* decreases.
- Resistivity saturates at low *T* as phonons freeze out.
- Discovered in 1930s that this doesn't work for metals with dilute magnetic impurities.
- Minimum in resistivity at materialdependent temperature scale.





- Perturbative treatment by Kondo (1964).
- Spin-flip scattering leads to *antiferromagnetic exchange* between local spin and conduction electrons.
- Enhanced scattering = increased ρ
- Characteristic temperature scale T_K







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- Perturbative treatment by Kondo (1964).
- Spin-flip scattering leads to *antiferromagnetic exchange* between local spin and conduction electrons.
- Enhanced scattering = increased ρ
- Characteristic temperature scale T_K
 - Ground state: many-body singlet

$$\frac{1}{\sqrt{2}}\left(\left| \phi \phi \right\rangle - \left| \phi \phi \right\rangle \right)$$

T << T_K, ρ becomes constant.




Kondo in single-electron devices

Kondo leads to prominent features in differential conductance.







Kondo in single-electron devices

Kondo leads to prominent features in differential conductance.



- Result is many-body Kondo state.
- In this case, *forward* scattering.



• At *T* = 0, unpaired spin is screened; *resonant conduction* maximized.



Kondo physics – terminology

 Γ = width of localized level, due to coupling with leads.

- In SMT, fixed by geometry.
- In semiconductor dot, tunable.
- Width of Coulomb deg. point at T = 0 sets Γ in units of gate voltage.

ε = difference between localized level and Fermi energy of leads.

• In SMT and semiconductor dots, **tuned** by gate voltage.

U = on-site repulsion, $E_{\rm c}$

$$T_{K} \sim \frac{\sqrt{\Gamma E_{c}}}{2} \exp\left(\frac{-\varepsilon(E_{c}-\varepsilon)}{\Gamma E_{c}}\right)$$





- Enhanced density of states at Fermi level of leads.
- Peak in conductance near zero bias

Two ways of extracting $T_{\rm K}$:

$$G(T) - G_{\rm b} = \frac{2e^2}{h} \frac{(4\Gamma_{\rm S}\Gamma_{\rm D})}{(\Gamma_{\rm S} + \Gamma_{\rm D})^2} f(T/T_{\rm K})$$
$$f(T/T_{\rm K}) = (1 + (2^{1/s} - 1)(T/T_{\rm K})^2)^{-s}$$
$$s \approx 0.22$$
$$@\ T = T_{\rm K} \ f = 1/2$$

Zero bias resonance FWHM proportional to $k_{\rm B}T_{\rm K}/e$ for $T \ll T_{\rm K}$.

 \mathbf{n}

fwhm =
$$\frac{2}{e}\sqrt{(\pi k_{\rm B}T)^2 + 2(k_{\rm B}T_{\rm K})^2}$$

Maximum $G-G_b = 2e^2/h$ for perfectly symmetric coupling to leads.





Kondo example: GaAs dot





Kondo example: GaAs dot



Can infer T_{κ} from T dependence of zero-bias conductance.

Must be careful, because there can be background conductance unrelated to Kondo physics.



Kondo example: GaAs dot

Finite-bias data contain more information than just the zero-bias conductance.

Challenge: In general, finite bias situation is complicated, nonequilibrium problem.

Interpretation is sometimes simple. e.g., Zeeman effect.

Applied (in-plane) magnetic field suppresses Kondo at zero-bias, splits peak by an amount $2g\mu_B B$.



Goldhaber-Gordon et al., PRL 81, 5225 (1998)



Kondo example: Carbon nanotube



Carbon nanotube case is different.

- "Shells" w/ each hold four electrons (two degenerate K points in nanotube band structure, each can accommodate spin-up + spin-down)
- Still have Kondo for two electrons added! SU(4) Kondo



Kondo in SMTs: C₆₀



Scott et al., PRB 79, 165413 (2009).



Kondo in SMTs: C₆₀



Inelastic tunneling process + Kondo physics.



Kondo in SMTs: C₆₀



Kondo resonance combined with ~ 35 meV parallel resonance.

Inelastic tunneling process + Kondo physics.



Inelastic satellites and Kondo



Photon (rather than phonon) Kondo sidebands are visible in GaAs dots in Kondo regime.

Active topic: how does dissipation affect Kondo state?



Kondo in transition metal complexes

Can deliberately get Kondo physics by working with molecules that contain unpaired electrons.





$$T_{K} \sim \frac{\sqrt{\Gamma E_{c}}}{2} \exp\left(\frac{-\varepsilon(E_{c}-\varepsilon)}{\Gamma E_{c}}\right)$$

(Quadratically) exponentially sensitive to V_{G} when gating away from charge degeneracy!

Confirmed experimentally in GaAs quantum dots.

Goldhaber-Gordon et al., PRL 81, 5225 (1998) 10 (a) T_K (mK) 0.6 0.8 ~e0/1 0= -2 0 2 6 4 $-\epsilon_0/\Gamma$ В 1000 T_{κ} FWHM (mK) 400 -420 -416 -412 -408 -404 424 V_{al} (mV)

Van der Wiel et al., Science 289, 2105 (2000)



Anomalous gate dependence

- $T_{\rm K}$ **not** exponentially dependent on $V_{\rm G}$ in these devices.
- Demonstrates that SMTs have nontrivial many-body physics.



Yu et al., PRL 95, 256803 (2005).



Weak $V_{\rm G}$ dependence seen in past experiments:



Liang et al., Nature **417**, 725 (2002).

Yu and Natelson, Nano Lett 4, 79 (2004).

Not universal – varies from molecule to molecule.



Model Hamiltonian for molecular case

Leads (KE) dot (KE) Constant Gate
interaction coupling

$$H = \sum_{k,\sigma,\alpha\in S,D} \epsilon_{\alpha\sigma}(k) c^{\dagger}_{\alpha k\sigma} c_{\alpha k\sigma} + \sum_{\nu\sigma} \epsilon_{\nu\sigma} d^{\dagger}_{\nu\sigma} d_{\nu\sigma} + E_c N^2 - eV_G N$$

$$N \equiv \sum_{\nu\sigma} d^{\dagger}_{\nu\sigma} d_{\nu\sigma}$$

$$+ \sum_{k,\sigma,\nu,\alpha\in S,D} t_{\nu k\alpha}(\{x_l\}) c^{\dagger}_{\alpha k\sigma} d_{\nu\sigma} + \text{H.c. Dot-lead coupling}$$

$$H_v = \sum_l \hbar \omega_l a^{\dagger}_l a_l, \quad x_l \propto a^{\dagger}_l + a_l \quad \text{local vibrational modes}$$

$$H_{ev} = \sum_{l\nu\sigma} \lambda_{\nu l} x_l \hbar \omega_l d^{\dagger}_{\nu\sigma} d_{\nu\sigma} \quad \text{local vibrational coupling}$$

$$H_{ph} = \sum_q \hbar \Omega_q b^{\dagger}_q b_q \quad H_{v-ph} = \sum_{lq} \beta_{lq} x_l X_q, \quad X_q \propto (b^{\dagger}_q + b_q)$$

$$\text{bulk phonons} \quad \text{local vibration to bulk phonons}$$



Coupling to local vibrational modes = renormalization of energy scales

Anderson-Holstein model

Moderate coupling to local phonon mode leads to renormalized Kondo J: enhanced $T_{\rm K}$, weak gate dependence.



Balsiero et al., PRB 74, 235409 (2006).



Are all Kondo systems (spin ½, SU(2)) created equal?

In truly ideal Kondo dot model, at zero T and zero V, only natural energy scale is $k_{\rm B}T_{\rm K}$.

Makes sense that one should then be able to describe full response *near* that limit in a universal form.

$$\begin{split} \frac{\Delta G(V,T)}{G_0} &= f\left(\frac{eV}{k_{\rm B}T_{\rm K}},\frac{T}{T_{\rm K}}\right)\\ \frac{eV}{k_{\rm B}T_{\rm K}} < 1, \quad \frac{T}{T_{\rm K}} < 1 \end{split}$$



Finite bias Kondo scaling

Universal scaling at finite bias in the Kondo regime is predicted (up to $T \sim 0.1-0.2 T_{\rm K}, eV_{\rm SD} \sim 0.1-0.2 k_{\rm B}T_{\rm K}$).

$$\frac{G(T,0) - G(T,V)}{c_T G_0} = F\left(\frac{T}{T_K}, \frac{eV}{kT_K}\right)$$
$$\approx \alpha \left(\frac{eV}{kT_K}\right)^2 - c_T \gamma \left(\frac{T}{T_K}\right)^2 \left(\frac{eV}{kT_K}\right)^2$$

Tested in GaAs dot, $T_{\rm K} \simeq 240$ mK:



Grobis et al., PRL 100, 246601 (2008)



Finite bias Kondo scaling





Finite bias Kondo scaling

$$\frac{G(T,0) - G(T,V)}{c_T G_0} \approx \alpha \left(\frac{eV}{k_B T_K}\right)^2 - c_T \gamma \left(\frac{T}{T_K}\right)^2 \left(\frac{eV}{k_B T_K}\right)^2$$



- The candidate functional form for scaling does work.
- Very good consistency across devices with wide-ranging $T_{\rm K}$ and asymmetry.
- Systematic difference in our alpha and that seen in GaAs dot.
- Systematic difference in our alpha and theory predictions (~ 0.15 0.3).





Consider a quantum dot coupled to *ferromagnetic leads*.

FM leads can have spin waves.

Usual Kondo: local spin interacts w/ conduction electrons.

Ground state: Kondo singlet (Fermi liquid)

Gate voltage tunes $T_{\rm K}$.

Gate voltage *also tunes* coupling of local moments to spin waves, *g*.

Large enough g: Kondo singlet disrupted.





Idea: As function of V_G , should be able to tune from Kondo to NFL regime. Identify these regimes by T dependence of zero-bias conductance.



Roch et al., Nature 453, 633 (2008)



Singlet (Fermi liquid) to underscreened spin-1 Kondo in C₆₀ SMT.





Unclear: why does gate tune energy of singlet and triplet states this way.



- Semiconductor and molecular junctions can be described by similar language.
- Energy scales are different lots of physics in molecular systems not relevant in quantum dots.
- In general, finite bias = fundamentally nonequilibrium problem.
- Nonequilibrium = nonthermal distributions of electrons + vibrations.
- Good structures for quantum impurity physics; again, molecular physics a bit different.



There is great interest in moving beyond dc transport, in both dots + molecular junctions.

In molecular junctions in particular, great need for further information.

Force measurements @ breaking (inferring effective temperature)



Xu et al., Nano Lett. 6, 1240-1244 (2006)



Reddy et al., Science 315, 1568-1571 (2007)



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Djukic and van Ruitenbeek, Nano Lett. 6, 789-793 (2006)

Optical response



Wu et al., Science 312, 1362-1365 (2006)



Johnson-Nyquist noise

Fluctuation-dissipation theorem \rightarrow noise in *equilibrium* conductors

Johnson + Nyquist (1928)



"White" noise

- $S_I = 4k_BT \cdot G$ A²/Hz (for $f < \sim$ optical freq)
- $S_V = 4k_BT\cdot R$ V²/Hz (for $f < \sim$ optical freq)



Conductance: tells us *average current* under certain voltage bias.

If charge was *continuous*, that would be the end of the story. However, charge comes in discrete lumps....

Theorist fantasy: ordered list of arrival times for each electron.

16:07:23.0000315 16:07:23.0000319 16:07:23.0000371 16:07:23.0000389 16:07:23.0000400 16:07:23.0000422 16:07:23.0000430 16:07:23.0000463

Now we can compute $\langle I \rangle$, as before, as well as $\langle (I - \langle I \rangle)^2 \rangle$ (within some bandwidth)



Direct observation of individual tunneling events

Capacitively coupled quantum point contact





Direct observation of individual tunneling events





Shot noise

http://www.geocities.com/bioelectrochemistry/schottky.htm

Classical: Schottky (1918)

Noninteracting electrons

Arrivals as Poisson process.

$$S_{I,cl} = \left\langle \left(I - \left\langle I \right\rangle \right)^2 \right\rangle = 2e \left\langle I \right\rangle$$



What if *e*⁻ arrivals are not independent? More generally:

$$S_I = 2e\langle I \rangle \cdot F$$
 F = Fano factor



Shot noise





- Fano factor tells you about correlations between electron arrivals.
- e.g., *F* = 2 for Poissonian arrival of *pairs*, as in SC tunnel junction.
- In this sense, *F* tells you about *effective charge* of excitations.
- *F* → 0 in macroscopic systems at moderate temperatures inelastic scattering effectively smears out the conductance channels.



Shot noise – quantum case

$$S_I = 2eV \frac{2e^2}{h} \sum_i \tau_i (1 - \tau_i)$$

$$S_I = 4k_B T \frac{2e^2}{h} \sum_i \tau_i^2 + 2eV \frac{2e^2}{h} \operatorname{coth}\left(\frac{eV}{2k_B T}\right) \cdot \sum_i \tau_i (1 - \tau_i)$$

If conductance quantization *really* comes from Landauer physics, expect **suppression** of noise whenever $\tau_i \sim 1$.

Blanter and Büttiker, Phys. Reports 336, 1-166 (2000)








Advantage: Gets rid of (nominally uncorrelated) amplifier noise, with sufficient averaging.





Shows expected shot noise suppression when conductance is quantizes – confirms quantum nature of transport!







Low frequency method: challenges

Capacitive attenuation of signal

 $\nu_{\rm roll-off} \approx \frac{1}{2\pi RC}$

Minimal stray capacitance on order of hundreds of pF

$$\frac{1}{G_0} = \frac{h}{2e^2} \approx 12.9 \text{ k}\Omega$$

 $\rightarrow \nu_{\rm roll-off} \approx 10 {\rm s~of~kHz}$



May be mitigated partially by characterization of *C*, but still limiting.

Note that relevant voltages to be measured are small! At I = 100 nA, $G \sim G_0$ (ignoring suppression), $S_V = 2eI/(G^2) \approx 5.3 \times 10^{-18} \text{ V}^2/\text{Hz}$ $\rightarrow (\delta V)_{\text{rms}} \approx 2.4 \text{ nV}/\sqrt{\text{Hz}}$



Resistance fluctuations w/ distribution of relaxation times leads to voltage fluctuations w/ 1/f power spectrum.



Interestingly, still visible in nanocontacts.





Another challenge: 1/f noise

Fortunately, can distinguish this experimentally from shot noise.

$$I\delta R \to \delta V \quad S_{V, 1/f} \propto I^2$$

Need to look at scaling of noise signal w/ bias current.





There are predictions of modified Fano factors.

Example: diffusive mesoscopic wire $\ F
ightarrow 1/3$





Prediction of modified Fano factors







Prediction of modified Fano factors

Enhanced Fano factor due to *e*-vib coupling



Heuristically, electron-vibrational coupling renormalizes



Modified Fano factors in the Kondo regime



Sela et al., PRL 97, 086601 (2006)

Prediction that finite V leads to modification of Fano factor.

Idea: back-scattering + creation of e-h pair = some two-particle contribution.



Experimental evidence





Zarchin et al., PRB 77, 241303(R) (2008)



Higher frequency approach to noise measurement

There are several higher frequency methods for measuring the noise.

The example at right is one approach – directly measure rf power.

Using lock-in synced to bias eliminates Nyquist-Johnson contribution.

Improvements (not shown): onchip impedance matching; low-*T* amplifiers.



Higher frequency approach to noise measurement



Test this approach using a vacuum photodiode as shot noise source.

When corrected for impedance mismatch, find $S_1 = 2 \text{ e } I$ to within 2%.





Higher frequency approach to noise measurement

Wheeler et al., Nano Lett. 10, 1287 (2010)



Shot noise suppression at quantized conductance survives at 300 K.

Neat demonstration that quantum coherence is relevant at the few nm scale even at room temperature.



Optics and transport in nanojunctions

What happens in the presence of light?

Things can become very complicated very quickly.

IR/visible light = molecular energy scales; microwaves = semiconductor dot scales





Internal state spectroscopy



Plasmons

Plasmons = collective modes of (incompressible) electronic fluid



- Light can excite plasmons in metal nanostructures big local electric fields.
- Optical antennas, producing voltages at optical frequencies.
- Those voltages are hard to measure, but they do have consequences....



Plasmons = sound waves in the electron fluid.





Plasmons and surface-enhancement







Plasmons and surface-enhancement





Plasmons = sound waves in the electron fluid.



metal nanoparticle dimer

- Local electric field can be much larger ($g(\omega)$) than incident field!
- Raman scattering rate ~ $g(\omega)^2 g(\omega')^2$
- If $g(\omega)$, $g(\omega') \sim 1000$ each, then Raman enhanced by 10^{12} .
- Single-molecule sensitivity possible in surface-enhanced Raman spectroscopy (SERS).



What are the plasmon modes here?



- EM calculations (FDTD) show that nanometer-scale protrusions can lead readily to intensity enhancements approaching 10⁶ (!).
- Where do these highly local plasmon modes come from?



Hybridization



Hybridization





Plasmon hybridization

Same ideas can apply to plasmon modes in complex structures.



E. Prodan et al., Science **302** 419-422 (2003).



Plasmon hybridization

In our case, each electrode supports a *continuum* of edge plasmons.



Very local interaction = series of localized plasmon resonances "built out of" hybridized edge/surface plasmons from the electrodes.



Tunneling nonlinearity can lead to DC current from AC bias.

$$I(V) = I_0(V_{\rm dc}) + \left(\frac{\partial I}{\partial V}\right)_{V_{\rm dc}} V_{\rm ac} \cos(\omega t) + \frac{1}{2} \left(\frac{\partial^2 I}{\partial V^2}\right)_{V_{\rm dc}} (V_{\rm ac} \cos(\omega t))^2 + \dots$$

$$= \left[I_0(V_{\rm dc}) + \frac{1}{4} \left(\frac{\partial^2 I}{\partial V^2}\right)_{V_{\rm dc}} V_{\rm ac}^2\right] + \left(\frac{\partial I}{\partial V}\right)_{V_{\rm dc}} V_{\rm ac} \cos(\omega t) - \frac{1}{4} \left(\frac{\partial^2 I}{\partial V^2}\right)_{V_{\rm dc}} V_{\rm ac}^2 \cos(2\omega t) + \dots$$

Light induces some V_{opt} across our gap, oscillating at ~ 10¹⁵ Hz.

Rectification (photocurrent) can lead to a means of quantitatively estimating the field enhancement factor! (*provided that tunneling is fast*!)



Optical rectification

This has been shown to work quantitatively at microwave frequencies.

THE JOURNAL OF CHEMICAL PHYSICS 124, 021105 (2006)

Atomic-scale rectification at microwave frequency

X. W. Tu, J. H. Lee,^{a)} and W. Ho^{b)}

Department of Physics and Astronomy and Department of Chemistry, University of California, Irvine, California 92697-4575





Validity of classical rectification

In general, correct quantum treatment = **photon-assisted tunneling**.

Tien-Gordon (perturbative) approach:

$$\alpha \equiv \frac{eV_{\rm ac}}{\hbar\omega}$$

$$I(V_{\rm dc}; \alpha, \omega) = \sum_{n=-\infty}^{\infty} J_n^2(\frac{\alpha}{2}) I_0(V_{\rm dc} + n\hbar\omega/e)$$

First order in alpha:

$$I(V_{\rm DC}, V_{\rm opt}, \omega) - I(V_{\rm DC}) = I(V_{\rm dc}; \alpha, \omega) - I_0(V_{\rm dc})$$

$$= \frac{1}{4} V_{\rm ac}^2 \left[\frac{I(V_{\rm dc} + \hbar\omega/e) - 2I(V_{\rm dc}) + I(V_{\rm dc} - \hbar\omega/e)}{(\hbar\omega/e)^2} \right]$$

If $\alpha \ll 1$ and nonlinearity varies little (i.e., DOS is "boring") over $[(E_{\rm F} + eV_{\rm dc}) - \hbar\omega/e, (E_{\rm F} + eV_{\rm dc}) + \hbar\omega/e]$

then classical rectification picture is reasonable.



Validity of classical rectification

Viljas and Cuevas, PRB 75, 075406 (2007)



DFT calculations originally done for Au contacts show that we are likely in luck as far as DOS goes, as long as junctions are *clean*.



Optical rectification

How would this work?

- Use low freq measurement ($\omega_{low} = 2\pi \times 2 \text{ kHz}$) with known V_{ac} , and use lock-in at $2\omega_{low}$ to measure (d^2I/dV^2) as a function of V_{dc} .
- Simultaneously, measure the photocurrent as a function of V_{dc} (use a second lock-in and chop the light).
- Adjust V_{ac} until the two signals (2nd harmonic + photocurrent) are identical. Voila V_{ac} should now = V_{opt} .





Cross-checks







Examples:



dI/dV in units of nA/V.

Quantitative agreement between I_{photo} and $(1/4)d^2I/dV^2 V_0^2$ happens when $V_0 = 32.4$ mV.

Measured dI/dV at $V_{dc} = 0$ implies an interelectrode gap of ~ 0.092 nm, implying local field = 3.6 x 10⁸ V/m.

Implied field enhancement ~ 1230x



Optics provides additional access to microscopic distributions.



- Cross sections typically 10⁻²⁹ cm² very small!
- Stokes/anti-Stokes ratio can tell you temperature due to Boltzmann occupancy factor.



Raman spectroscopy of nanoscale gaps



Nanoscale gaps are *ideal* for surface-enhanced Raman spectroscopy.






Vibrational Spectroscopy



- At nanogap, large SERS signal, "blinking", and spectral diffusion.
- Simultaneous transport + Raman would open *many* possibilities.



Vibrational Spectroscopy



Remember, data so far taken in air, at room temperature.



Transport + SERS



- Enhancement "turns on" as junction is migrated.
- Inter-electrode plasmon modes form once conductance $\sim 10^{-4}$ S.



Transport + SERS

- Raman and transport correlate very strongly in time.
- Demonstrates singlemolecule Raman sensitivity.





Simultaneous conduction + SERS





$$\frac{AS(\omega')}{S(\omega)} = \left(\frac{\sigma_{AS}}{\sigma_{S}}\right) \left(\frac{g(\omega')}{g(\omega)}\right)^{2} \left(\frac{\omega'}{\omega}\right)^{4} \exp\left(-\frac{\hbar\delta\omega}{k_{B}T_{eff}}\right)$$

- Ratio of antiStokes to Stokes intensities provides a measure of excited state population, and therefore *effective* temperature.
- The exponential makes things challenging.

Ignoring cross-section and enhancement issues, 450 cm⁻¹ mode at 80 K \rightarrow AS/S = 3.8 × 10⁻⁴. So, 10000 Stokes counts \rightarrow 3.8 antiStokes counts

• SERS itself can lead to optical pumping of excited state.

Can we see bias-driven effects?



Detection of heating in current-carrying molecular junctions by Raman scattering

ZVI IOFFE[†], TAMAR SHAMAI[†], AYELET OPHIR, GILAD NOY, ILAN YUTSIS, KOBI KFIR, ORI CHESHNOVSKY* AND YORAM SELZER*

Nature Nanotechnology 3, 727 - 732 (2008)



Suggestive, though puzzling.



Electrical vibrational pumping

As bias is increased and current starts to flow, antiStokes Raman lines turn on!





Electrical vibrational pumping

As bias is increased and current starts to flow, antiStokes Raman lines turn on!

From AS/S ratio, can infer *effective* vibrational temperatures – really a measure of vibrational occupancy.





Electrical and optical vibrational pumping

A second example....



D. Ward et al., Nature Nano. 6, 33-38 (2011).



Electrical and optical vibrational pumping

Optically pumped line always well above ambient *T*.

Asymmetry in conduction = asymmetry in heating.





Electronic heating, too.



- SERS Stokes continuum thought to be *electronic Raman*.
- AntiStokes only possible due to electrons above the Fermi energy.
- AntiStokes continuum increases with bias!
- Can fit using Fermi distribution to find **effective** *electron* temperature.

D. Ward et al., Nature Nano. 6, 33-38 (2011).



Significant electronic heating is a surprise



- Landauer-Buttiker picture of transport assumes that all dissipation happens "far away" from the junction....
- Right-moving carriers are at chemical potential of left side until they reach right contact.
- Left-moving carriers are at chemical potential of right side until they reach left contact.
- Bold curve represents average of chemical potential.



- Noise provides valuable information beyond basic dc transport.
- Specific predictions exist for noise and how it is modified by, e.g., Kondo, though not in the case of molecules.
- Optical methods provide other ways of accessing local physics in molecular junctions, including vibrational and electronic distributions.
- However, the cost is an increase in complexity, including thorny issues about equilibration and thermalization.